



## CHAPTER V

### RESULT AND DISCUSSION

#### 5.1 Stochastic Simulation Results

The process of dendritic deposition is very complex and difficult to predict. The particle deposition process has been simulated stochastically using Monte-Carlo technique, under various filtration conditions of convective Brownian diffusion as well as inertial impaction.

##### 5.1.1 Convective Brownian diffusional deposition

The dendritic growth of convective diffusional deposition was simulated using stochastic model for various filtration conditions. The dendrites caused increase in the collection efficiency of a dust-loaded fiber. The positions of particles deposited on the fiber can be obtained by the stochastic simulation. Figures 5.1-5.30 show the configuration of dendrites. The typical dendrites were densely packed when the interception parameter  $R$  was small but was more porous when  $R$  was large. Furthermore, the configuration of the dendrites was tall and slender at a large  $Pe$ . On the other hand, the particles were captured more uniformly over the entire fiber surface at a small  $Pe$ .

The particle collection efficiency was evaluated using the Monte-Carlo simulation results. The clean fiber collection efficiency can be obtained from the equation of Stechkina and Fuchs (1966). The collection efficiency raising factor  $\lambda$  listed in Table 5.1 and Table 5.2 shows the difference in  $\lambda$  between the previous stochastic study (Kanaoka et al., 1983) and the present study. According to the previous study,  $\lambda$  values were higher than the present corresponding values for the case of  $R=0.1$  but were nearly equal to those  $\lambda$  for the corresponding case of  $R=0.2$ . In the present study, the starting point of an incoming particle was at the generation plane of Kuwabara's cell. But in previous study, they reduced the required

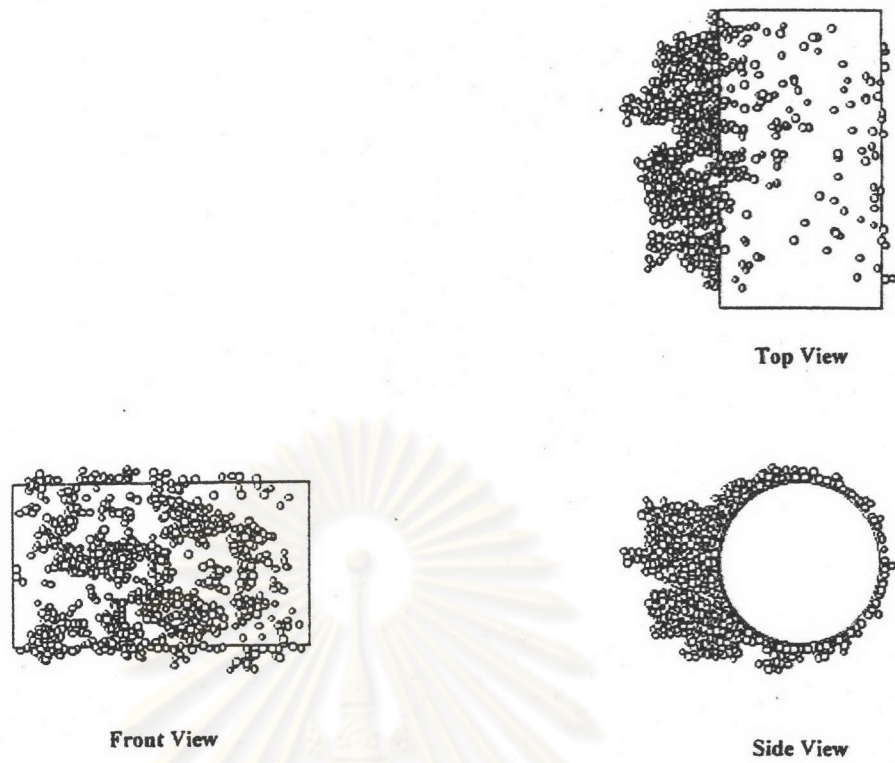


Figure 5.1. Typical configurations of dendrites for  $R=0.05$  and  $Pe=200$

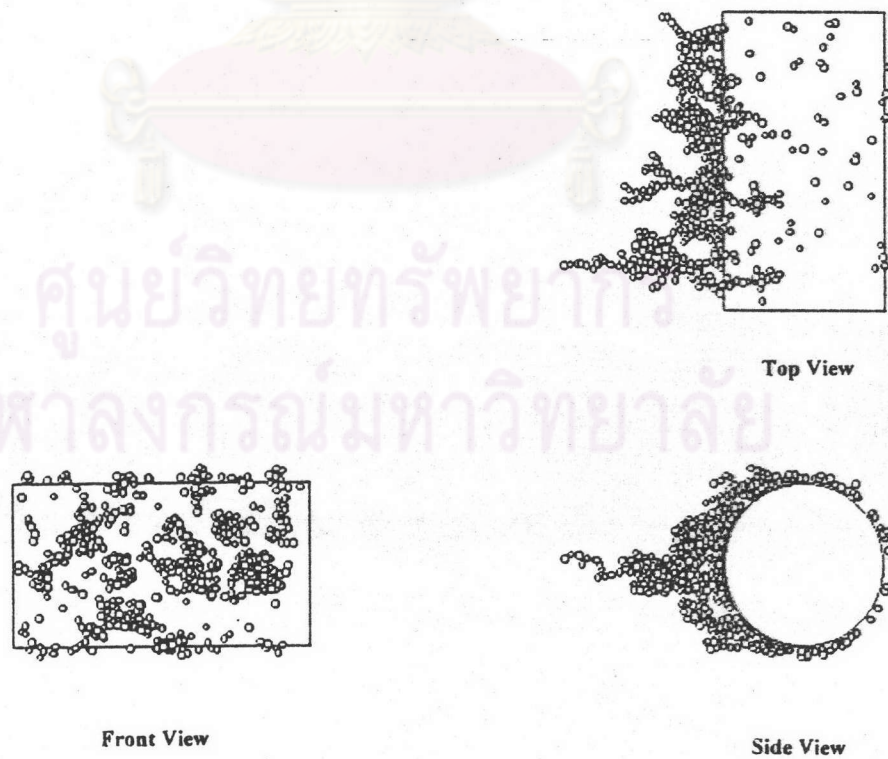


Figure 5.2. Typical configurations of dendrites for  $R=0.05$  and  $Pe=500$



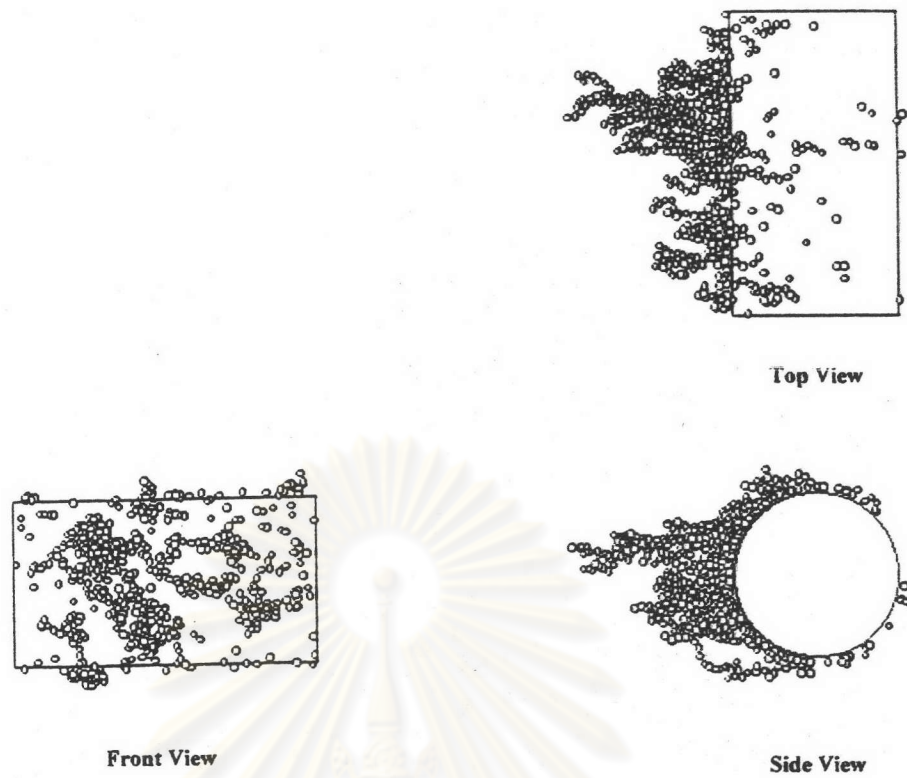


Figure 5.3. Typical configurations of dendrites for  $R=0.05$  and  $Pe=1000$

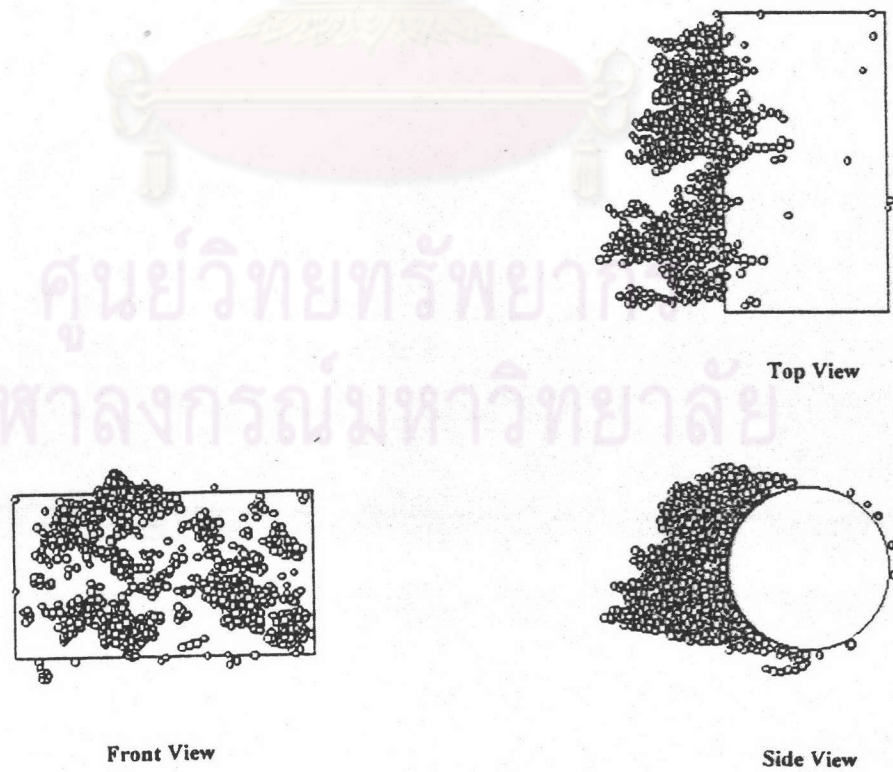


Figure 5.4. Typical configurations of dendrites for  $R=0.05$  and  $Pe=2500$

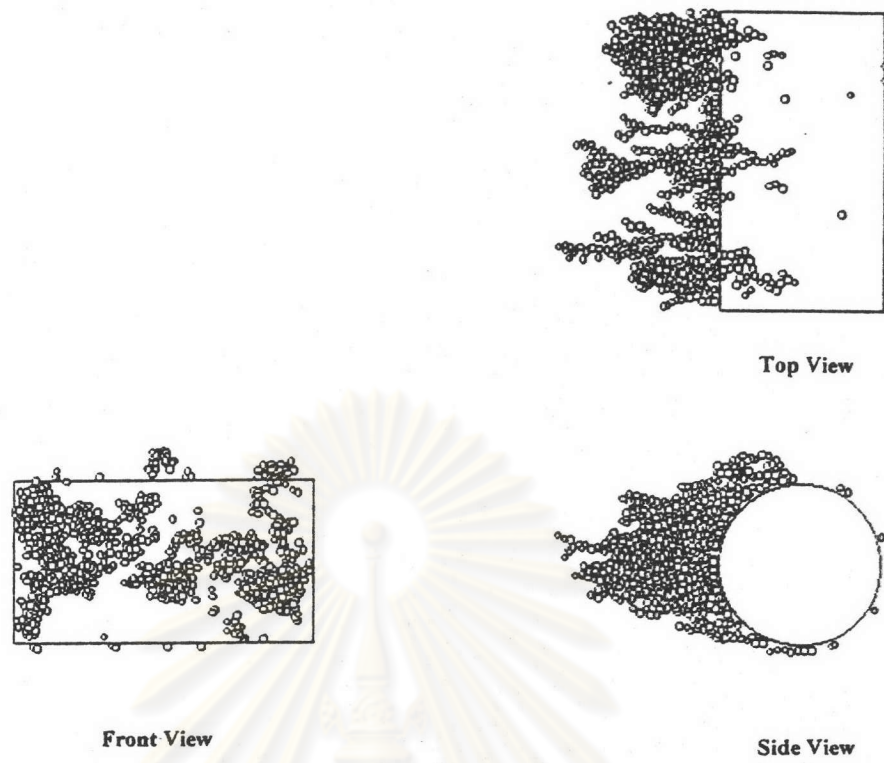


Figure 5.5. Typical configurations of dendrites for  $R=0.05$  and  $Pe=5000$

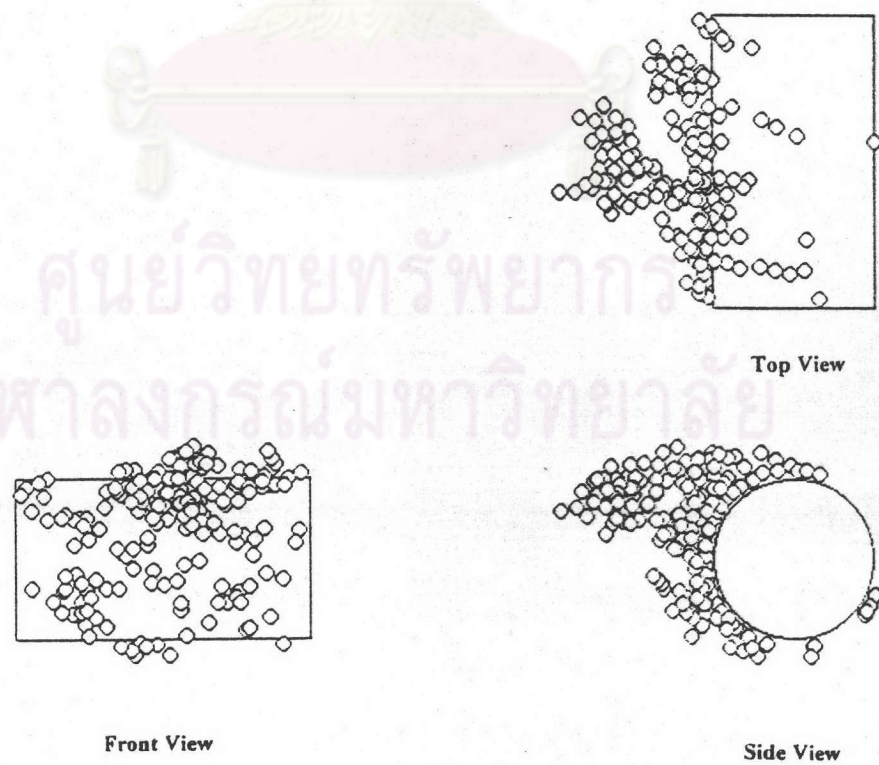


Figure 5.6. Typical configurations of dendrites for  $R=0.1$  and  $Pe=200$



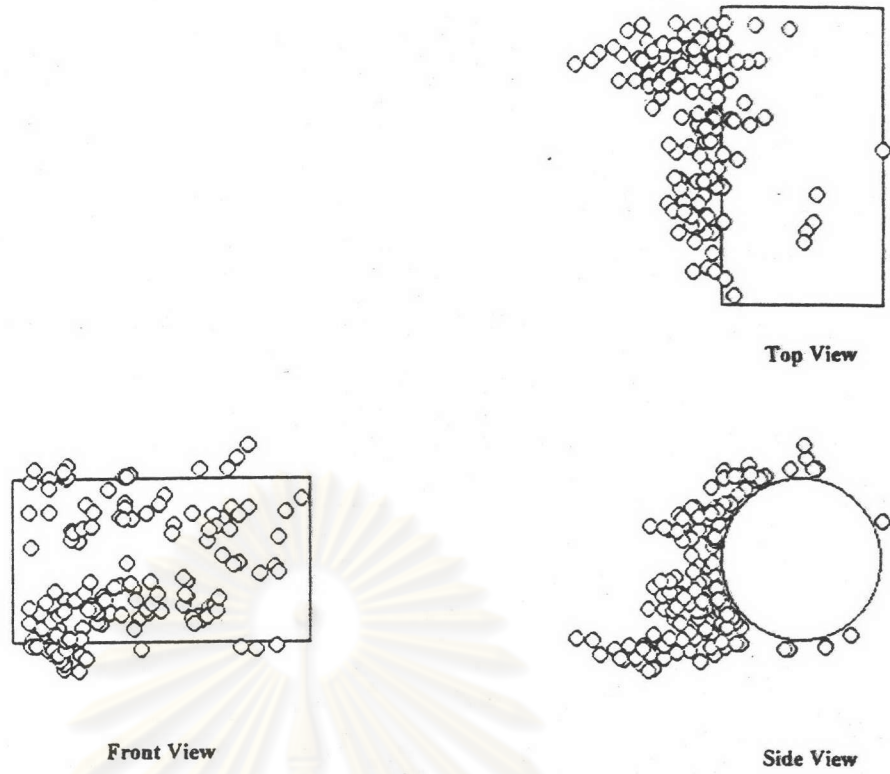


Figure 5.7. Typical configurations of dendrites for  $R=0.1$  and  $Pe=500$

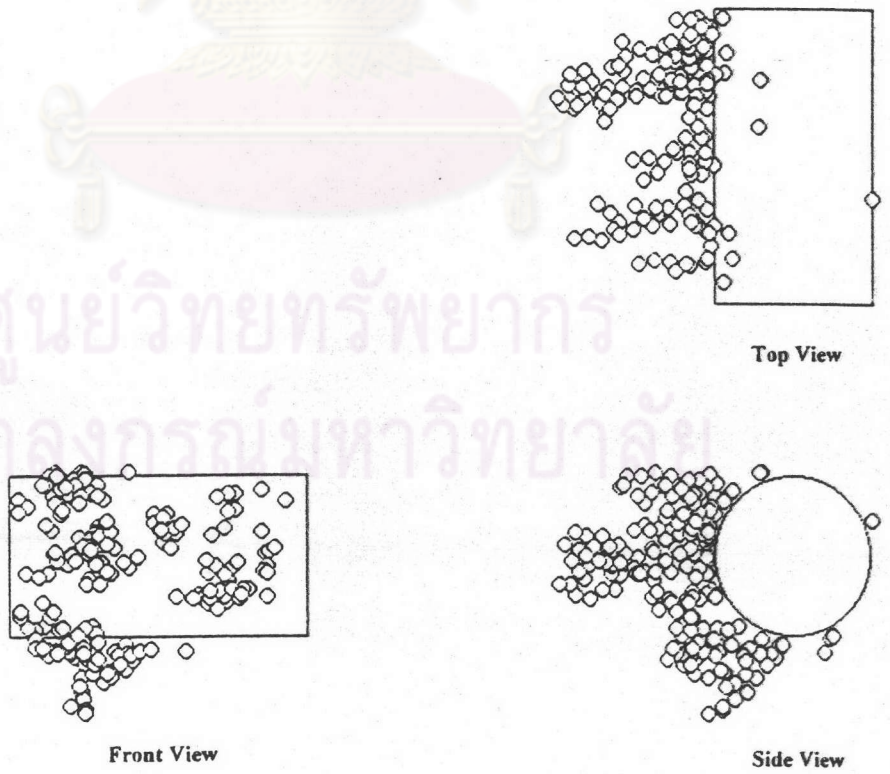


Figure 5.8. Typical configurations of dendrites for  $R=0.1$  and  $Pe=1000$

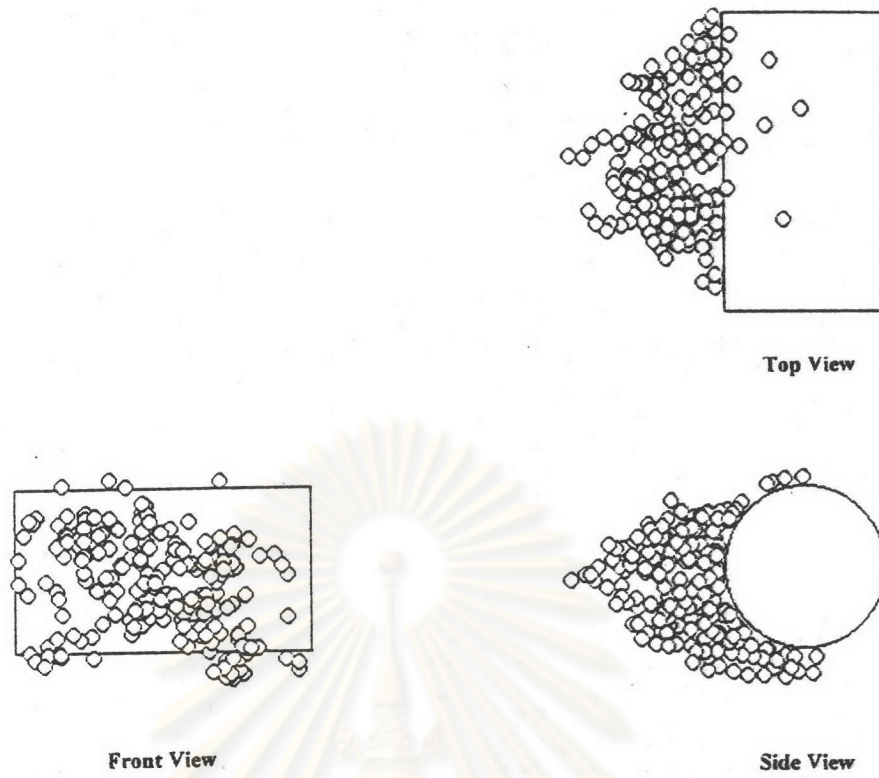


Figure 5.9. Typical configurations of dendrites for  $R=0.1$  and  $Pe=2500$

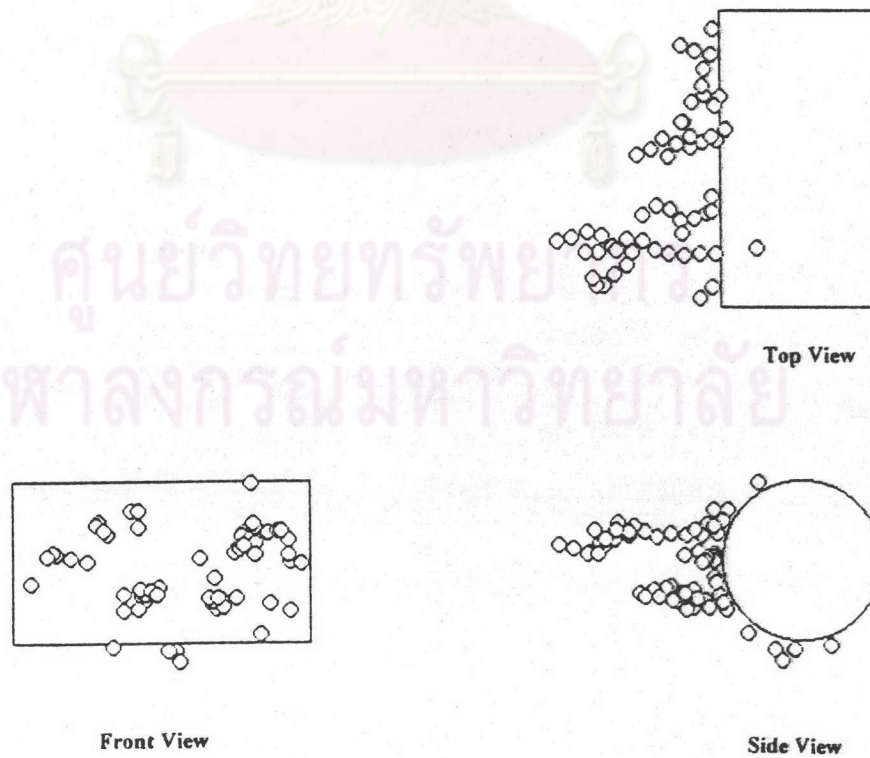


Figure 5.10. Typical configurations of dendrites for  $R=0.1$  and  $Pe=5000$

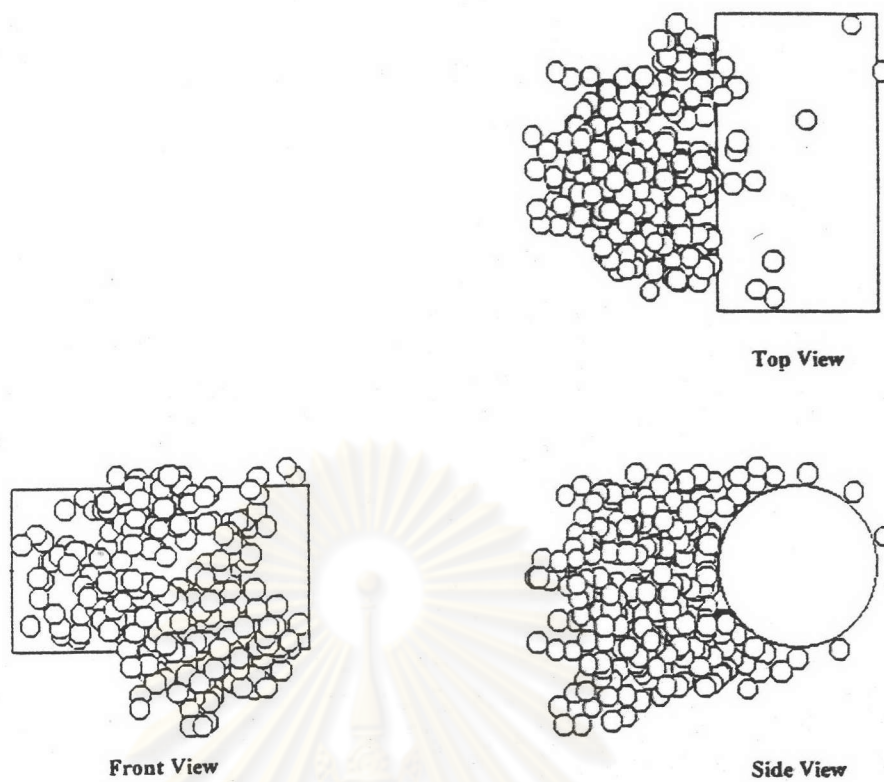


Figure 5.11. Typical configurations of dendrites for  $R=0.13$  and  $Pe=200$

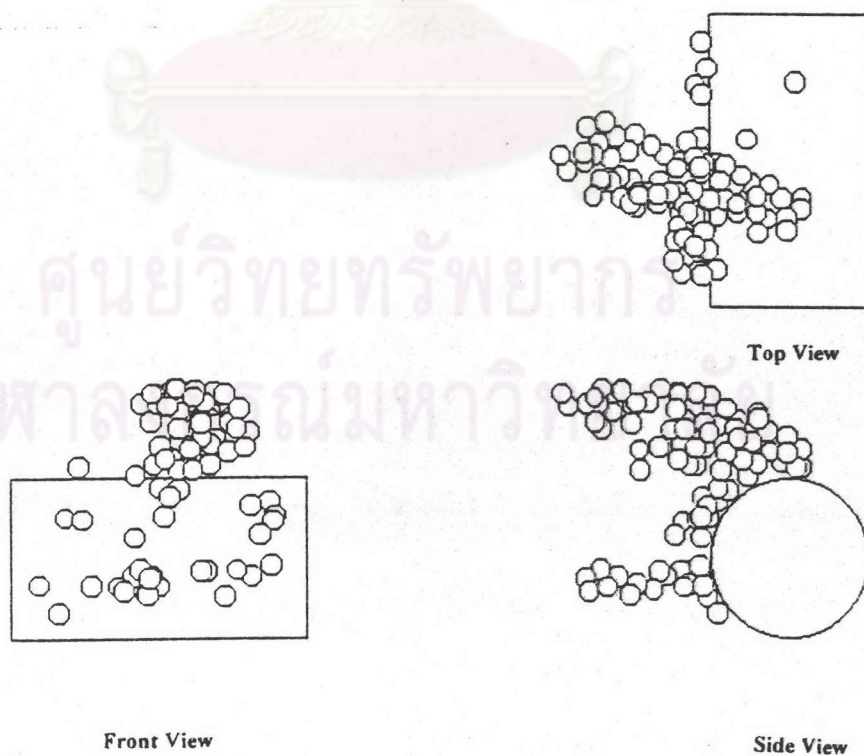


Figure 5.12. Typical configurations of dendrites for  $R=0.13$  and  $Pe=500$



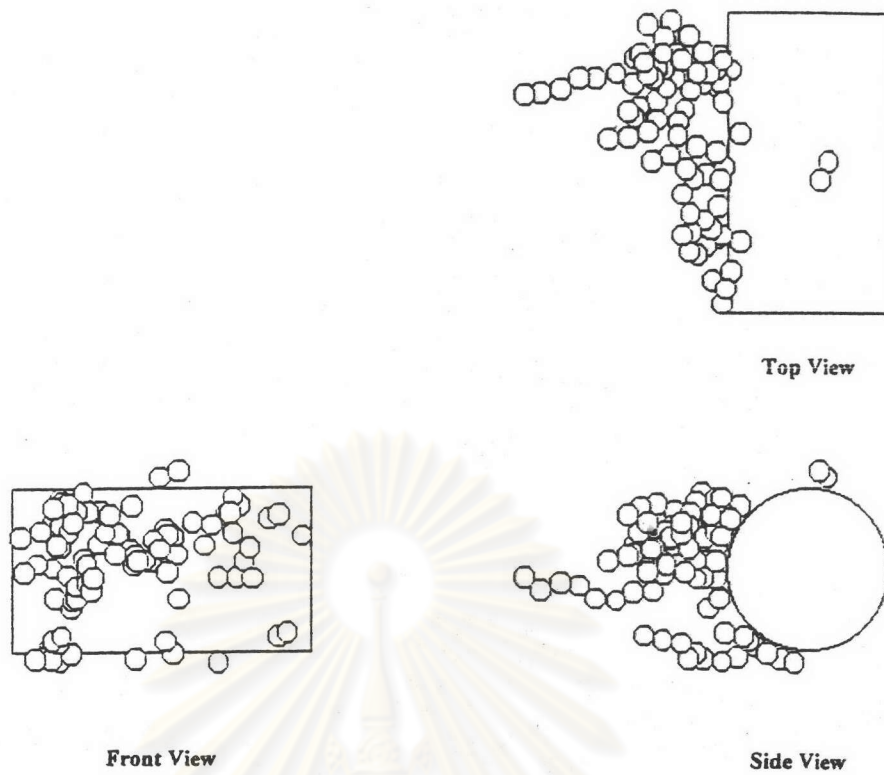


Figure 5.13. Typical configurations of dendrites for  $R=0.13$  and  $Pe=1000$

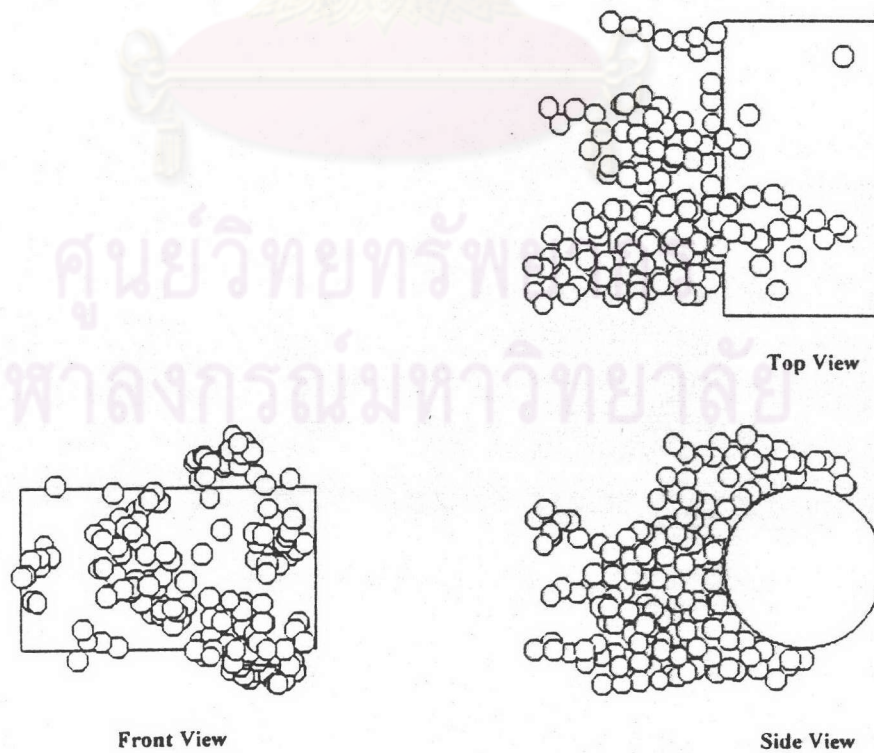


Figure 5.14. Typical configurations of dendrites for  $R=0.13$  and  $Pe=2500$

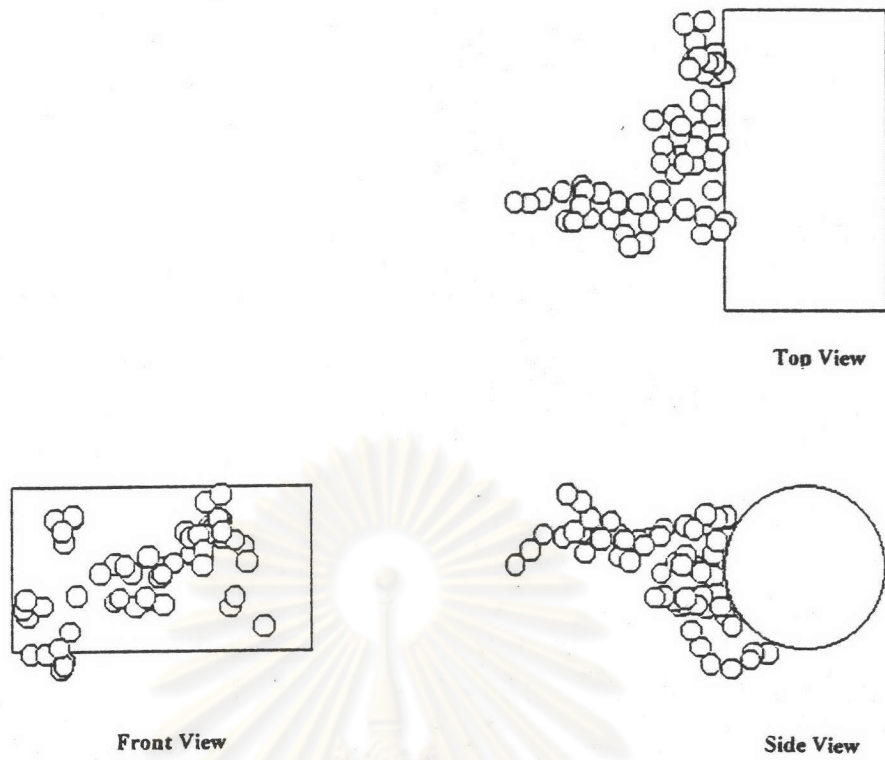


Figure 5.15. Typical configurations of dendrites for  $R=0.13$  and  $Pe=5000$

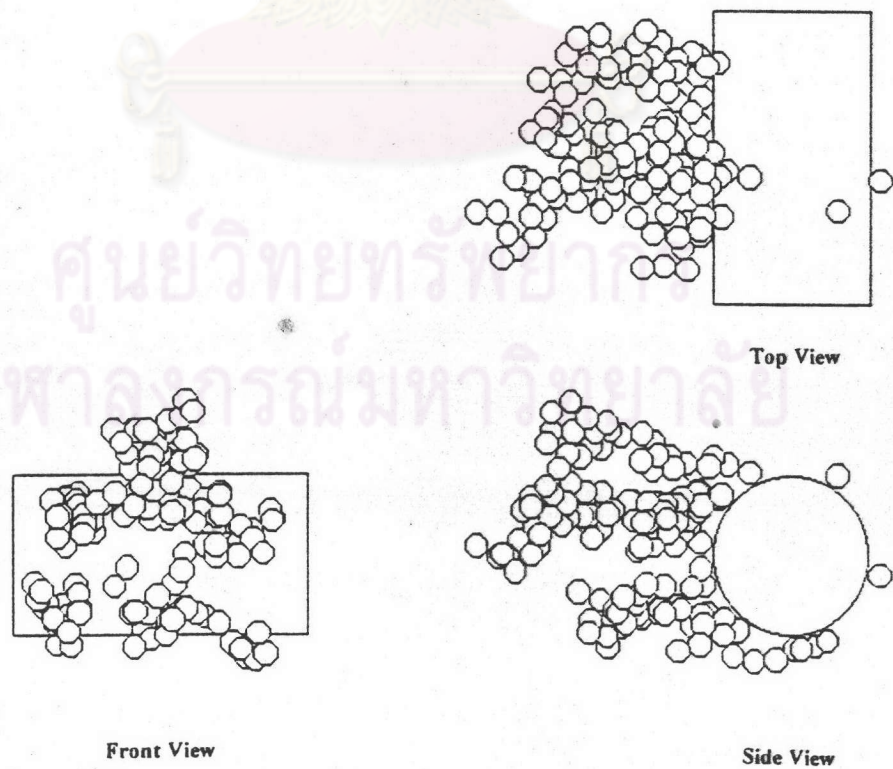


Figure 5.16. Typical configurations of dendrites for  $R=0.15$  and  $Pe=200$

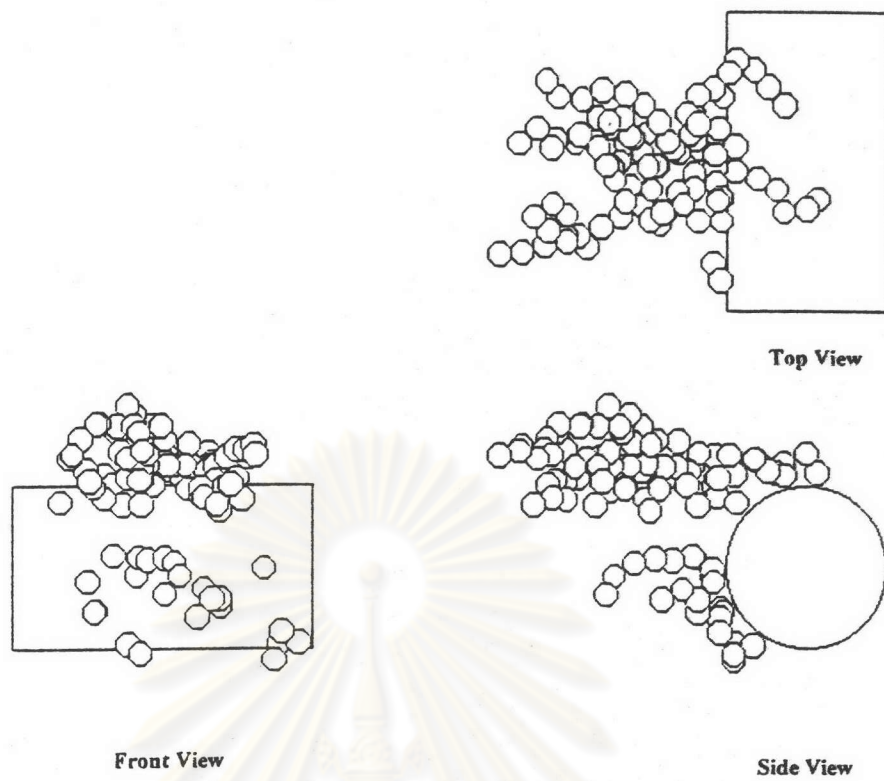


Figure 5.17. Typical configurations of dendrites for  $R=0.15$  and  $Pe=500$

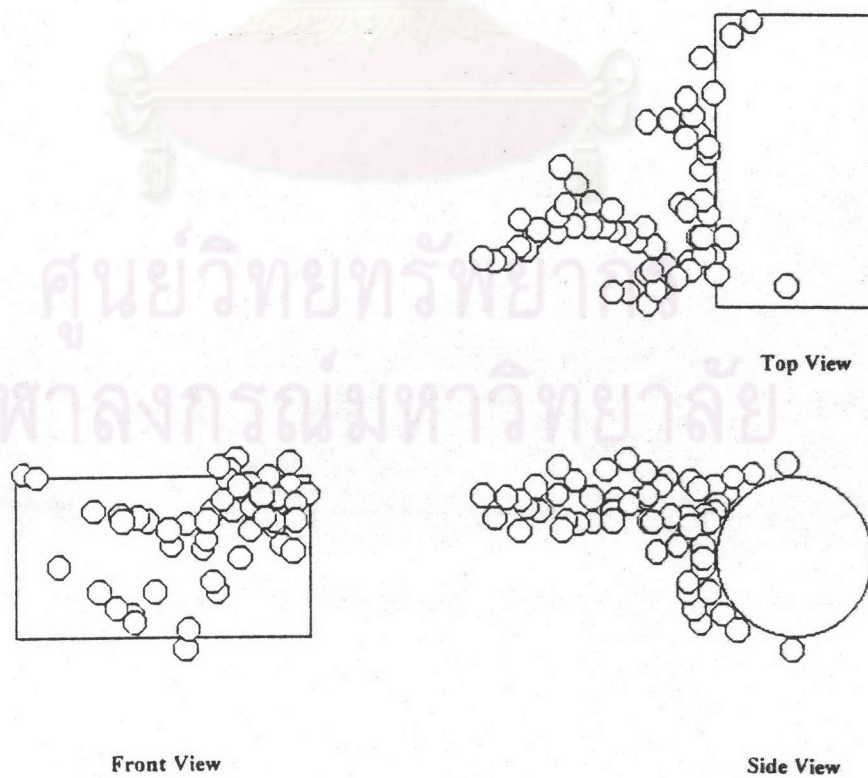


Figure 5.18. Typical configurations of dendrites for  $R=0.15$  and  $Pe=1000$



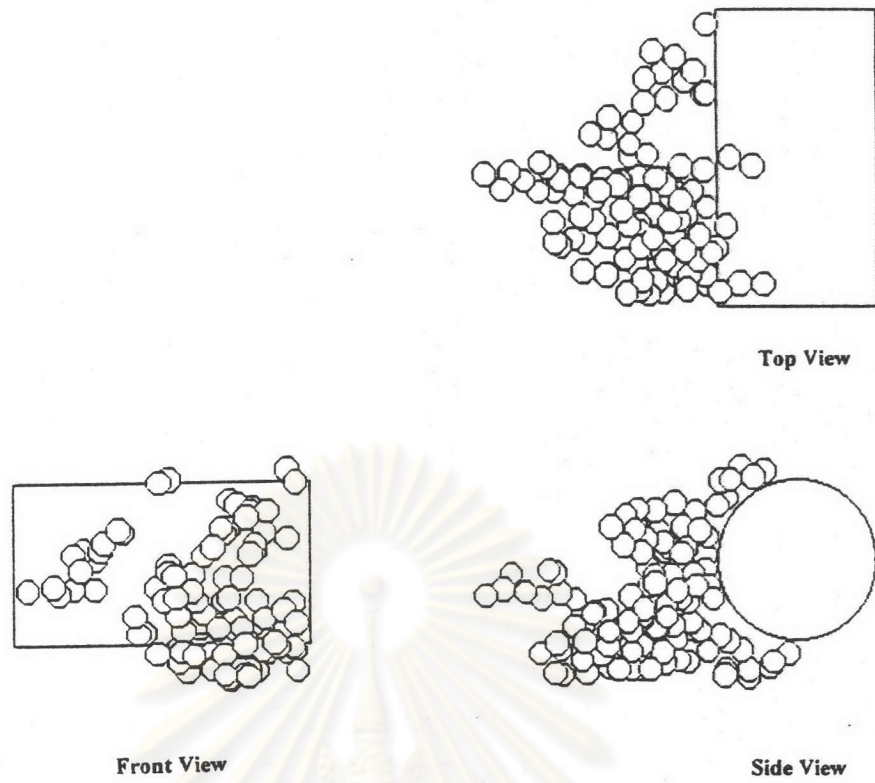


Figure 5.19. Typical configurations of dendrites for  $R=0.15$  and  $Pe=2500$

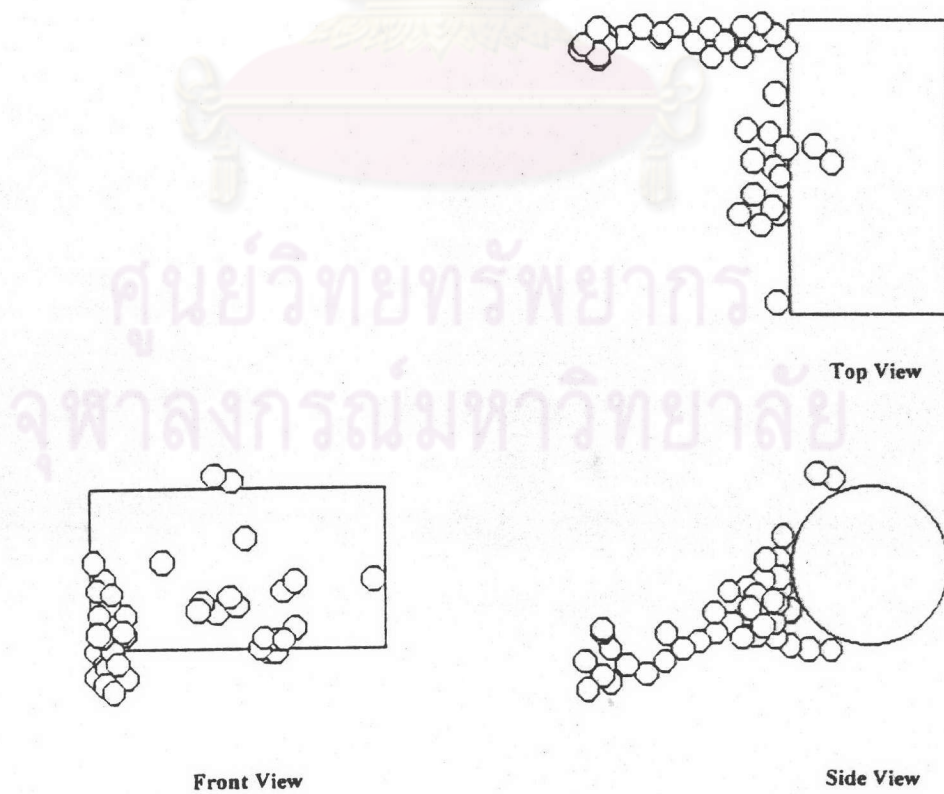


Figure 5.20. Typical configurations of dendrites for  $R=0.15$  and  $Pe=5000$

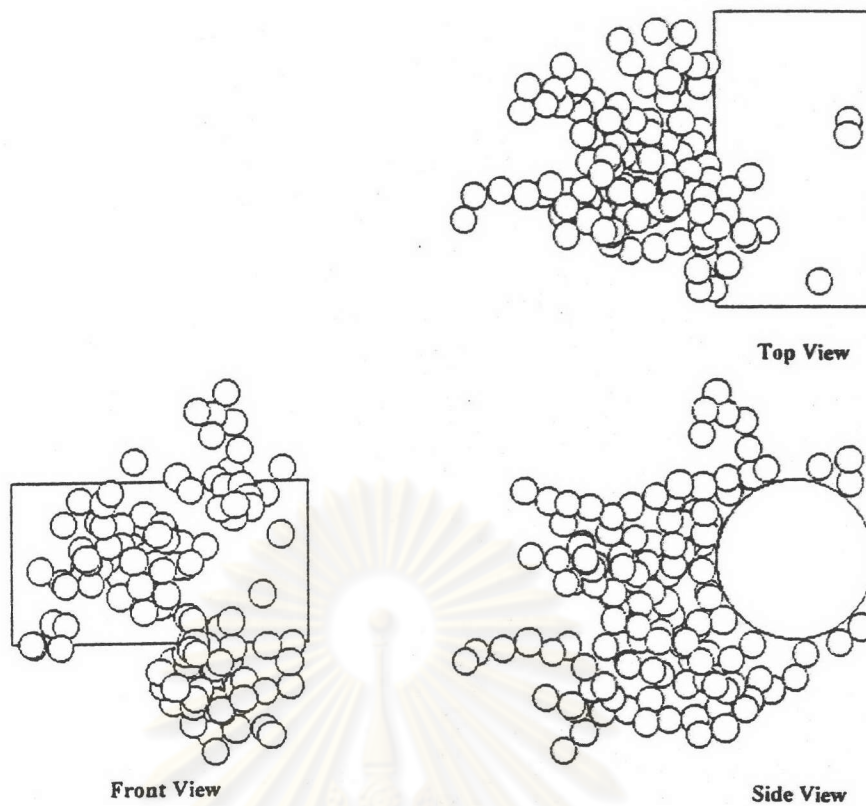


Figure 5.21. Typical configurations of dendrites for  $R=0.17$  and  $Pe=200$

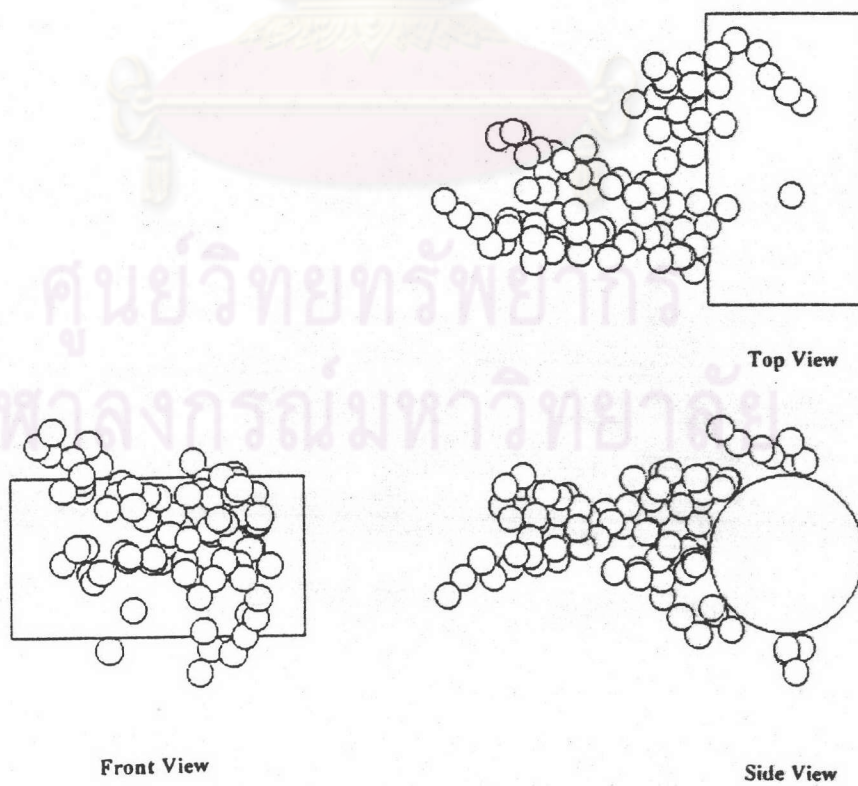


Figure 5.22. Typical configurations of dendrites for  $R=0.17$  and  $Pe=500$

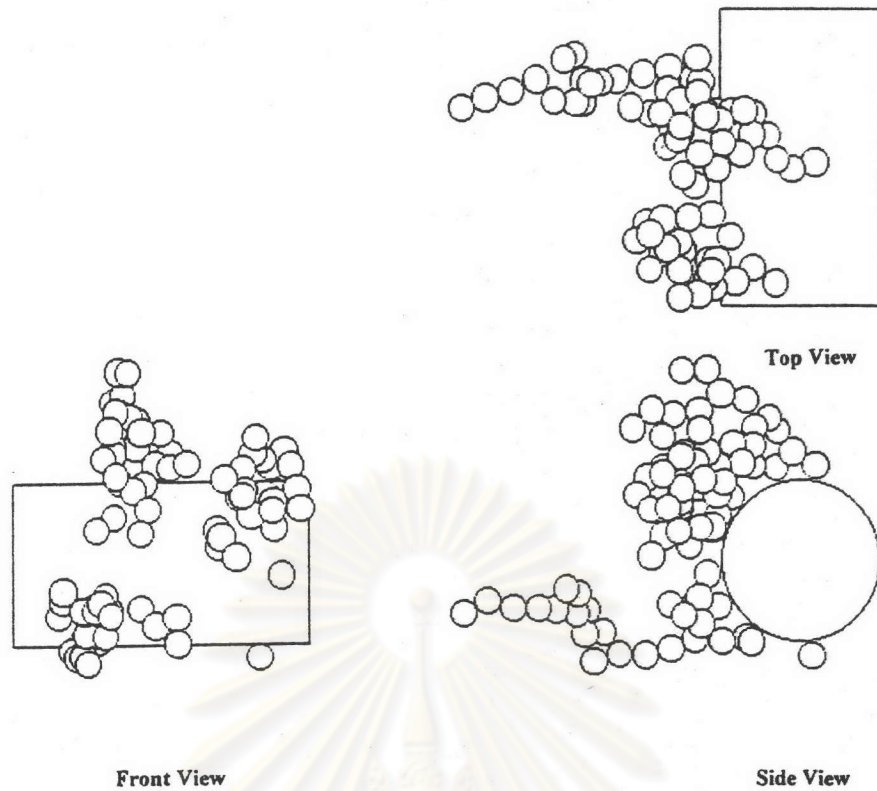


Figure 5.23. Typical configurations of dendrites for  $R=0.17$  and  $Pe=1000$

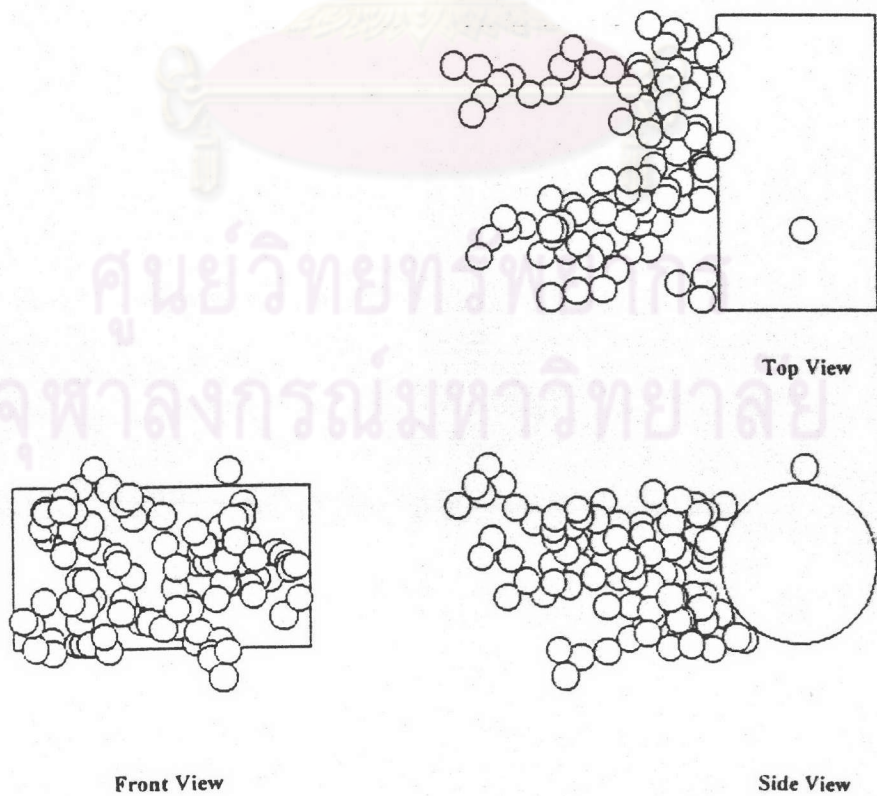


Figure 5.24. Typical configurations of dendrites for  $R=0.17$  and  $Pe=2500$



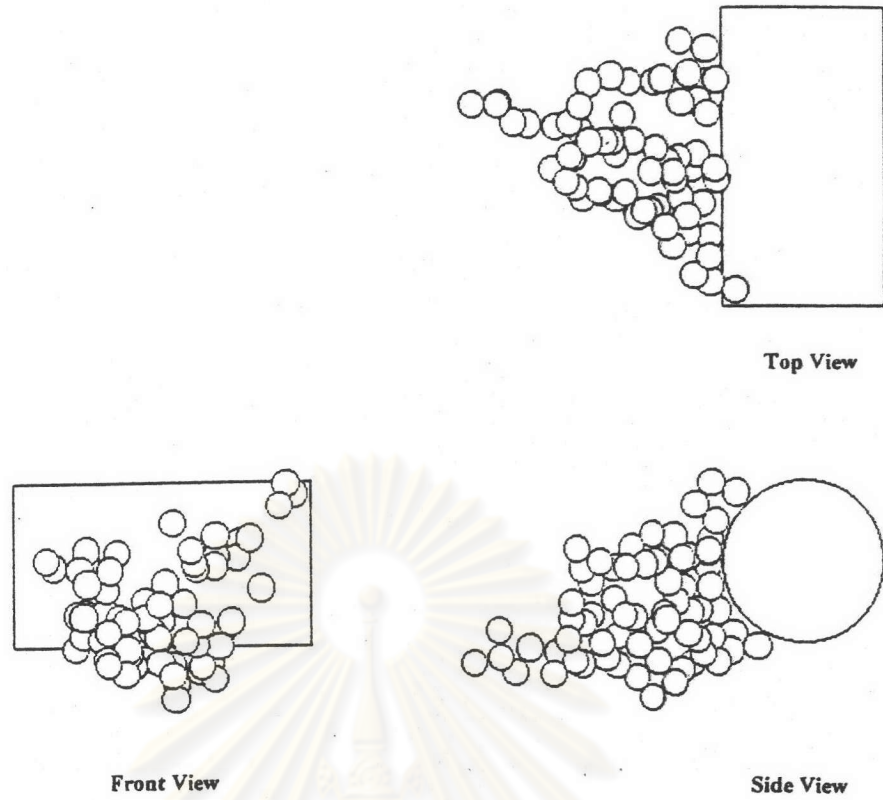


Figure 5.25. Typical configurations of dendrites for  $R=0.17$  and  $Pe=5000$

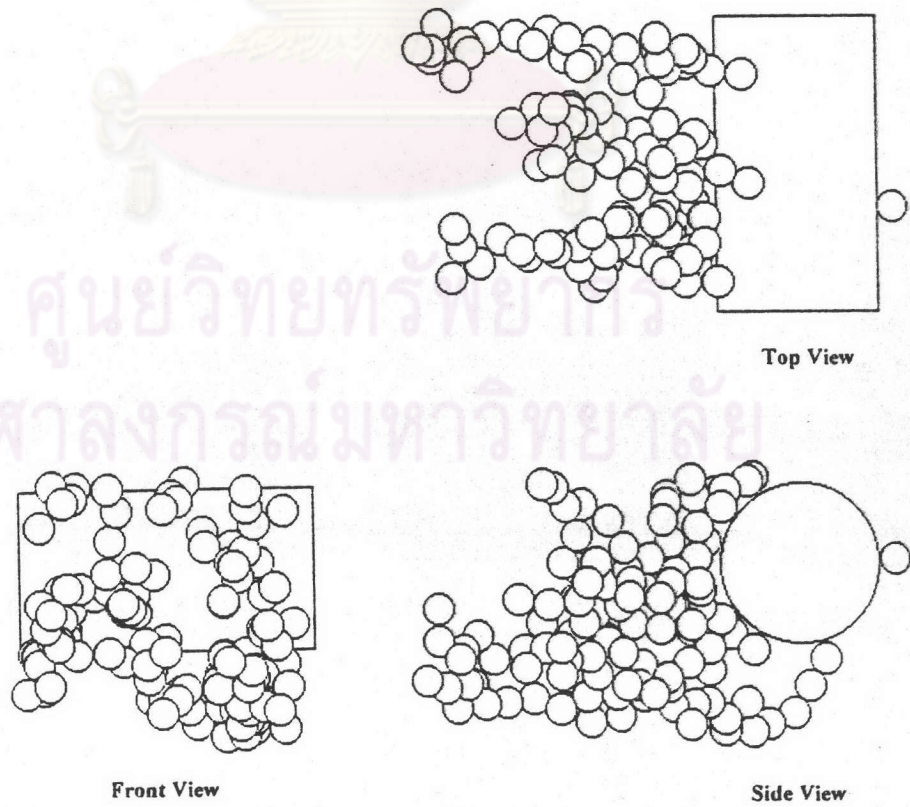


Figure 5.26. Typical configurations of dendrites for  $R=0.2$  and  $Pe=200$

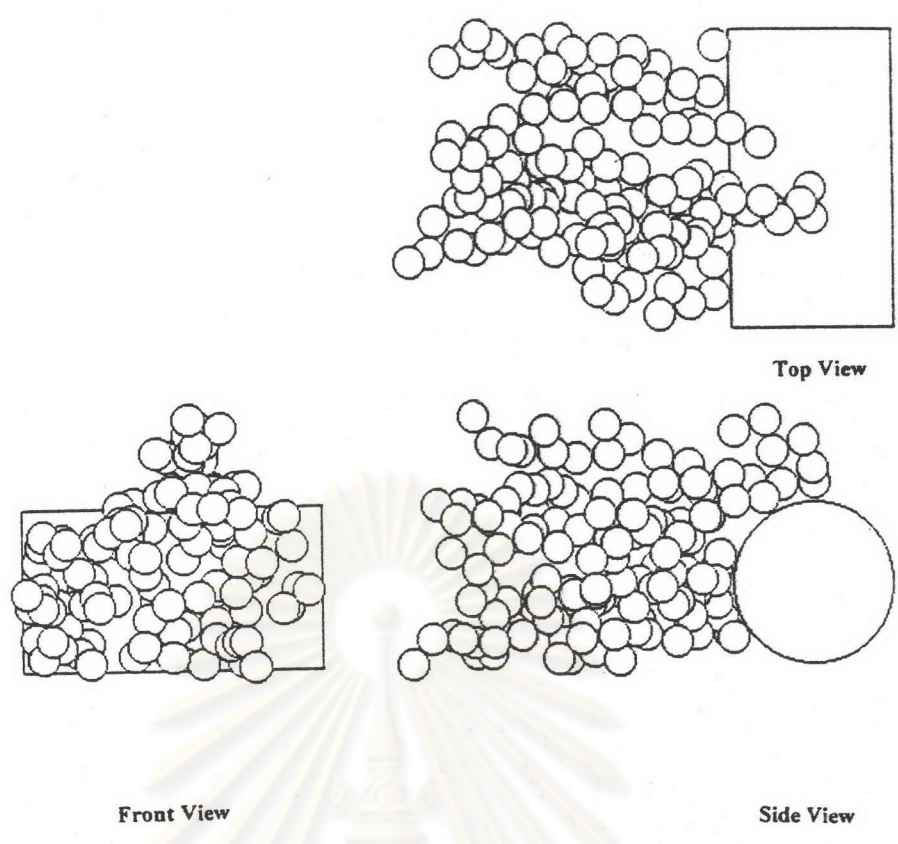


Figure 5.27. Typical configurations of dendrites for  $R=0.2$  and  $Pe=500$

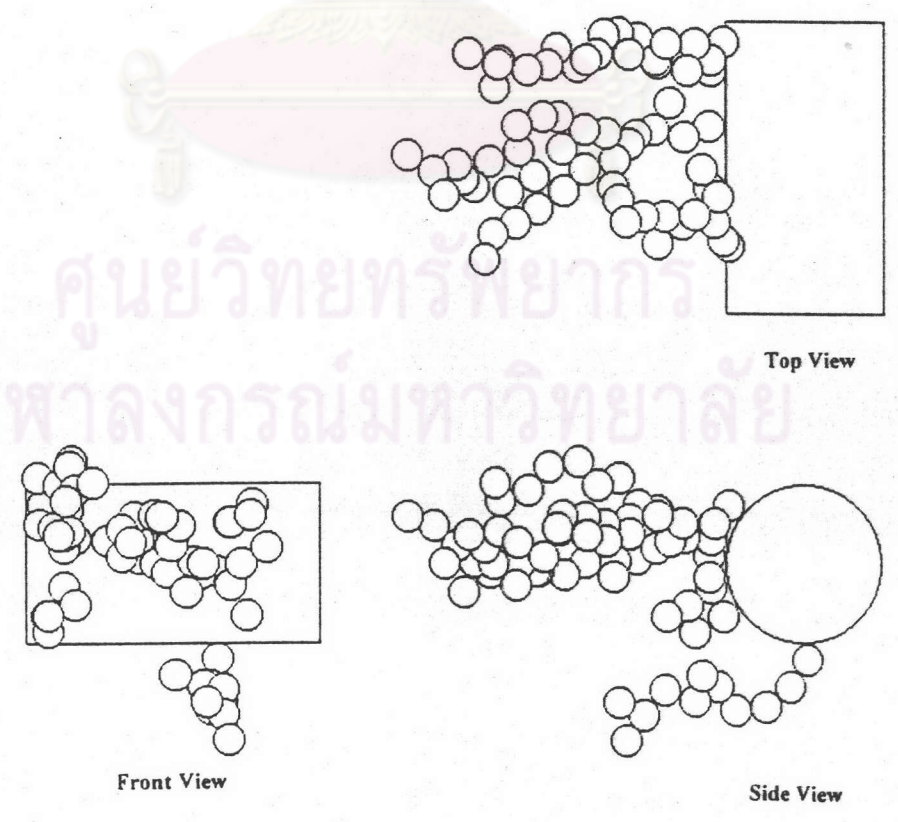


Figure 5.28. Typical configurations of dendrites for  $R=0.2$  and  $Pe=1000$

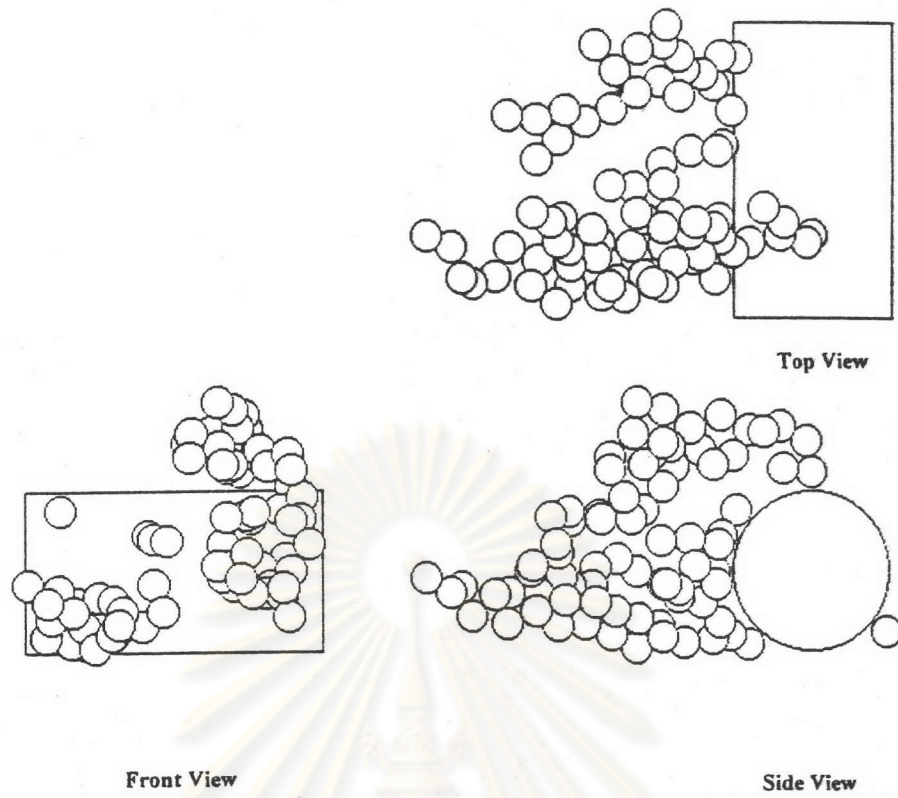


Figure 5.29. Typical configurations of dendrites for  $R=0.2$  and  $Pe=2500$

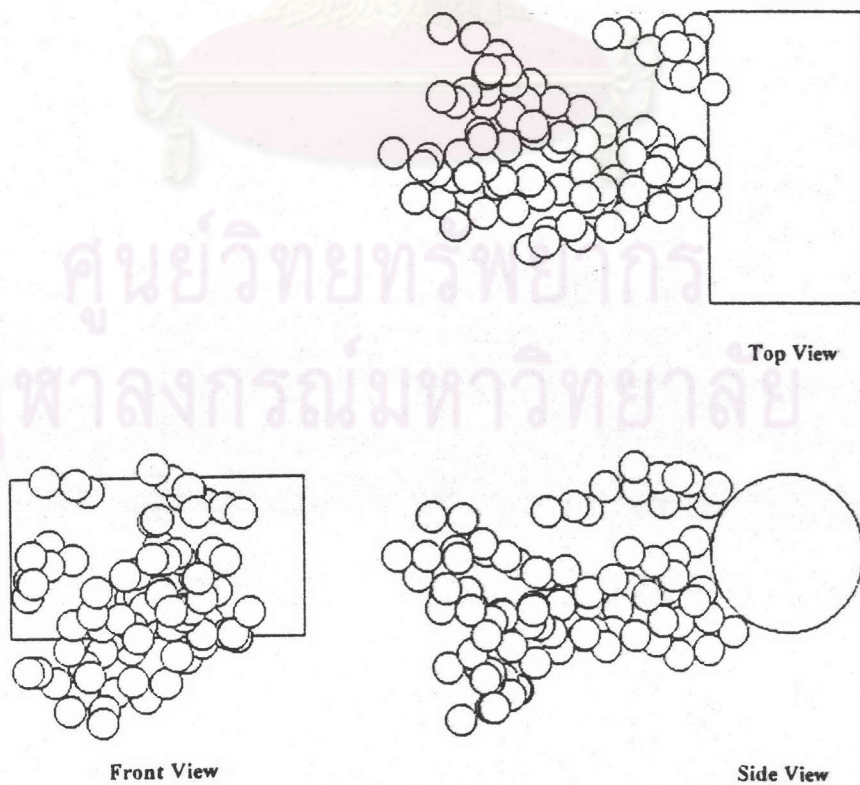


Figure 5.30. Typical configurations of dendrites for  $R=0.2$  and  $Pe=5000$



Table 5.1. Collection efficiency raising factor  $\lambda$  for convective diffusion

Pe	R					
	0.05	0.1	0.13	0.15	0.17	0.2
200		0.789*				0.588*
	0.5210	0.6159	0.6843	0.6272	0.5966	0.5267
500	1.1920	1.0550	1.192	1.0670	0.8668	0.8100
1000		2.19*				1.07*
	2.3870	1.9970	1.472	1.3780	1.258	1.0000
2500	4.6320	3.1190	2.525	1.8080	1.629	1.3870
5000		3.84*				1.42*
	6.2790	3.3570	2.694	1.6540	1.715	1.4840

\* Kanaoka et al., 1983

Table 5.2 Difference of  $\lambda$  between the previous study (Kanaoka et.al., 1983) and the present study for convective diffusion (%)

Pe	R	
	0.05	0.1
200	21.94	10.43
1000	8.8100	6.5400
5000	12.5800	4.5100

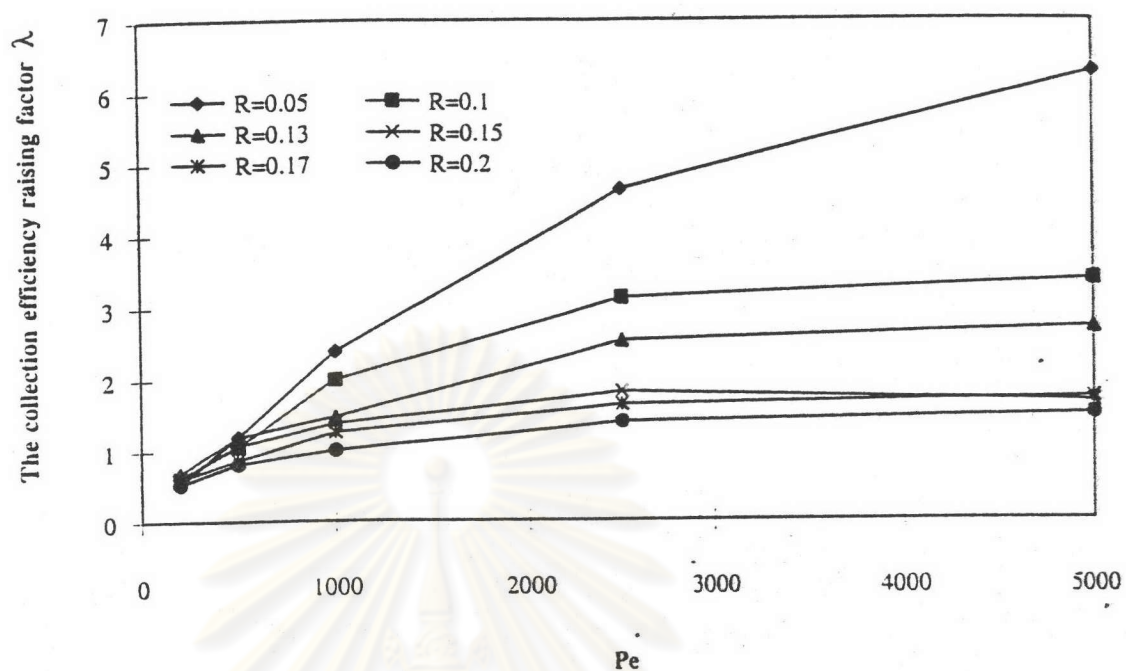


Figure 5.31. Relationship between  $\lambda$  and  $Pe$  with  $R$  as parameter (Stochastic simulation)

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computational time by using only the upper half of Kuwabara's cell. Thus, the present study was more realistic than the previous study.

Figure 5.31 shows the relationship between  $\lambda$  and Pe with R as parameter based on stochastic results. As expected, the value of  $\lambda$  is larger at a large Pe and small R than at a small Pe and large R.

### 5.1.2 Inertial impactional deposition

The dendritic growth via inertial impaction was also simulated stochastically for various filtration conditions. Figures 5.32-5.61 show the configuration of the dendrites. The particles were captured only on the front surface of the fiber. Similar to convective diffusion, the typical dendrites in the case of inertial impaction were densely packed when the interception parameter R was small but was more porous when R was large. When the mechanism of particle deposition is purely interception ( $St=0$ ), most particles were captured on upper and lower far sides of the fiber surface and the dendrites was tall. In contrast, many particles were captured around the stagnation point of the fiber surface at small St. Furthermore, the particles were densely packed and the dendrites were shorter length at large St.

The collection efficiency was evaluated from Monte-Carlo simulation results. The clean fiber collection efficiency  $\eta_0$  was obtained from the limiting trajectory theory. Figures 5.62 and 5.63 show respectively relationship between  $\eta_0$  and R with St as parameter based on Stechkina's equation (Stechkina et al., 1969), and based on the limiting trajectory theory which integrated equations (3.24) and (3.25) numerically. In the limiting trajectory theory,  $\eta_0$  increased only slightly at a large St but this was not observed in Stechkina's result, because Stechkina's equation was accurate at  $St \ll 1$  only.

The resulting collection efficiency raising factor  $\lambda$  for inertial impaction was listed in Table 5.3, including those obtained by Kanaoka et.al.(1980). Table 5.4 shows the difference in  $\lambda$  between the previous stochastic study (Kanaoka et.al., 1980) and the present study. The relative difference never exceeded 30% in all cases. For the majority of the cases, the difference was less than 10%. In the previous study, a three-dimensional mesh network was constructed beforehand for containing captured



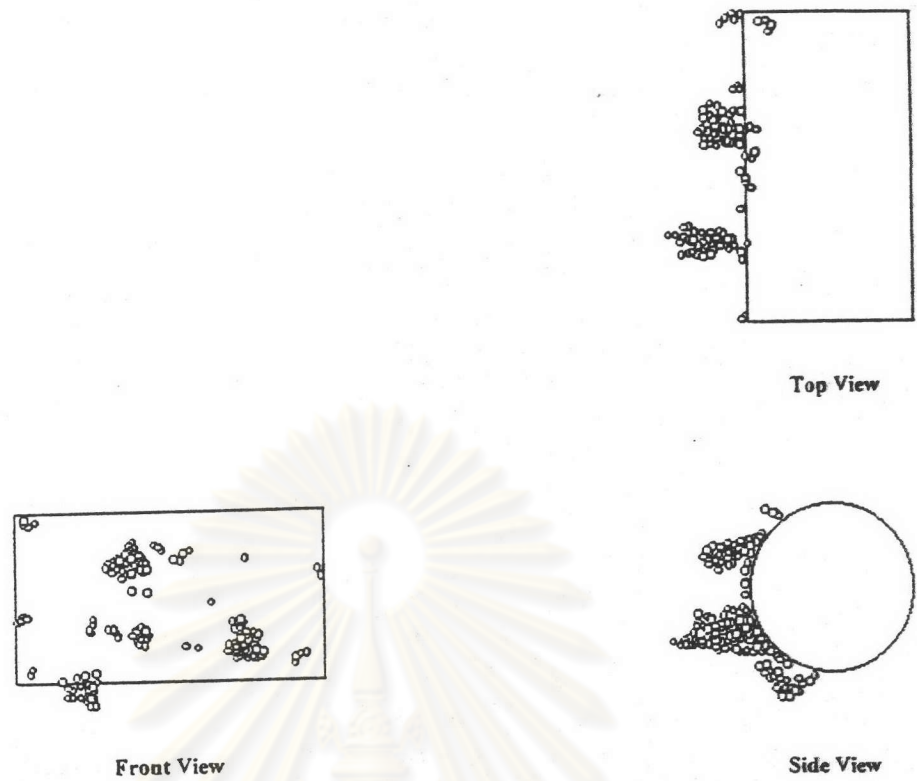


Figure 5.32. Typical configurations of dendrites for  $R=0.05$  and  $St=0.0$



Figure 5.33. Typical configurations of dendrites for  $R=0.05$  and  $St=0.6$

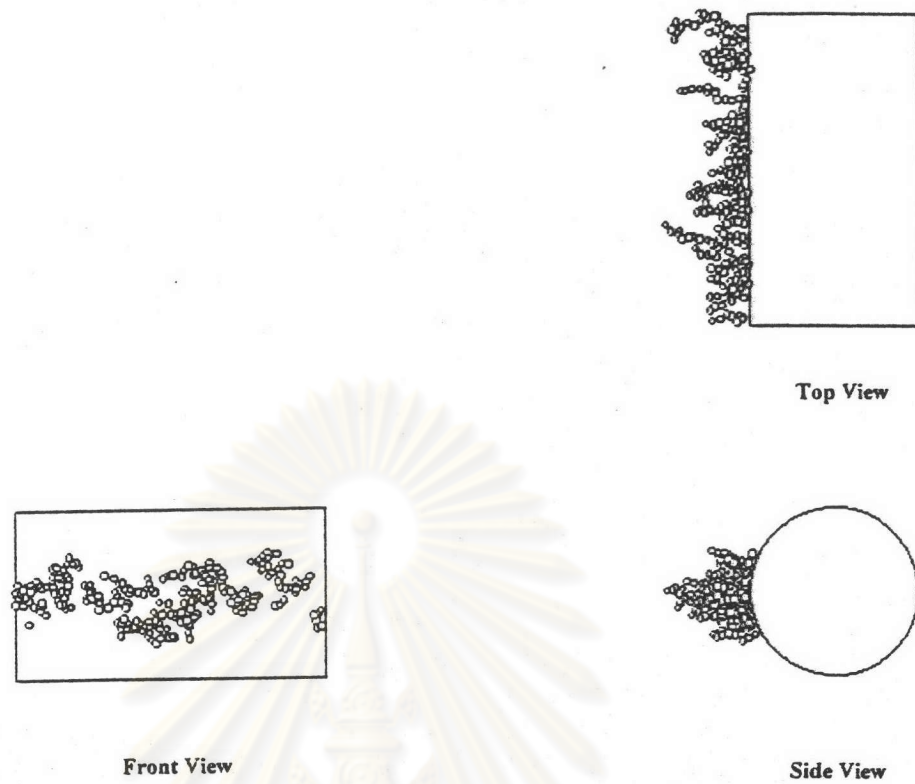


Figure 5.34. Typical configurations of dendrites for  $R=0.05$  and  $St=1.0$

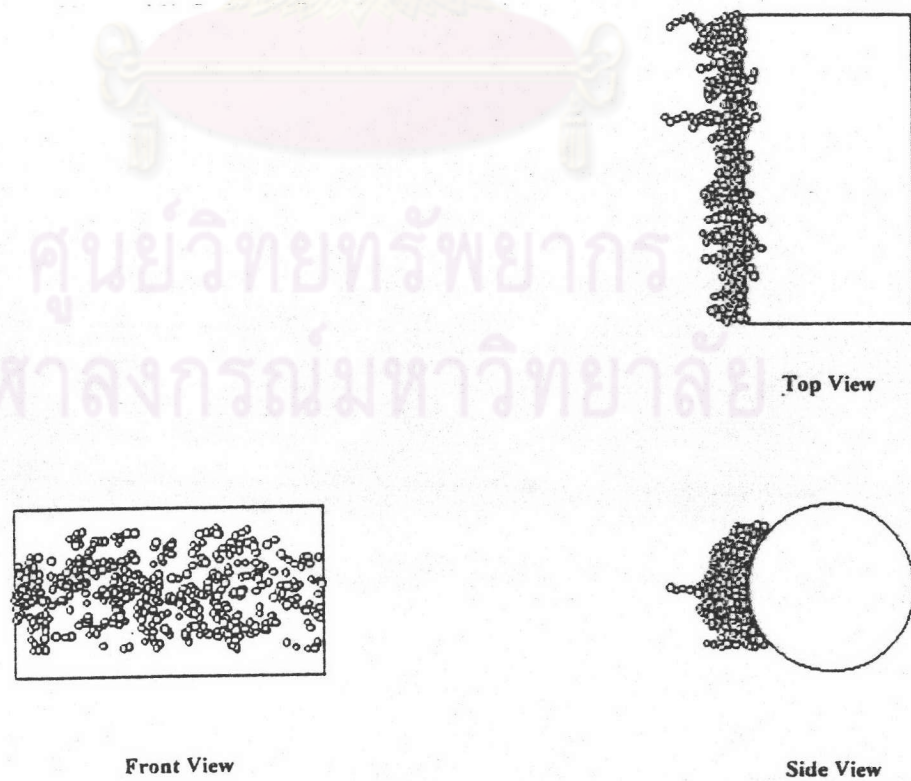


Figure 5.35. Typical configurations of dendrites for  $R=0.05$  and  $St=1.4$

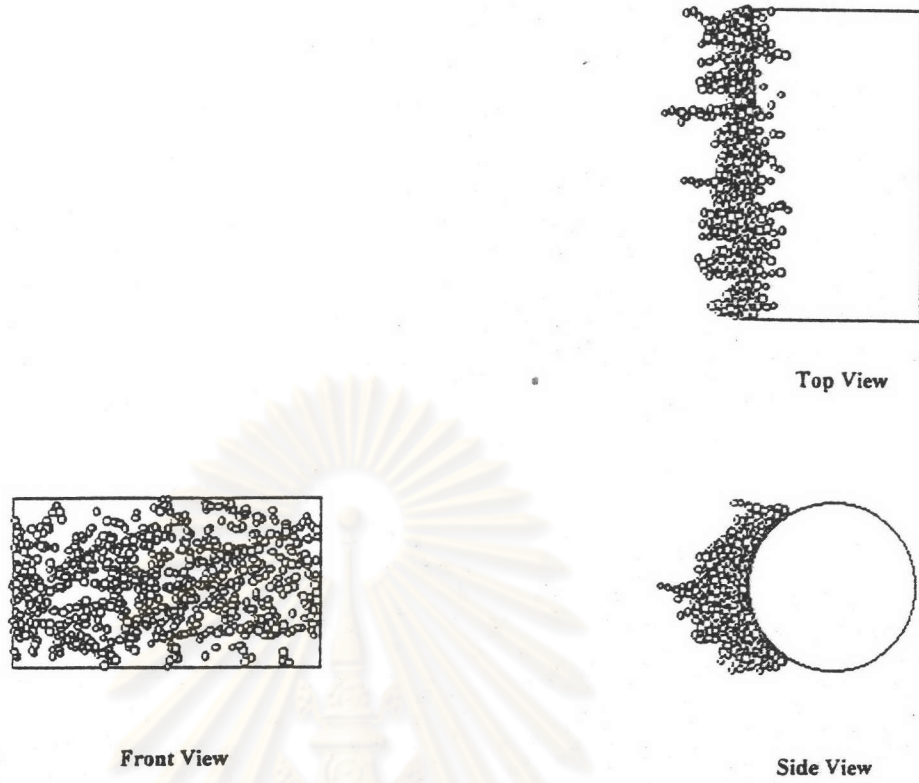


Figure 5.36. Typical configurations of dendrites for  $R=0.05$  and  $St=2.0$

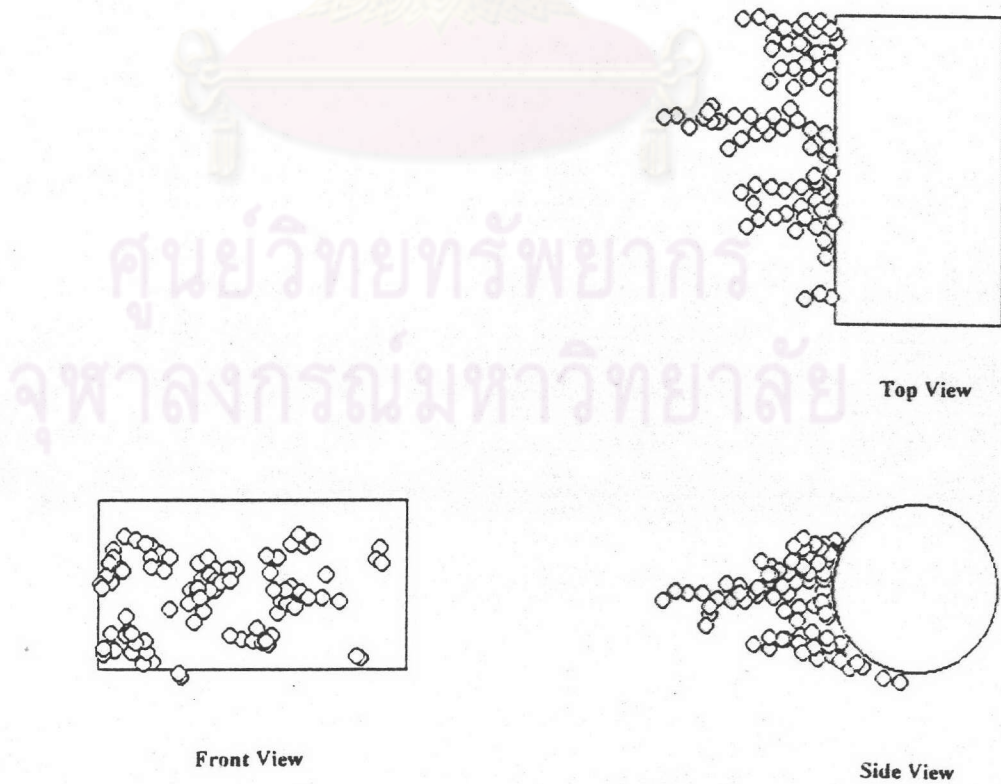


Figure 5.37. Typical configurations of dendrites for  $R=0.1$  and  $St=0.0$



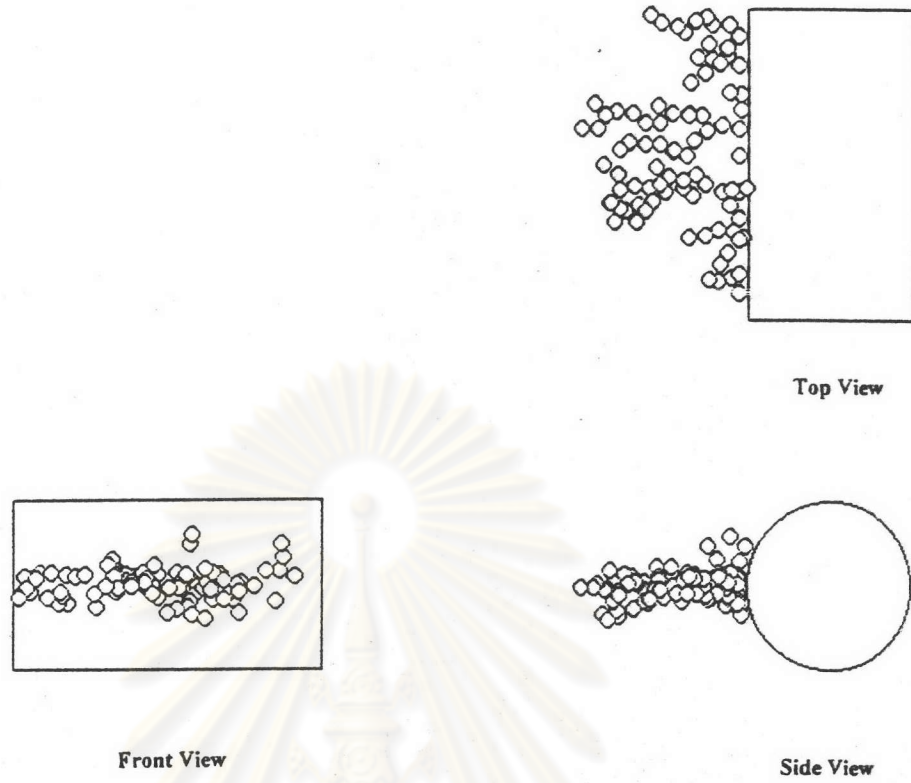


Figure 5.38. Typical configurations of dendrites for  $R=0.1$  and  $St=0.6$

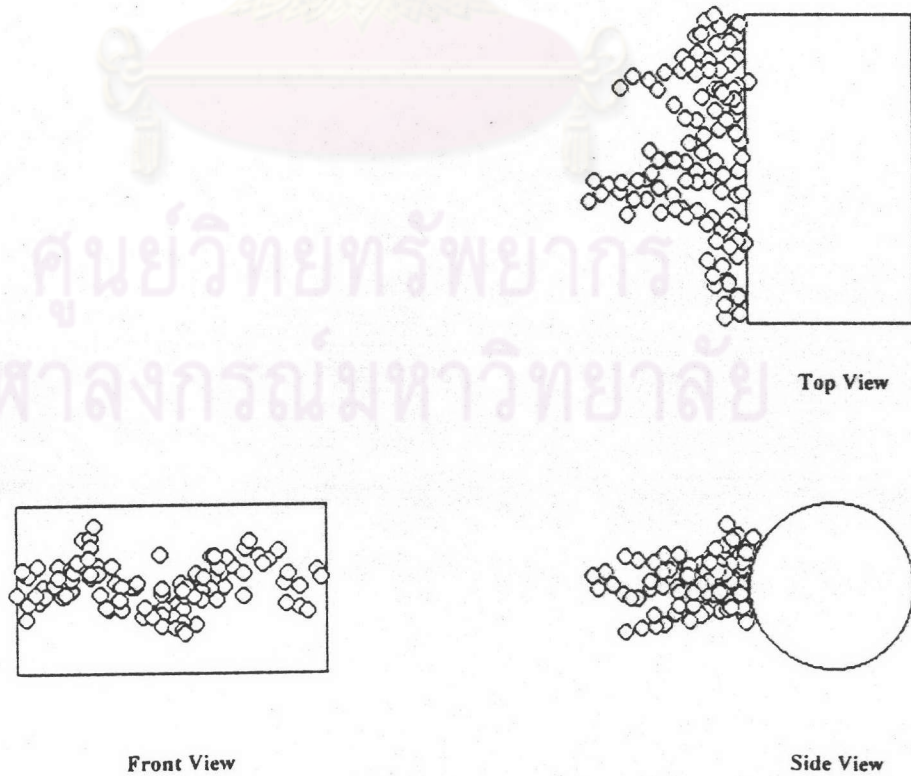


Figure 5.39. Typical configurations of dendrites for  $R=0.1$  and  $St=1.0$

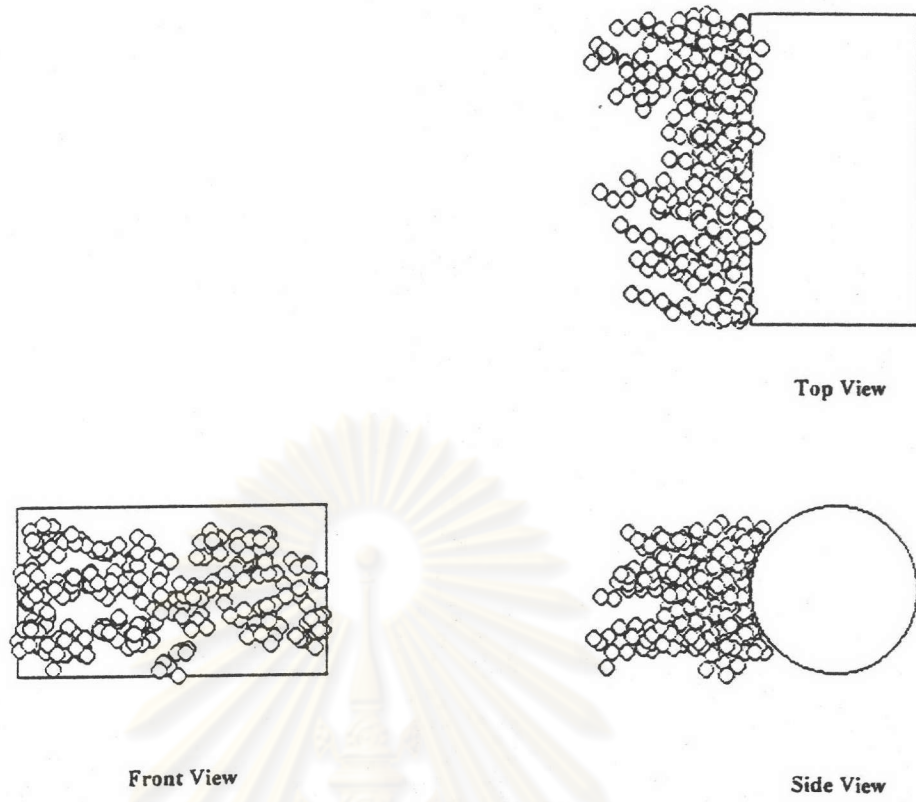


Figure 5.40. Typical configurations of dendrites for  $R=0.1$  and  $St=1.4$

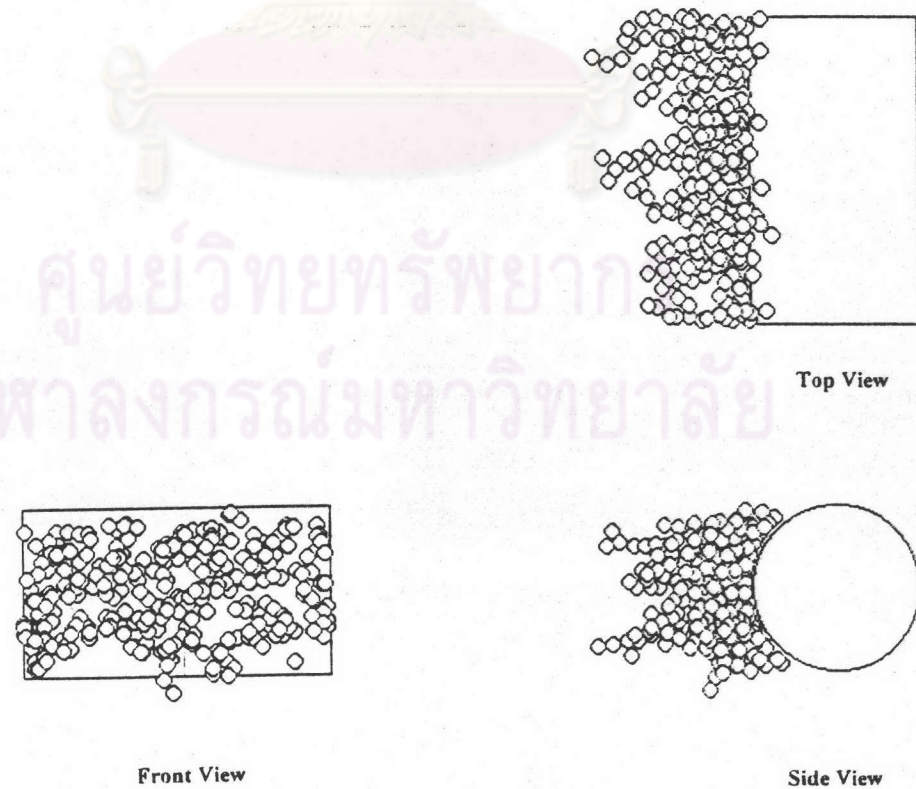


Figure 5.41. Typical configurations of dendrites for  $R=0.1$  and  $St=2.0$

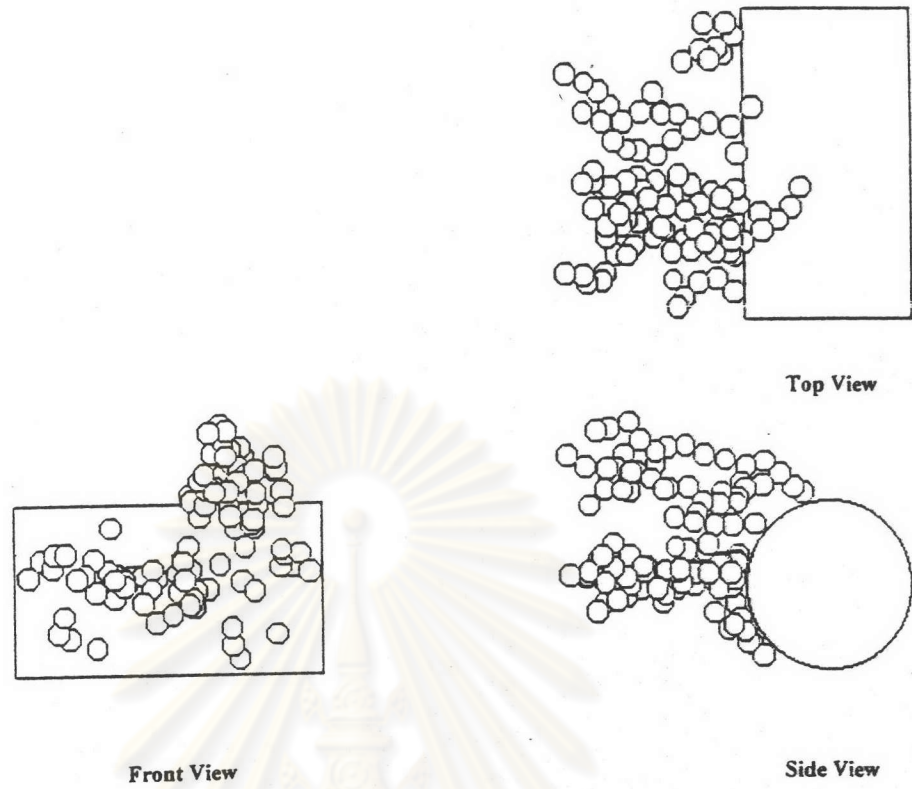


Figure 5.42. Typical configurations of dendrites for  $R=0.13$  and  $St=0.0$

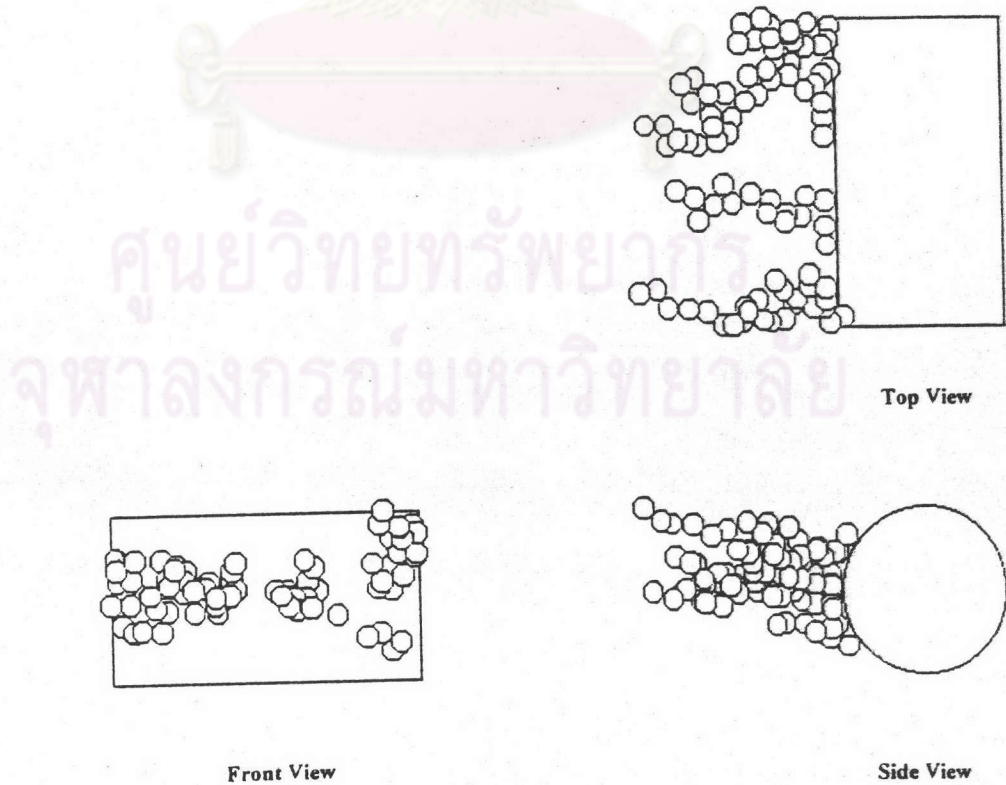


Figure 5.43. Typical configurations of dendrites for  $R=0.13$  and  $St=0.6$



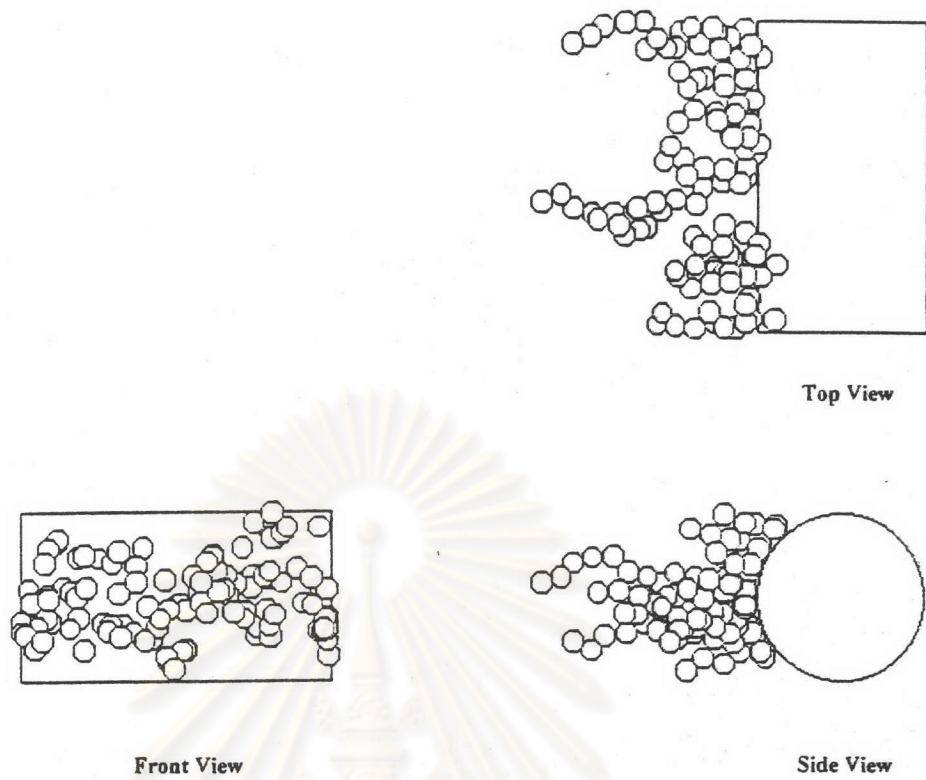


Figure 5.44. Typical configurations of dendrites for  $R=0.13$  and  $St=1.0$

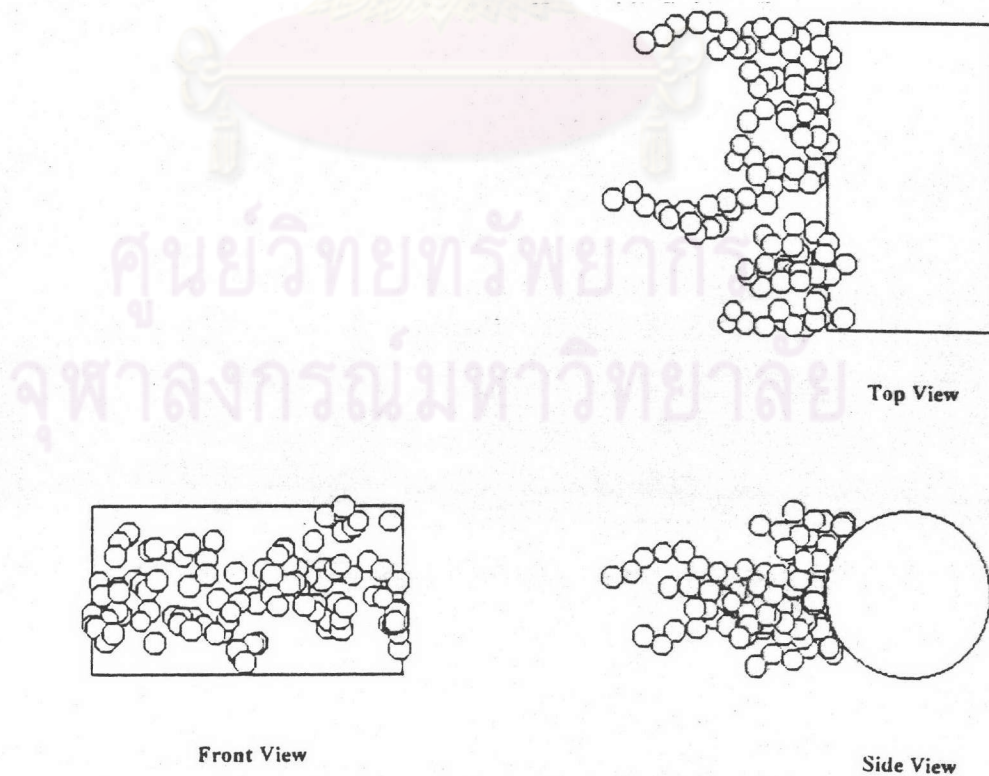


Figure 5.45. Typical configurations of dendrites for  $R=0.13$  and  $St=1.4$

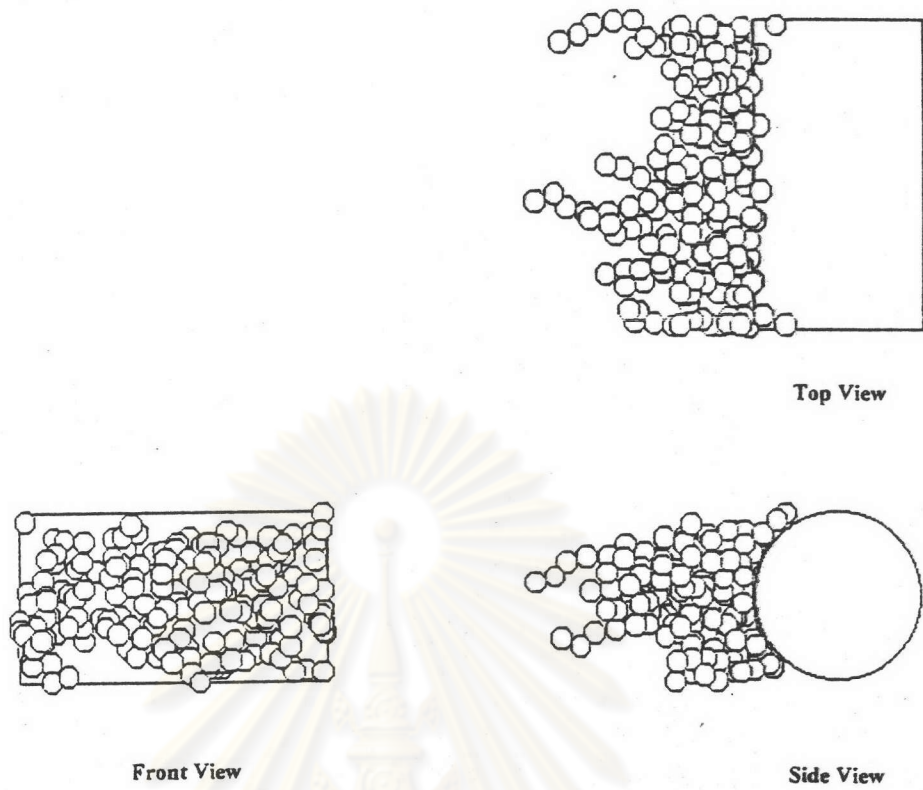


Figure 5.46. Typical configurations of dendrites for  $R=0.13$  and  $St=2.0$

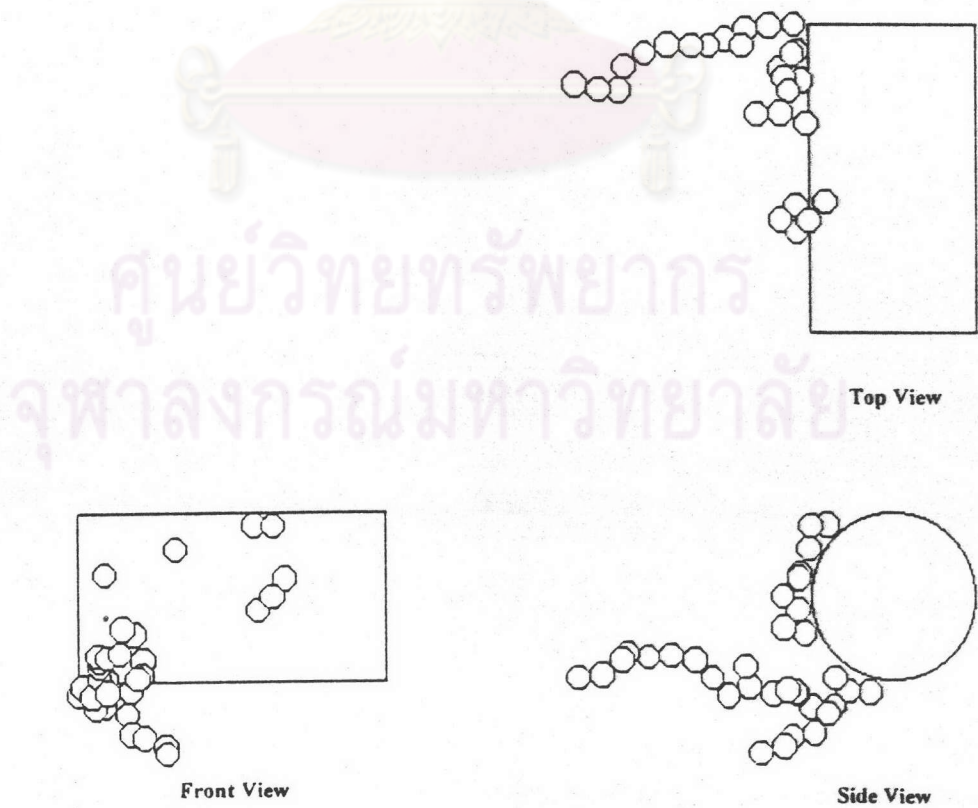


Figure 5.47. Typical configurations of dendrites for  $R=0.15$  and  $St=0.0$

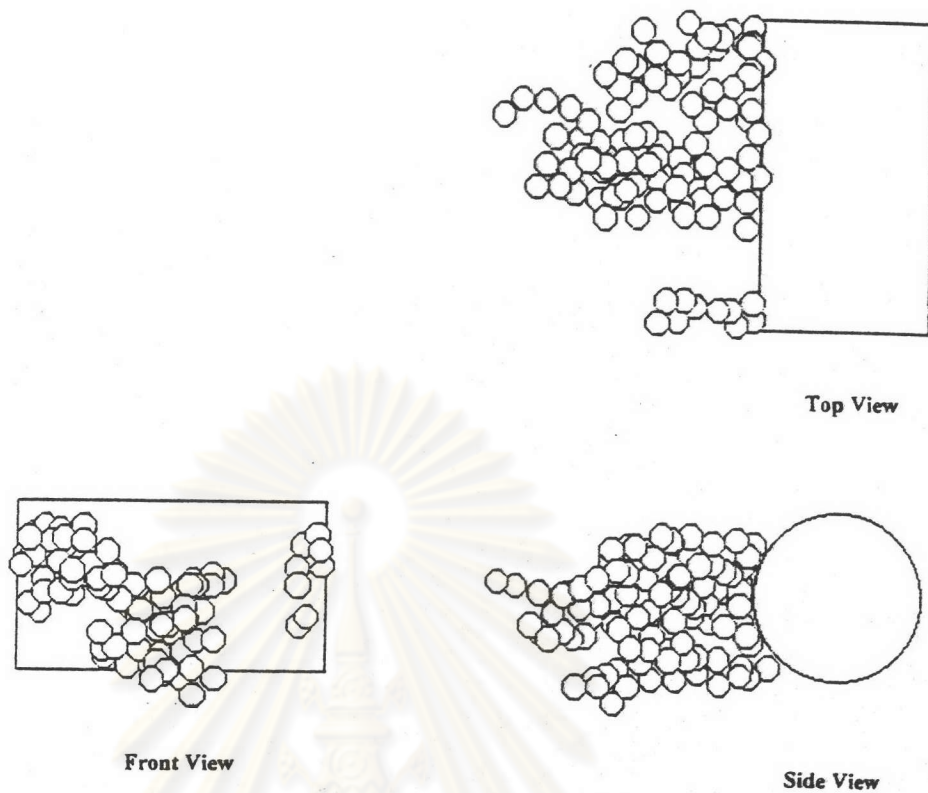


Figure 5.48. Typical configurations of dendrites for  $R=0.15$  and  $St=0.6$

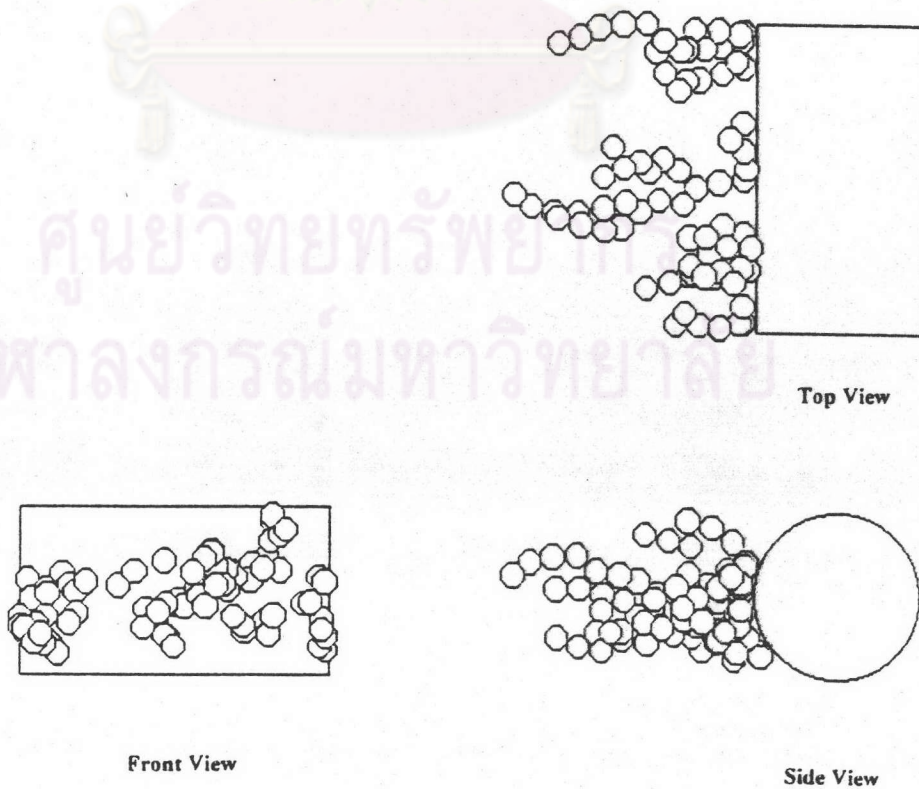


Figure 5.49. Typical configurations of dendrites for  $R=0.15$  and  $St=1.0$



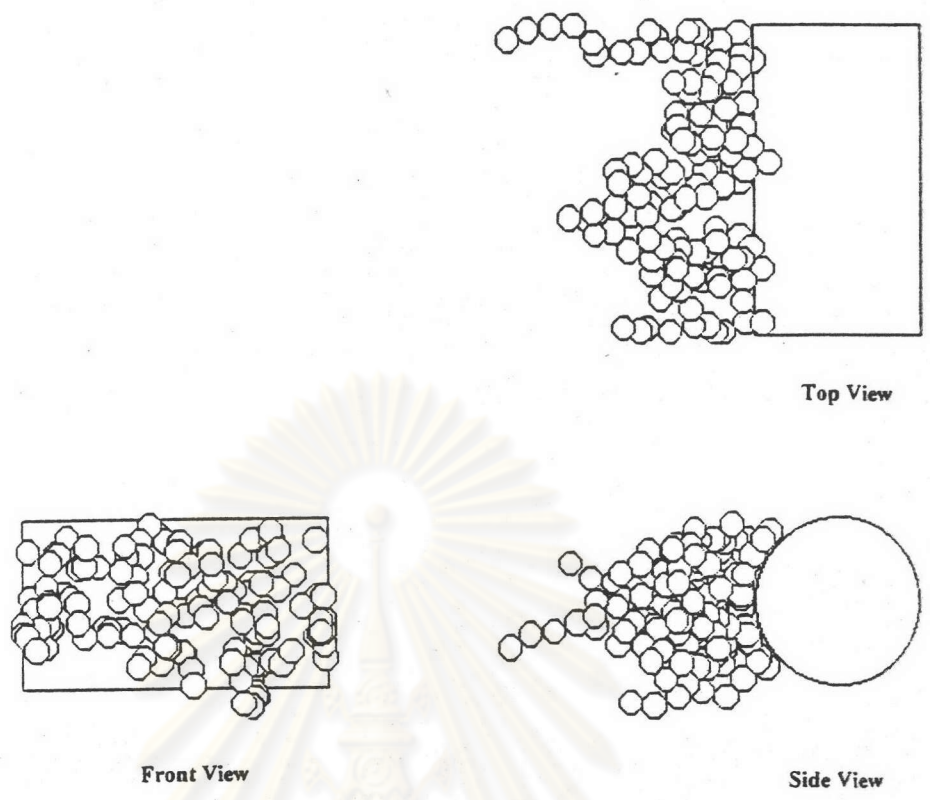


Figure 5.50. Typical configurations of dendrites for  $R=0.15$  and  $St=1.4$

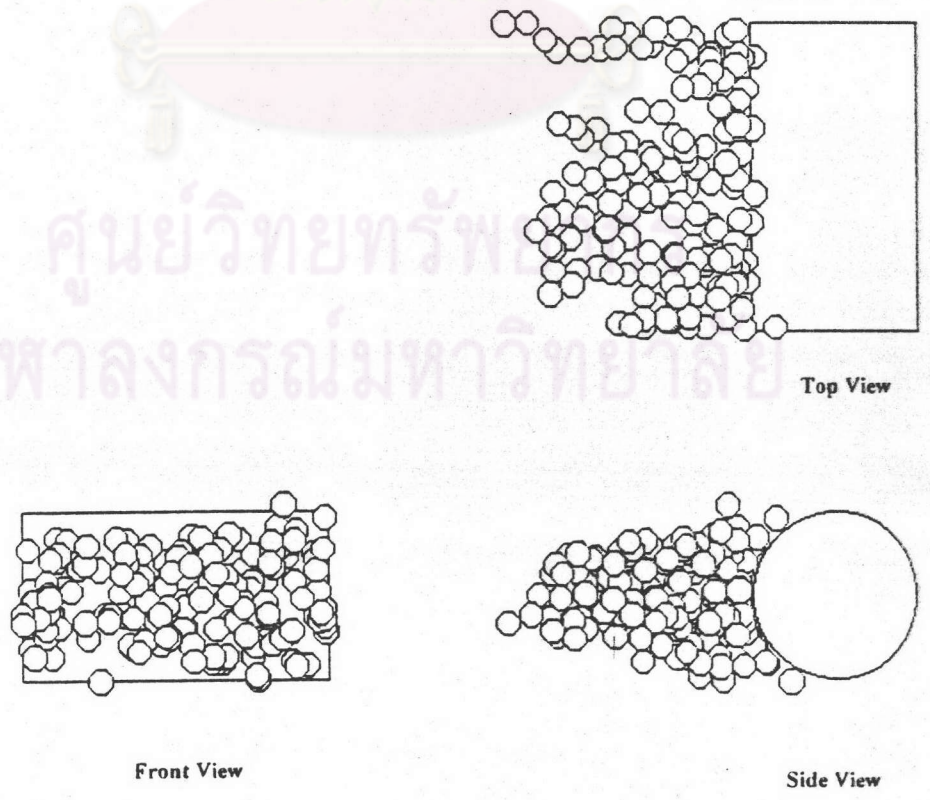


Figure 5.51. Typical configurations of dendrites for  $R=0.15$  and  $St=2.0$

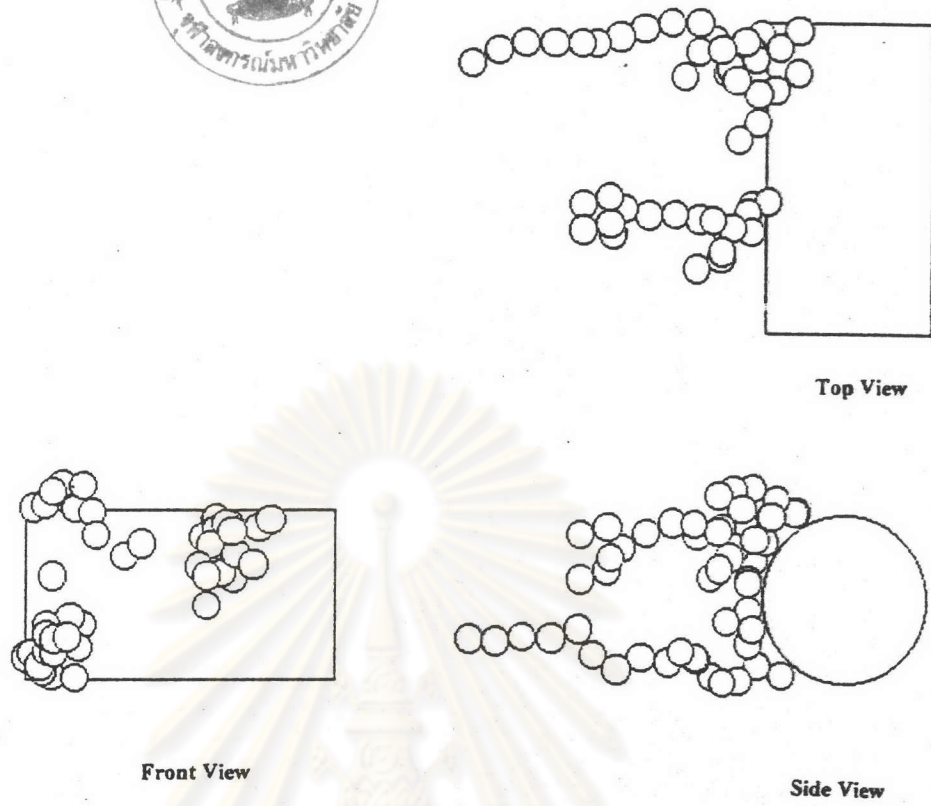


Figure 5.52. Typical configurations of dendrites for  $R=0.17$  and  $St=0.0$

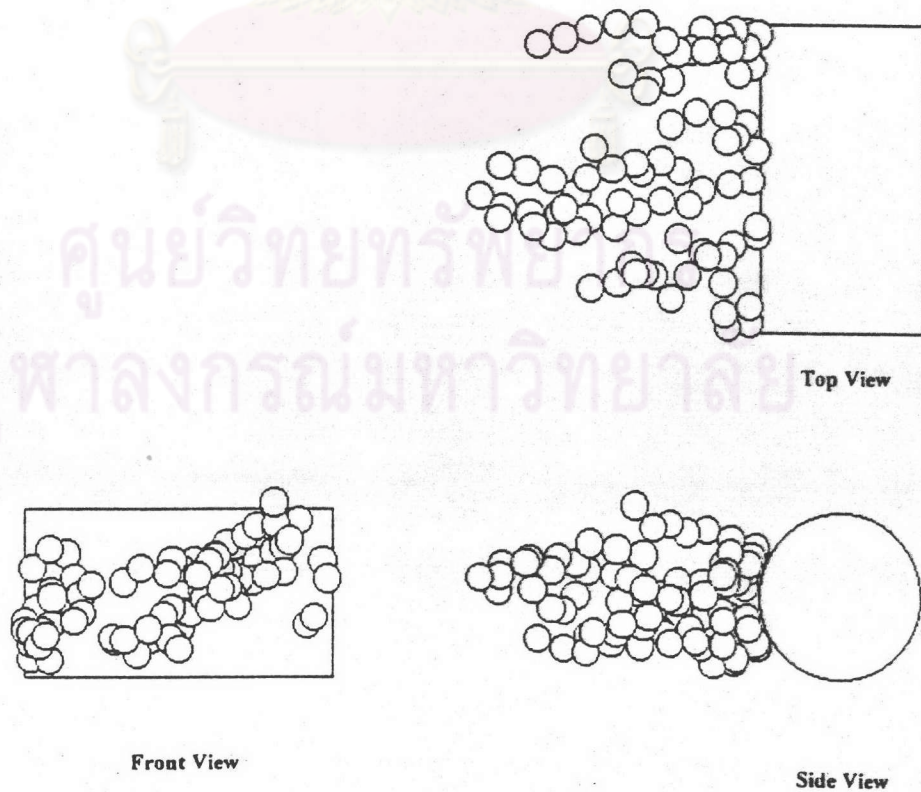


Figure 5.53. Typical configurations of dendrites for  $R=0.17$  and  $St=0.6$

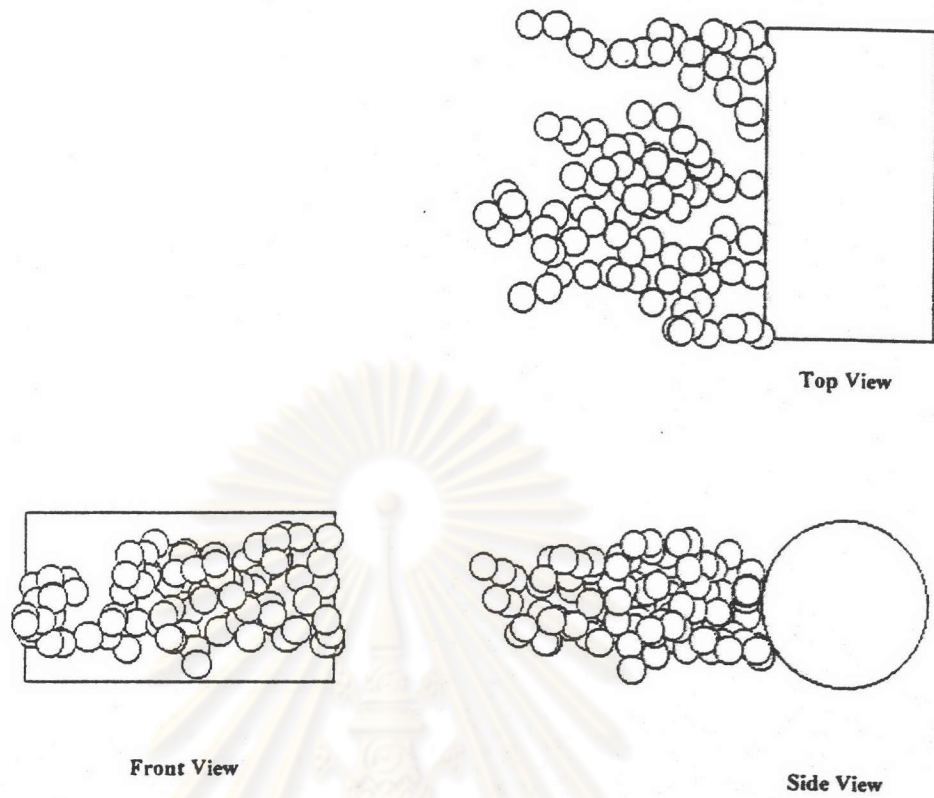


Figure 5.54. Typical configurations of dendrites for  $R=0.17$  and  $St=1.0$

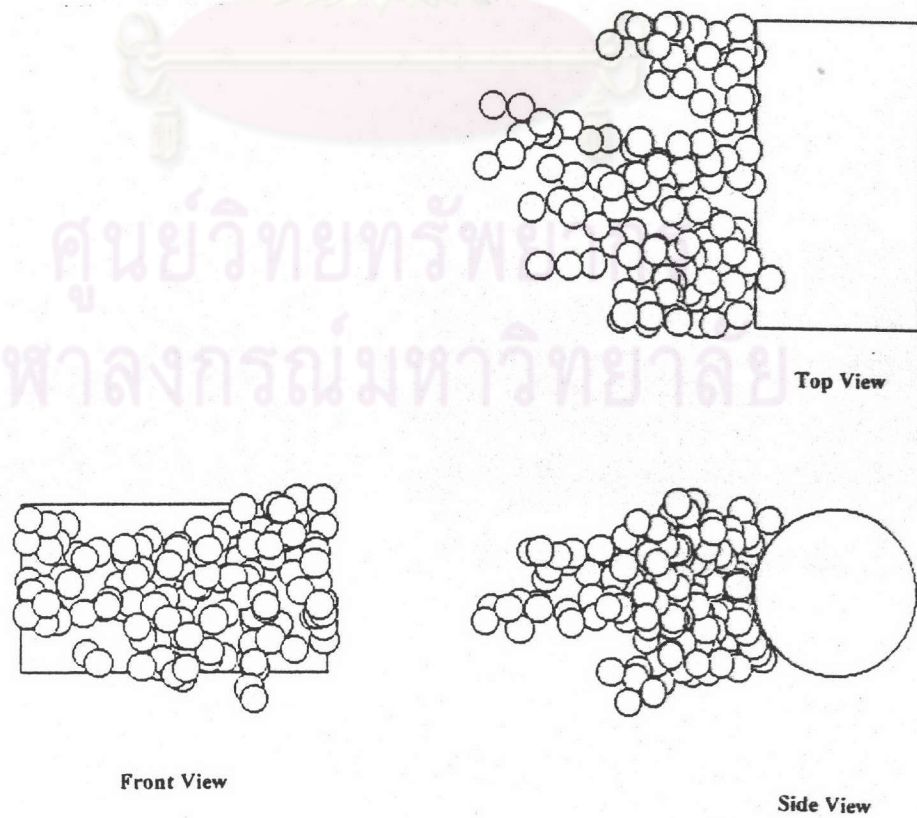


Figure 5.55. Typical configurations of dendrites for  $R=0.17$  and  $St=1.4$



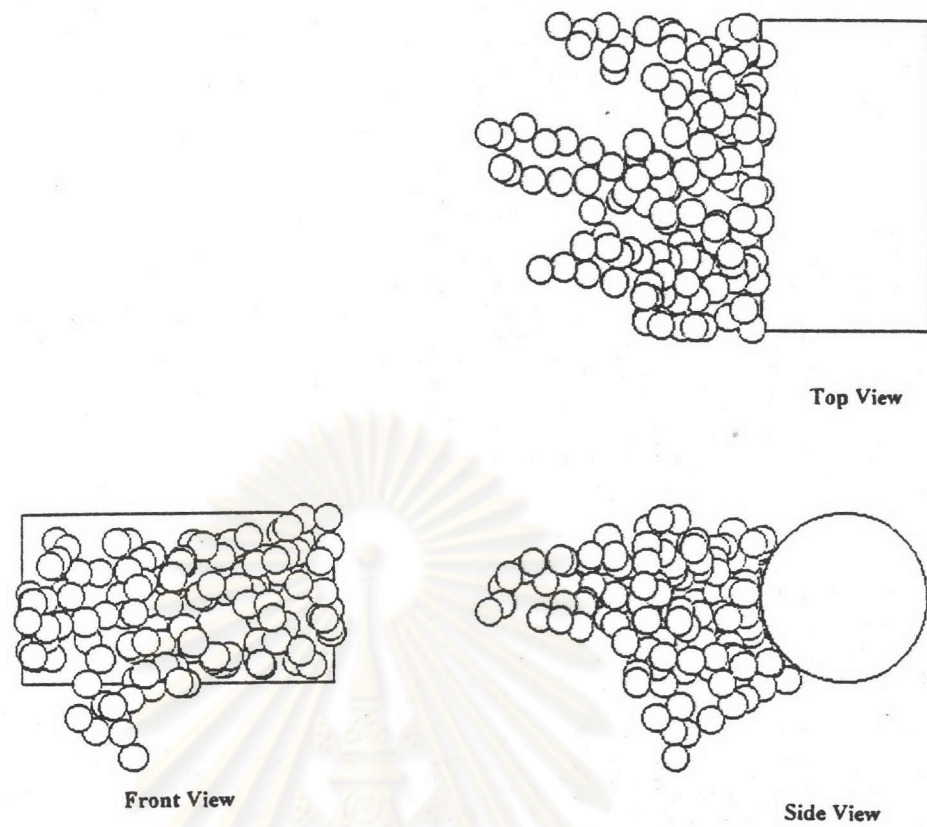


Figure 5.56. Typical configurations of dendrites for  $R=0.17$  and  $St=2.0$

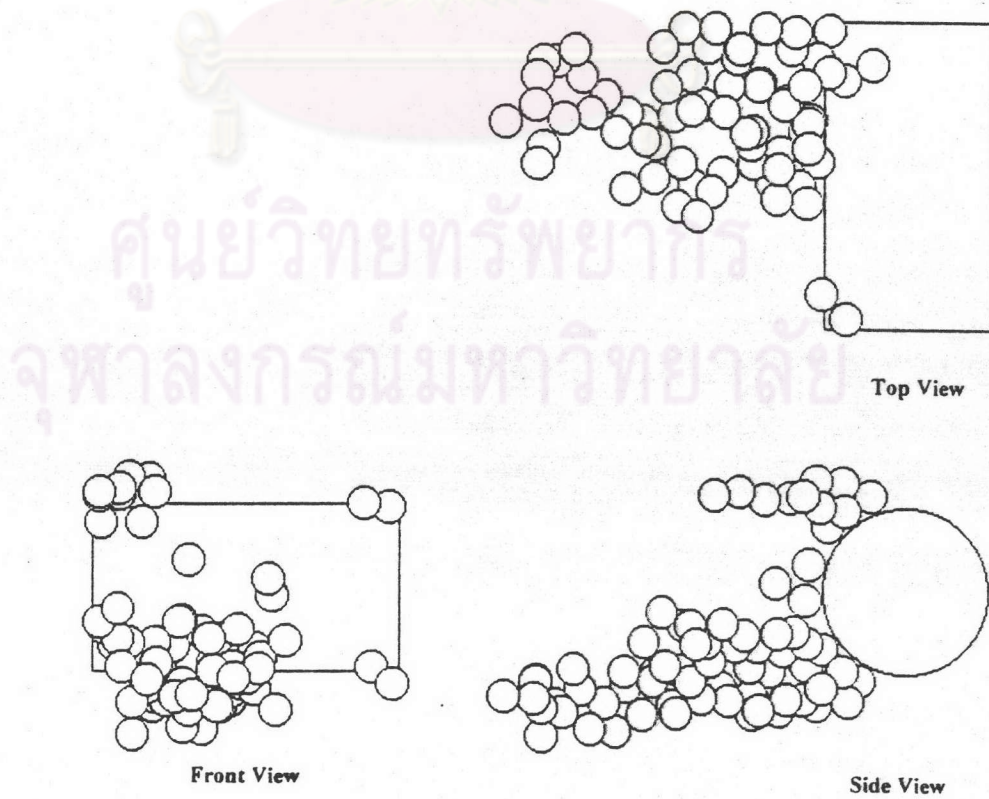


Figure 5.57. Typical configurations of dendrites for  $R=0.2$  and  $St=0.0$

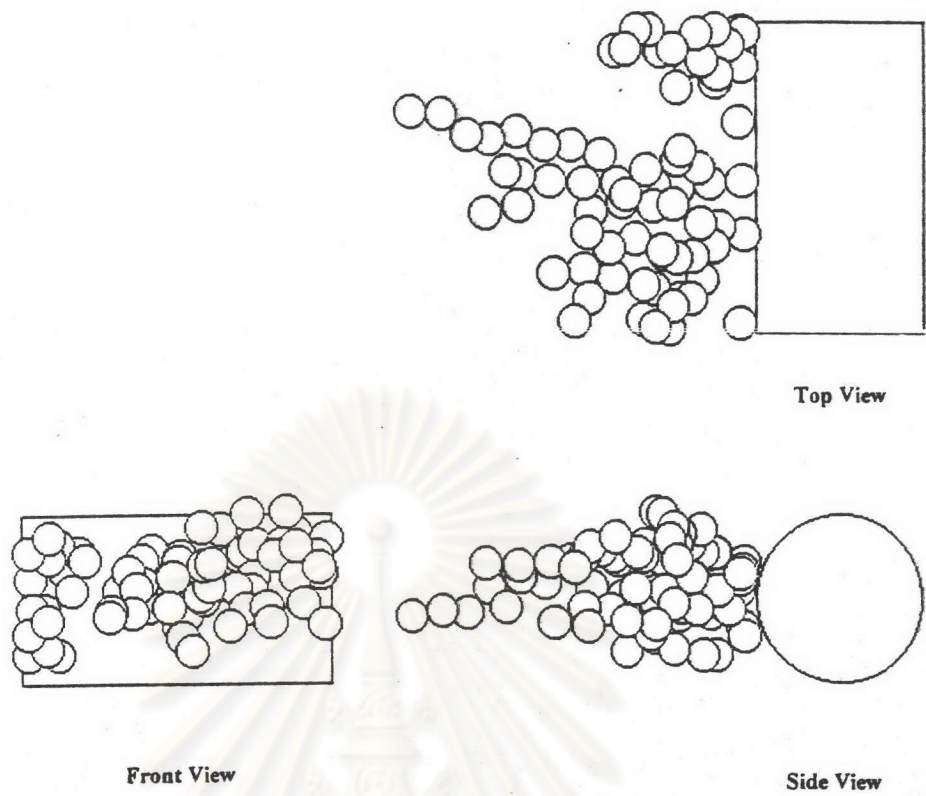


Figure 5.58. Typical configurations of dendrites for  $R=0.2$  and  $St=0.6$

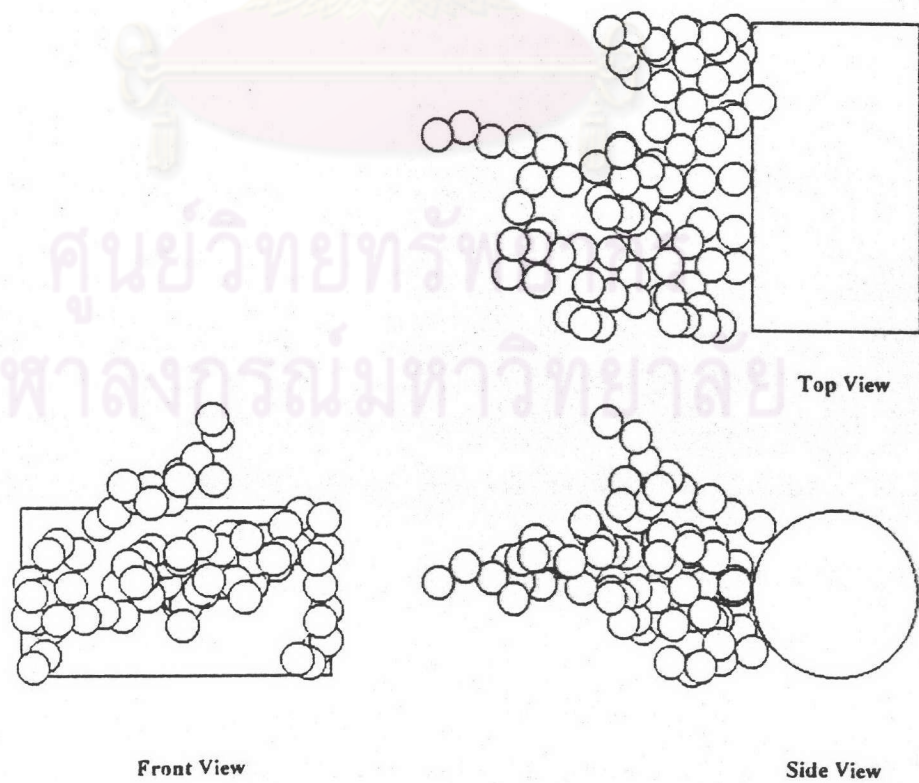


Figure 5.59. Typical configurations of dendrites for  $R=0.2$  and  $St=1.0$

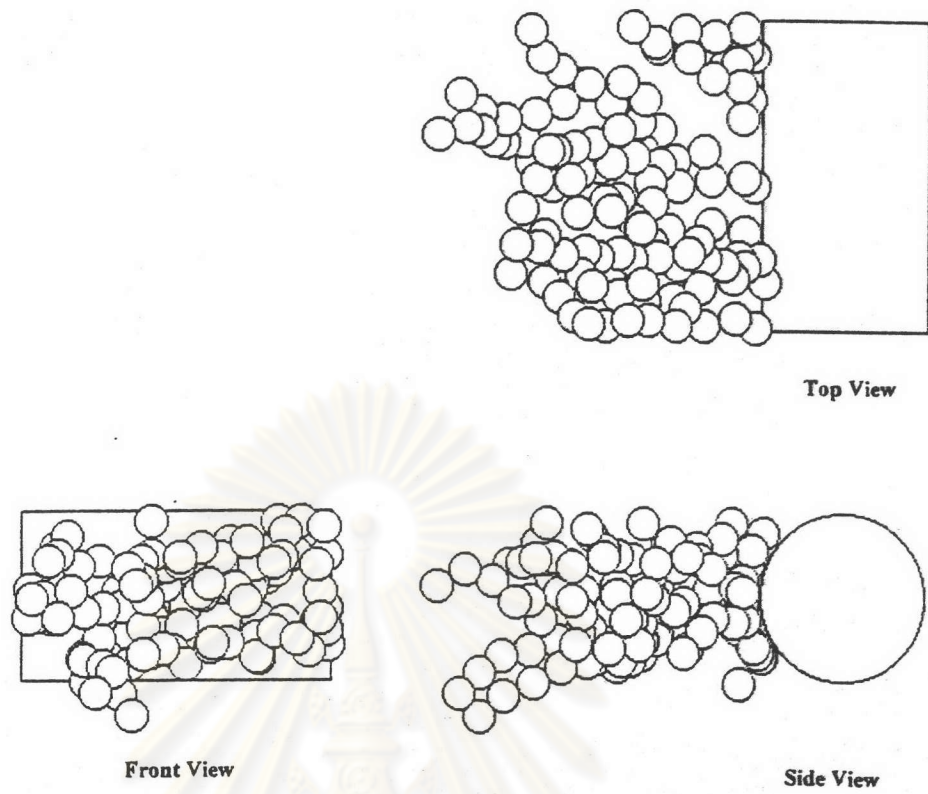


Figure 5.60. Typical configurations of dendrites for  $R=0.2$  and  $St=1.4$

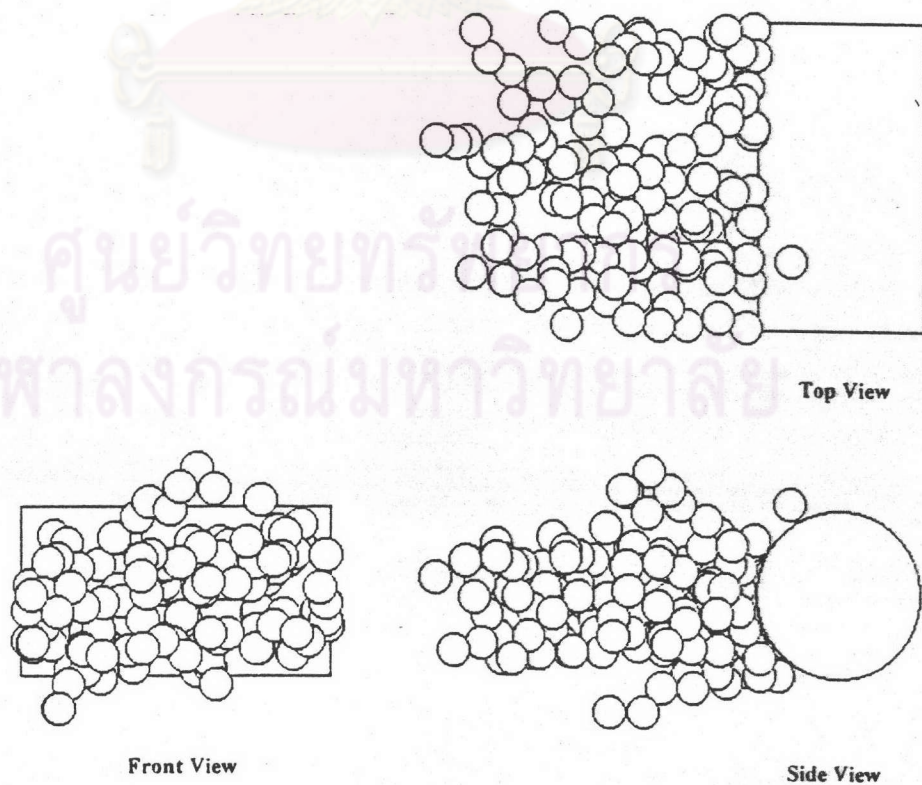


Figure 5.61. Typical configurations of dendrites for  $R=0.2$  and  $St=2.0$



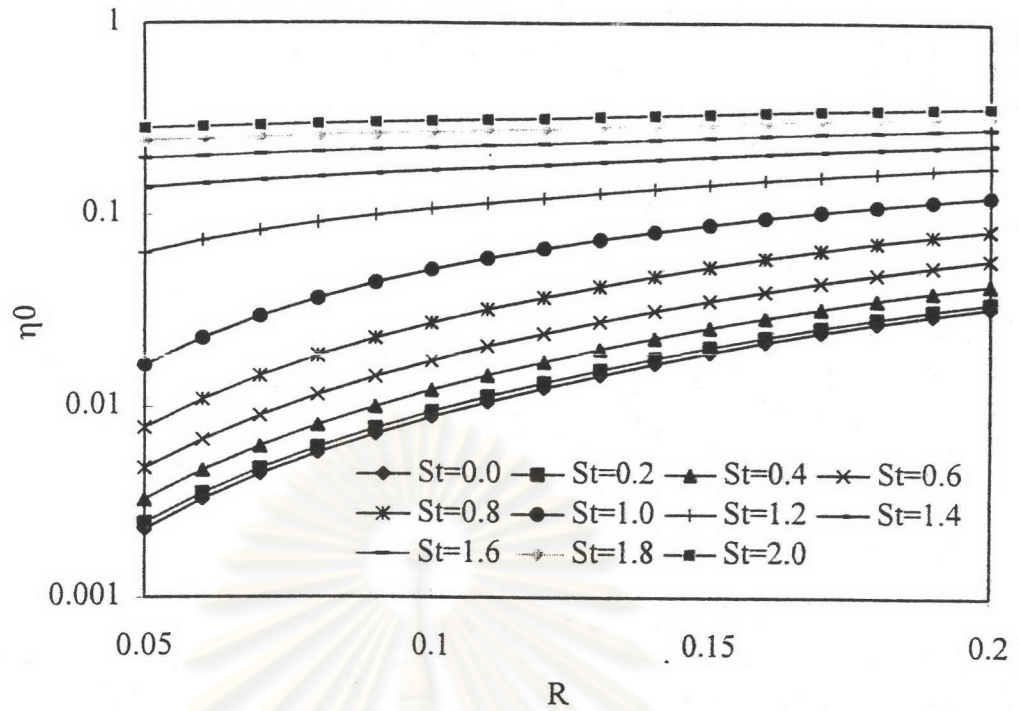


Figure 5.62. Relationship between  $\eta_0$  and  $R$  with  $St$  as parameter (Limiting trajectory theory)

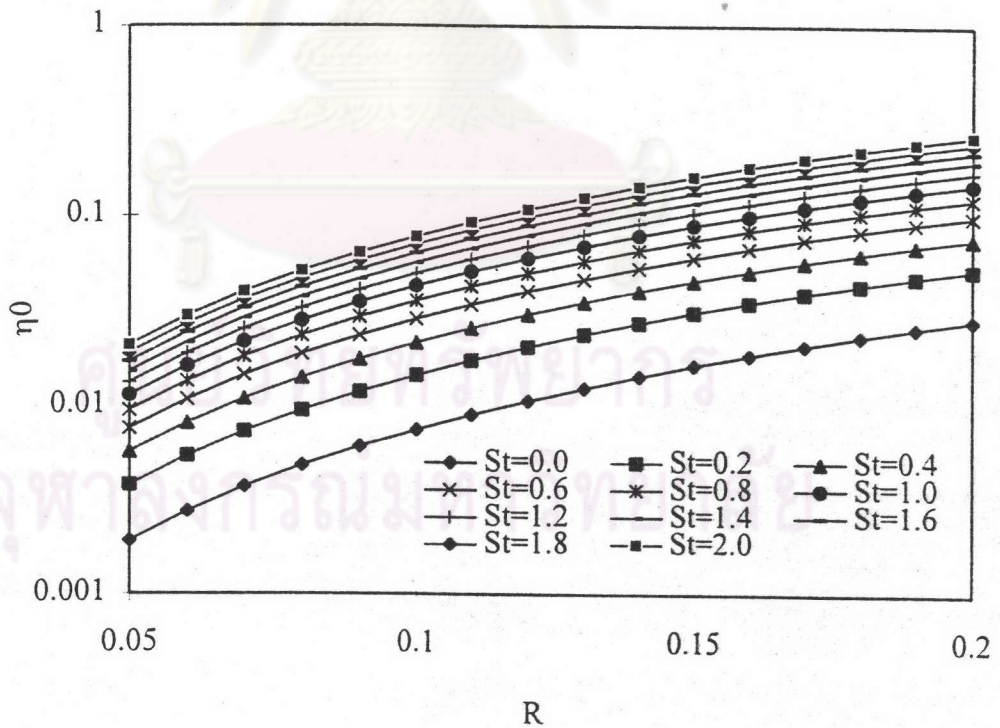


Figure 5.63. Relationship between  $\eta_0$  and  $R$  with  $St$  as parameter (Stechkina's equation)

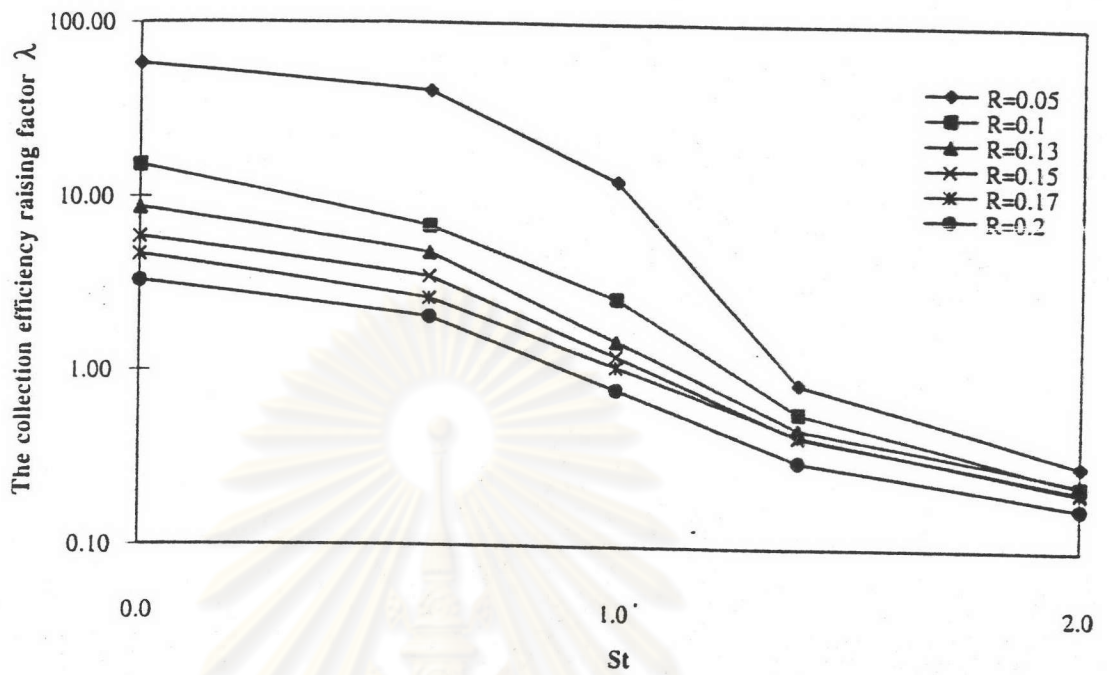


Figure 5.64. Relationship between  $\lambda$  and  $St$  with  $R$  as parameter (Stochastic simulation)

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Table 5.3 Collection efficiency raising factor  $\lambda$  for inertial impaction

St	R					
	0.05	0.1	0.13	0.15	0.17	0.2
0	56.1*	14.8*				3.09*
	57.770	15.180	8.673	5.883	4.664	3.307
0.6	45.7*					1.82*
	40.440	6.841	4.811	3.501	2.628	2.049
1	16.4*	2.89*				0.783*
	12.530	2.660	1.514	1.234	1.072	0.794
1.4	0.874*					
	0.867	0.594	0.482	0.433	0.441	0.313
2	0.238*	0.253*				0.144*
	0.306	0.236	0.243	0.222	0.216	0.176

\* Kanaoka et al., 1980

Table 5.4 Difference of  $\lambda$  between another previous study (Kanaoka et al., 1980) and the present study for inertial impaction (%)

St	R		
	0.05	0.1	0.2
0	2.98	2.57	7.02
0.6	11.510	-	12.580
1	23.600	7.960	1.400
1.4	0.800	-	-
2	28.570	6.720	22.220



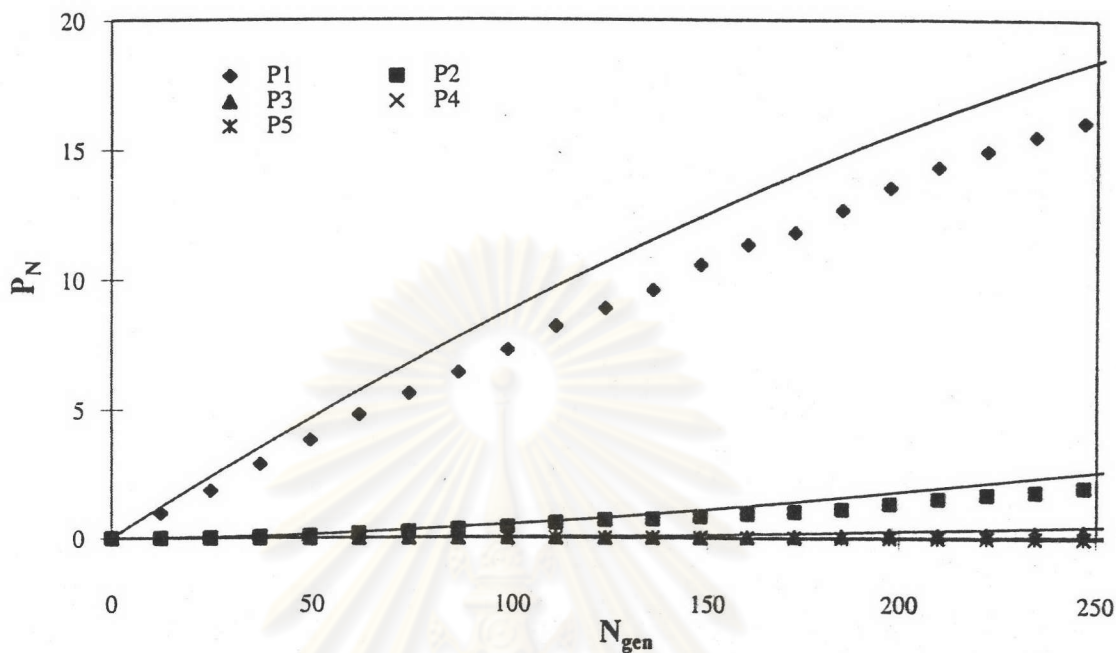


Figure 5.65. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $Pe=200$

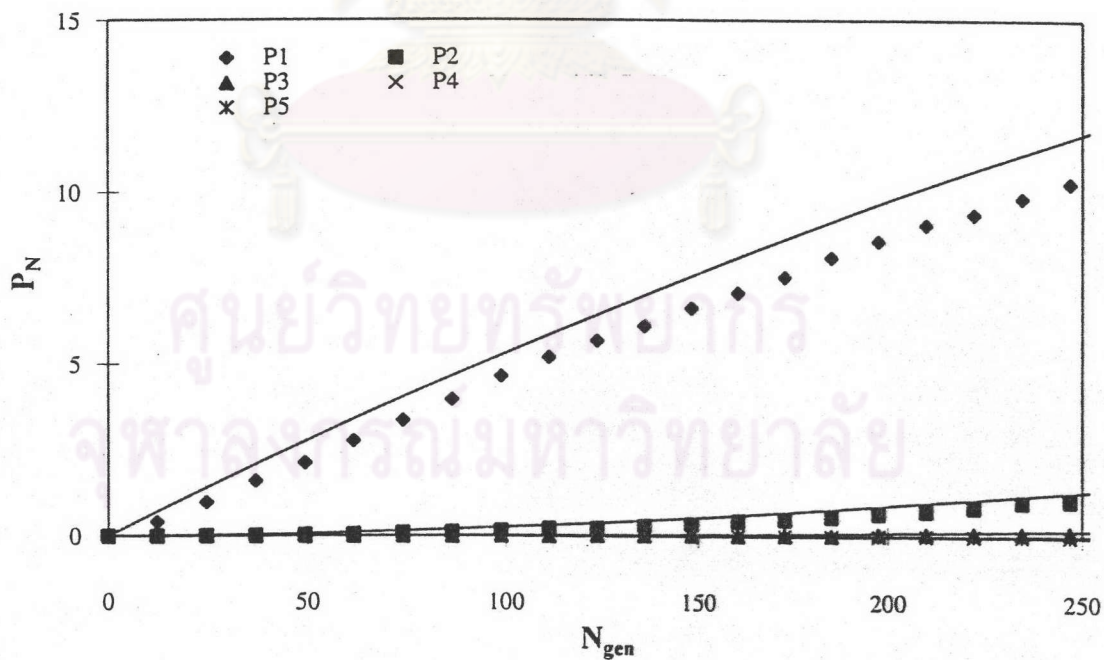


Figure 5.66. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $Pe=500$

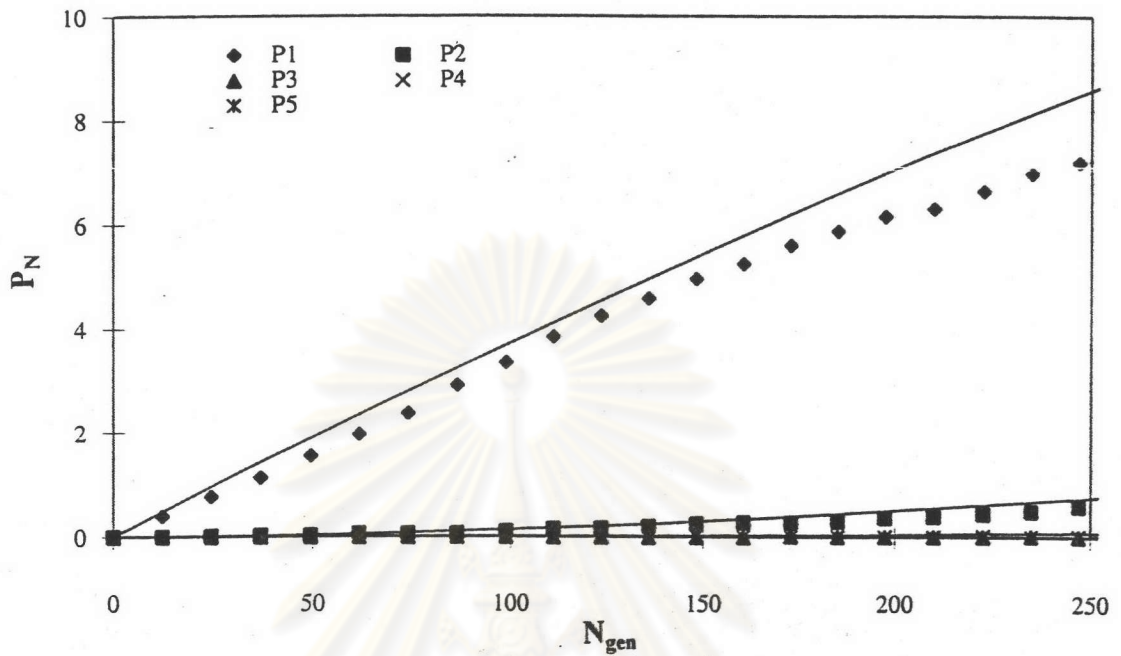


Figure 5.67. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $Pe=1000$

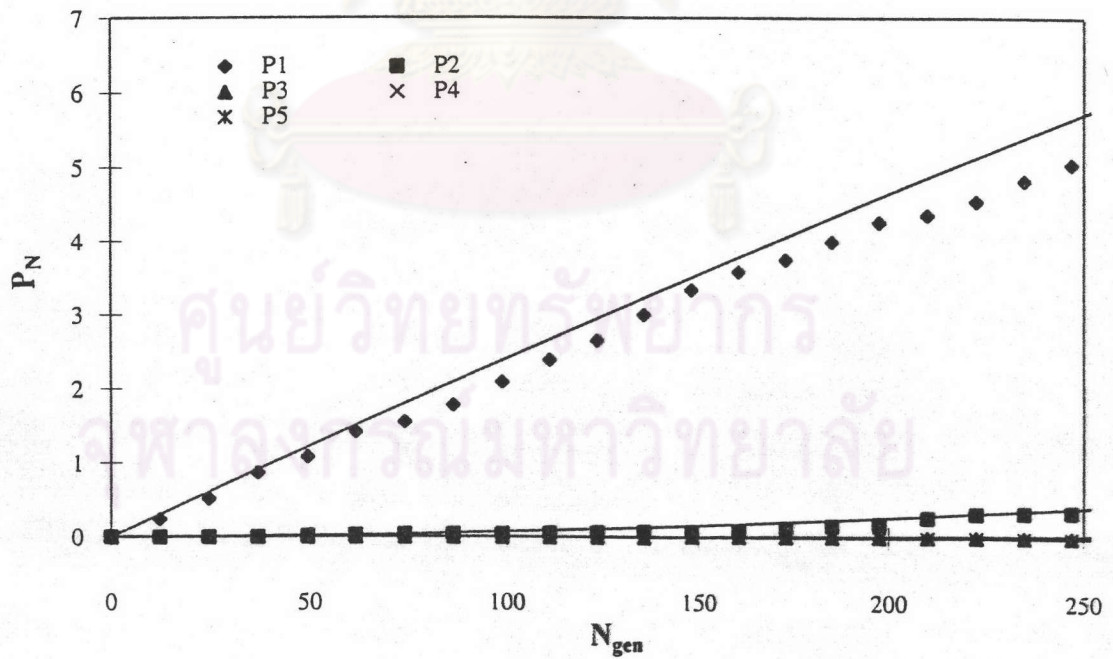


Figure 5.68. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $Pe=2500$

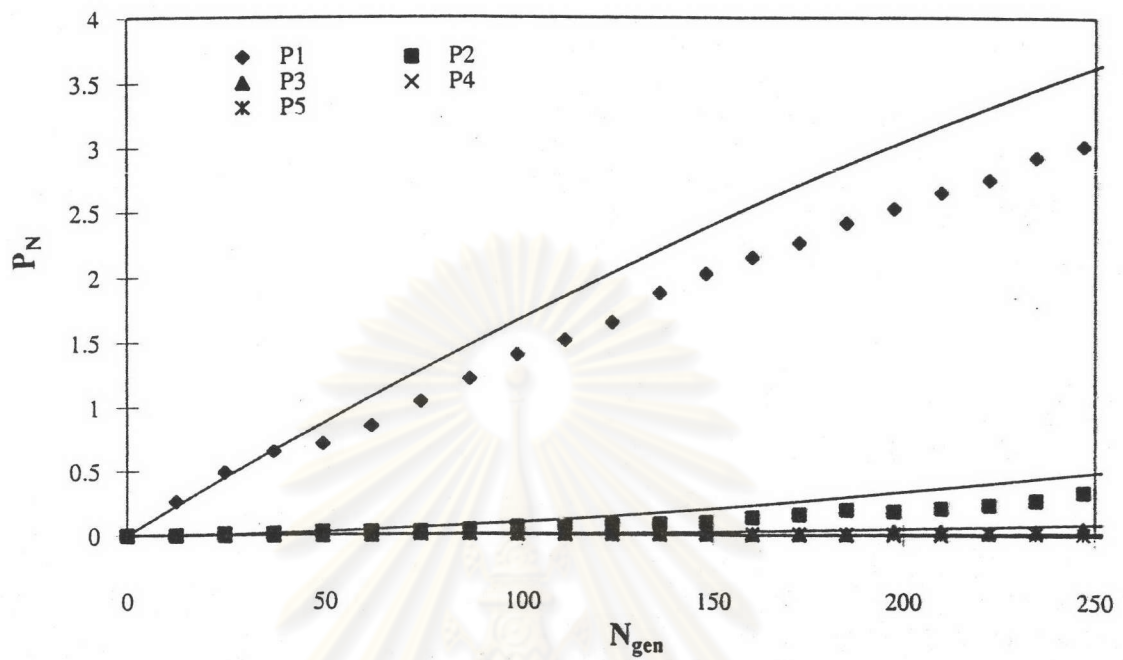


Figure 5.69. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $Pe=5000$

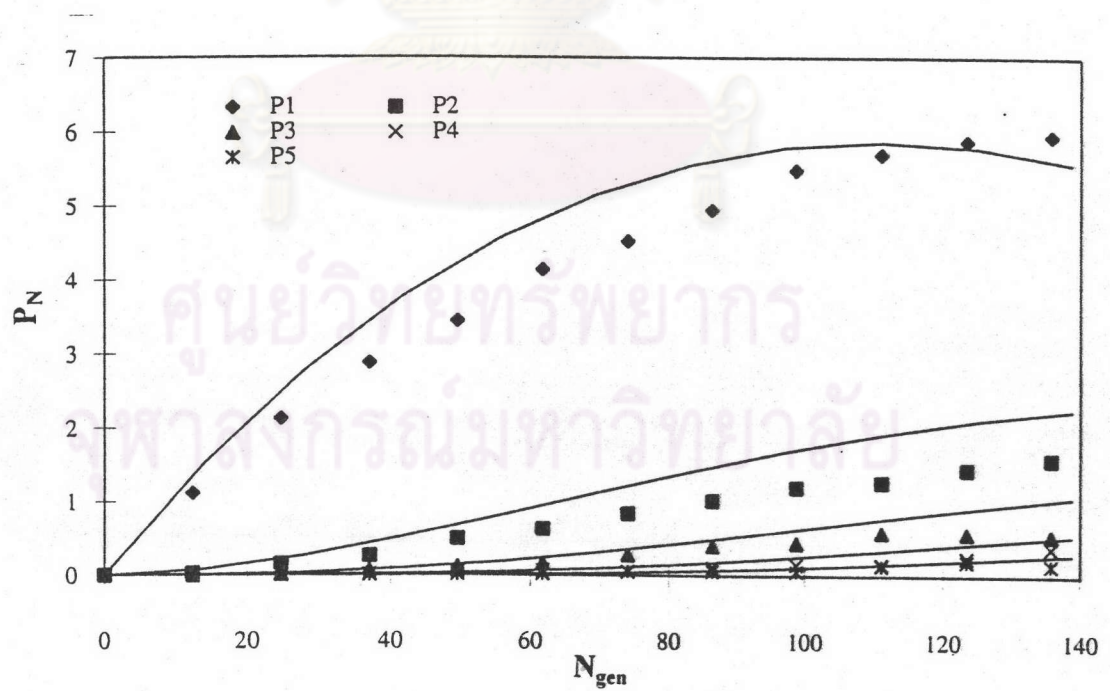


Figure 5.70. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $Pe=200$



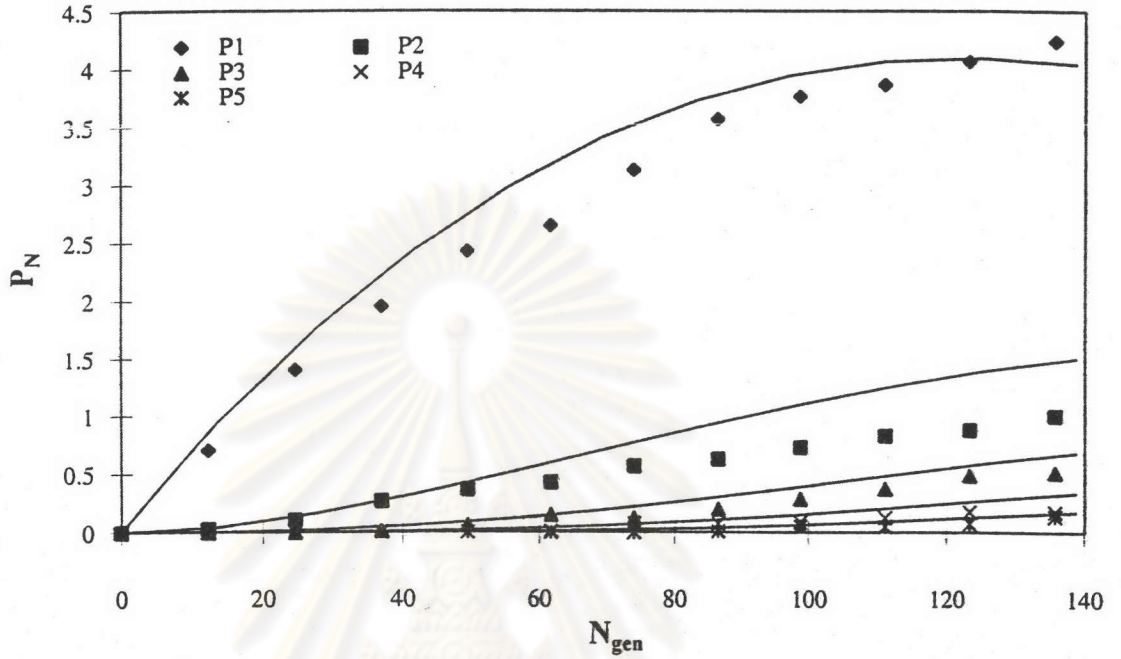


Figure 5.71. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $Pe=500$

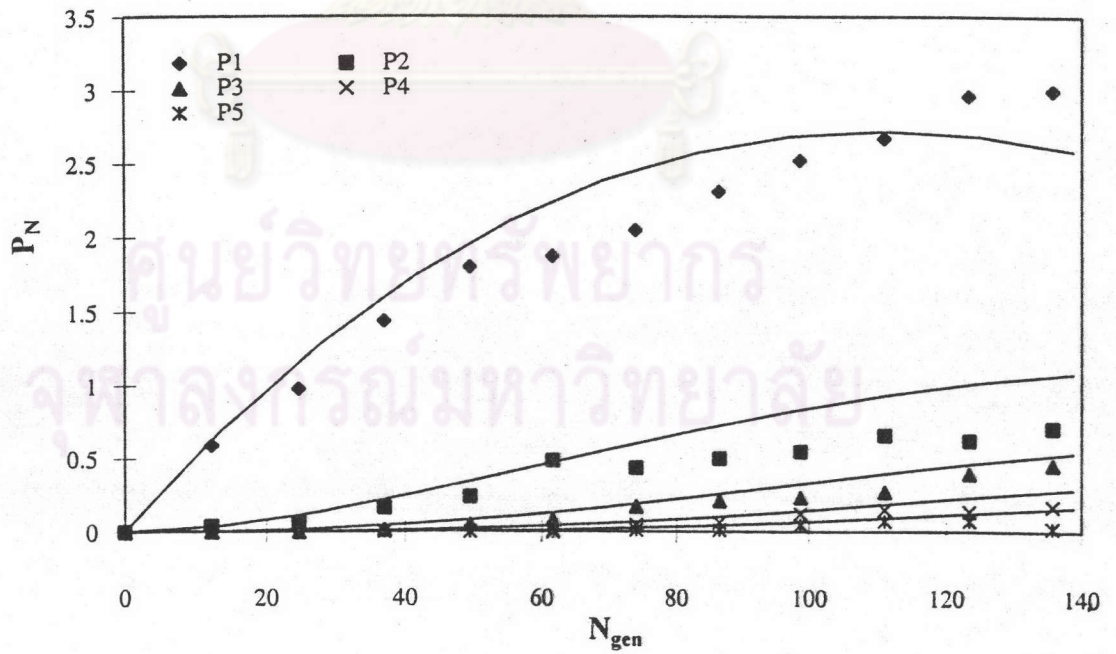


Figure 5.72. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $Pe=1000$

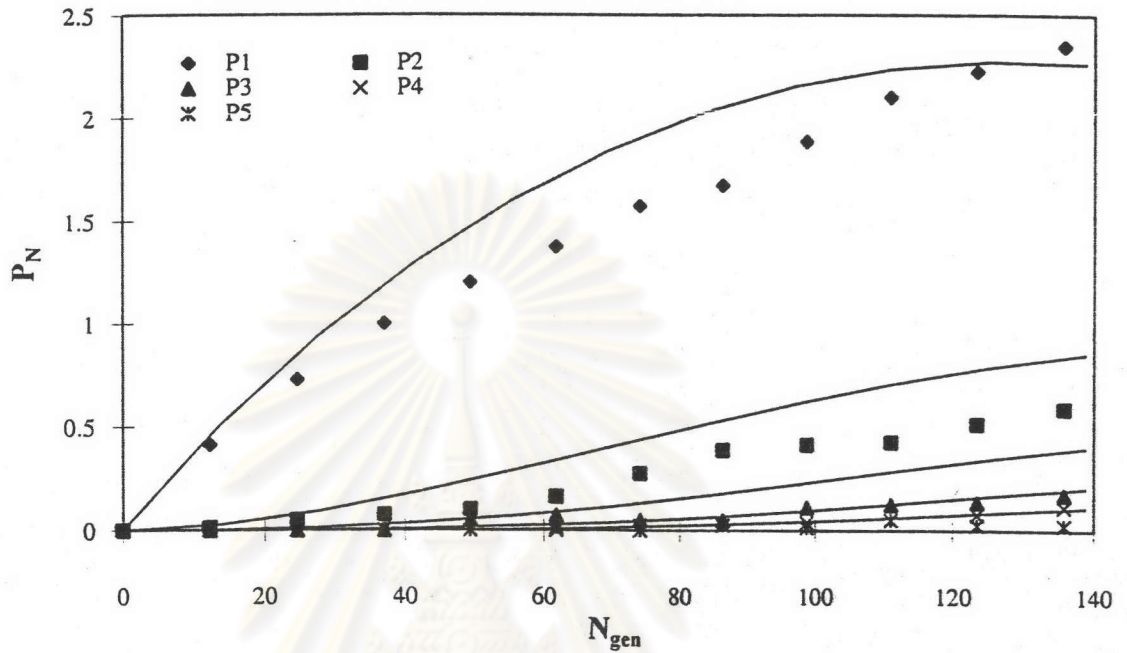


Figure 5.73. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $Pe=2500$

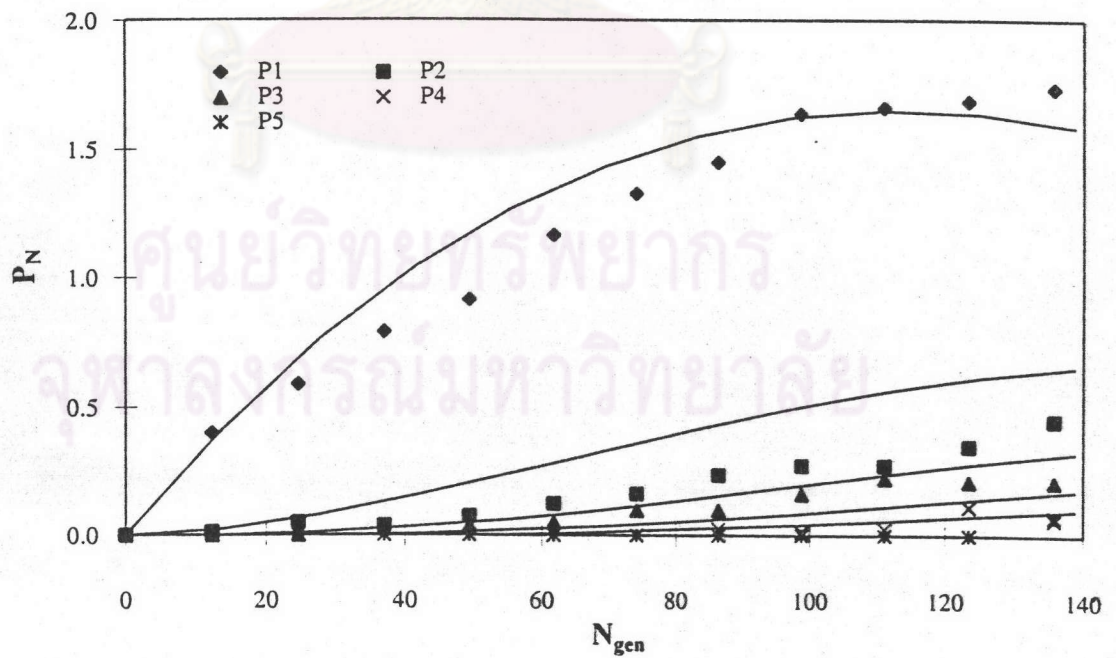


Figure 5.74. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $Pe=5000$

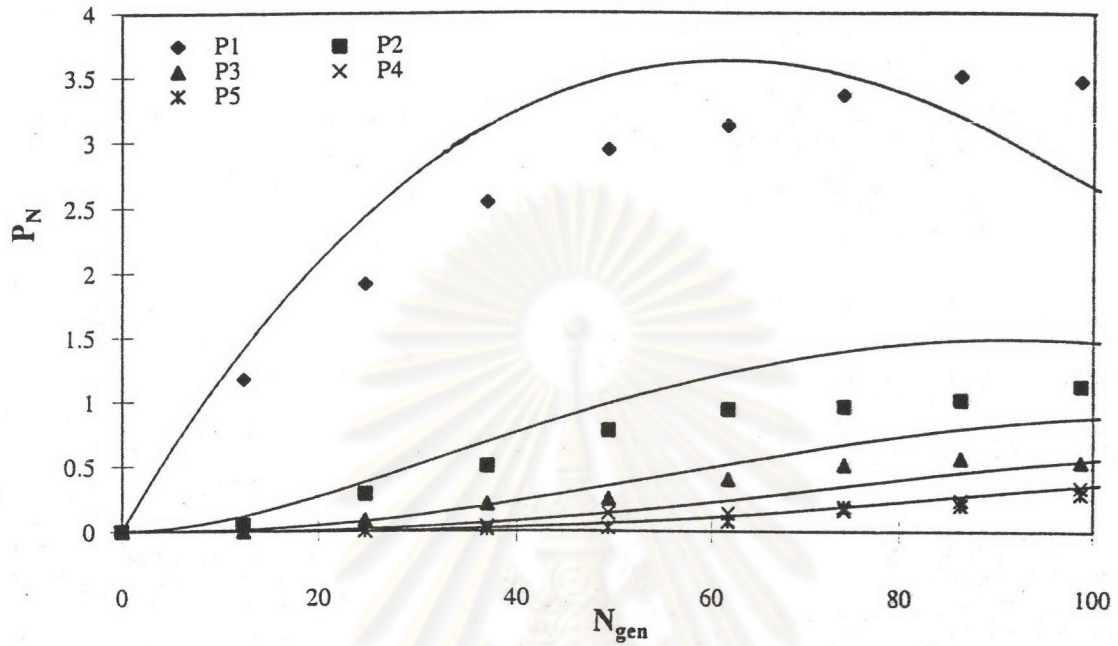


Figure 5.75. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $Pe=200$

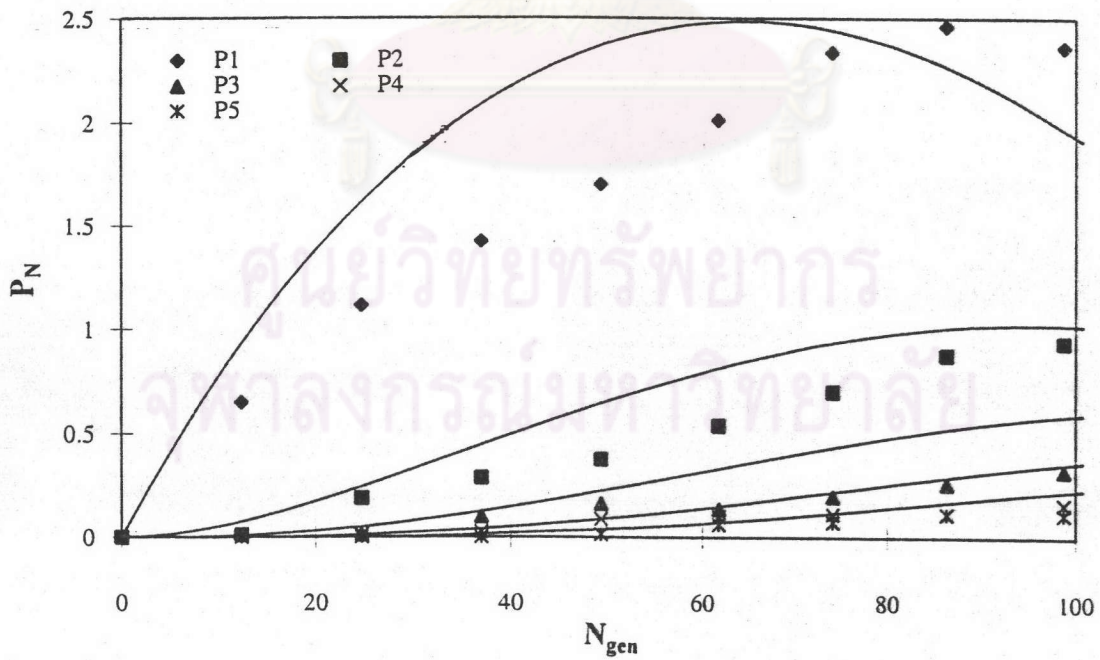


Figure 5.76. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $Pe=500$



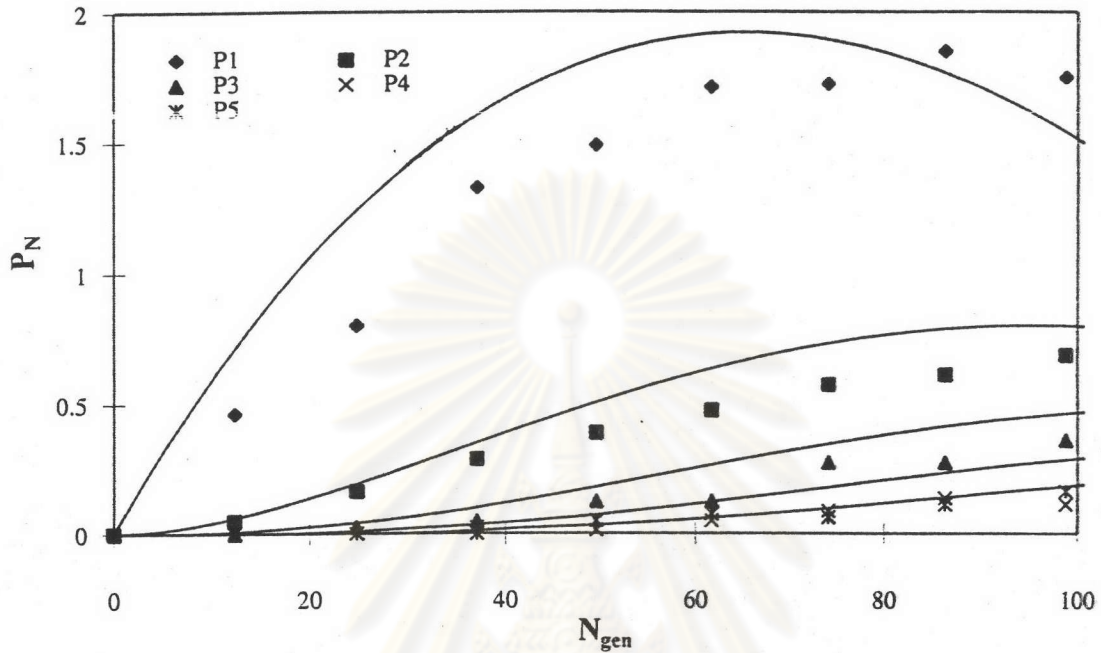


Figure 5.77. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $Pe=1000$

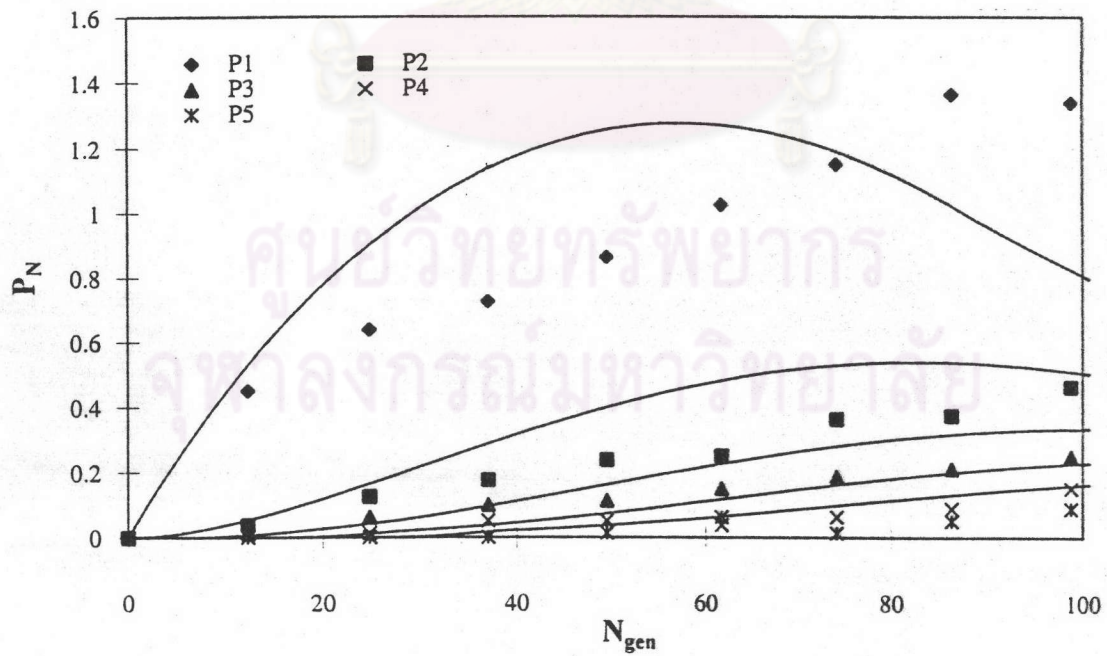


Figure 5.78. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $Pe=2500$

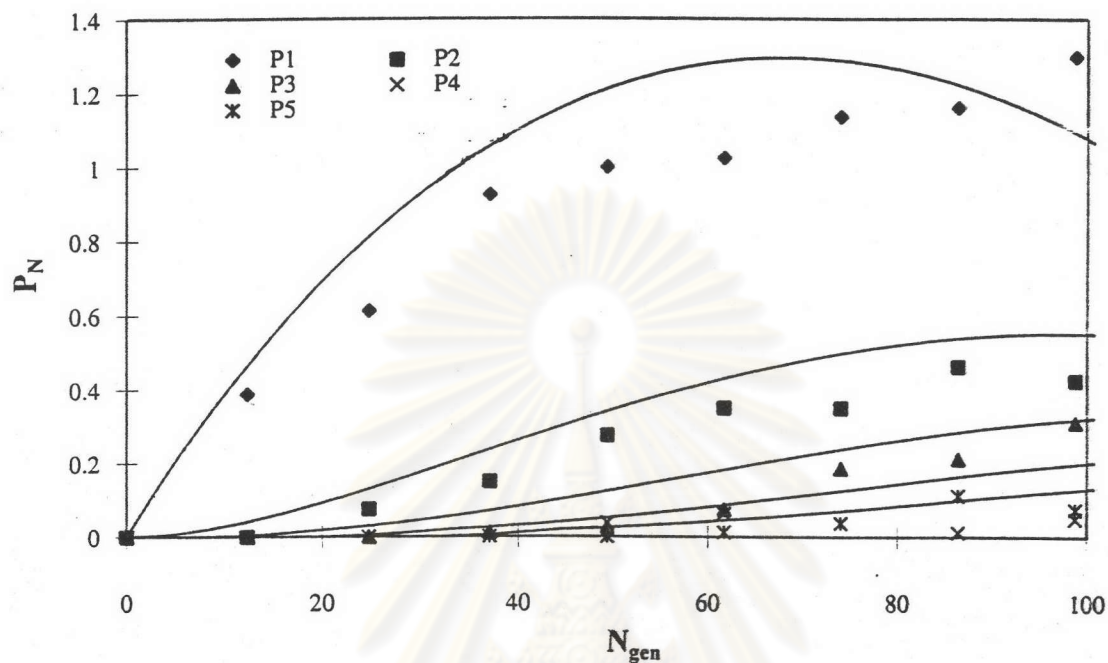


Figure 5.79. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $Pe=5000$

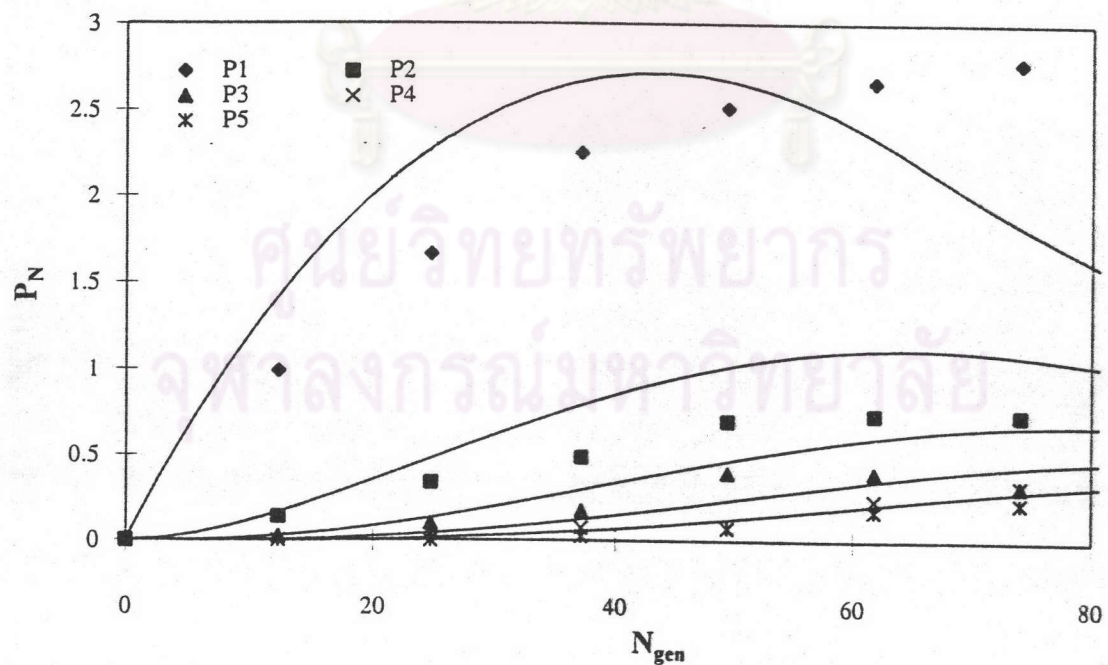


Figure 5.80. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $Pe=200$

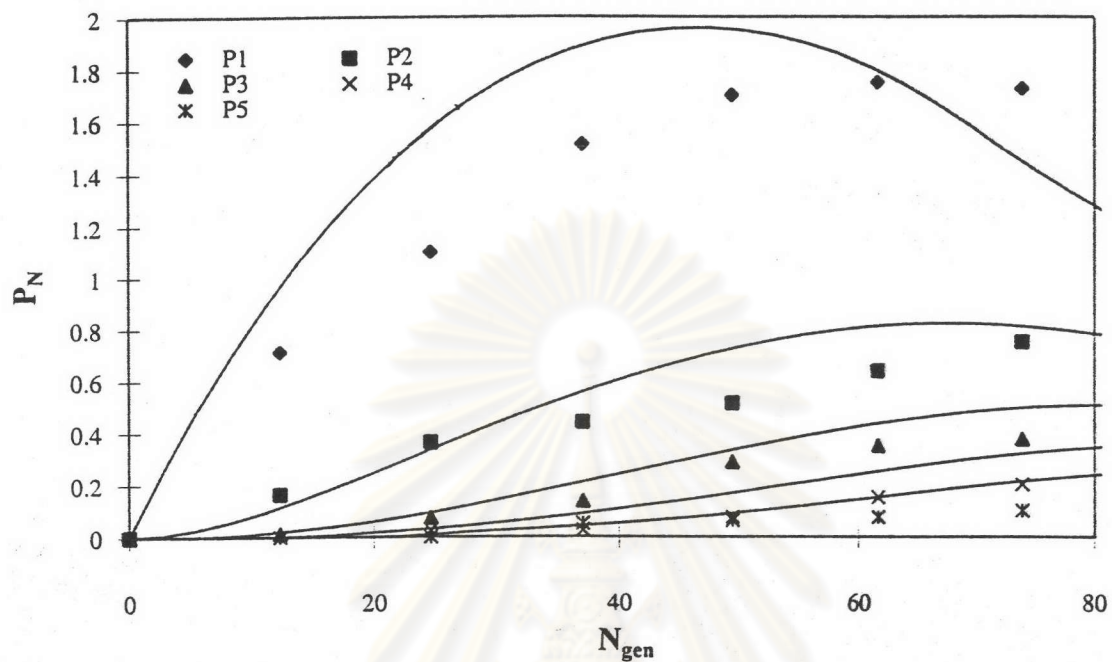


Figure 5.81. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $Pe=500$

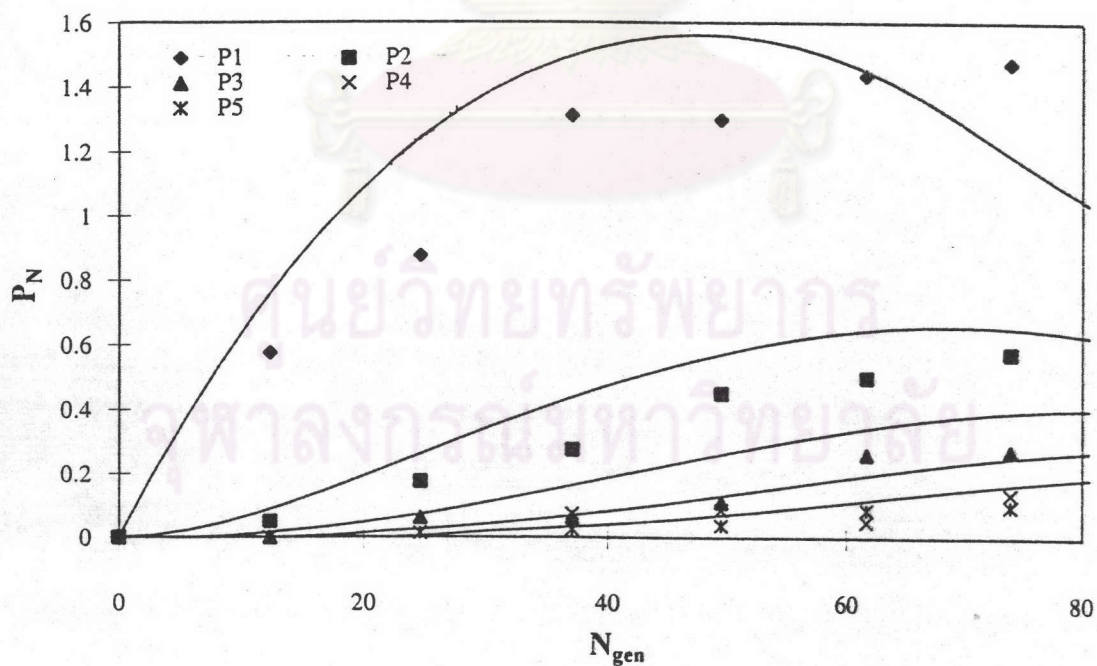


Figure 5.82. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $Pe=1000$



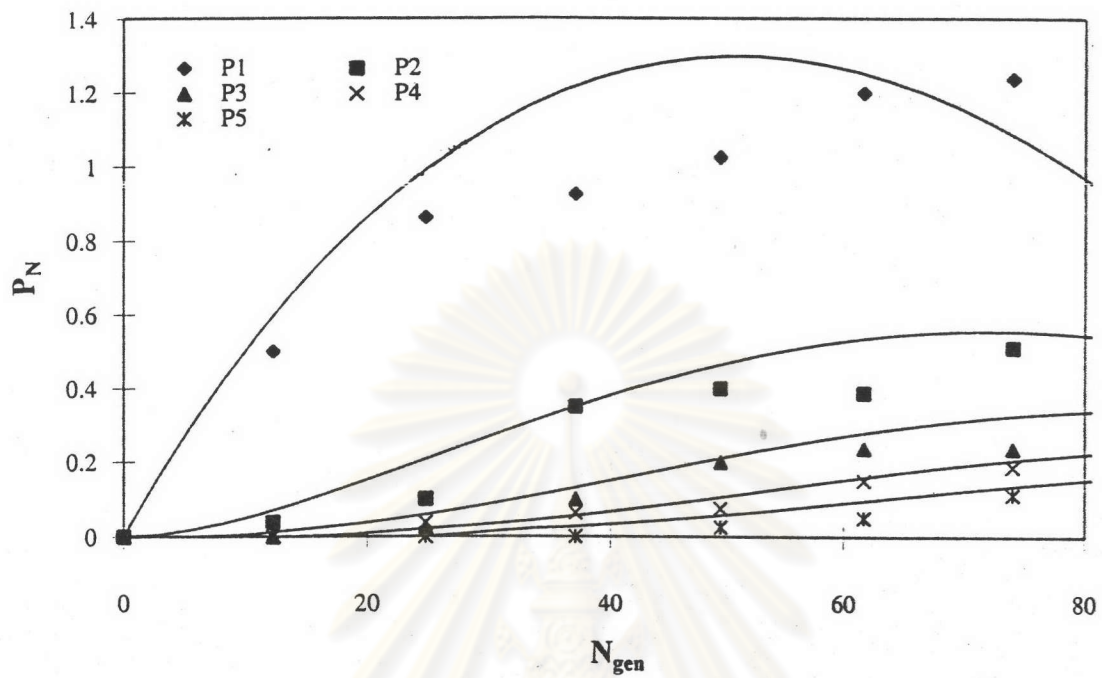


Figure 5.83. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $Pe=2500$

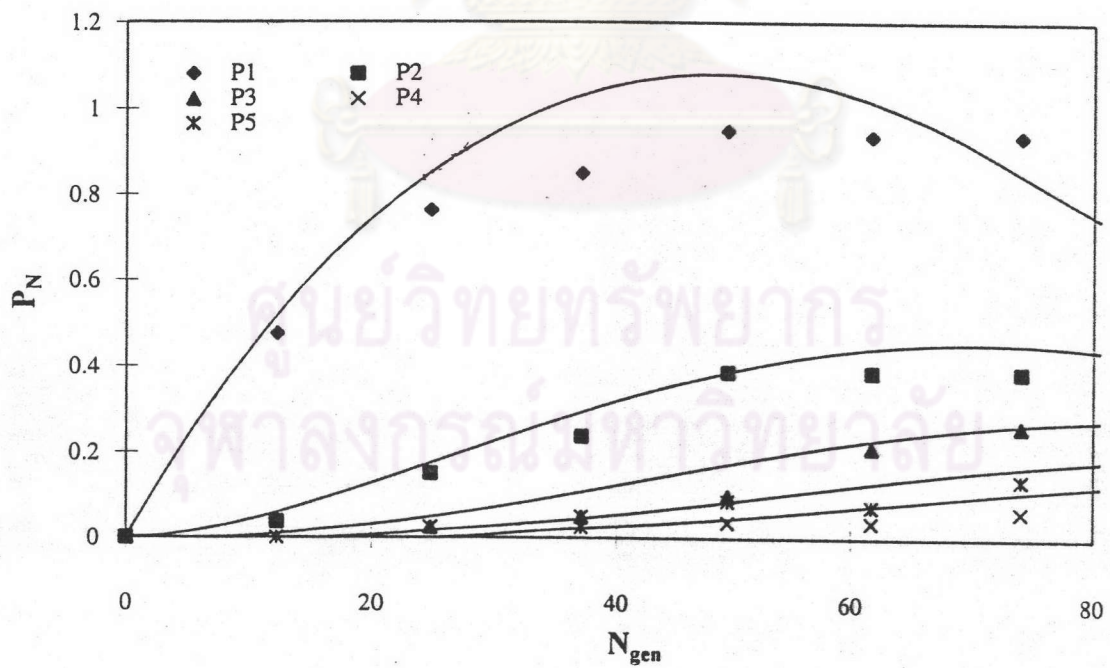


Figure 5.84. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $Pe=5000$

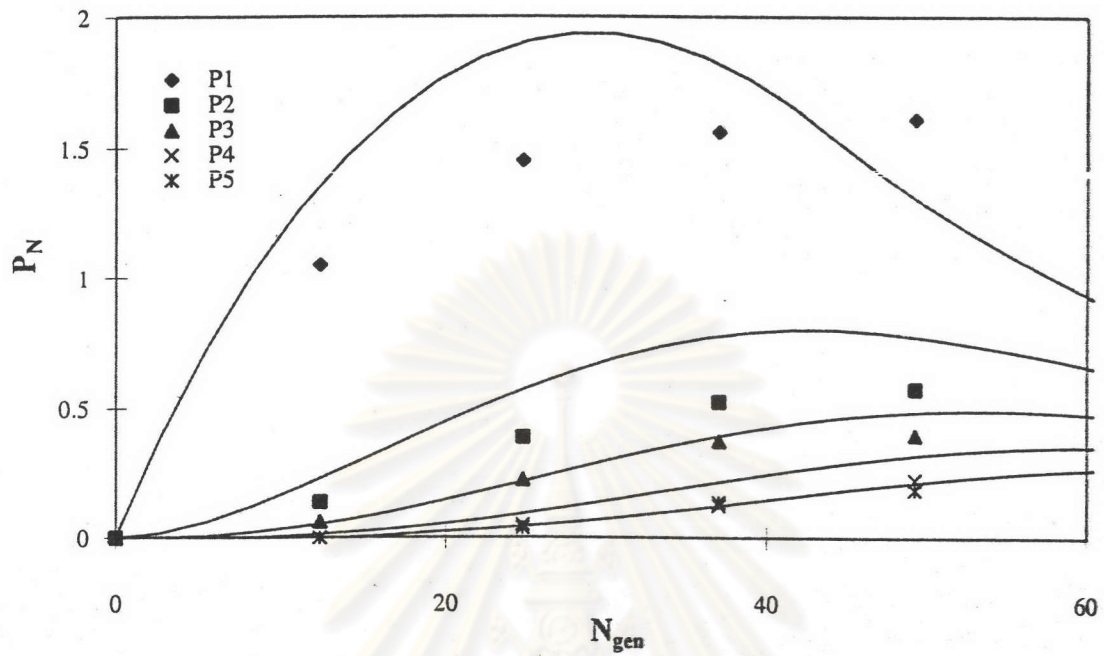


Figure 5.85. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $Pe=200$

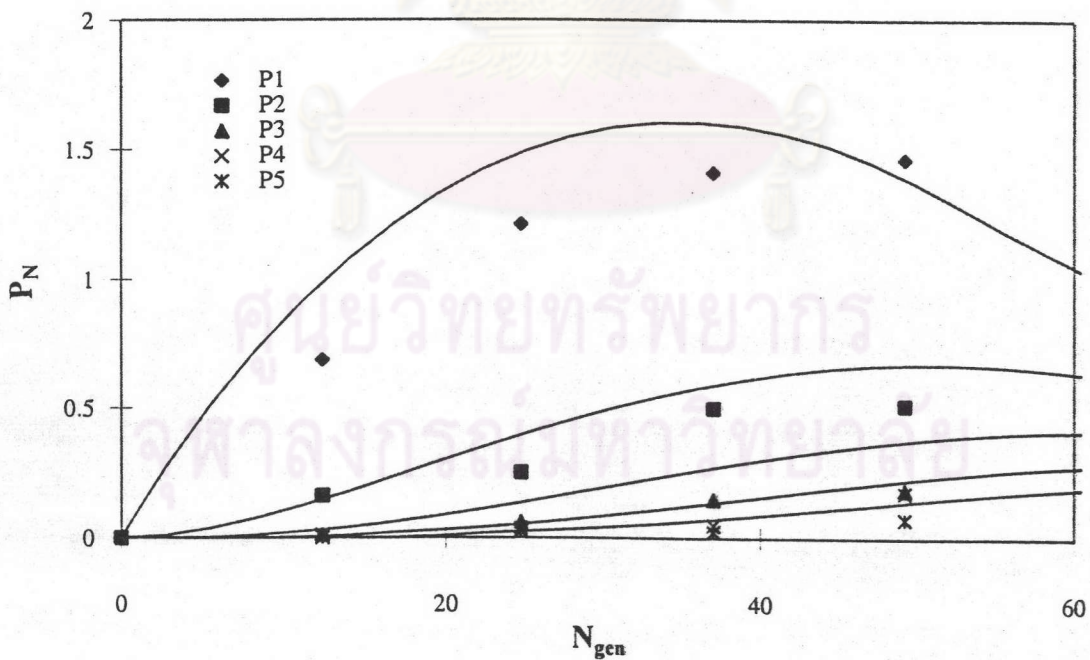


Figure 5.86. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $Pe=500$

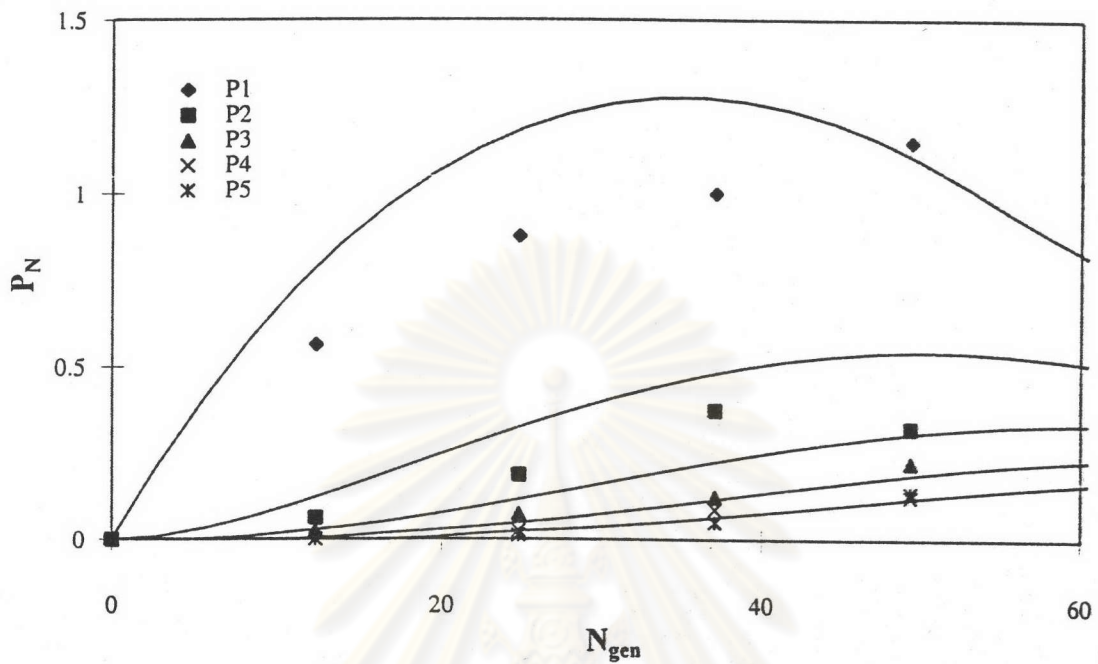


Figure 5.87. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $Pe=1000$

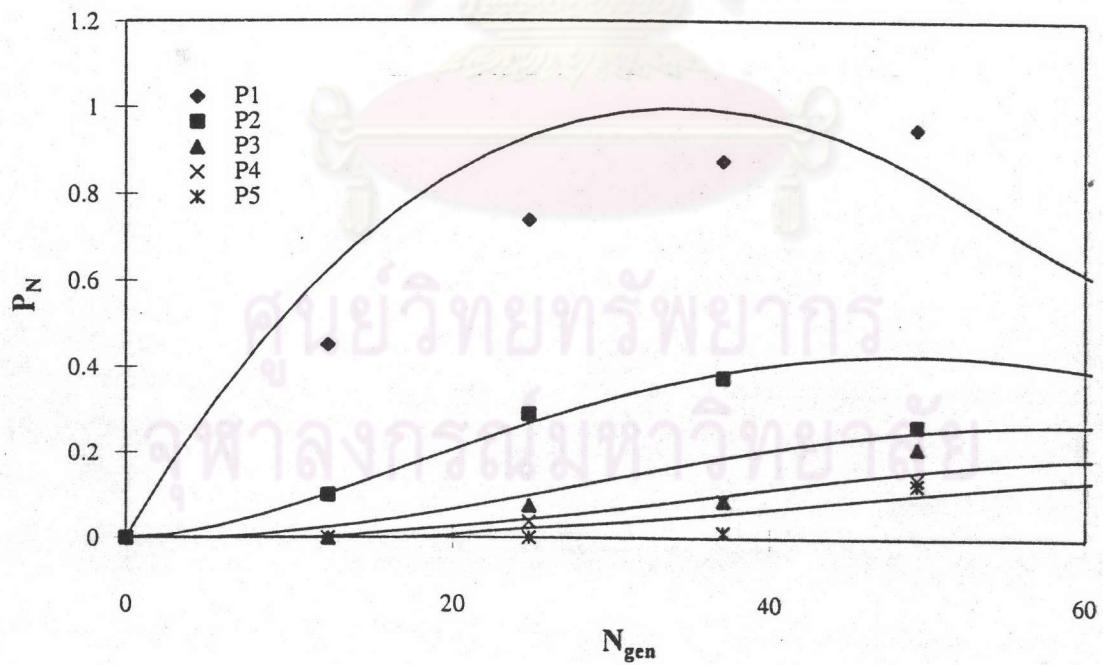


Figure 5.88. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $Pe=2500$



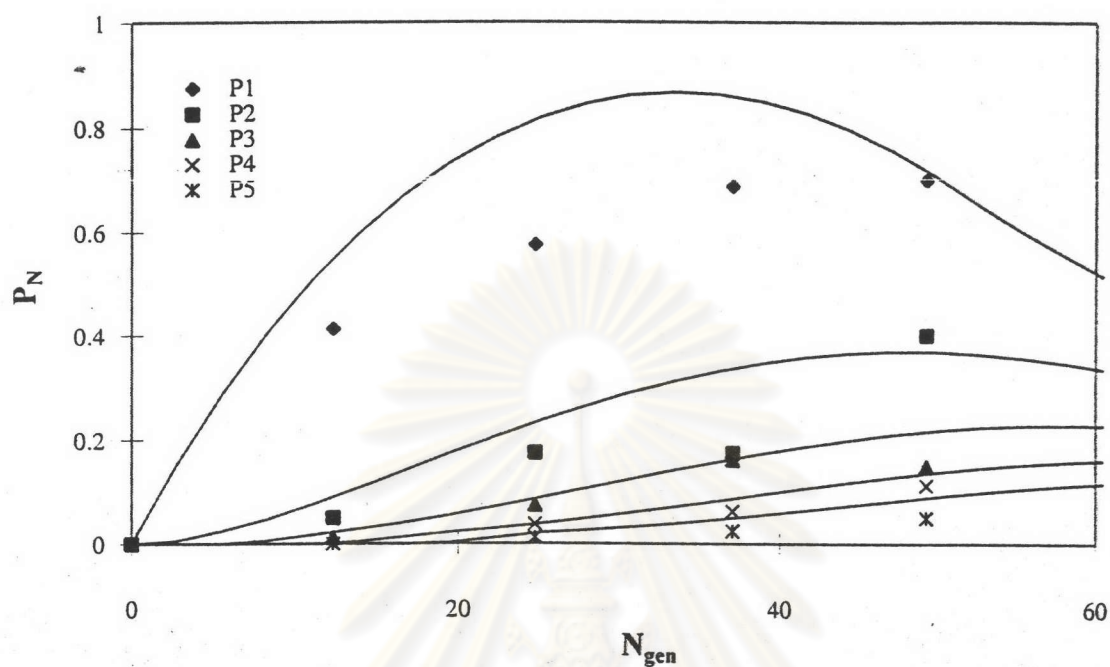


Figure 5.89. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $Pe=5000$

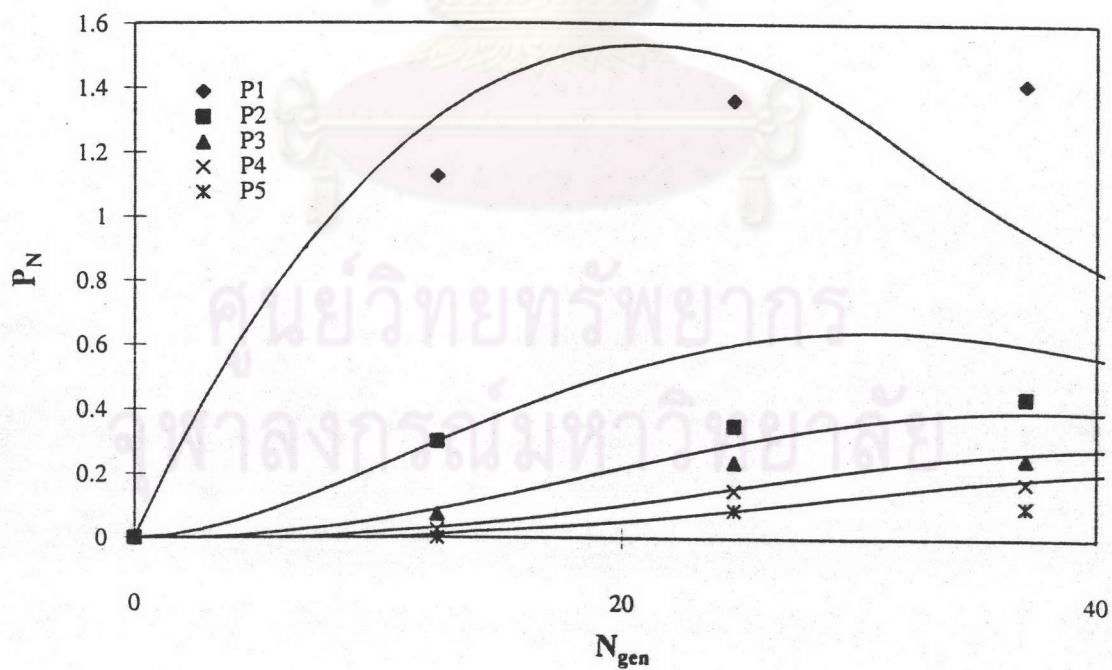


Figure 5.90. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $Pe=200$

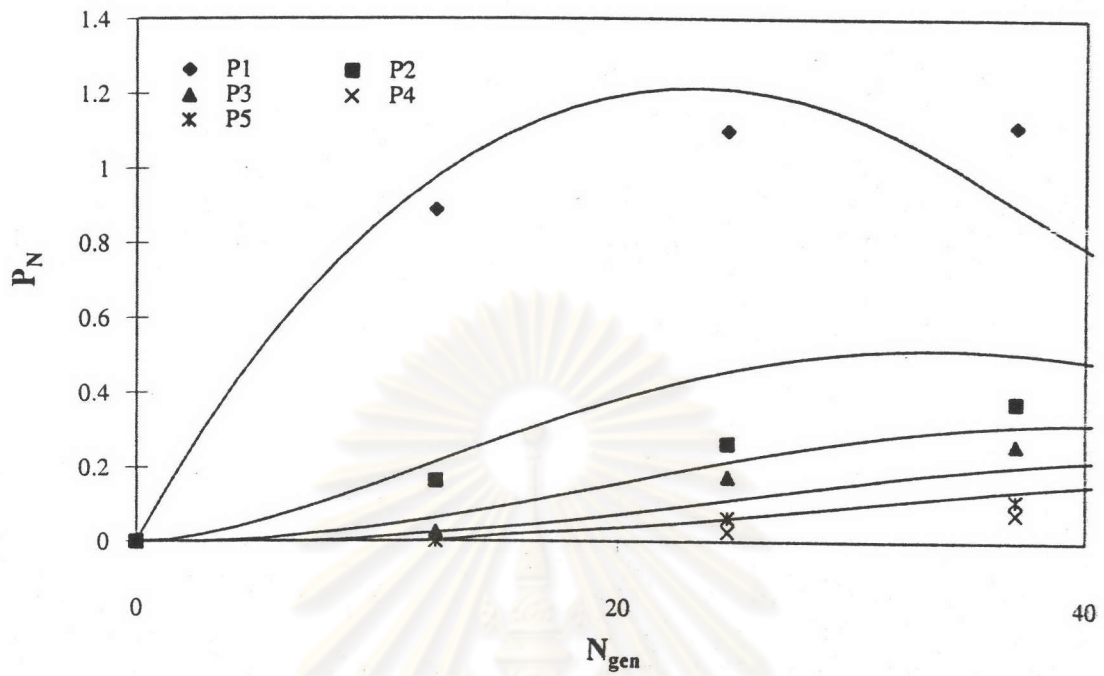


Figure 5.91. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $Pe=500$

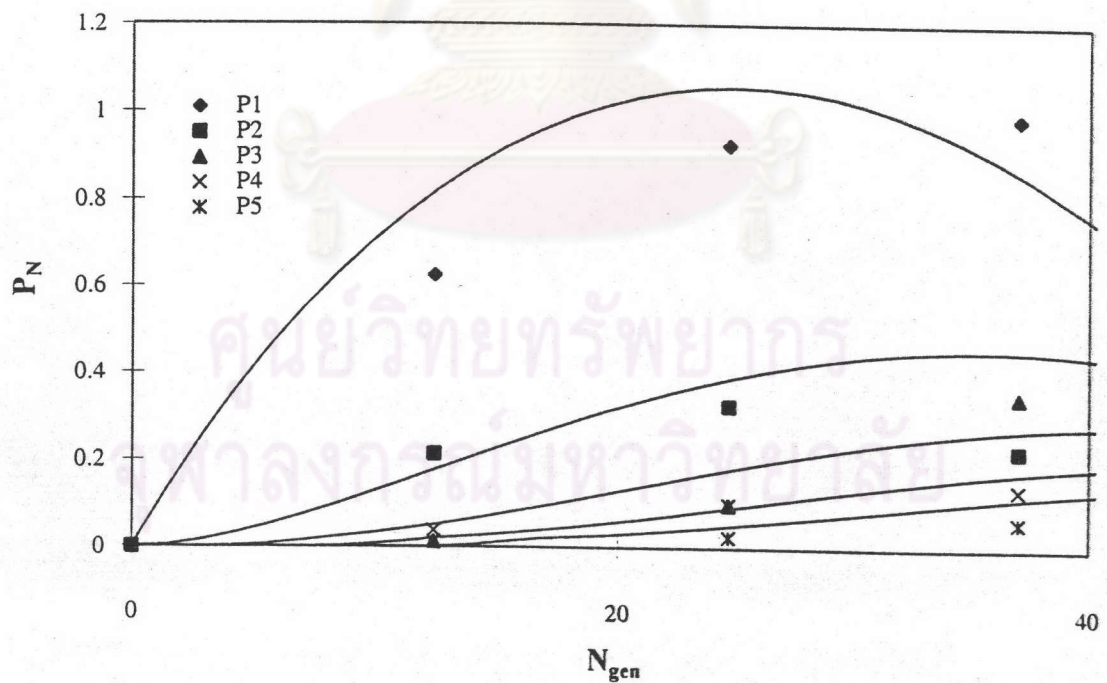


Figure 5.92. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $Pe=1000$

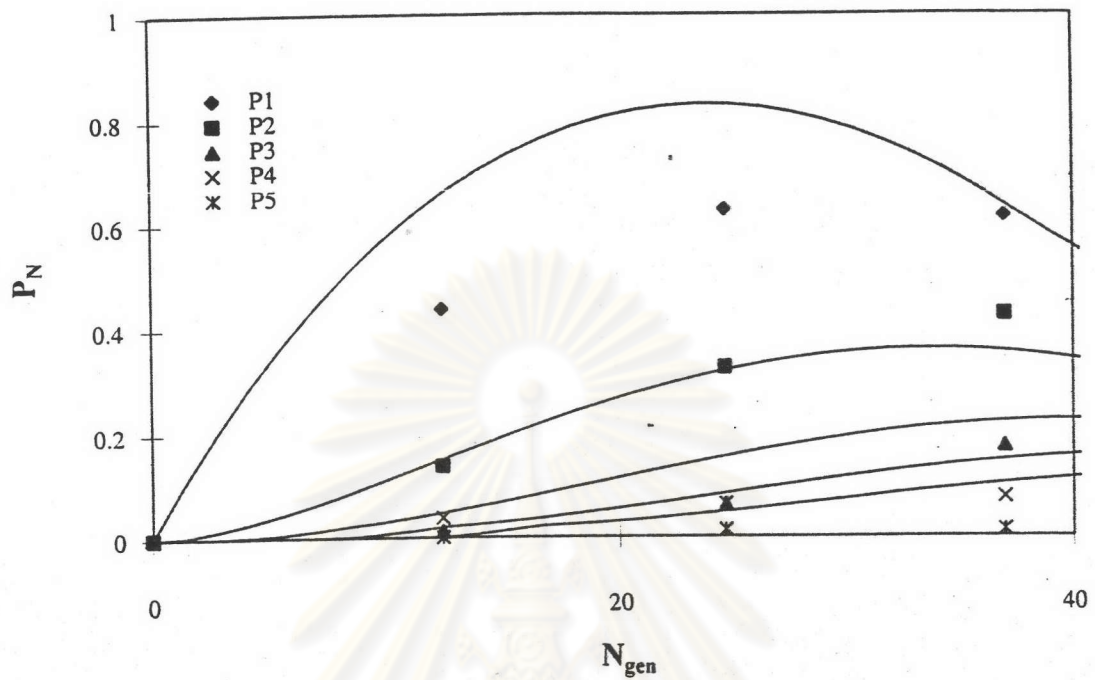


Figure 5.93. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $Pe=2500$

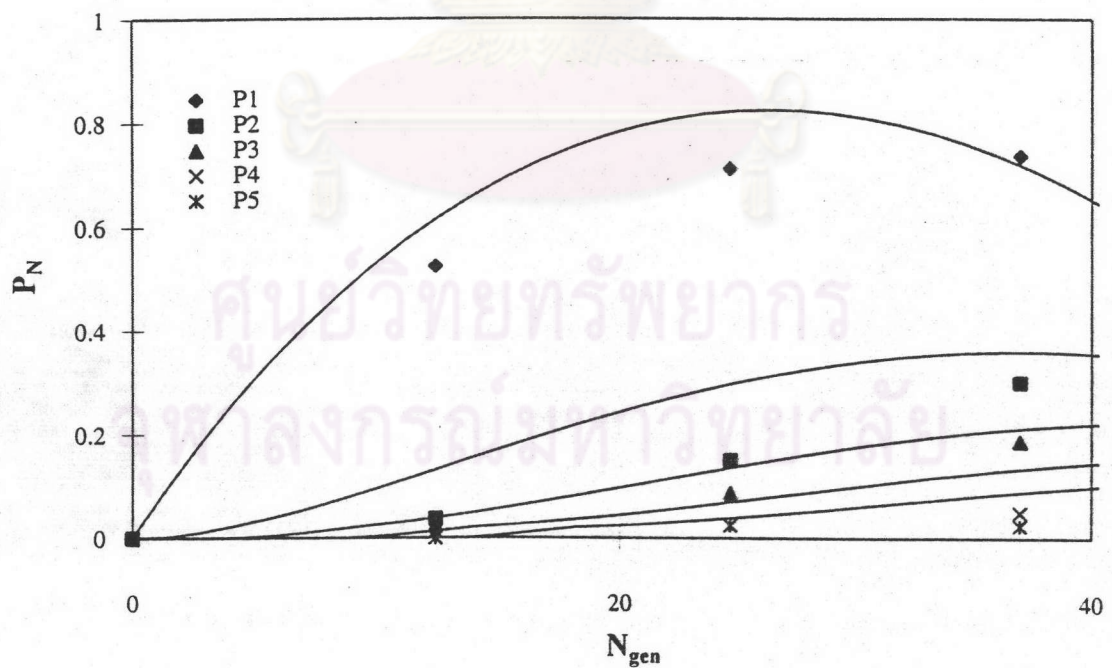


Figure 5.94. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $Pe=5000$



particles, so the locations of deposition was limited in advance. But in the present study, the particles were deposited at their collision points. Furthermore, in the present study the effective fiber length ( $Z=3.6$ ) was shorter than Kanaoka's ( $Z=10$ ) because of limitation in personal computer memory.

Figure 5.64 shows the relationship between  $\lambda$  and  $St$  with  $R$  as parameter based on the stochastic results. The value of  $\lambda$  decreased with increasing  $St$  and changed greatly at large  $St$ . Moreover, the value of  $\lambda$  was higher value at a smaller  $R$ . This means that the collection efficiency increased more rapidly with dust load at small  $St$  and  $R$ .

At the simulation conditions at  $Pe=\infty$  for the case of convective diffusion and at  $St=0$  for the case of inertial impaction, neither the effect of diffusion nor inertia is present in the motion of the aerosol particle in fluid flow. Thus particles are captured on the fiber via interception mechanism only. As seen the figures 5.31 and 5.64, the value of  $\lambda$  at  $Pe=5000$  is slightly smaller than that of  $\lambda$  at  $St=0$  for the same  $R$ . It is reasonable to conclude that the values of  $\lambda$  at  $Pe=\infty$  equal the corresponding values of  $\lambda$  at  $St=0$ .

## 5.2 Deterministic simulation results

The optimal values of the parameters  $e_N$  and  $e'_N$  for the deterministic model were estimated by comparison with the stochastic results at each filtration condition for the case of convective diffusion and inertial impaction. The non-linear simplex method was used for estimating the parameters  $e_N$  and  $e'_N$  by minimizing the objective function shown in Equation (4.2).

### 5.2.1 Convective diffusional deposition

Figures 5.65-5.94 compare the change with time in the number concentration of dendrites of sizes  $N=1$  to  $N=5$ . The solid lines are the results predicted by the present model and the dots belong to the stochastic model. As seen from the figures, the predicted concentration of dendrites of smaller sizes increased faster at the initial stage but dropped faster as  $N_{gen}$  increased. Also the predicted concentration of

Table 5.5 Optimal value of the parameters  $e_N$  and  $e'_N$  for convective diffusion

Pe	R	0.05	0.1	0.13	0.15	0.17	0.2
200	en	2.531	3.159	3.234	3.252	3.644	3.442
	en'	2.022	2.078	1.794	1.803	1.886	1.629
	Lamda	0.510	0.540	0.554	0.483	0.517	0.453
	Obj fun	9.313	4.321	3.951	4.182	2.295	1.282
	Obj fun/pt	0.085	0.079	0.088	0.119	0.077	0.064
500	en	3.411	4.744	4.774	4.928	4.619	4.648
	en'	2.243	2.780	2.583	2.162	2.107	1.835
	Lamda	1.168	0.982	0.843	0.922	0.739	0.703
	Obj fun	4.628	2.250	5.013	1.603	1.982	1.129
	Obj fun/pt	0.042	0.041	0.111	0.046	0.066	0.056
1000	en	3.883	7.499	6.463	6.234	6.115	5.631
	en'	1.533	3.877	3.103	2.670	2.405	1.906
	Lamda	2.350	1.811	1.292	1.188	1.091	0.931
	Obj fun	2.962	1.934	2.052	1.889	1.594	0.697
	Obj fun/pt	0.027	0.035	0.046	0.054	0.053	0.035
2500	en	5.029	9.680	10.272	8.000	8.095	7.424
	en'	0.433	4.088	4.287	2.852	2.912	2.267
	Lamda	4.596	2.796	2.302	1.716	1.524	1.289
	Obj fun	1.278	3.203	2.770	0.713	1.089	0.587
	Obj fun/pt	0.012	0.058	0.062	0.020	0.036	0.029
5000	en	13.238	12.606	10.363	8.817	9.090	7.579
	en'	7.057	6.213	4.016	4.012	3.514	2.211
	Lamda	6.181	3.196	2.441	1.602	1.640	1.342
	Obj fun	2.839	2.394	1.804	0.715	0.949	0.638
	Obj fun/point	0.026	0.044	0.040	0.020	0.032	0.032
Ngen		1000	500	400	350	300	200
No. point		110	55	45	35	30	20



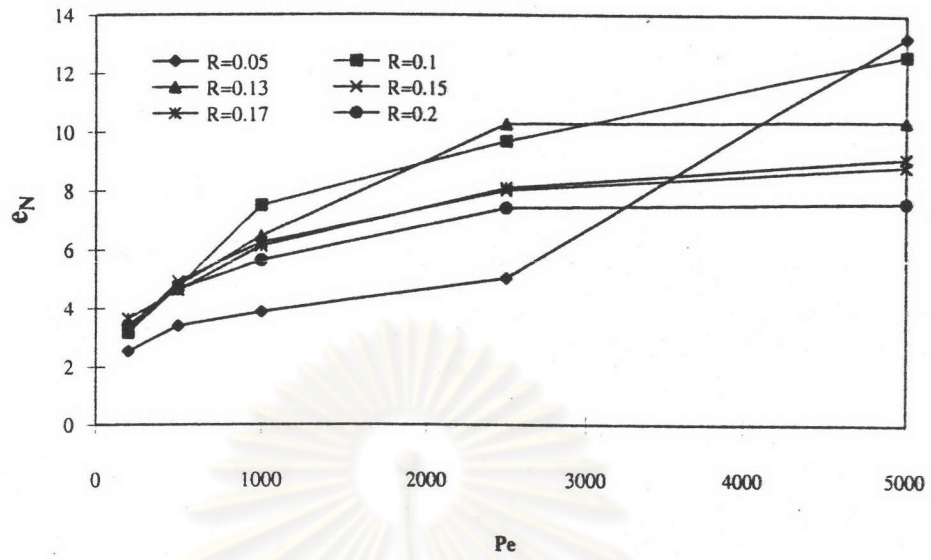


Figure 5.95. Relationship between the parameter  $e_N$  and  $Pe$

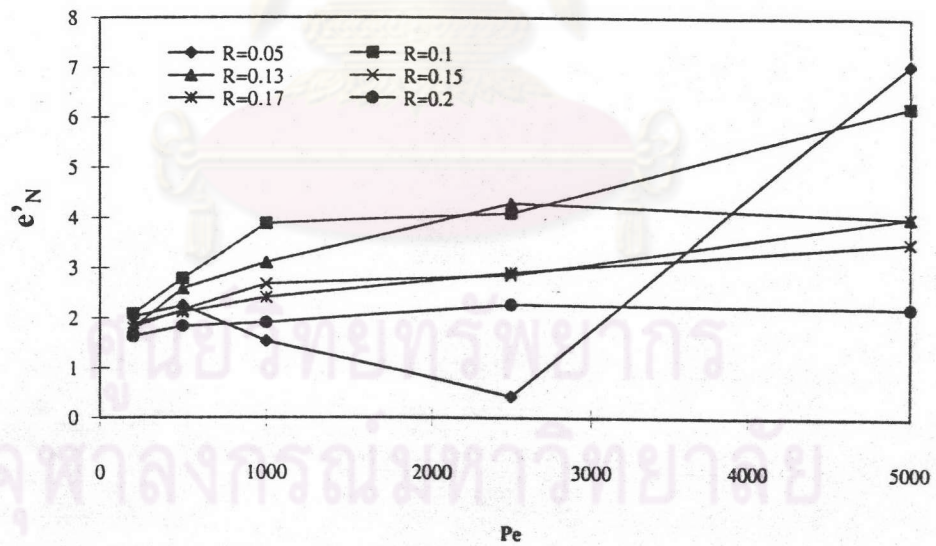


Figure 5.96. Relationship between the parameter  $e'_N$  and  $Pe$



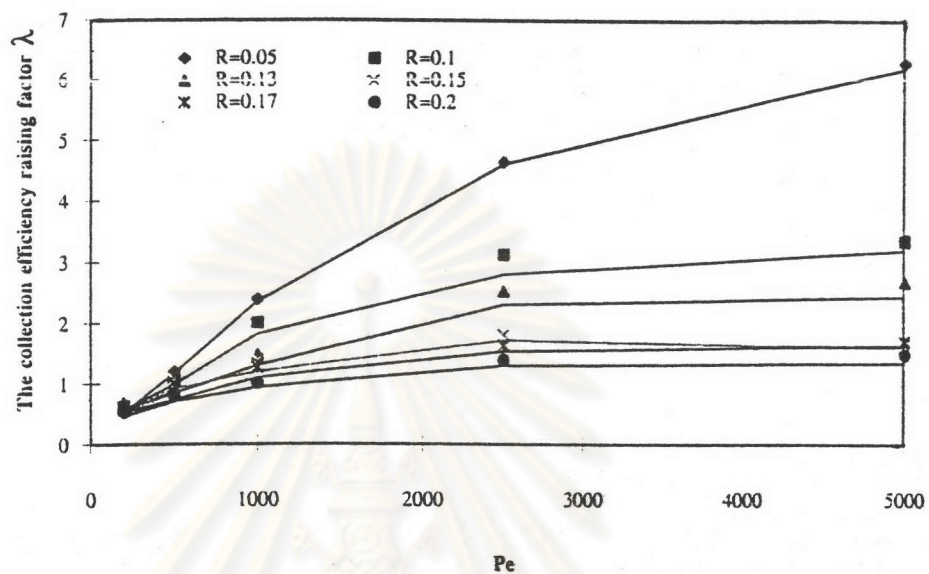


Figure 5.97. Comparison of  $\lambda$  between stochastic and simplified models for convective diffusion  
(The dots are stochastic results, the lines are deterministic ones)

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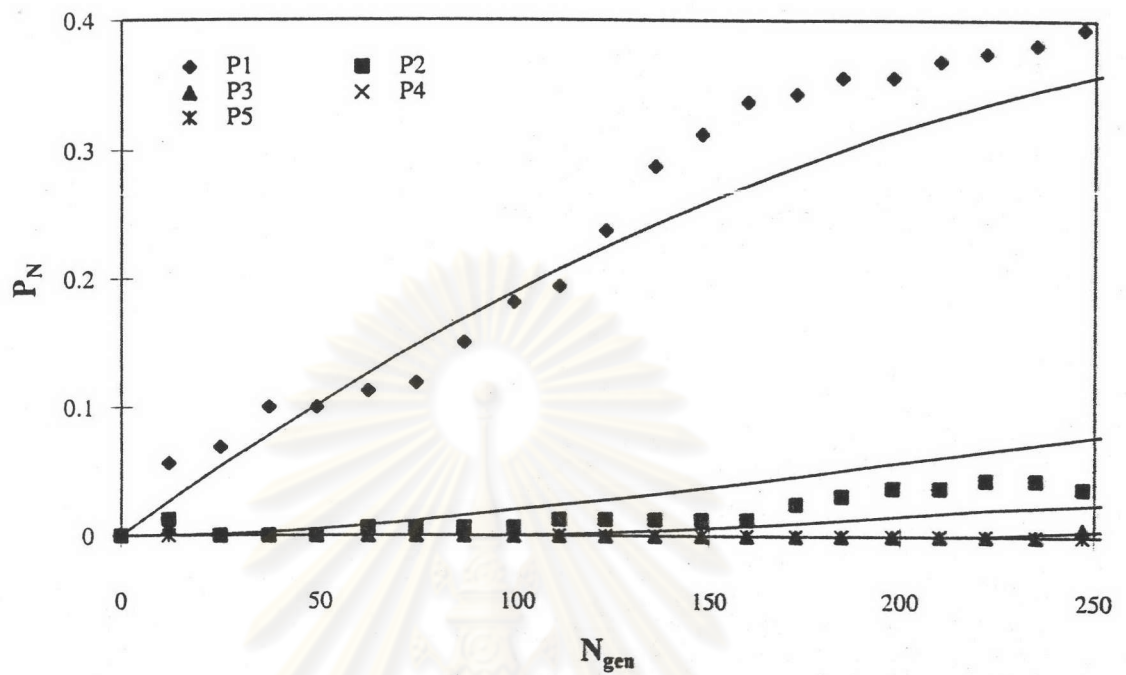


Figure 5.98. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $St=0.0$

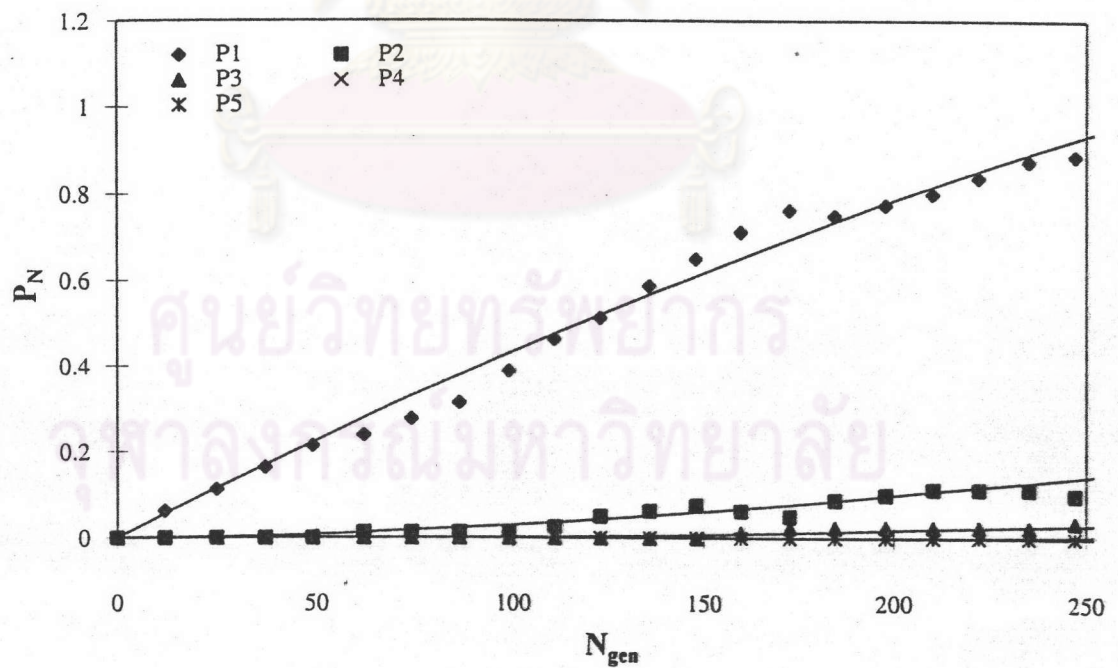


Figure 5.99. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $St=0.6$

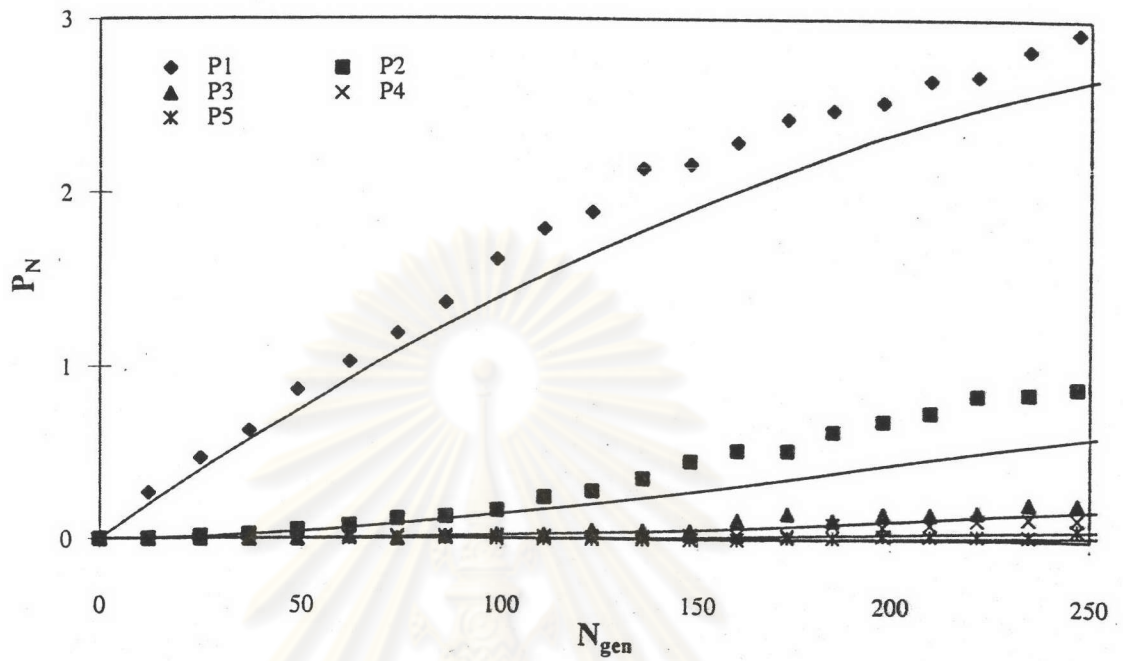


Figure 5.100. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $St=1.0$

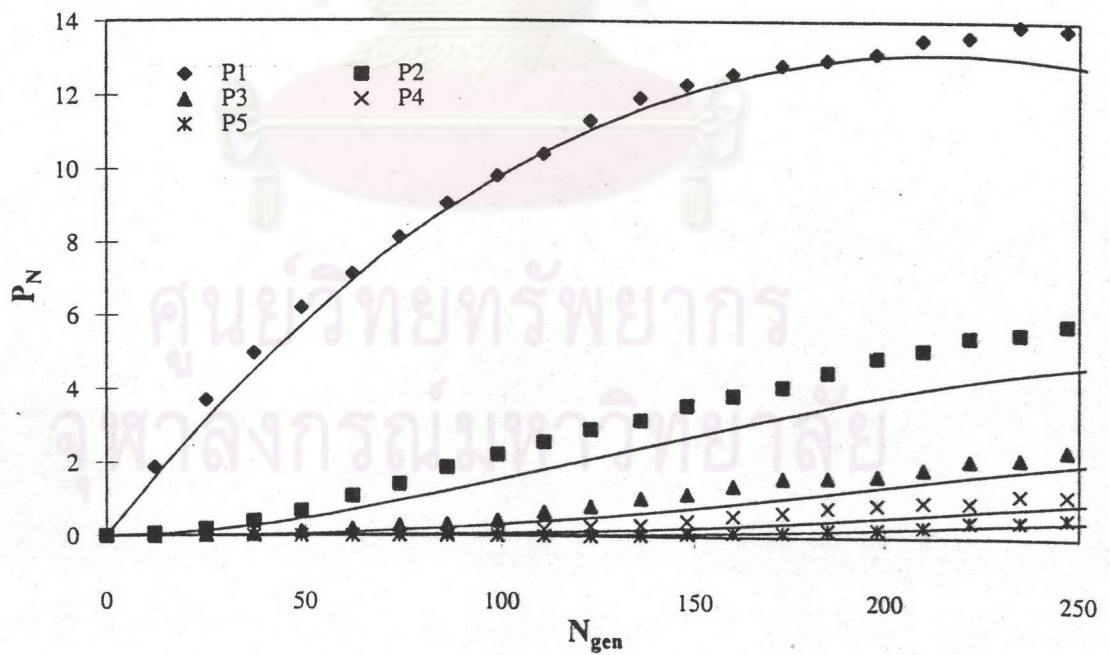


Figure 5.101. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $St=1.4$



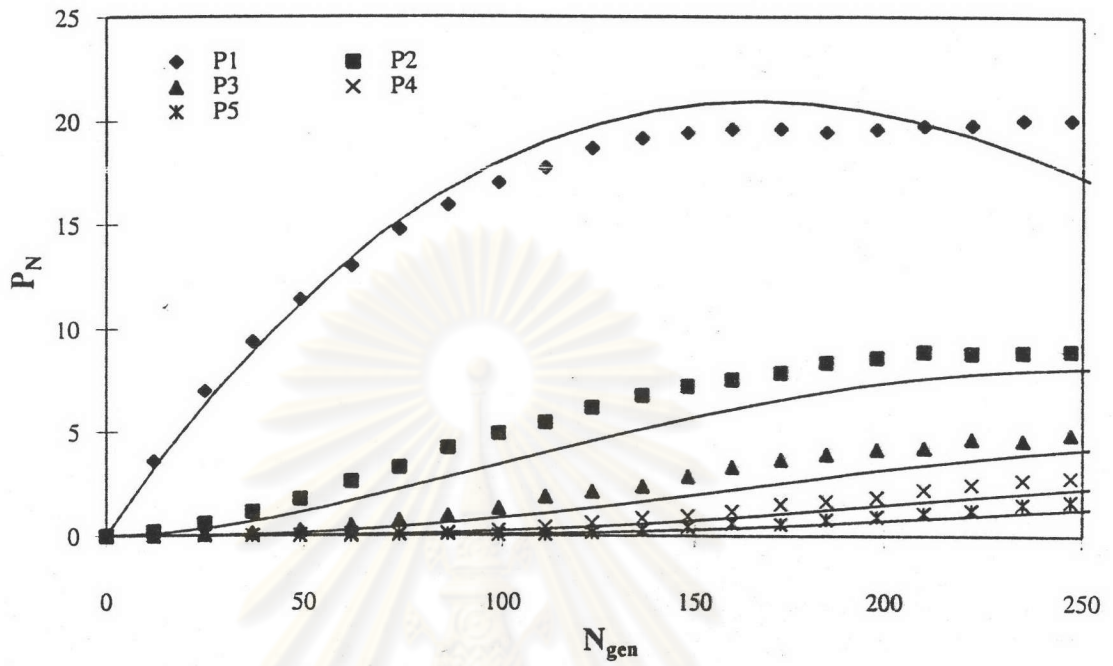


Figure 5.102. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.05$  and  $St=2.0$

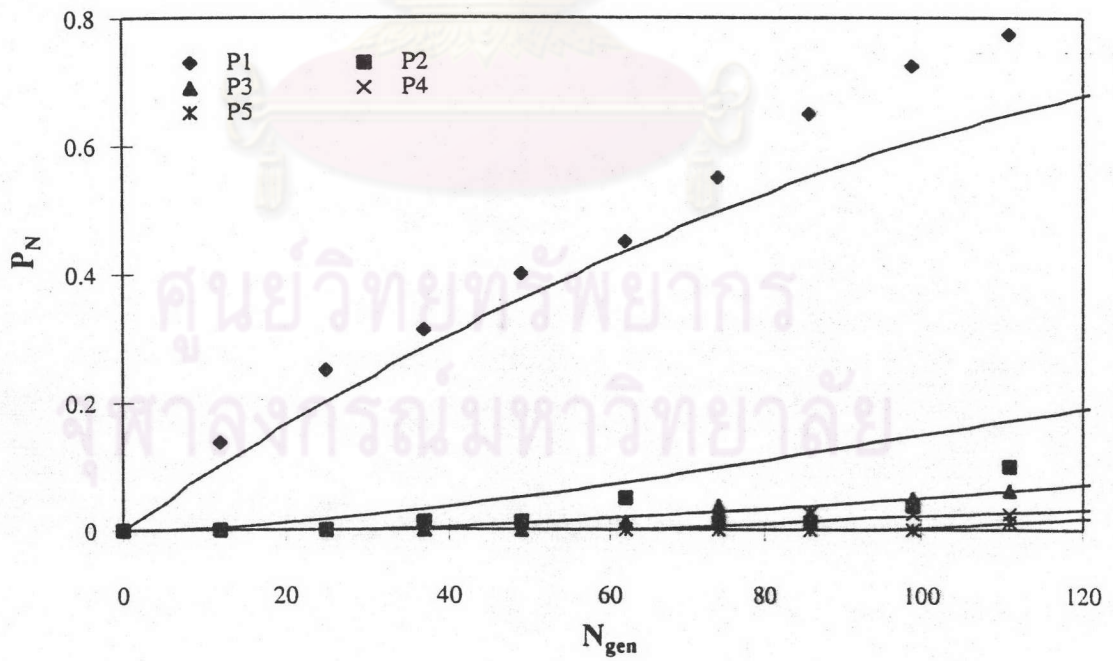


Figure 5.103. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $St=0.0$

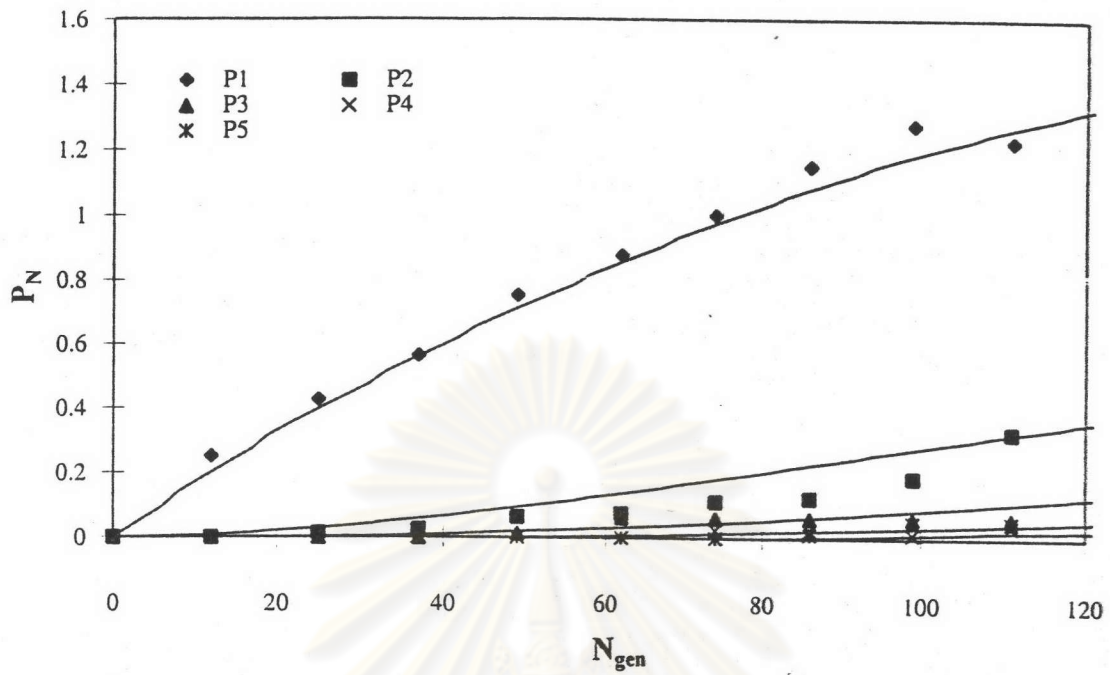


Figure 5.104. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $St=0.6$

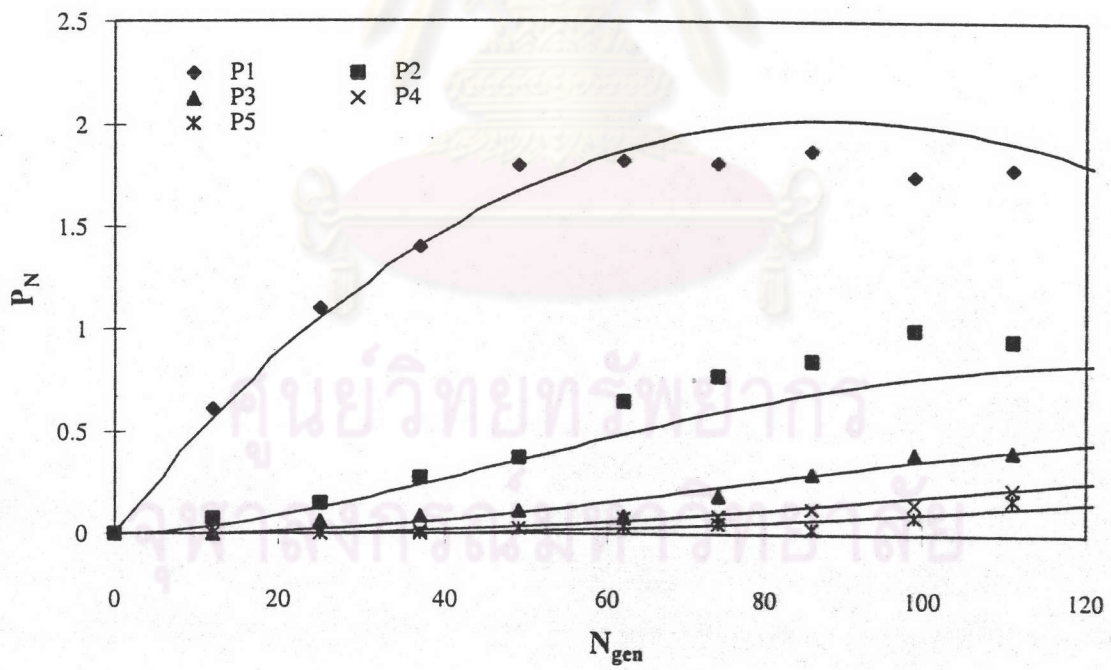


Figure 5.105. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $St=1.0$

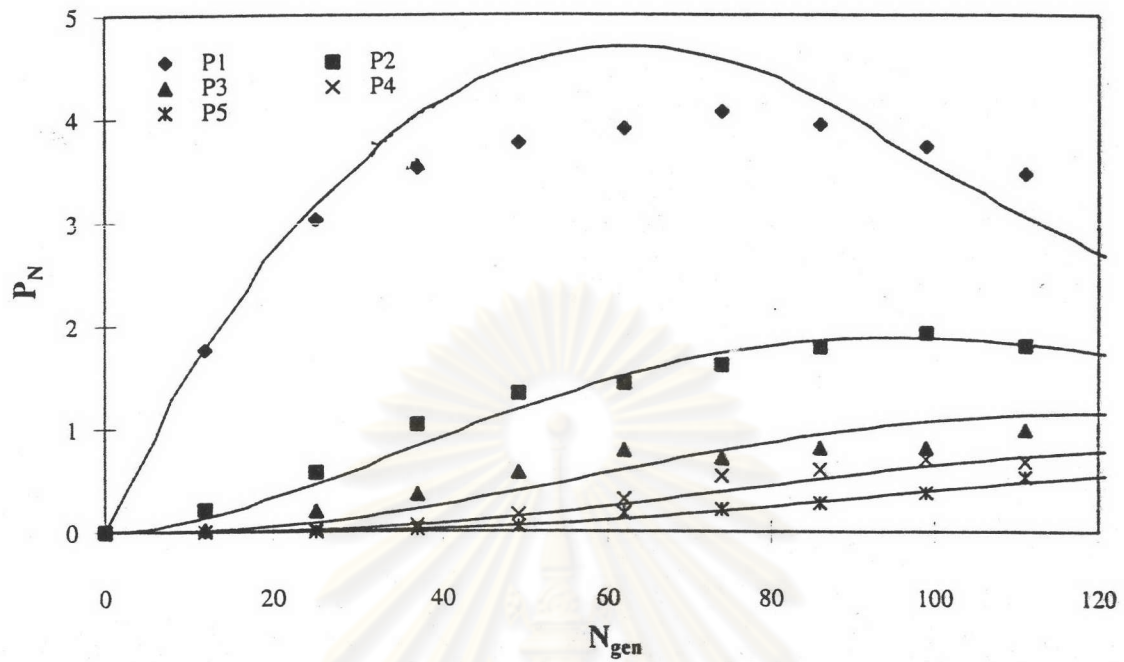


Figure 5.106. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $St=1.4$

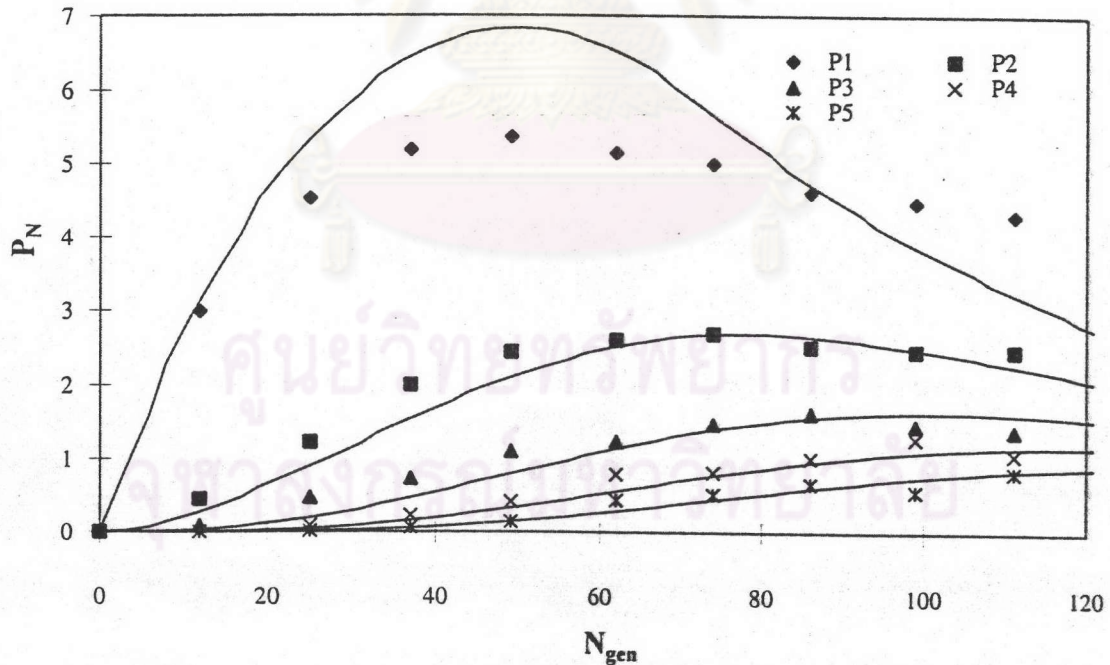


Figure 5.107. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.1$  and  $St=2.0$



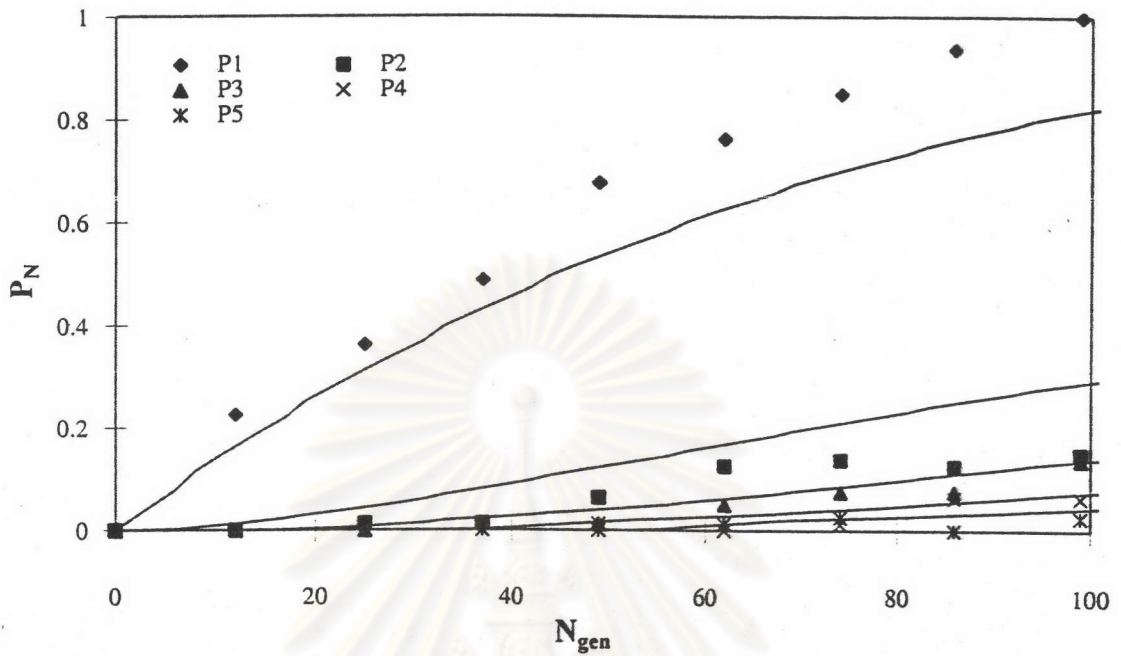


Figure 5.108. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $St=0.0$

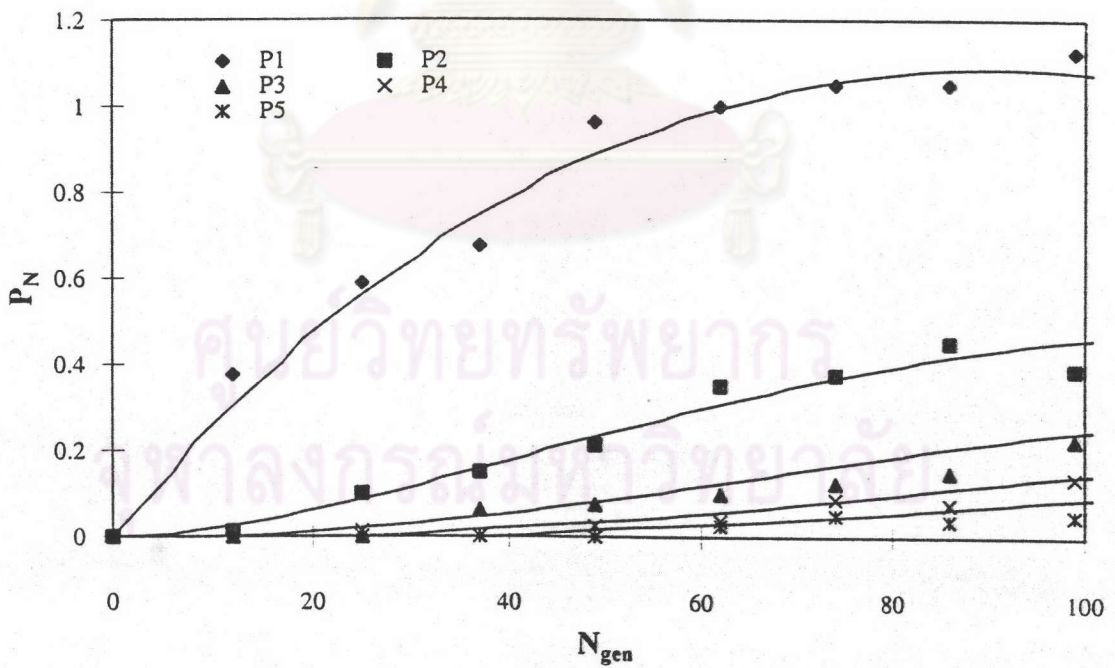


Figure 5.109. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $St=0.6$

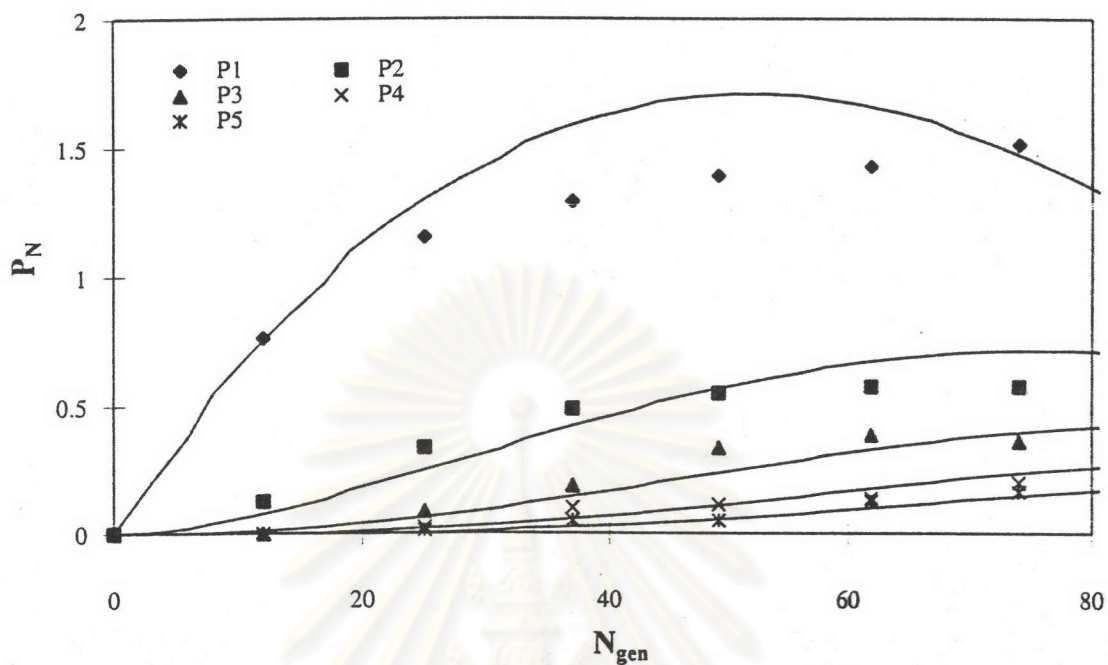


Figure 5.110. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $St=1.0$

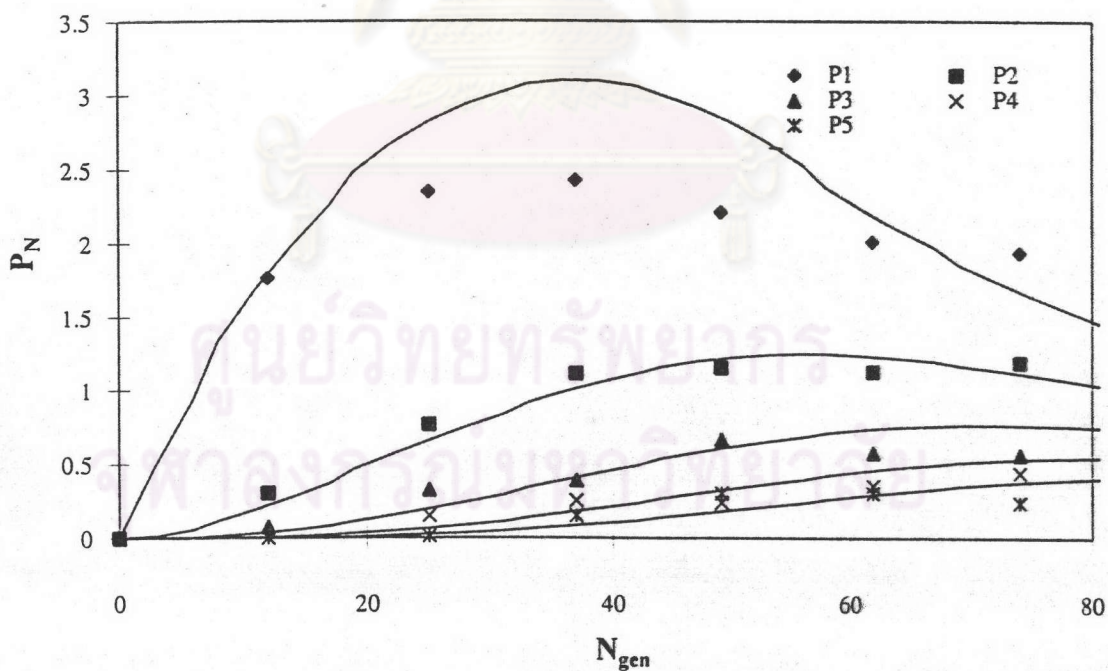


Figure 5.111. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $St=1.4$

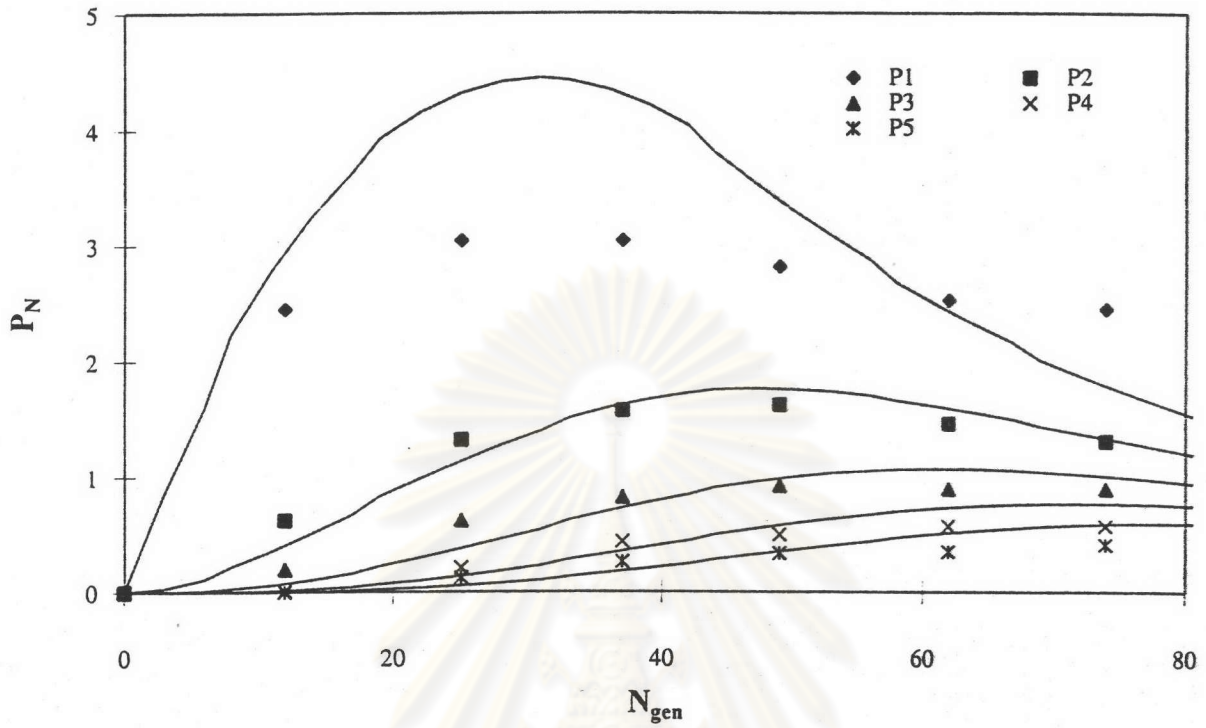


Figure 5.112. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.13$  and  $St=20$

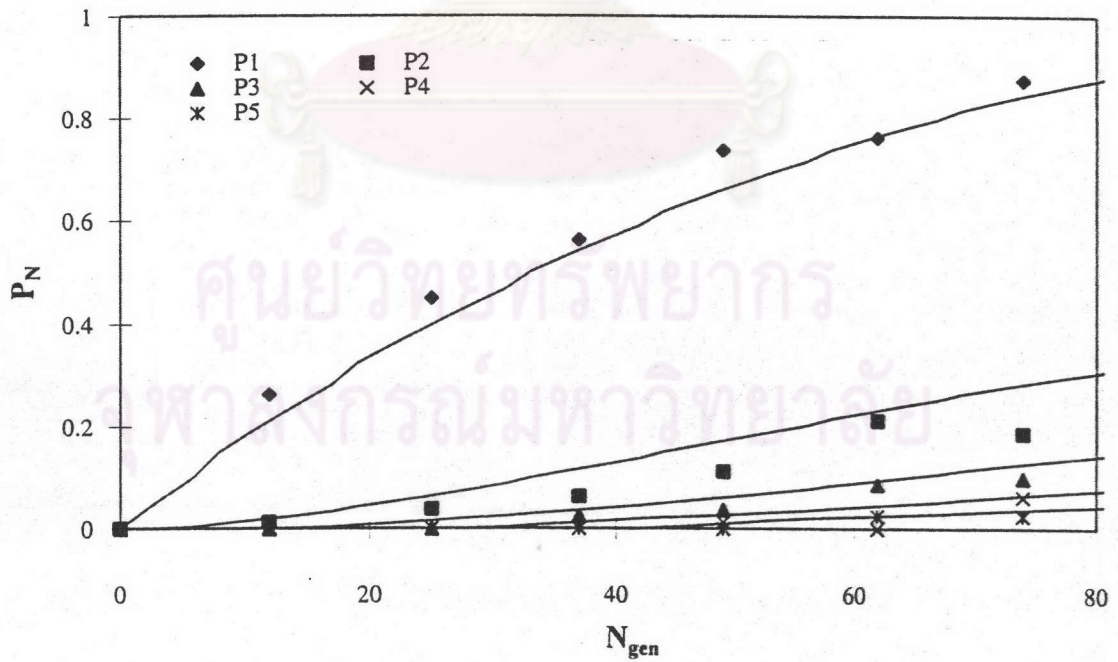


Figure 5.113. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $St=0.0$



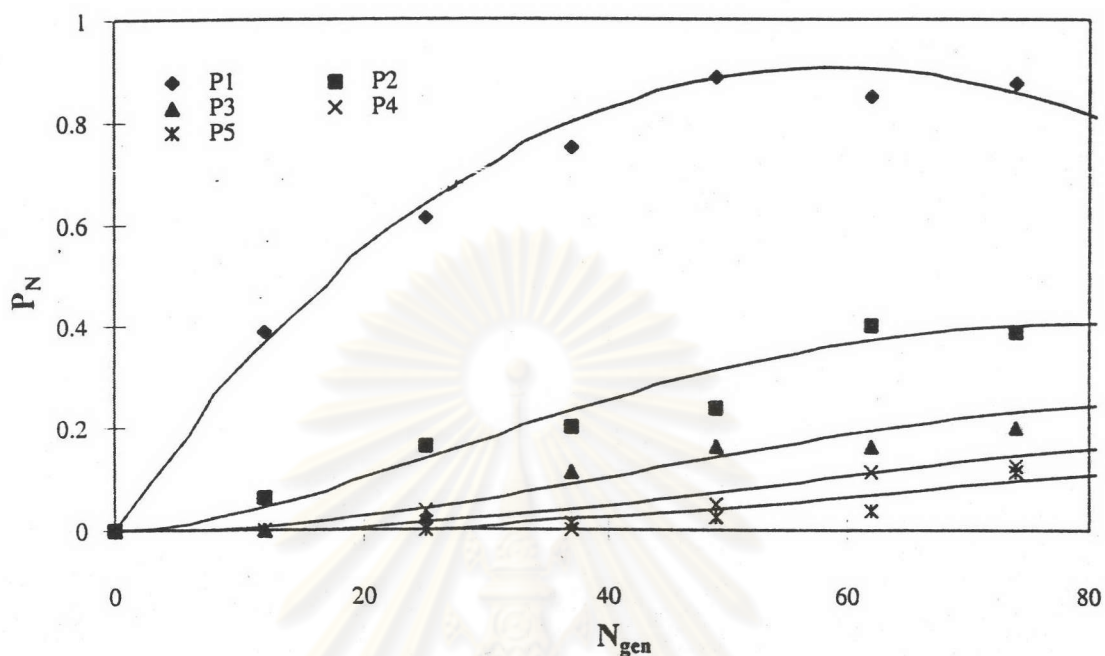


Figure 5.114. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $St=0.6$

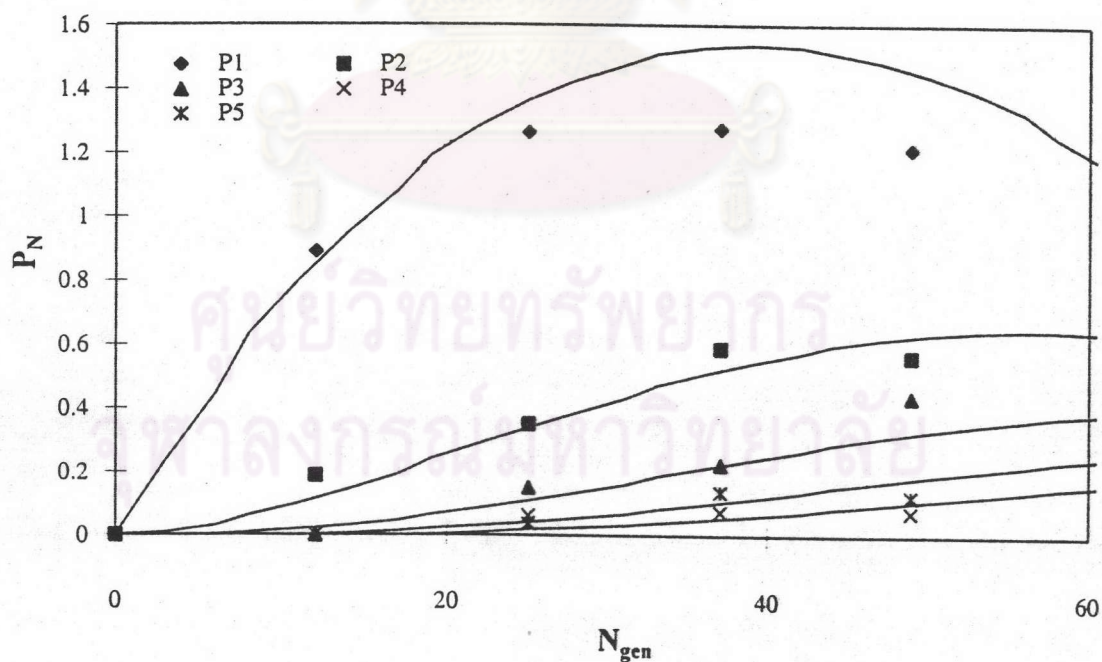


Figure 5.115. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $St=1.0$

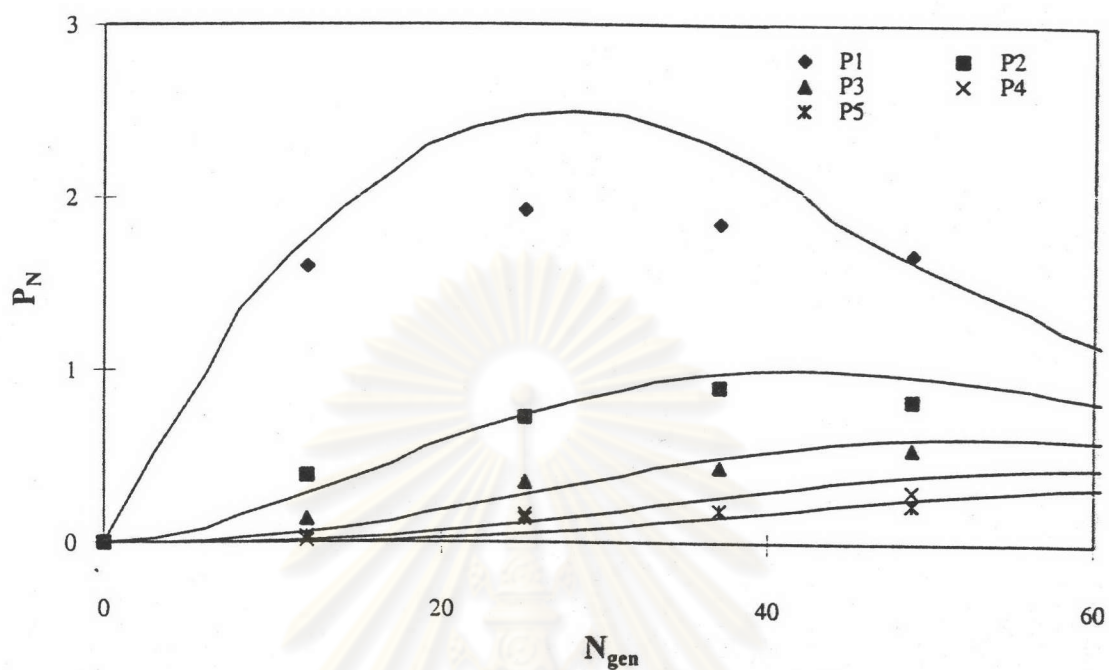


Figure 5.116. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $St=1.4$

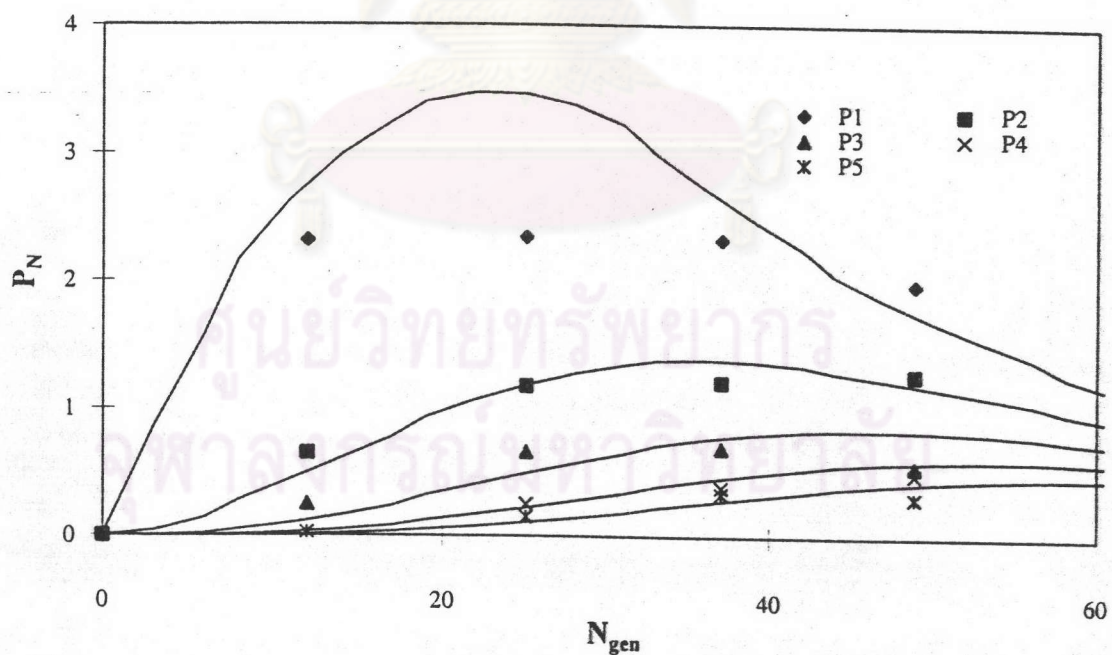


Figure 5.117. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.15$  and  $St=2.0$

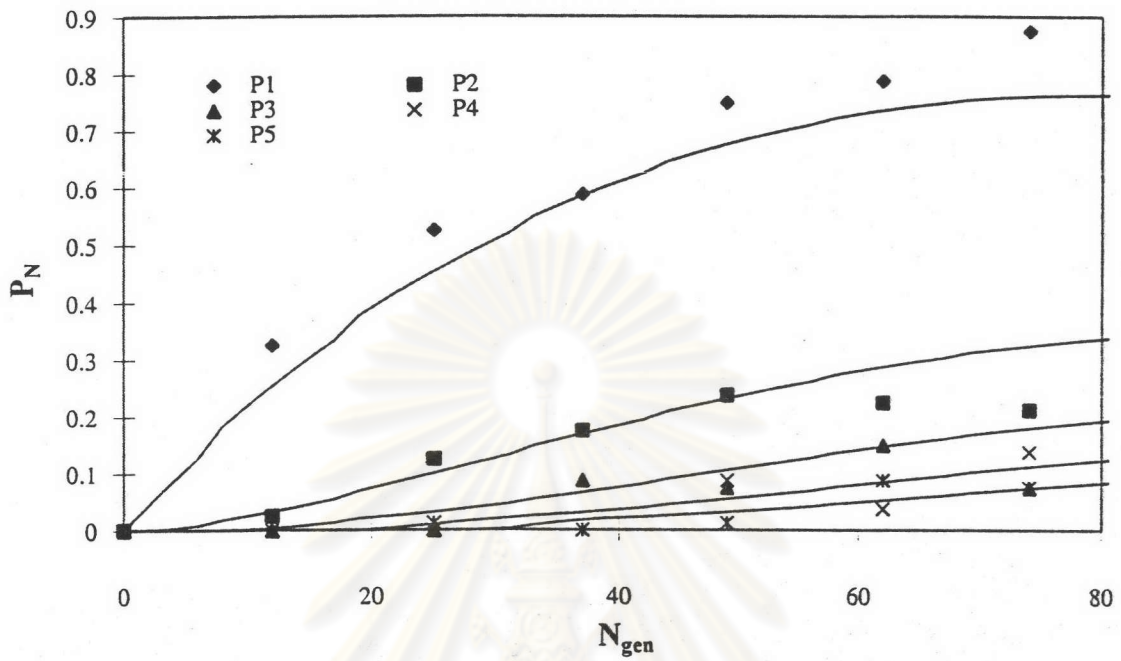


Figure 5.118. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $St=0.0$

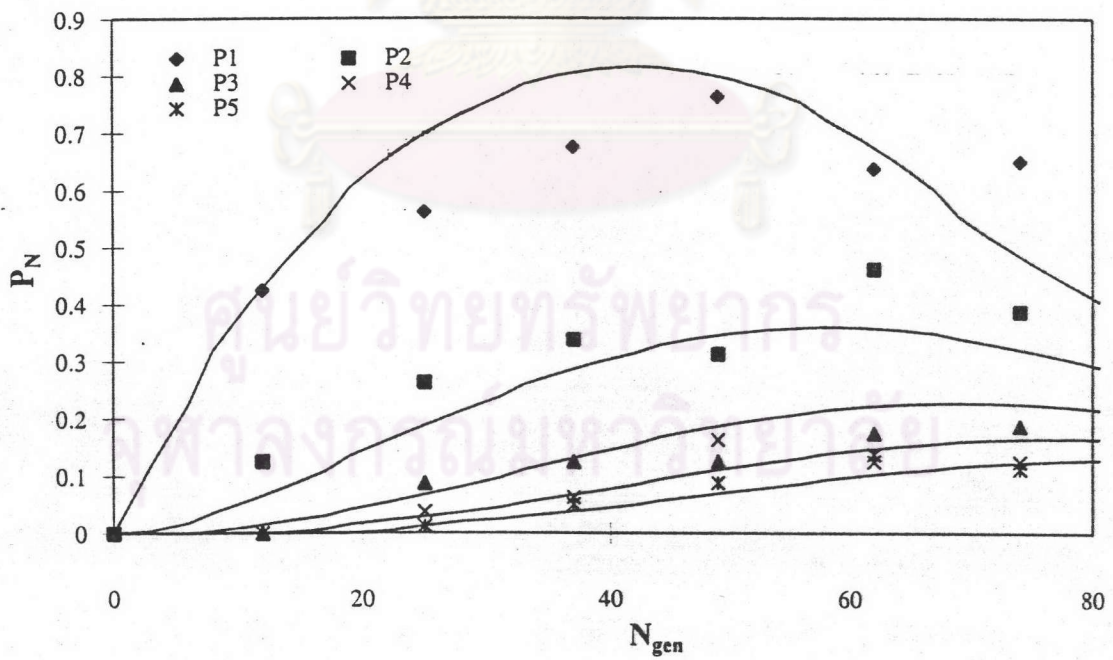


Figure 5.119. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $St=0.6$



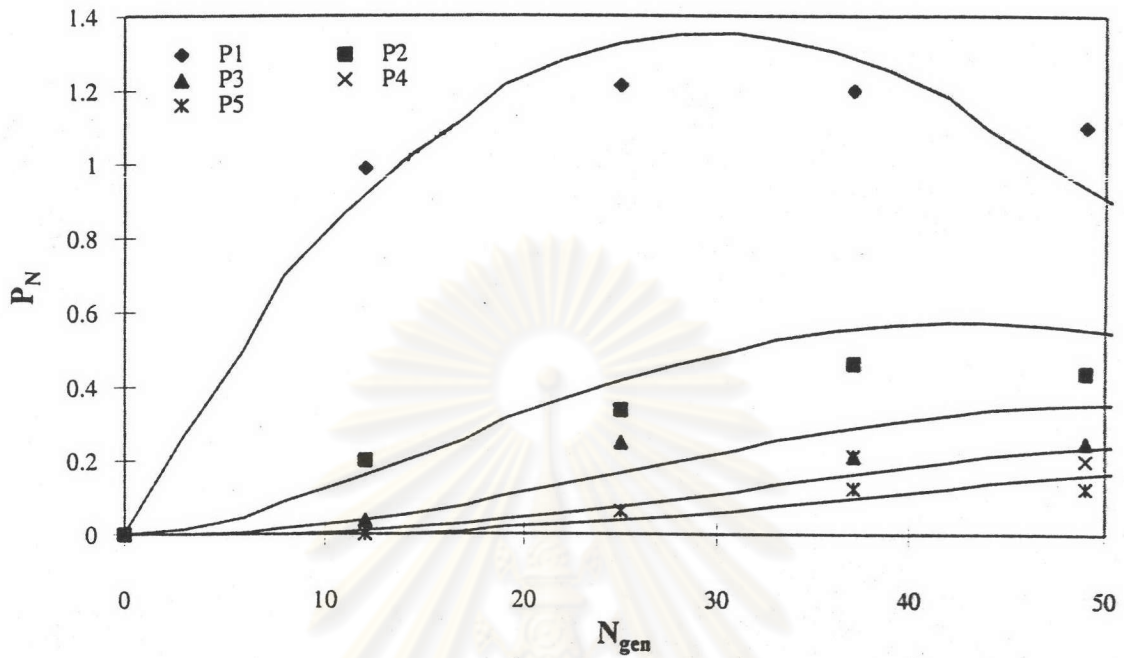


Figure 5.120. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $St=1.0$

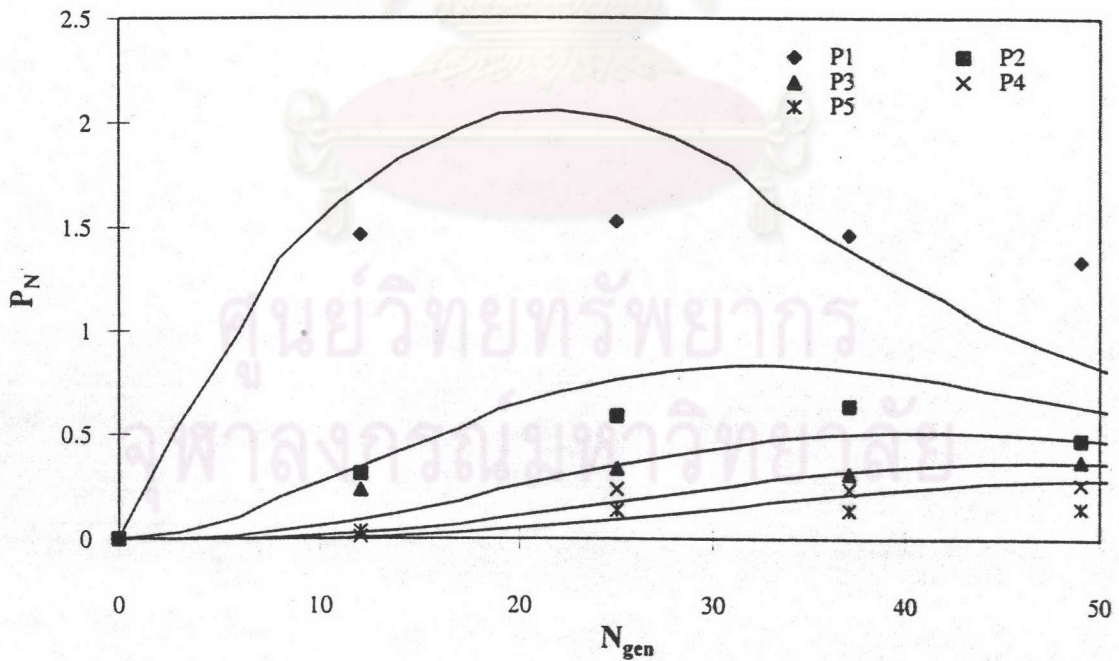


Figure 5.121. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $St=1.4$

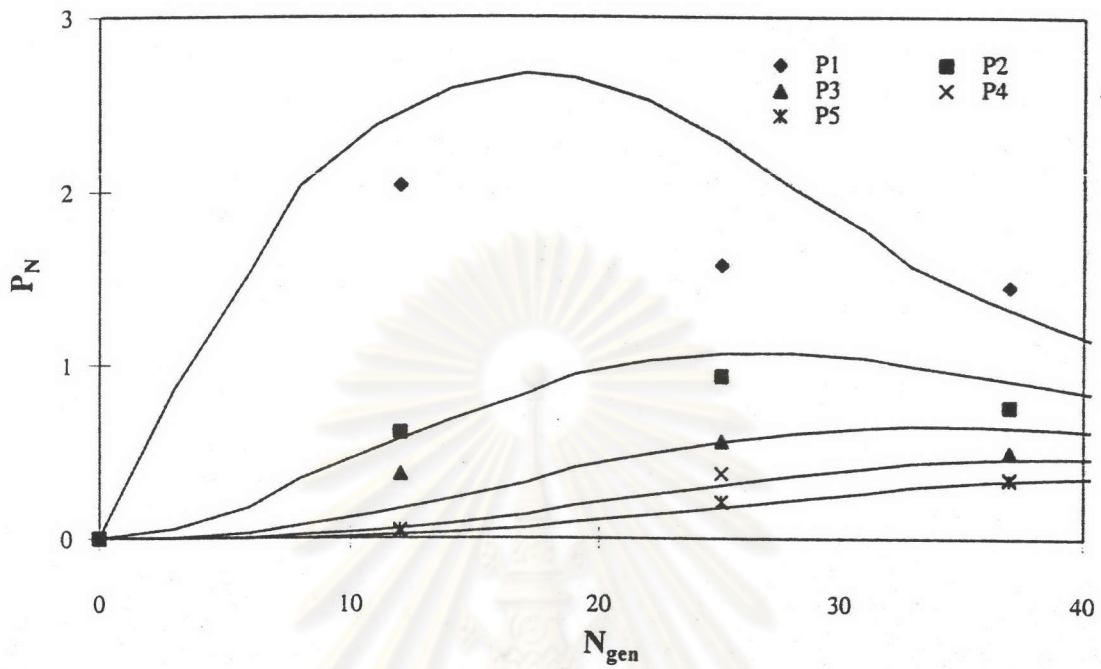


Figure 5.122. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.17$  and  $St=2.0$

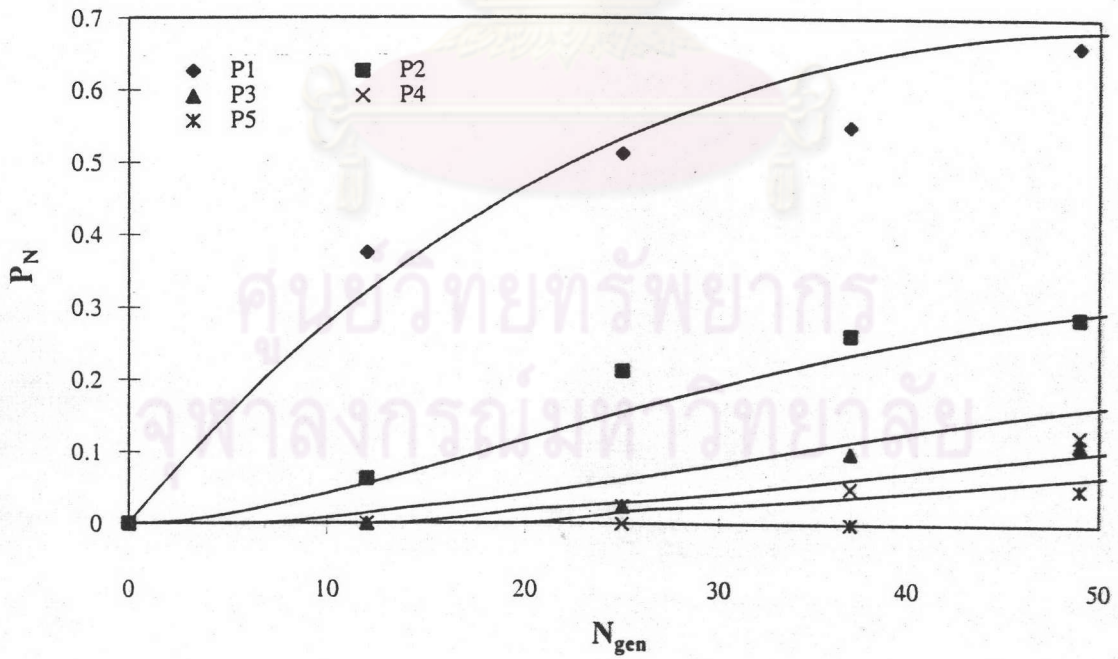


Figure 5.123. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $St=0.0$

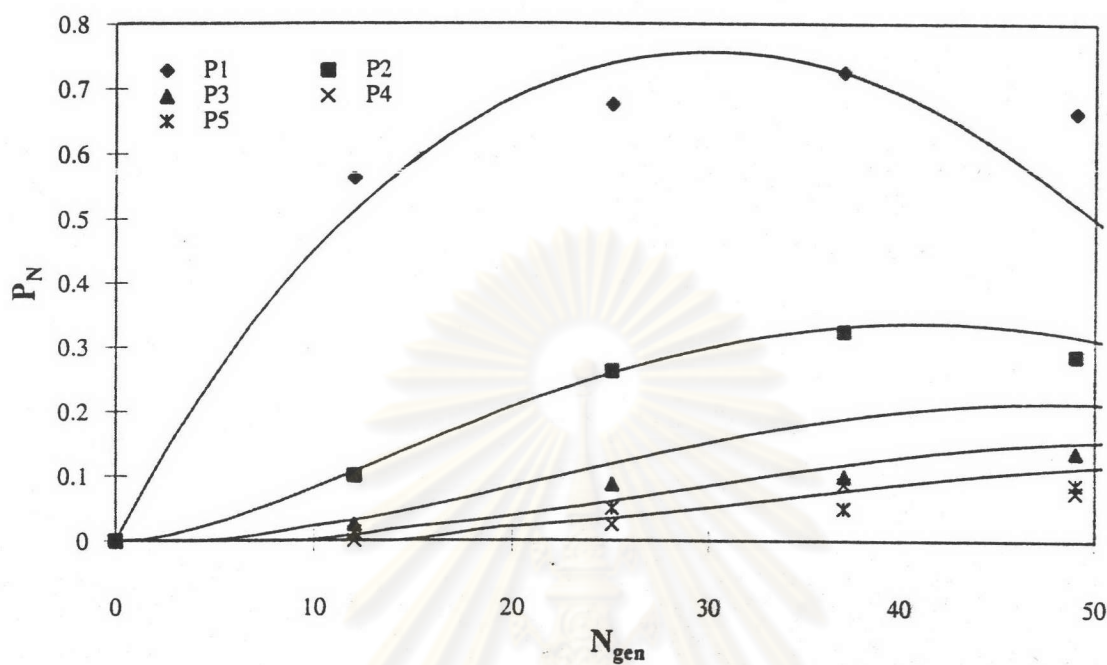


Figure 5.124. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $St=0.6$

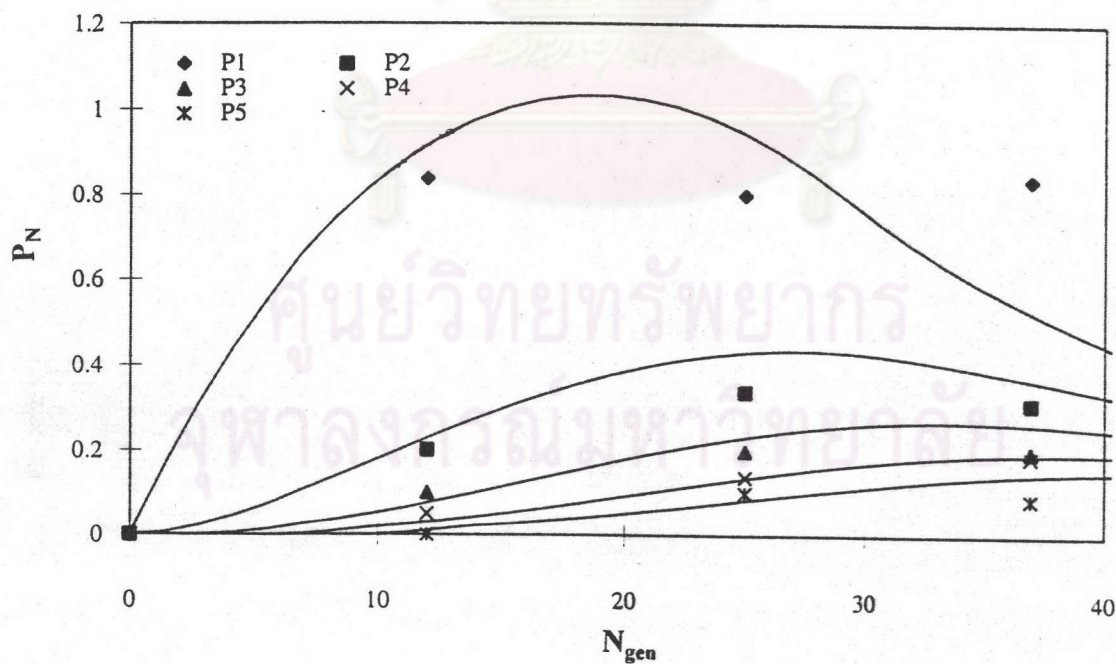


Figure 5.125. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $St=1.0$



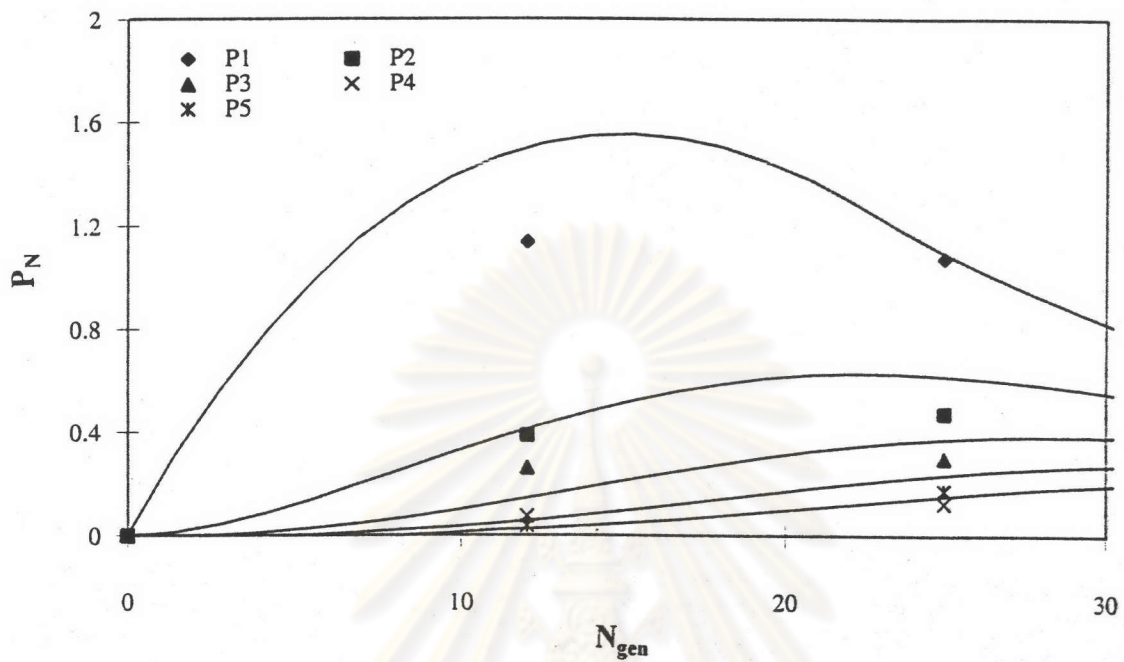


Figure 5.126. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $St=1.4$

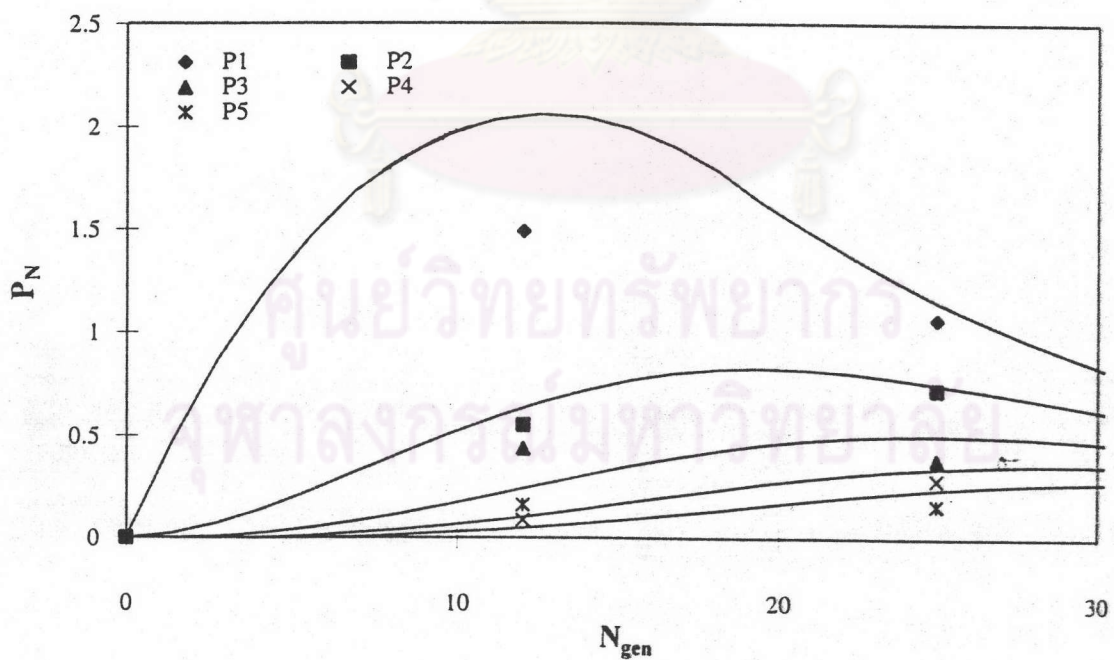


Figure 5.127. Comparison of dendrite distribution between stochastic and simplified model for  $R=0.2$  and  $St=2.0$

dendrites was larger at a small  $R$  and  $Pe$  than a large  $R$  and  $Pe$ . The dendritic growth predicted by the present model agreed quite well with that of the stochastic model at a small  $R$  and fairly well at a large  $R$ .

The values of the parameters  $e_N$  and  $e'_N$  were summarized in Table 5.5. Figures 5.95 and 5.96 show the relationship between  $e_N$  and  $Pe$ , and between  $e'_N$  and  $Pe$ , respectively. The parameters  $e_N$  and  $e'_N$  increased along with  $Pe$  but decreased against  $R$  as the dendrites tended to be more slender and densely packed. However, the present results indicated that the trend of the parameters  $e_N$  and  $e'_N$  for the case  $R=0.05$ , differed from the other cases especially at a low  $Pe$ . The value of  $e_N$  was lower at  $Pe$  less than 2500 but became higher at  $Pe=5000$ . It could be possible that the relatively tiny particles ( $R=0.05$ ) was the threshold particle size below which dendritic formation became difficult and nondistinctive. Thus, the particles might be packed very densely on a fiber at low  $Pe$ . Therefore, the effective captured area increased at a large  $Pe$  and small  $R$ . Figure 5.97 compares the relationship between  $\lambda$  and  $Pe$  with  $R$  as parameter. As seen from the figure, the values of  $\lambda$  agreed well with that of the stochastic model.

### 5.2.2 Inertial impaction deposition

The dendritic growth of inertial impaction was shown in Figures 5.98-5.127. As seen from the figures, as in the case of convective diffusion, the number concentration of dendrites for inertial impaction predicted by the deterministic model increased faster at the initial stage but then dropped faster at the large  $N_{gen}$ . Furthermore, the concentration of dendrites was larger at a small  $R$  and large  $St$  than at a large  $R$  and small  $St$ . The dendritic growth of the present agreed quite well with that of the stochastic model at a small  $R$  but fairly well at a large  $R$ .

The optimal values of the parameters  $e_N$  and  $e'_N$  were summarized in Table 5.6. Figures 5.128 and 5.129 show the relationship between  $e_N$  and  $St$ , and between  $e'_N$  and  $St$ , respectively. The parameter  $e_N$  and  $e'_N$  decreased along with  $St$  and  $R$ . Thus the effective capturing area was smaller as  $St$  and  $R$  increased because the dendrites tended to be shorter and more loosely packed. The relationship of  $\lambda$  vs.  $\eta_0$  obtained from the present deterministic study is compared with some published experimental



Table 5.6 Optimal value of the parameters  $e_N$  and  $e'_N$  for inertial impaction 103

St	R	0.05	0.1	0.13	0.15	0.17	0.2
0	en	179.756	37.119	24.832	17.280	16.095	12.795
	en'	121.851	4.863	0.541	0.320	1.038	0.902
	Lamda	57.905	16.128	9.343	5.653	4.429	2.973
	Obj fun	0.266	0.378	0.545	0.460	0.351	0.155
	Obj fun/point	0.002	0.007	0.012	0.013	0.012	0.008
0.6	en	59.434	17.453	15.233	13.597	11.293	9.197
	en'	19.238	3.849	2.992	2.771	2.669	1.853
	Lamda	40.196	6.802	4.708	3.608	2.537	1.836
	Obj fun	0.141	0.467	0.194	0.198	0.310	0.310
	Obj fun/point	0.001	0.008	0.004	0.006	0.010	0.015
1	en	26.316	10.336	7.305	6.299	5.717	5.288
	en'	13.640	5.010	3.460	2.739	2.312	2.287
	Lamda	12.676	2.663	1.479	1.187	1.002	0.750
	Obj fun	2.195	0.597	1.035	0.927	0.870	0.813
	Obj fun/point	0.020	0.011	0.023	0.026	0.029	0.041
1.4	en	5.118	3.853	3.511	3.333	3.244	3.072
	en'	4.214	2.676	2.346	2.148	1.940	1.887
	Lamda	0.903	0.588	0.448	0.395	0.383	0.296
	Obj fun	7.972	1.744	2.791	2.429	2.449	1.322
	Obj fun/point	0.072	0.032	0.062	0.069	0.082	0.066
2	en	3.083	2.475	2.327	2.275	2.311	2.199
	en'	2.761	2.006	1.747	1.644	1.643	1.528
	Lamda	0.322	0.234	0.223	0.210	0.196	0.168
	Obj fun	14.530	4.396	5.271	3.988	3.497	1.679
	Obj fun/point	0.132	0.080	0.117	0.114	0.117	0.084
Ngen		1000	500	400	350	300	200
No. point		110	55	45	35	30	20



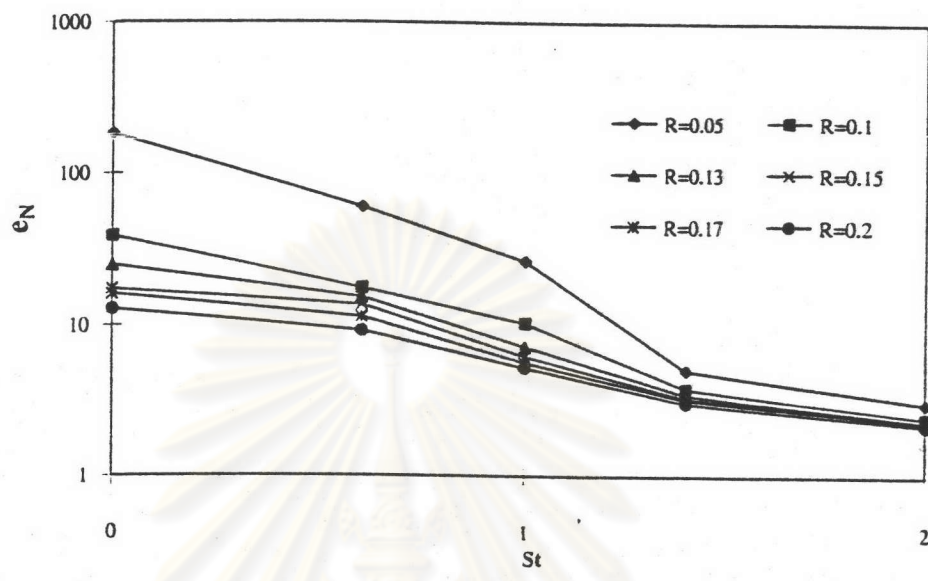


Figure 5.128. Relationship between the parameter  $e_N$  and  $St$

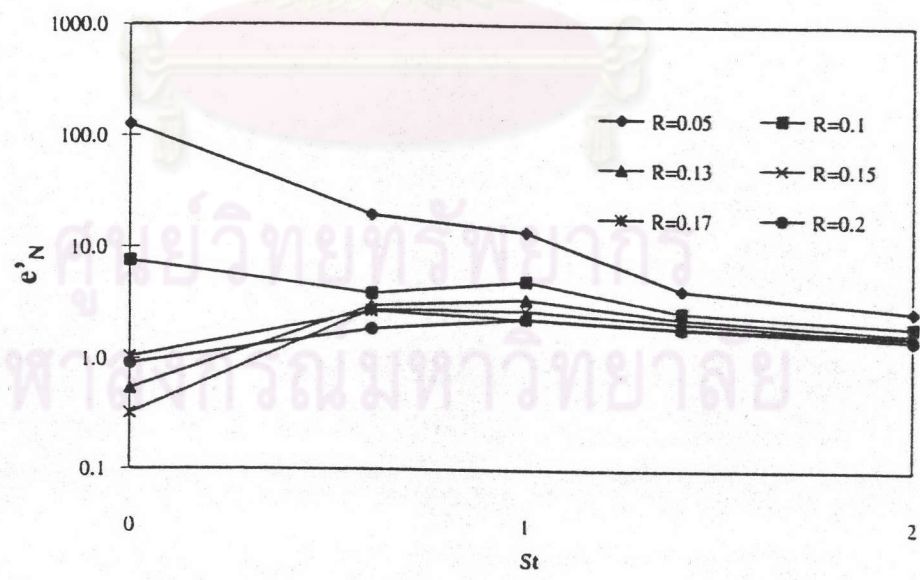


Figure 5.129. Relationship between the parameter  $e'_N$  and  $St$

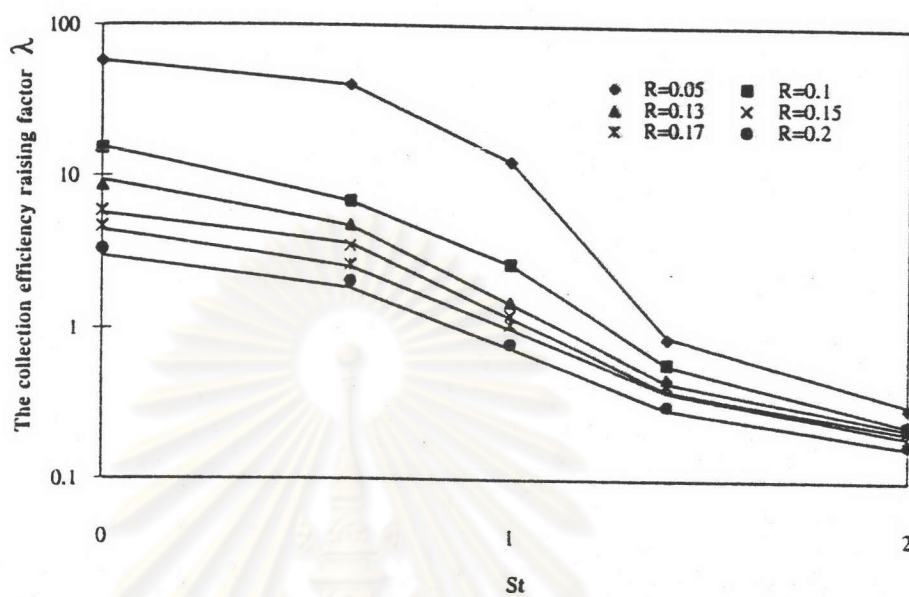


Figure 5.130. Comparison of  $\lambda$  between stochastic and simplified models for inertial impaction  
 (The dots are stochastic results, the lines are deterministic ones)

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results (Kimura et al., 1964, Yoshioka et al., 1969, and Myojo et al., 1984), as shown in Figure 5.131 a and b. Clearly the trend of the relationship obtained from this work is quite similar to the experimental one. As seen from Figure 5.131b,  $\lambda$  decreases while  $\eta_0$  increased as  $St$  increases. Table 5.7 reveals certain differences between the experimental results and the deterministic predictions. The predictions are about 103% higher than the experimental results because the configuration of the experimental filter is more complicated than the idealized filter in which all fibers lie parallel to one another. Moreover, re-entrainment and bridging of dendrites between dust-loaded fibers may occurred in the experimental study but are not taken into account in the simulation study.

It is obvious that the collection mechanism reduces to pure interception at  $Pe=\infty$  or  $St=0$ . Therefore the simulation results of  $Pe=\infty$  should equal those of  $St=0$ . The parameter  $e_N$  and  $\lambda$  for  $Pe=5000$  were slightly smaller than their counterparts for at  $St=0$ . In contrast, the parameter  $e'_N$  for  $Pe=5000$  was higher than that  $St=0$ . The reason for this discrepancy is that even at  $Pe=5000$  there remains appreciable diffusion effect. Theoretically speaking, as  $Pe$  approaches infinity, the values of  $e_N$  and  $e'_N$  of both cases should become identical.

The deterministic model has been shown to predict the dendrite distribution and the collection efficiency of the dust-loaded fiber which are in good agreement with the stochastic model for both the case of convective diffusion and inertial impaction. Table 5.8 shows the size of computer memory required to run deterministic and stochastic simulations. Tables 5.9 and 5.10 show the actual simulation times used in stochastic simulation for convective diffusion and inertial impaction, respectively. Tables 5.11 and 5.12 show the actual simulation times required by the simplified model for convective diffusion and inertial impaction, respectively. As seen from the tables, the simplified model required much less computer memory and much shorter computational time than the stochastic model at the same filtration conditions.

### 5.2.3 The contours of $\eta_0$ and $\lambda$ with respect to particle size and air velocity

The deterministic model was used to predict  $\eta_0$  and  $\lambda$  under various filtration conditions for the case of convective diffusion and inertial impaction. The



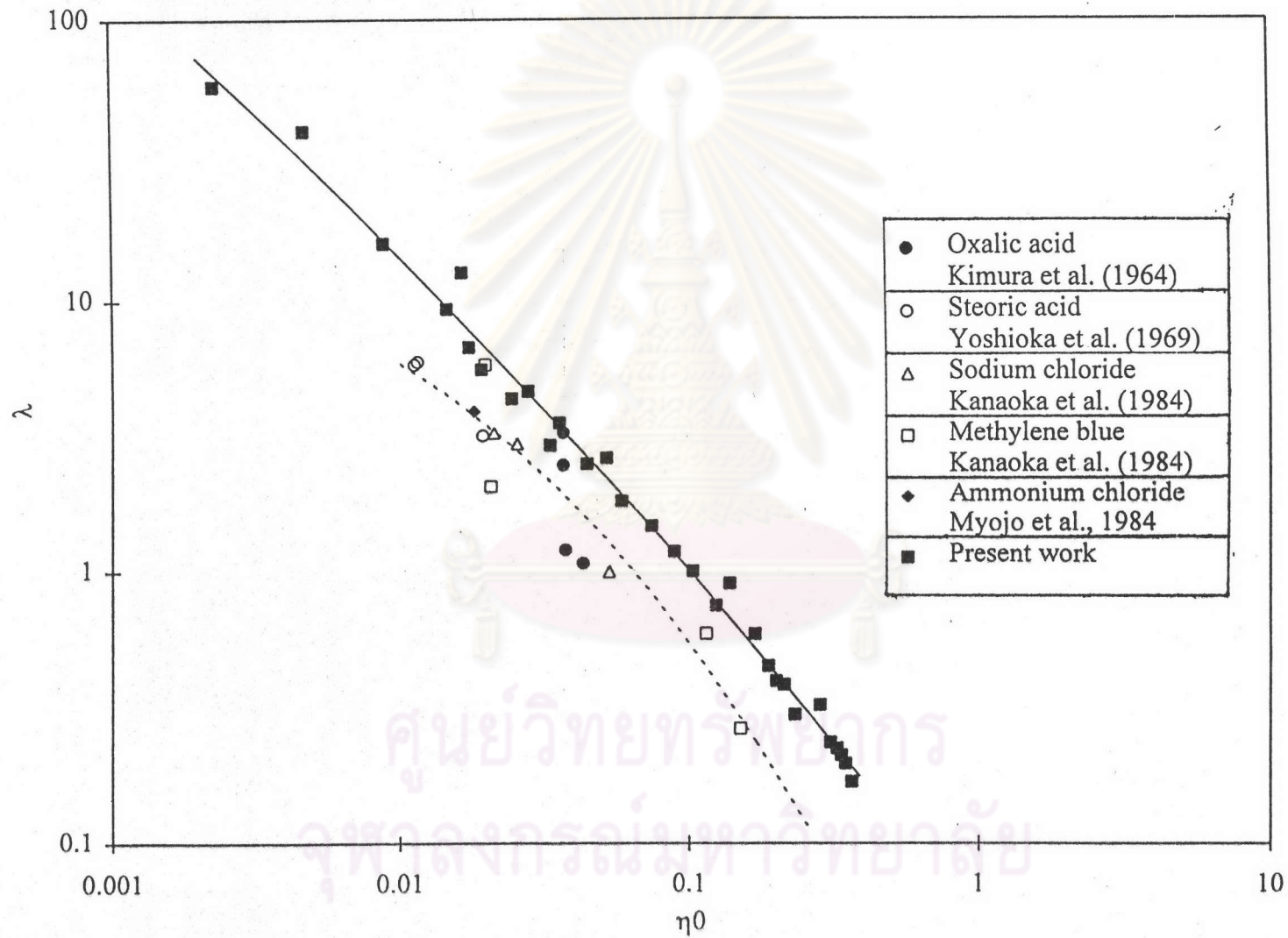


Figure 5.131a Comparison of  $\lambda$  vs.  $\eta_0$  between the deterministic results and experimental results

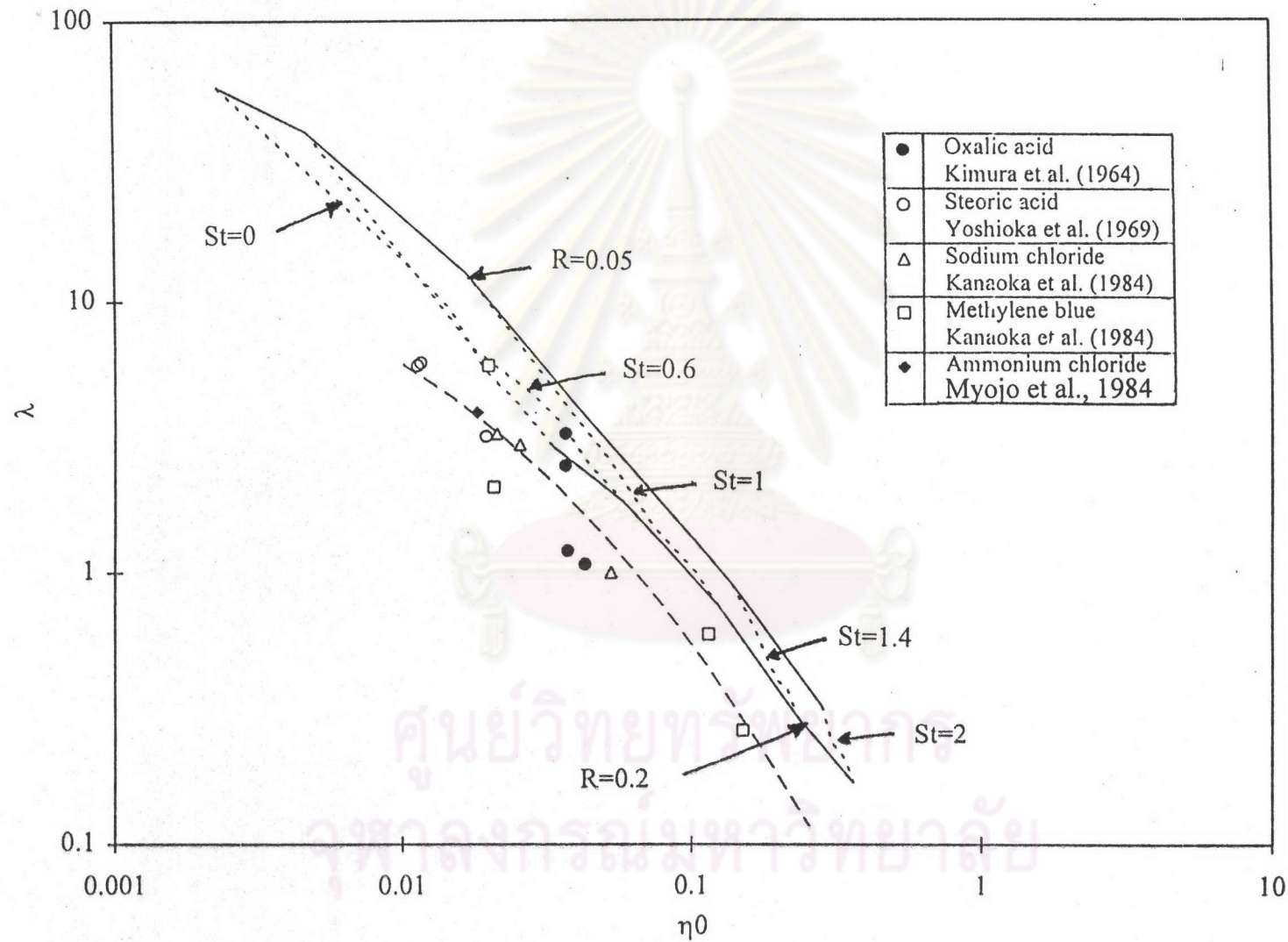


Figure 5.131b Comparison of  $\lambda$  vs.  $\eta_0$  between the deterministic results and experimental results with  $St$  and  $R$  as parameters

Table 5.7 Comparison between the experimental and the predicted values of  $\lambda$ 

range	$\eta_0$	$\lambda$ - exp	$\lambda$ - present	error(%)
1	0.010	5.96	14.40	142
2	0.015	4.50	9.27	106
3	0.023	3.20	5.90	84
4	0.034	2.14	3.71	73
5	0.051	1.35	2.30	71
6	0.076	0.80	1.41	76
7	0.114	0.45	0.86	92
8	0.171	0.23	0.51	119
9	0.256	0.12	0.30	162
error-avg(%)=				103

Table 5.8 Computer memory required to run deterministic and stochastic simulations

Required computer memory			
Deterministic		Stochastic	
181104	bit	49893056	bit
22638	byte	6236632	byte
22	KB	6090	KB



Table 5.9 Actual simulation time used in stochastic simulation (convective diffusion)

Pe	R					
	0.05	0.1	0.13	0.15	0.17	0.2
200	0:24:32	0:02:54	0:01:34	0:01:08	0:00:52	0:01:34
500	0:27:00	0:03:24	0:01:52	0:01:18	0:00:58	0:00:42
1000	0:34:34	0:03:40	0:01:54	0:01:20	0:01:00	0:00:40
2500	0:48:38	0:04:08	0:02:06	0:01:32	0:01:06	0:00:44
5000	0:50:32	0:04:20	0:02:18	0:01:32	0:01:12	0:00:42

Table 5.10 Actual simulation time used in stochastic simulation (inertial impaction)

St	R					
	0.05	0.1	0.13	0.15	0.17	0.2
0.0	1:18:58	0:25:24	0:12:28	0:22:42	0:12:22	0:10:52
0.6	0:25:18	0:18:24	0:09:24	0:16:48	0:12:14	0:08:06
1.0	0:15:24	0:19:06	0:06:48	0:12:40	0:08:24	0:06:10
1.4	0:09:24	0:09:22	0:05:04	0:09:42	0:07:22	0:05:14
2.0	0:05:00	0:07:22	0:04:06	0:08:04	0:06:08	0:04:26

Table 5.11 Actual simulation time used by the simplified model (convective diffusion)

Pe	R					
	0.05	0.1	0.13	0.15	0.17	0.2
200	0:00:15	0:00:08	0:00:08	0:00:08	0:00:08	0:00:06
500	0:00:15	0:00:08	0:00:08	0:00:08	0:00:07	0:00:05
1000	0:00:14	0:00:08	0:00:08	0:00:07	0:00:07	0:00:05
2500	0:00:14	0:00:08	0:00:08	0:00:08	0:00:07	0:00:05
5000	0:00:15	0:00:08	0:00:08	0:00:07	0:00:07	0:00:04

Table 5.12 Actual simulation time used by the simplified model (inertial impaction)

St	R					
	0.05	0.1	0.13	0.15	0.17	0.2
0.0	0:00:17	0:00:10	0:00:08	0:00:06	0:00:06	0:00:05
0.6	0:00:17	0:00:09	0:00:08	0:00:07	0:00:06	0:00:04
1.0	0:00:17	0:00:10	0:00:08	0:00:08	0:00:07	0:00:06
1.4	0:00:18	0:00:11	0:00:09	0:00:10	0:00:08	0:00:06
2.0	0:00:22	0:00:12	0:00:10	0:00:10	0:00:09	0:00:06

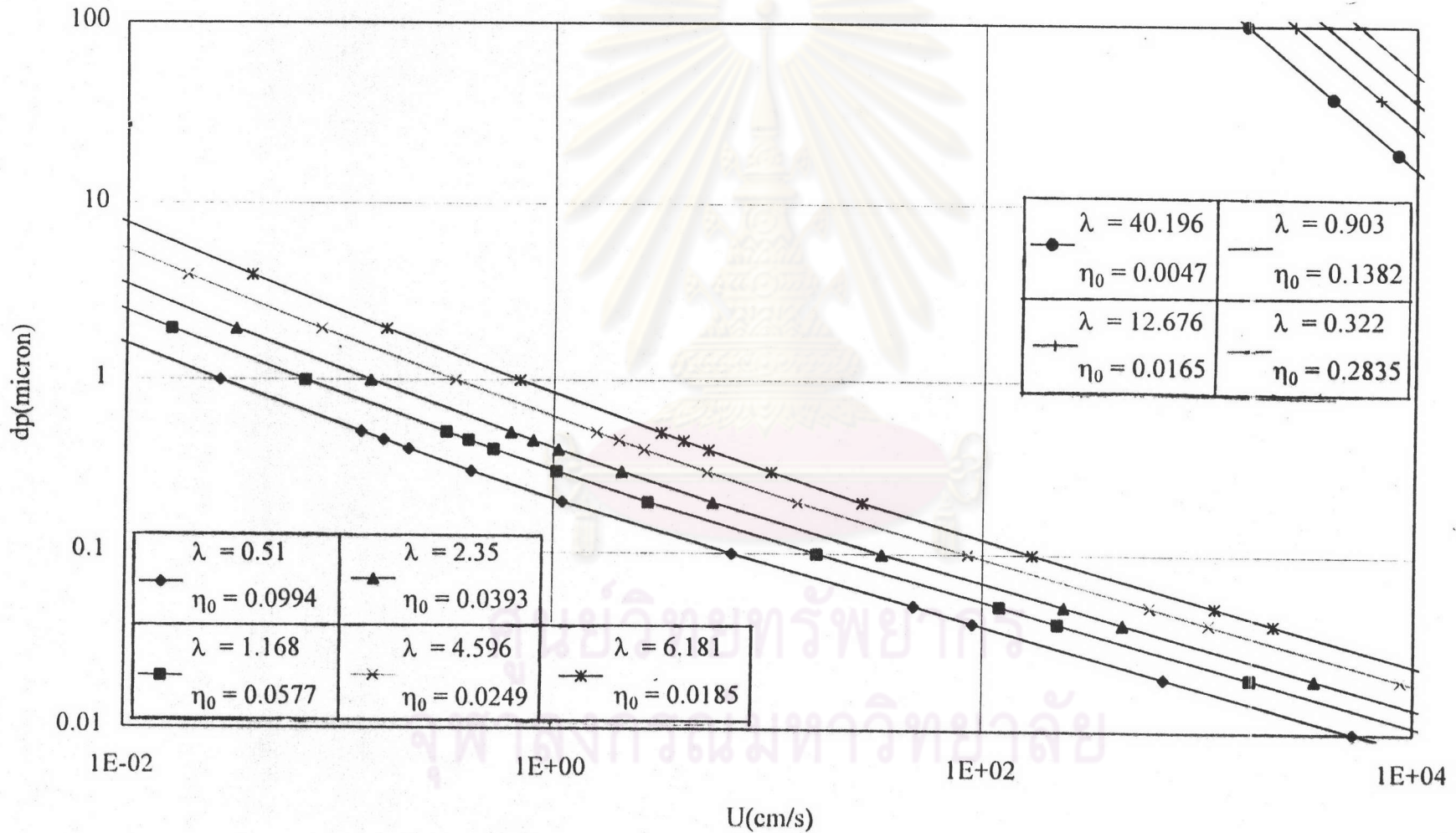


Figure 5.132 Relationship between  $d_p$  and  $U_\infty$  with  $\eta_0$  and  $\lambda$  as parameter for  $R=0.05$



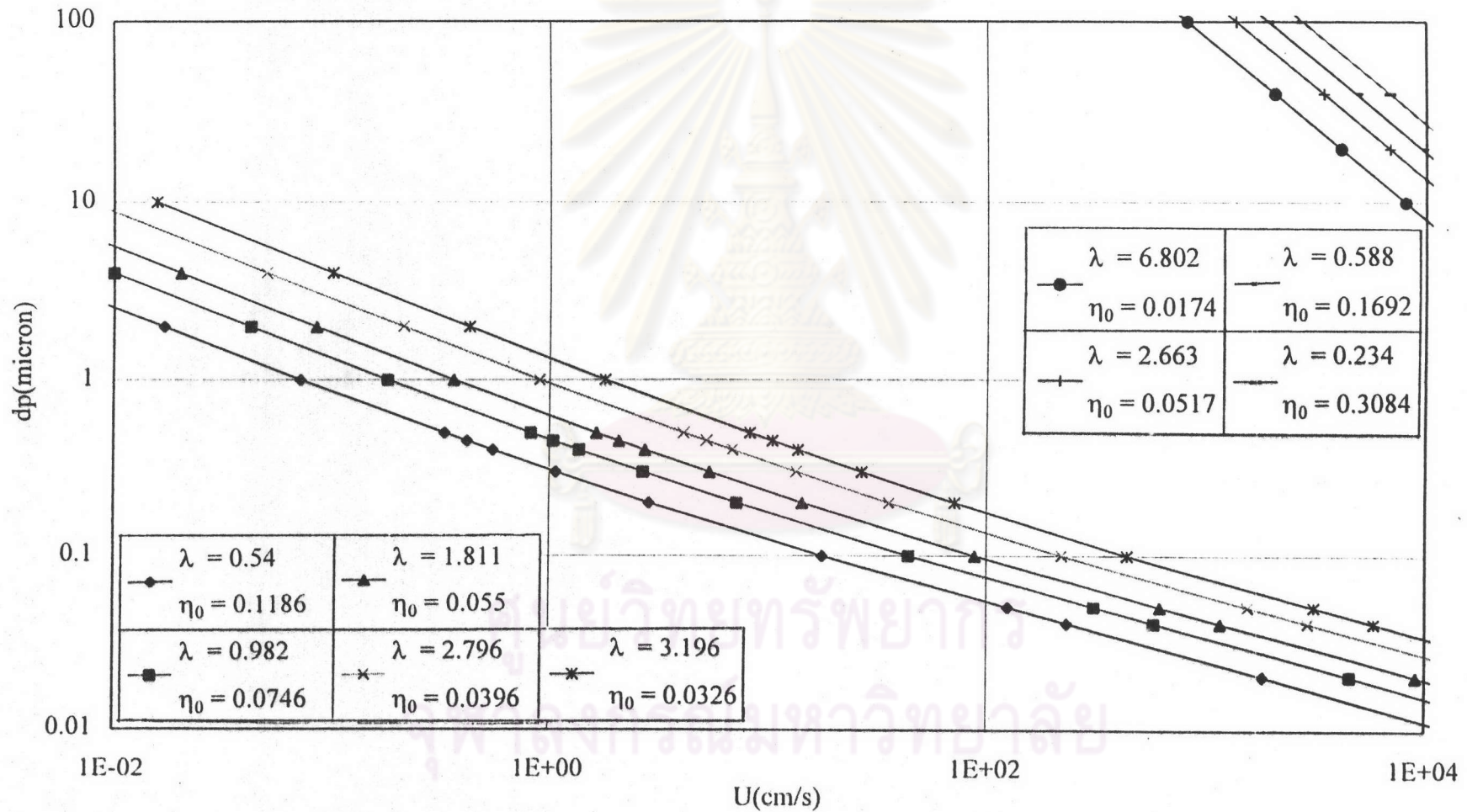


Figure 5.133 Relationship between  $d_p$  and  $U_w$  with  $\eta_0$  and  $\lambda$  as parameter for  $R=0.1$



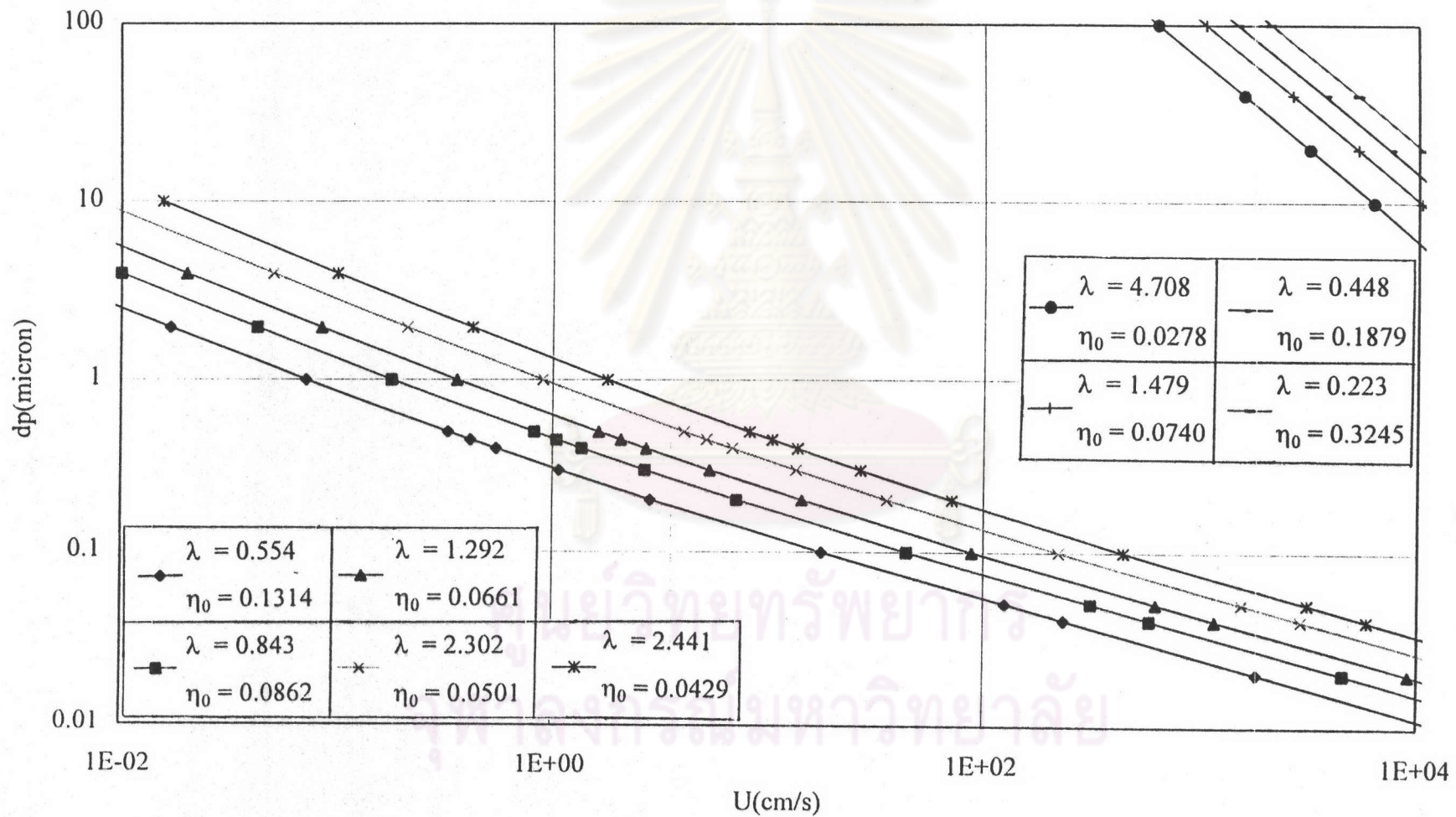


Figure 5.134 Relationship between  $d_p$  and  $U_\infty$  with  $\eta_0$  and  $\lambda$  as parameter for  $R=0.13$

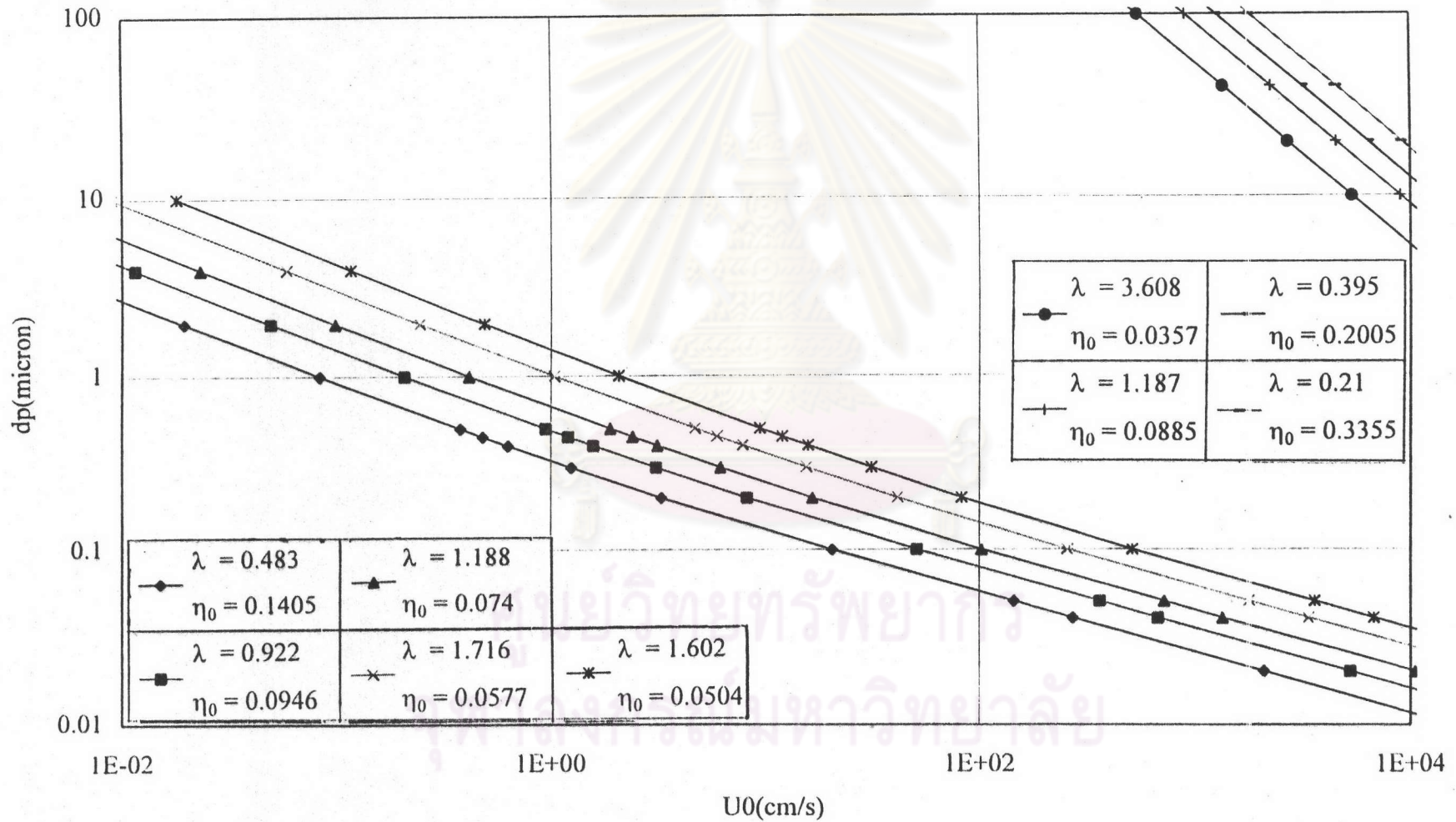


Figure 5.135 Relationship between  $d_p$  and  $U_\omega$  with  $\eta_0$  and  $\lambda$  as parameter for  $R=0.15$

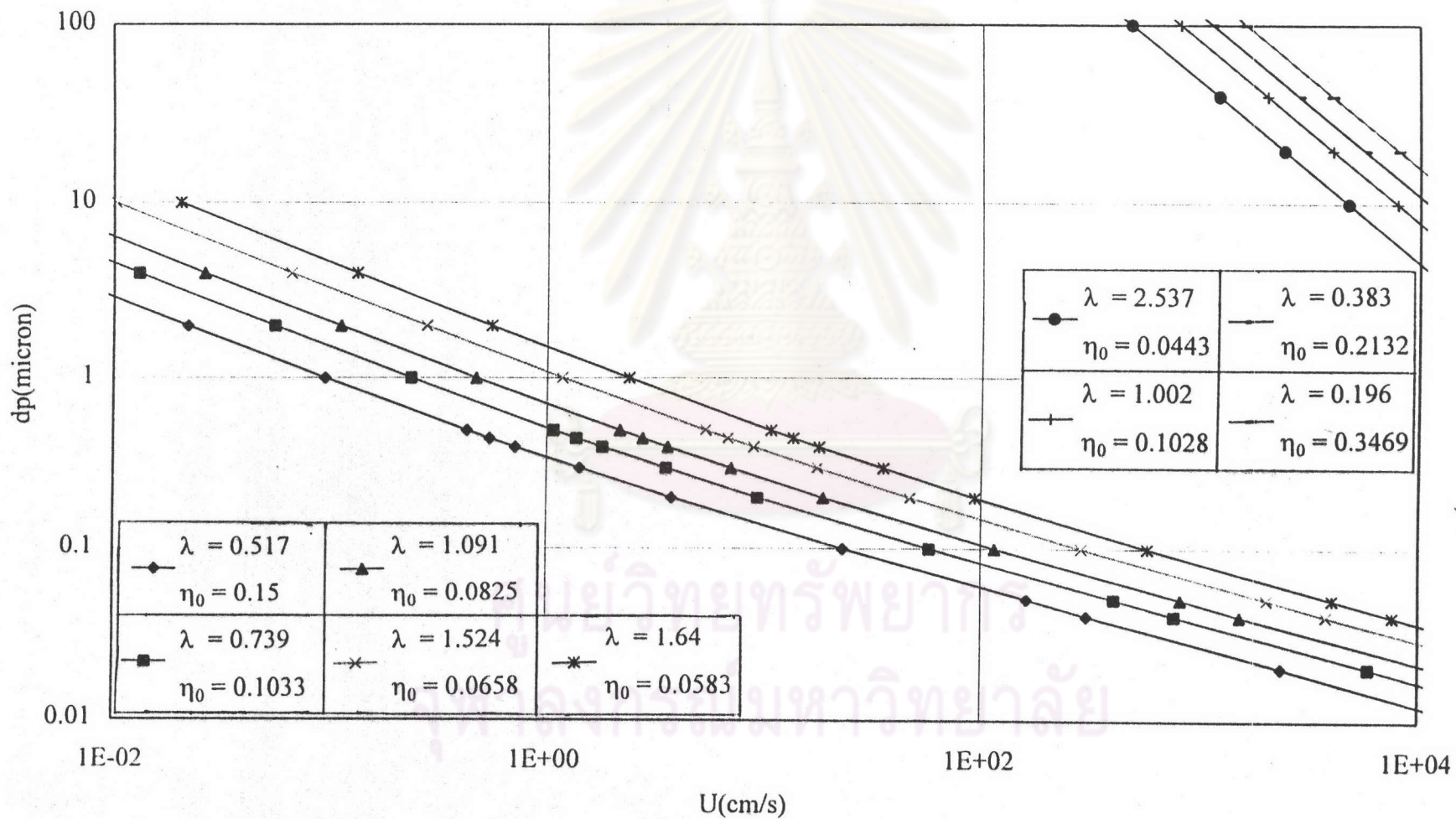


Figure 5.136 Relationship between  $d_p$  and  $U_\infty$  with  $\eta_0$  and  $\lambda$  as parameter for  $R=0.17$



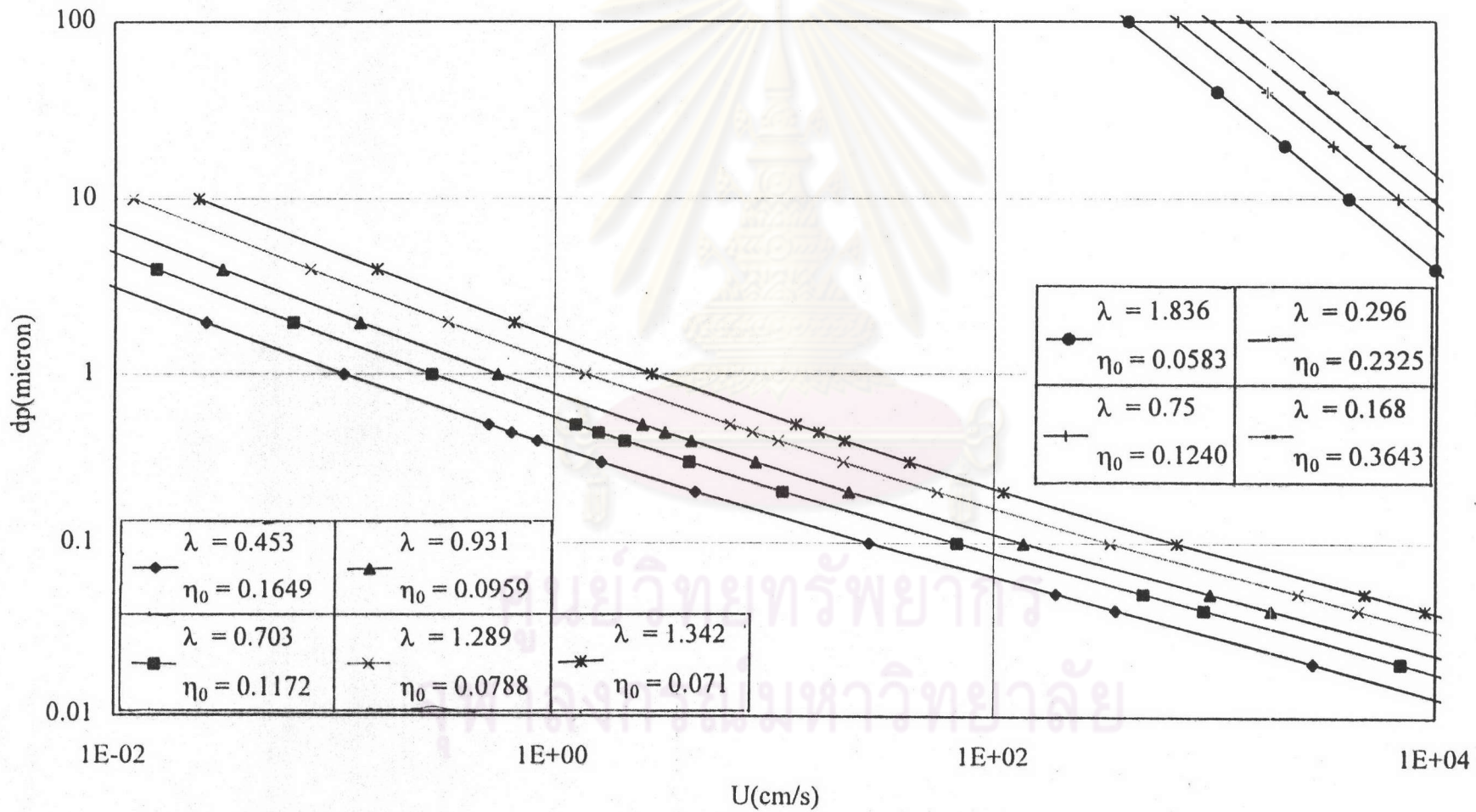


Figure 5.137 Relationship between  $d_p$  and  $U_w$  with  $\eta_0$  and  $\lambda$  as parameter for  $R=0.2$

dimensionless parameters such as  $R$ ,  $Pe$  and  $St$  were rewritten and solved for the air velocity and particle size. Thus the air velocity  $U_\infty$  could be expressed in terms the dimensionless variables  $Pe$  and  $St$ , respectively.

For convective diffusion

$$U_\infty = \frac{PeD_{BM}}{d_f} \quad (5.1)$$

For inertial impaction

$$U_\infty = \frac{9\mu d_f St}{C_m \rho_p d_p^2} \quad (5.2)$$

The contours of the clean fiber collection efficiency  $\eta_0$  and the collection efficiency raising factor  $\lambda$  were then plotted with respect to  $d_p$  and  $U_\infty$ . The clean fiber collection efficiency calculated from Stechkina and Fuchs's equation for convective diffusion and limiting trajectory theory for inertial impaction, respectively. Figures 5.132-5.137 show the relationships between  $d_p$  and  $U_\infty$  with  $\eta_0$  and  $\lambda$  as parameters for various  $R$ . As seen from the figures,  $\lambda$  increased but  $\eta_0$  decreased at a large  $d_p$  and  $U_\infty$  in the case of convective diffusion. On the other hand,  $\lambda$  increased but  $\eta_0$  decreased at a small  $d_p$  and  $U_\infty$  in the case of inertial impaction. Hence  $\lambda$  and  $\eta_0$  can be estimated quickly from these figures.

### 5.3 The behavior of the deterministic model

The average dendritic growth was already calculated under various filtration conditions for convective diffusion and inertial impaction by using the deterministic model. To see the individual effect of the parameters  $e_N$  and  $e'_N$ , as well as the dimensionless groups  $R$ ,  $Pe$ ,  $St$ , on the model behavior, the dendrite distribution, the average dendrite size, the total population of dendrites,  $\lambda$ , and  $\eta$  were plotted against  $N_{gen}$  (corresponding to filtration time) which varying slightly each of the parameters or groups.

#### 5.3.1 Convective diffusion

The effects of the parameters  $e_N$  and  $e'_N$ , the Peclet number  $Pe$  and the interception parameter  $R$  on the dendrite distribution, the average dendrite size, the

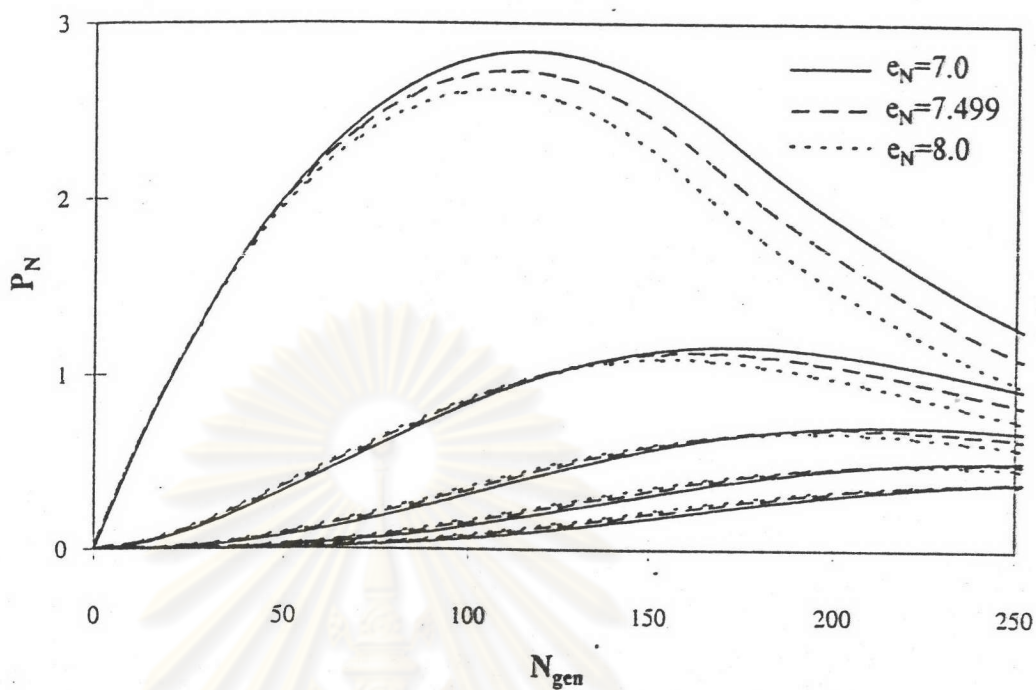


Figure 5.138 Dendrite distribution for convective diffusion of  $R=0.1$ ,  $Pe=1000$ , and  $e'_N=3.877$

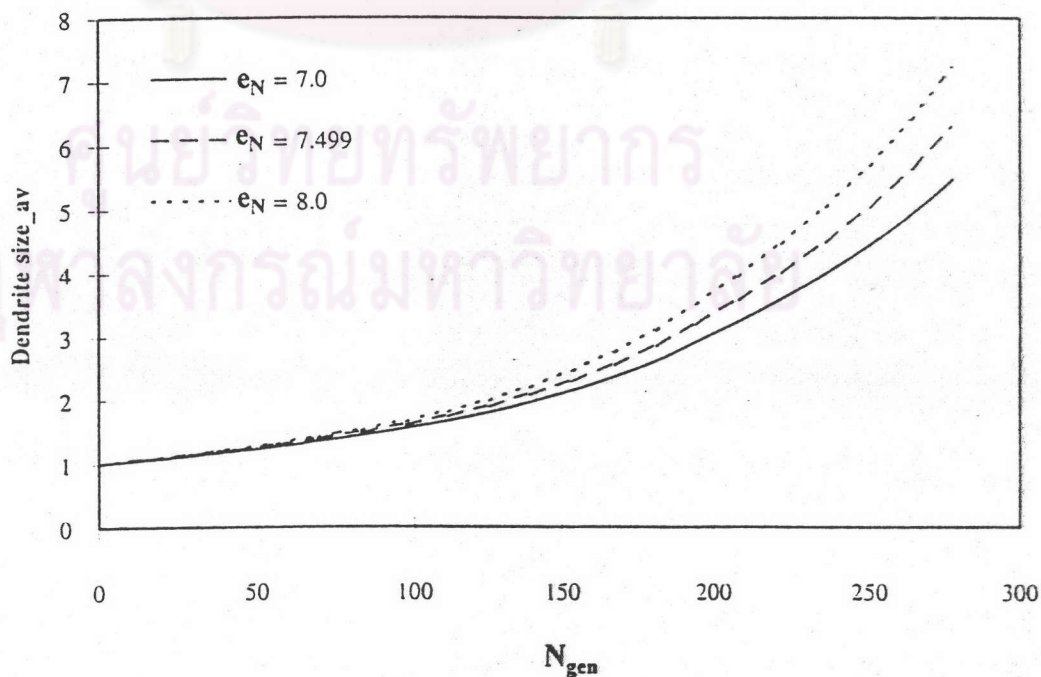


Figure 5.139 Dendrite average size for convective diffusion of  $R=0.1$ ,  $Pe=1000$ , and  $e'_N=3.877$



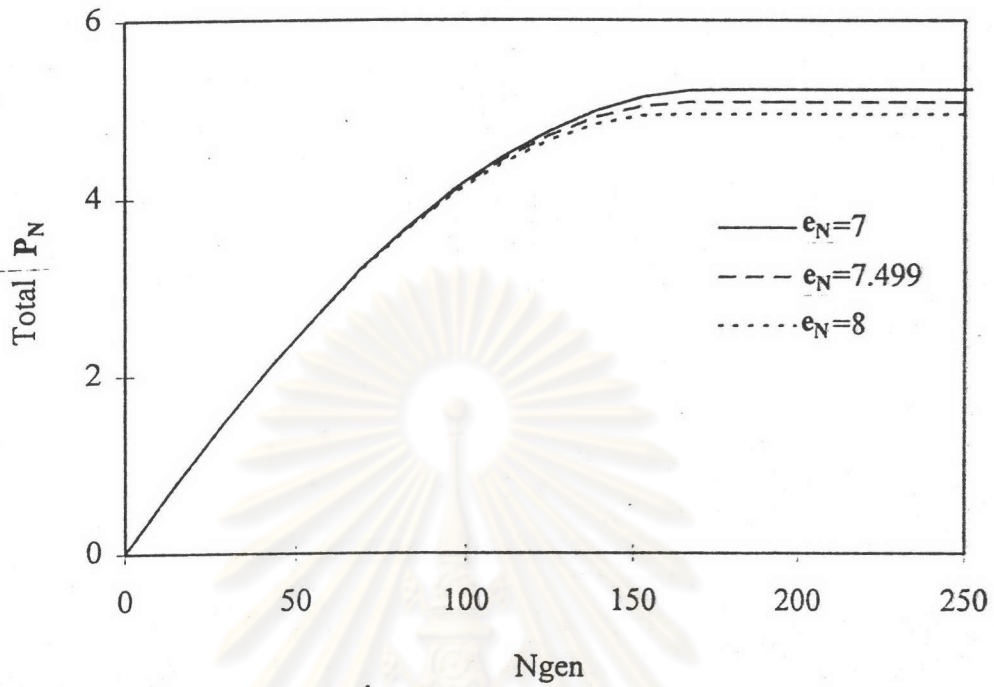


Figure 5.140 Total population of dendrites for convective diffusion  
( $R=0.1$ ,  $Pe=1000$  and  $e'_N=3.877$ )

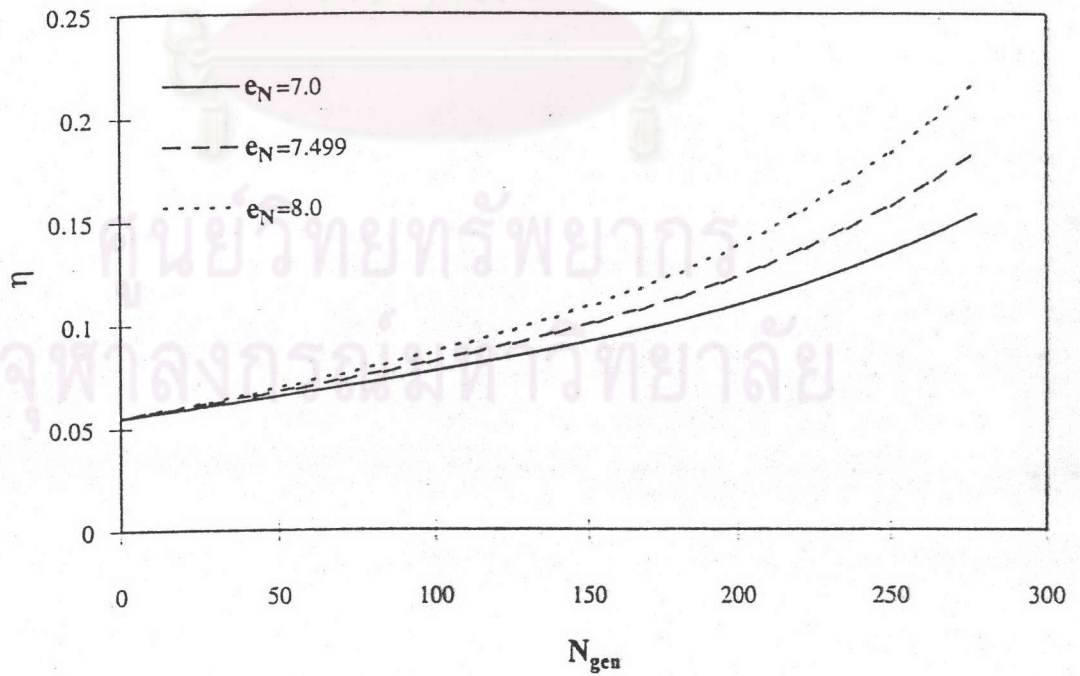


Figure 5.141 Collection efficiency for convective diffusion of  $R=0.1$ ,  $Pe=1000$ ,  
and  $e'_N=3.877$ .

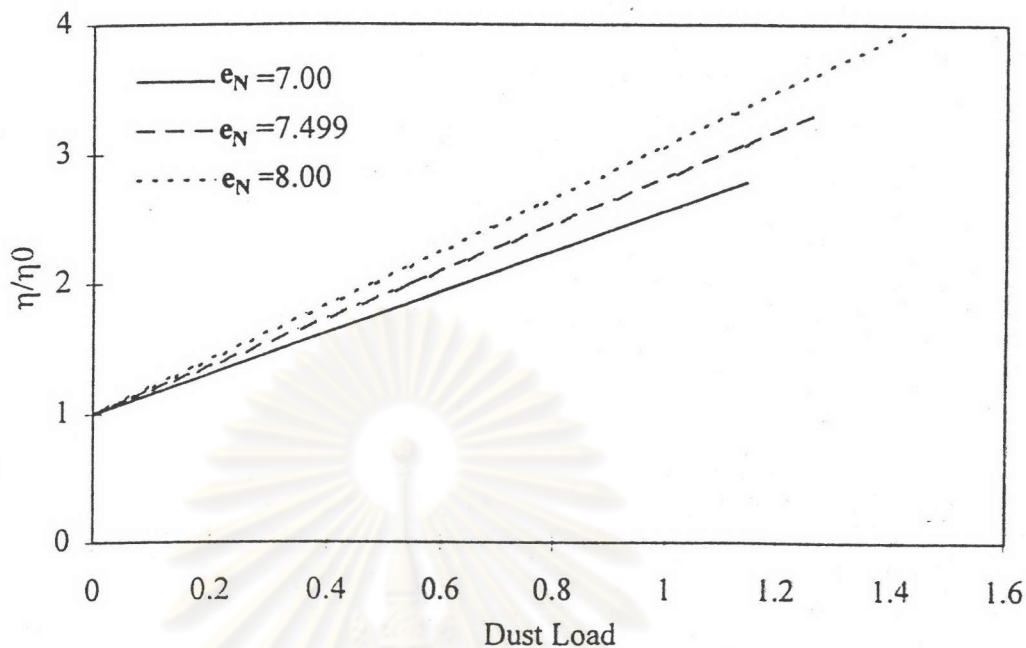


Figure 5.142 Normalized collection efficiency of dust load for  $R=0.1$ ,  $Pe=1000$ , and  $e'_N=3.877$

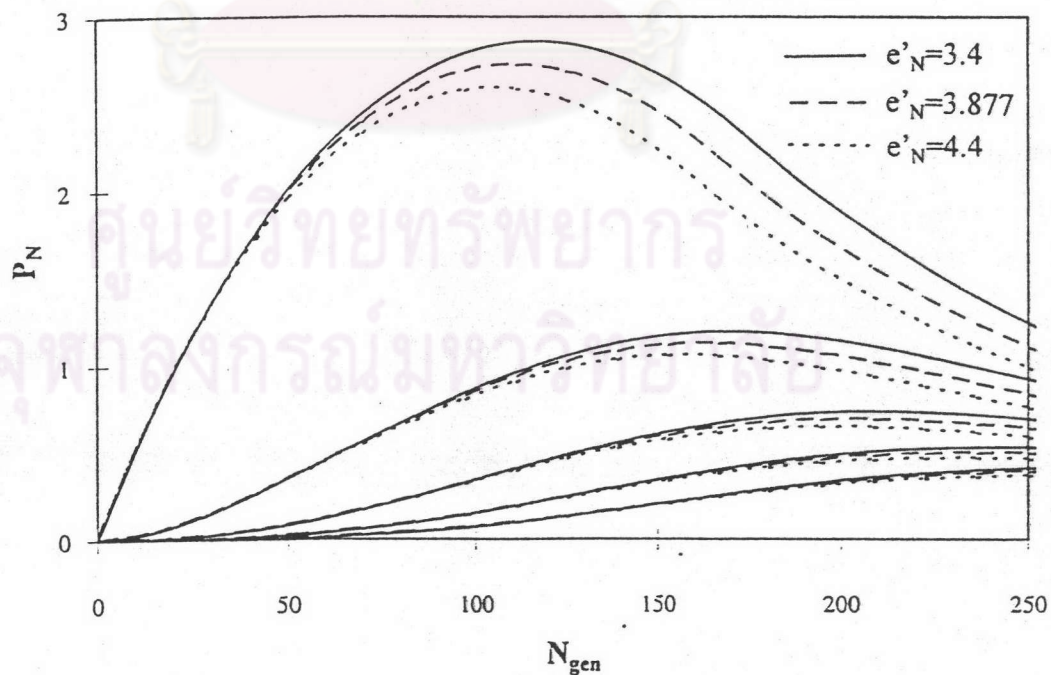


Figure 5.143 Dendrite distribution for convective diffusion of  $R=0.1$ ,  $Pe=1000$ , and  $e_N=7.499$

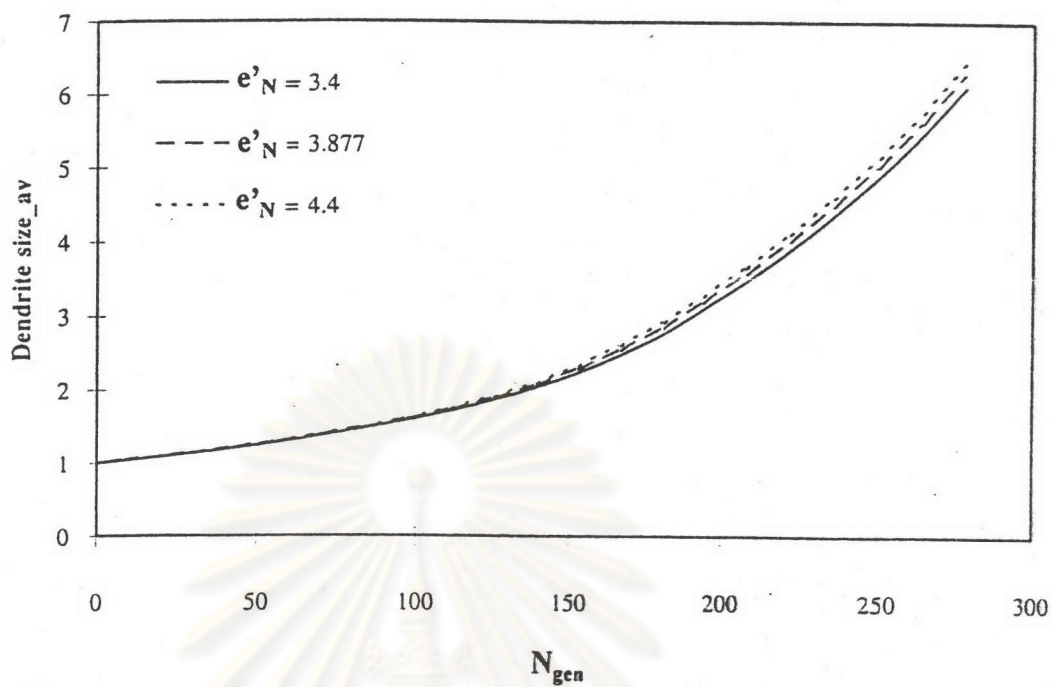


Figure 5.144 Dendrite average size for convective diffusion of  $R=0.1$ ,  $Pe=1000$ , and  $e_N=7.499$

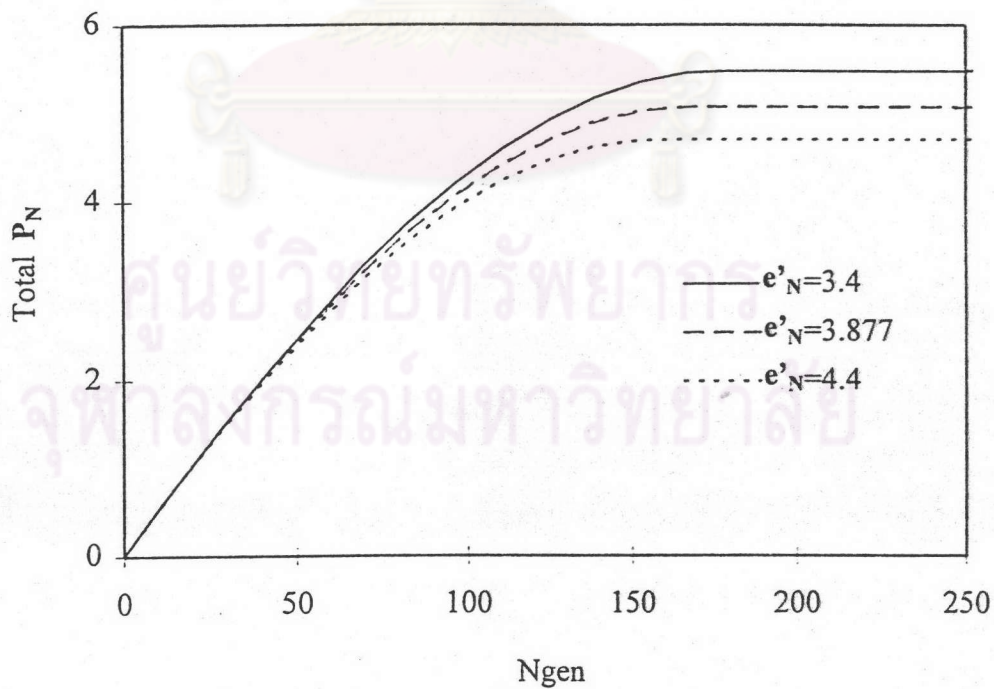


Figure 5.145 Total population of dendrites for convective diffusion ( $R=0.1$ ,  $Pe=1000$  and  $e_N=7.499$ )



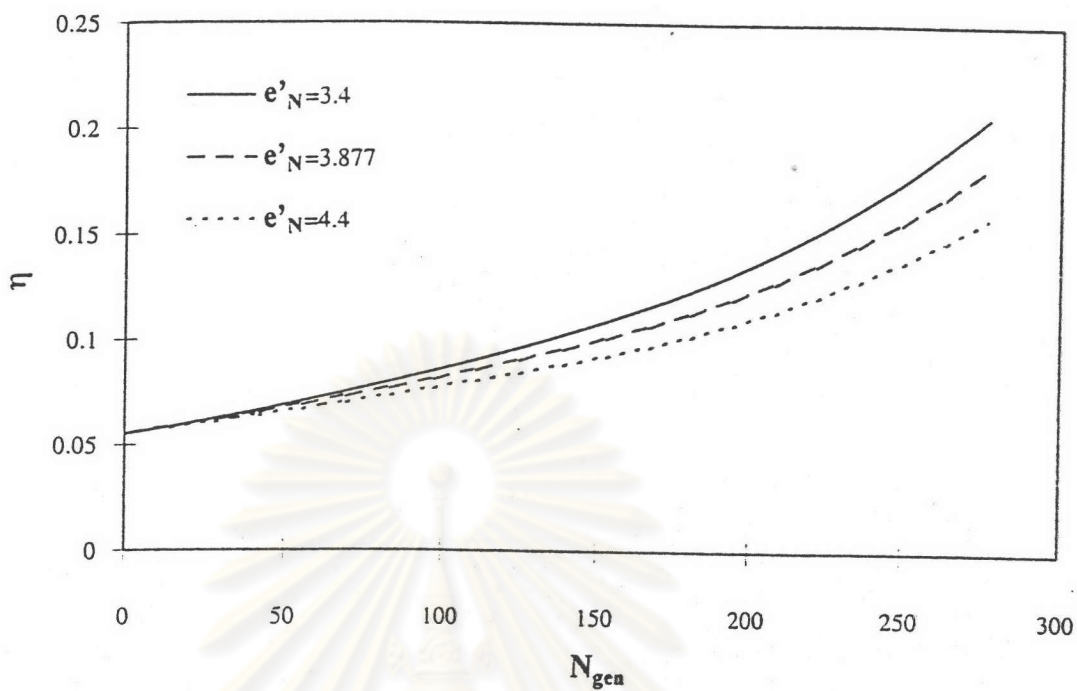


Figure 5.146 Collection efficiency for convective diffusion of  $R=0.1$ ,  $Pe=1000$ , and  $e_N=7.499$

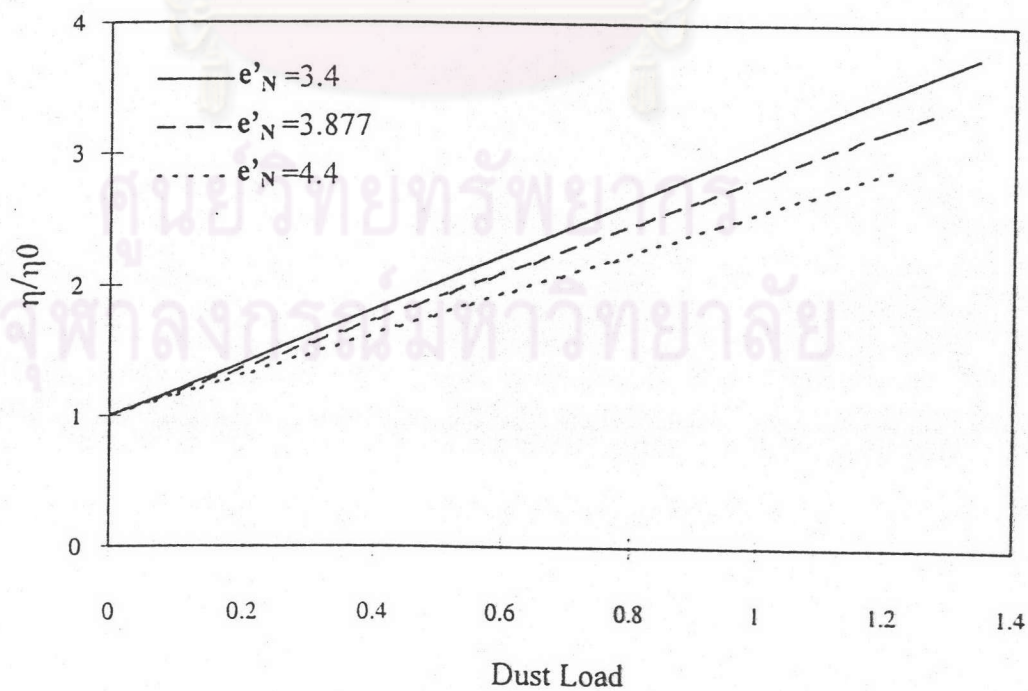


Figure 5.147 Normalized collection efficiency of dust load for  $R=0.1$ ,  $Pe=1000$ , and  $e_N=7.499$

collection efficiency raising factor  $\lambda$  and the collection efficiency  $\eta$  were investigated in section 5.3.1.

#### 5.3.1.1 Effect of the parameter $e_N$

The effects of the parameter  $e_N$  on the dendrite distribution, the average dendrite size, the total population of dendrites,  $\lambda$  and  $\eta$  were studied at  $R=0.1$ ,  $Pe=1000$  and  $e'_N=3.877$ . Figure 5.138 shows the resulting dendrite distribution with  $e_N$  as parameter. As seen from the figure, the number concentration of  $P_N$  initially increased slightly faster but subsequently decreased faster as the parameter  $e_N$  was increased. Figure 5.139 shows the average dendrite size with  $e_N$  as parameter. As seen from the figure, the average dendrite size was bigger when the parameter  $e_N$  increased. Figure 5.140 shows the comparative effect of  $e_N$  on the total population of dendrites. As seen from the figure, the resulting population of dendrites becomes smaller when  $e_N$  increases. Figure 5.141 shows the effect of  $e_N$  on  $\eta$ . At a larger  $e_N$ ,  $\eta$  increased more rapidly with  $N_{gen}$  because the effective capture area increased. Table 5.13 shows the effect of  $e_N$  on  $\lambda$ . Figure 5.142 shows the effect of  $e_N$  on  $\eta/\eta_0$  vs. dust-loaded. As seen from the Figure,  $e_N$  enhanced the normalized collection efficiency versus dust load.

#### 5.3.1.2 Effects of the parameter $e'_N$

As above, the effects of  $e'_N$  on the dendrite distribution, the average dendrite size, the total population of dendrites,  $\lambda$ , and  $\eta$  at  $R=0.1$ ,  $Pe=1000$  and  $e_N=10.336$  were investigated. Figure 5.143 shows the effect of  $e'_N$  on the dendrite distribution. As seen from the figure, the concentration  $P_N$  initially increased barely faster but subsequently decreased significantly faster when the parameter  $e'_N$  was raised. Figure 5.144 shows the effect of  $e'_N$  on the average dendrite size. As seen from the figure, the average dendrite size was almost the same as the parameter  $e'_N$  was raised. Figure 5.145 shows the comparative effect of  $e'_N$  on the total population of dendrites. As seen from the figure, the total population of dendrites also becomes smaller when  $e'_N$  increases. Figure 5.146 shows the effect of  $e'_N$  on  $\eta$ . As seen from the figure,  $e'_N$  negatively affected  $\eta$ . Table 5.14 lists  $\lambda$  with  $e'_N$  as parameter. Again e

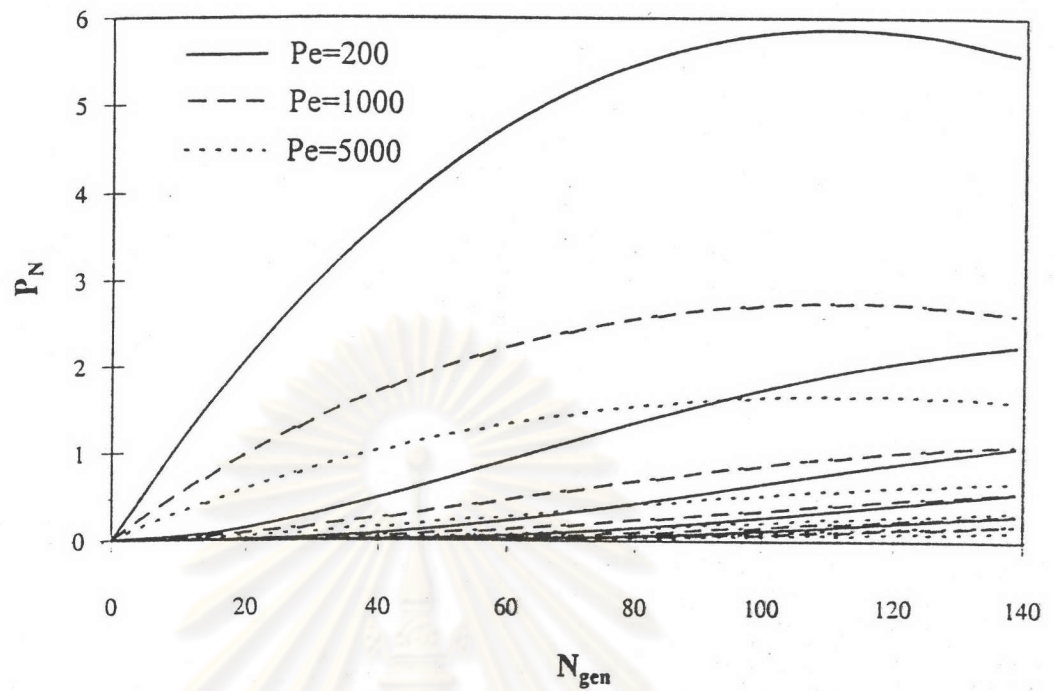


Figure 5.148 Dendrite distribution of convective diffusion with  $Pe$  as parameter for  $R=0.1$

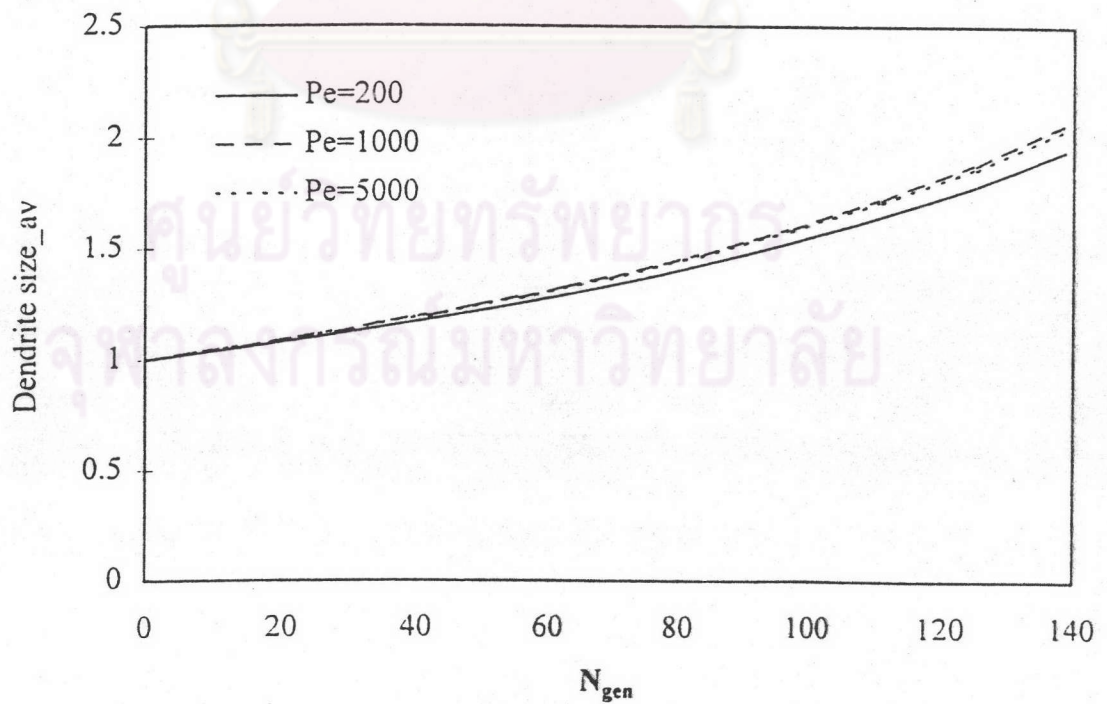


Figure 5.149 Dendrite average size of convective diffusion with  $Pe$  as parameter for  $R=0.1$



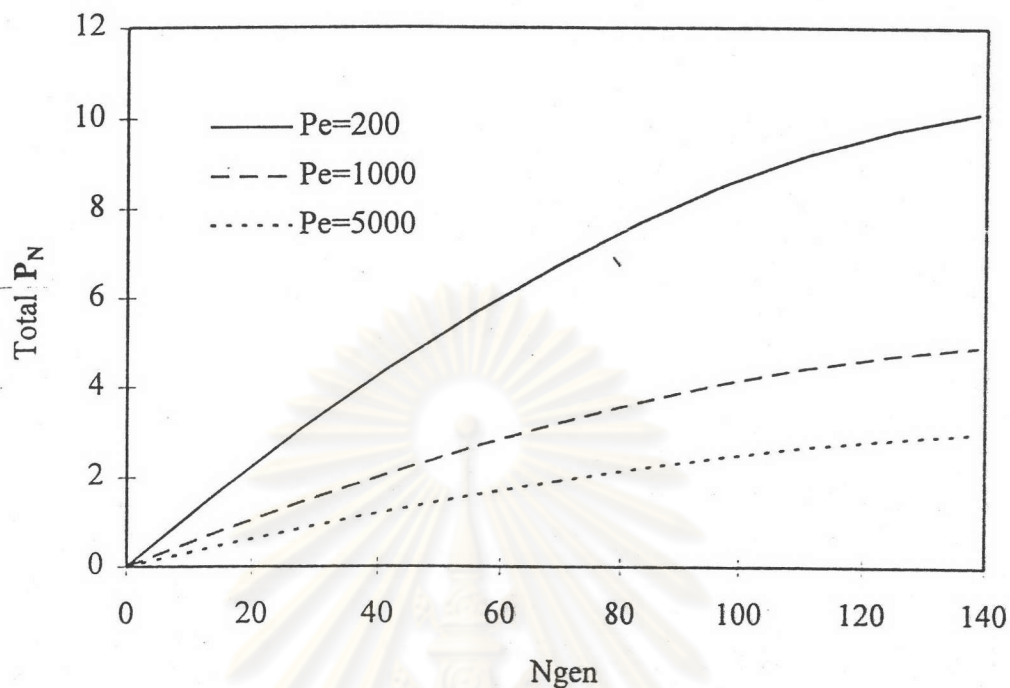


Figure 5.150 Total population of dendrites for convective diffusion ( $R=0.1$ )

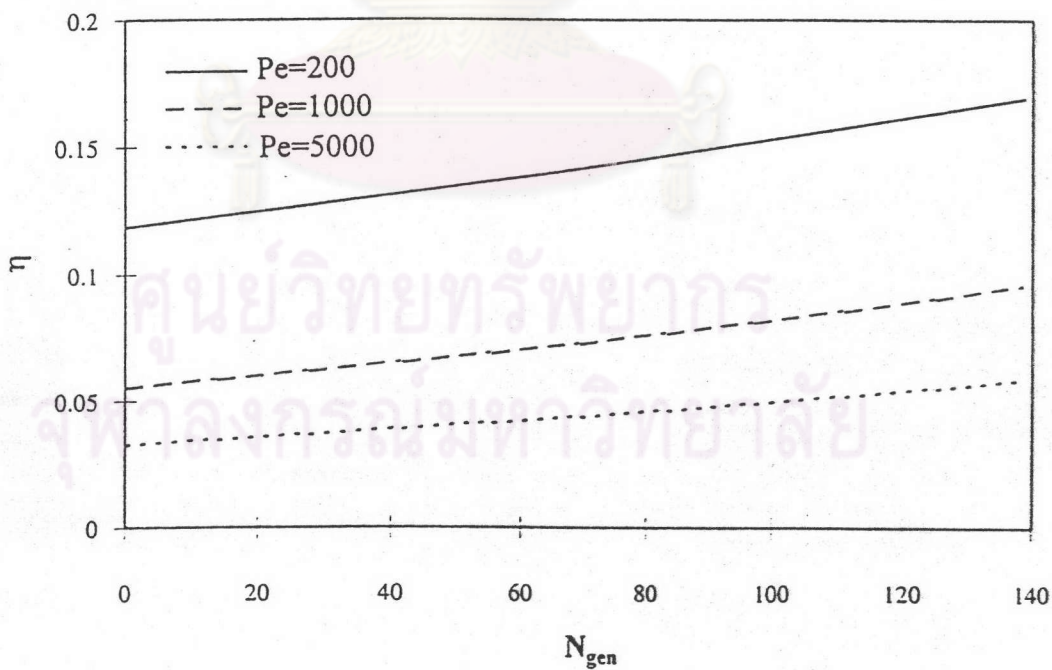


Figure 5.151 Collection efficiency of convective diffusion with  $Pe$  as parameter for  $R=0.1$

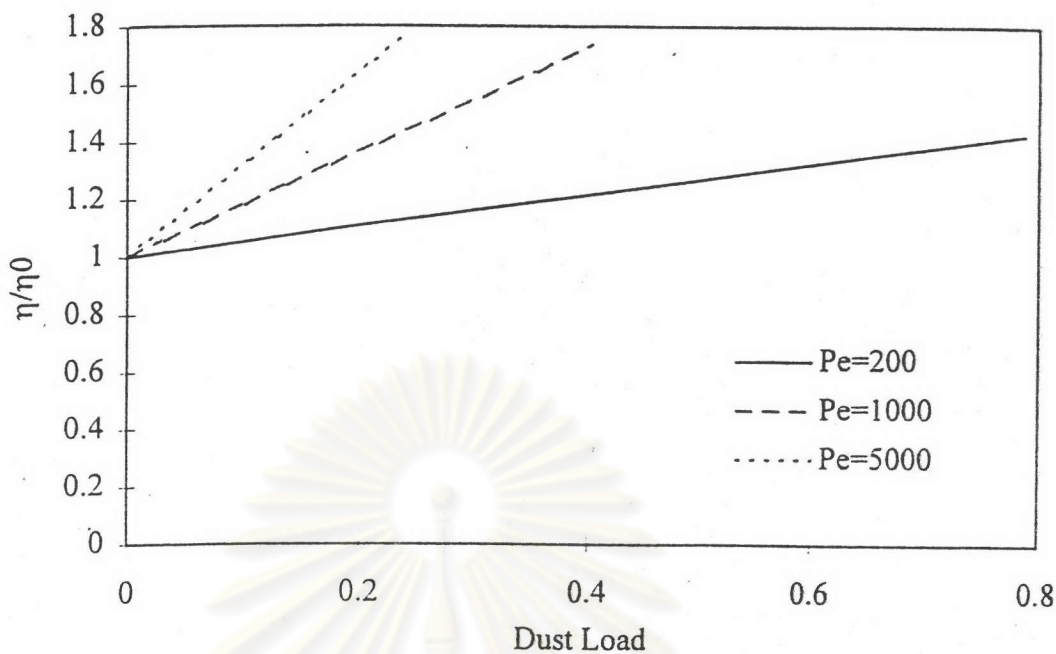


Figure 5.152 Normalized collection efficiency of dust load with Pe as parameter for  $R=0.1$

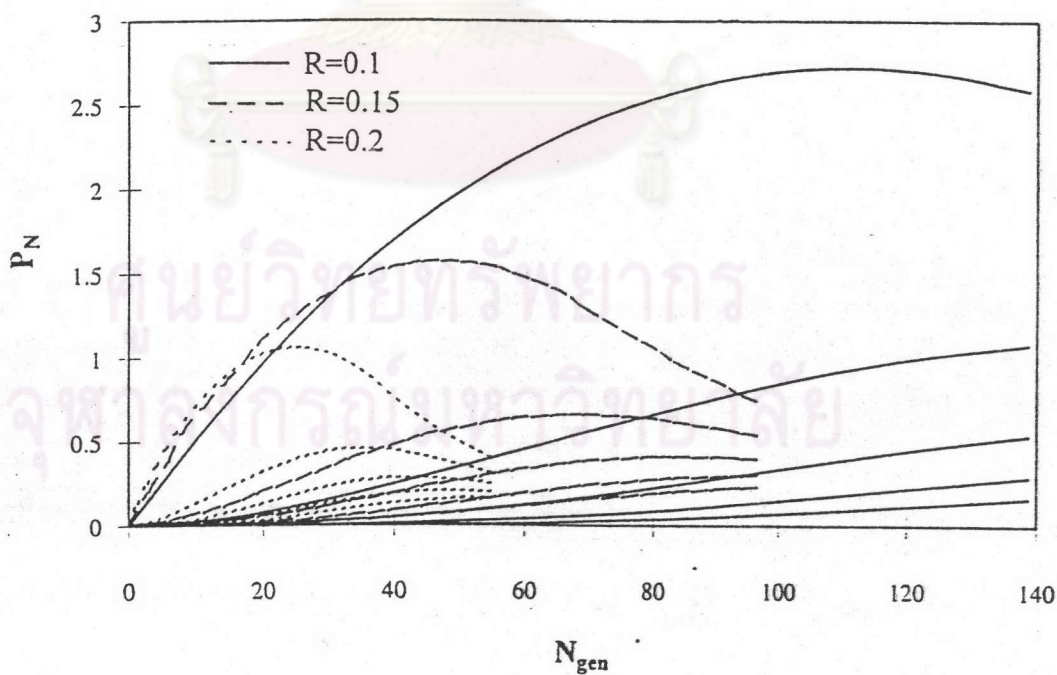


Figure 5.153 Dendrite distribution of convective diffusion with R as parameter for  $Pe=1000$

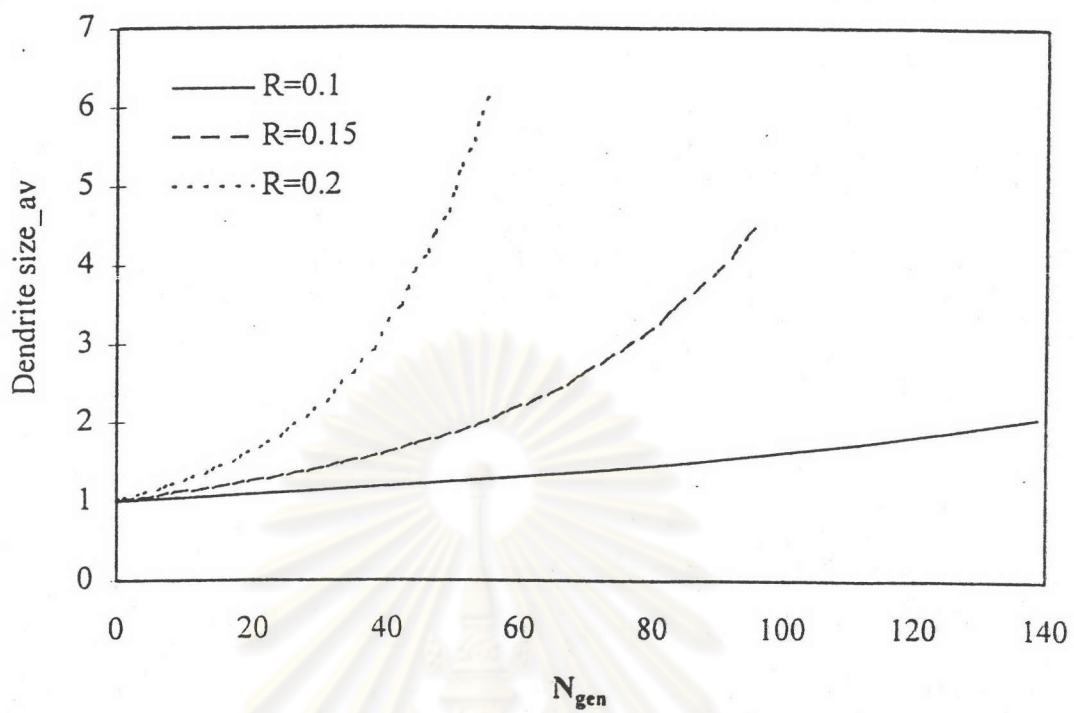


Figure 5.154 Dendrite average size of convective diffusion with  $R$  as parameter for  $Pe=1000$

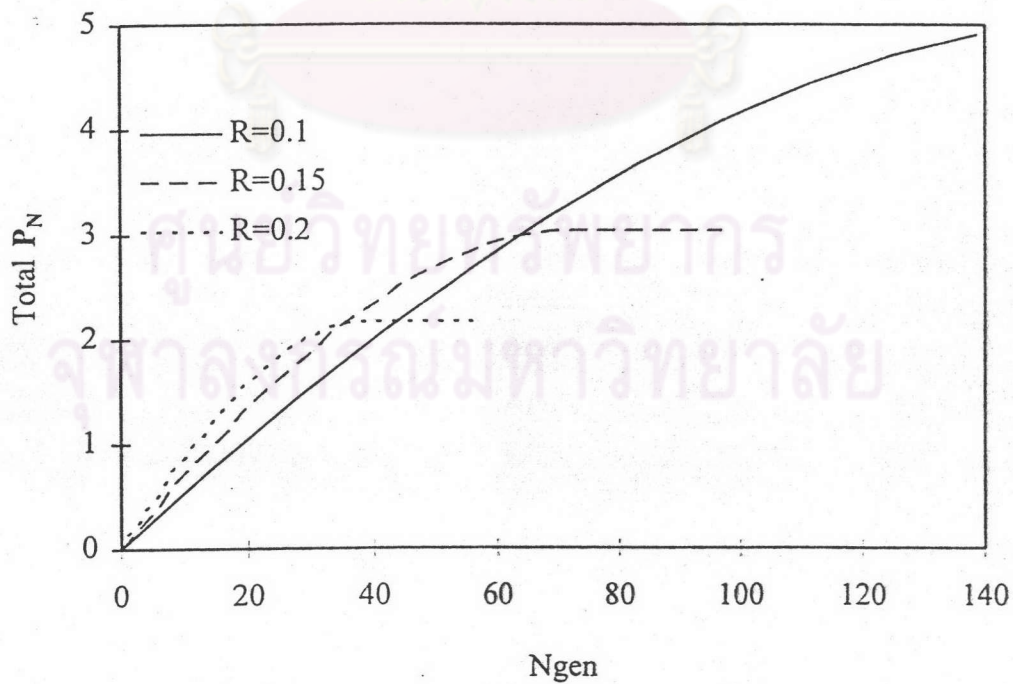


Figure 5.155 Total population of dendrites for convective diffusion ( $Pe=1000$ )



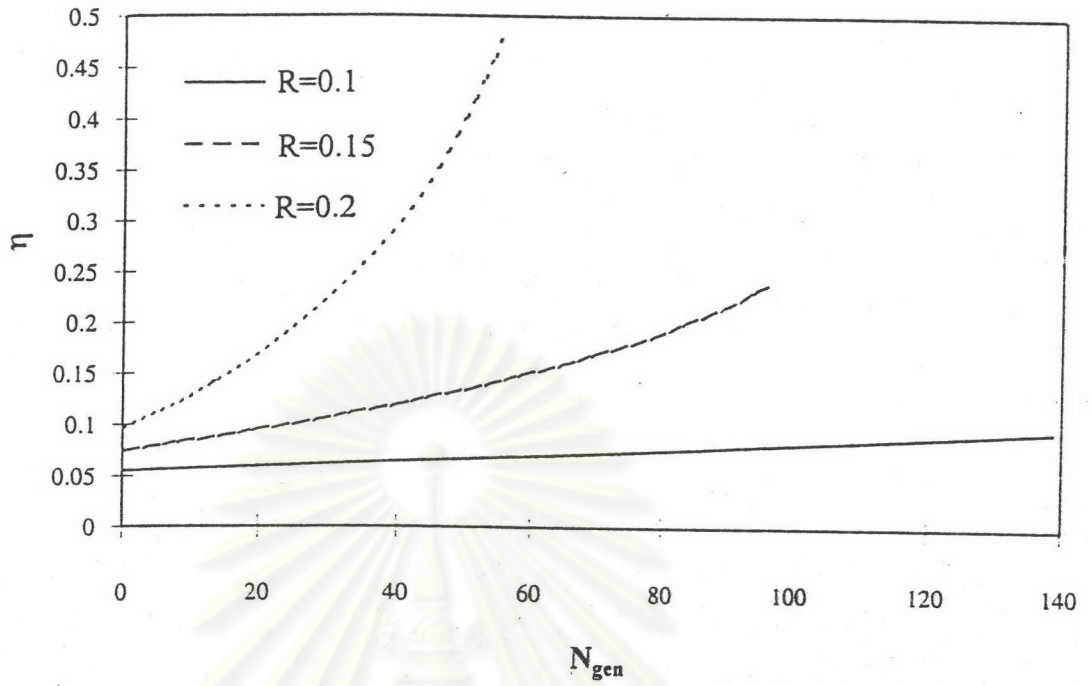


Figure 5.156 Collection efficiency of convective diffusion with  $R$  as parameter for  $Pe=1000$

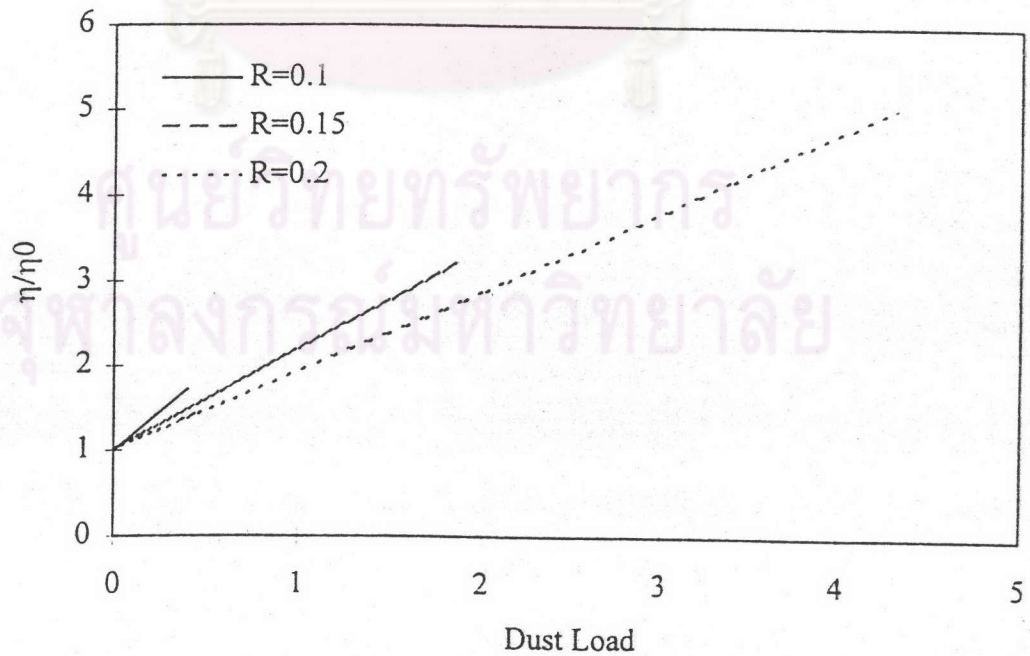


Figure 5.157 Normalized collection efficiency of dust load with  $R$  as parameter for  $Pe=1000$

$e_N$	7	7.499	8
$\lambda$	1.562	1.811	2.062

Table 5.13 The collection efficiency raising factor  $\lambda$  for  $R=0.1$   $Pe=1000$  and  $e'n=3.877$

$e'_N$	3.4	3.877	4.4
$\lambda$	2.05	1.811	1.55

Table 5.14 The collection efficiency raising factor  $\lambda$  for  $R=0.1$   $Pe=1000$  and  $e_n=7.499$

$Pe$	200	1000	5000
$e_N$	3.159	7.499	12.606
$e'_N$	2.078	3.877	6.213
$\lambda$	0.5405	1.8110	3.1965

Table 5.15 The collection efficiency raising factor  $\lambda$  for  $R=0.1$

$R$	0.1	0.15	0.2
$e_N$	7.499	6.234	5.631
$e'_N$	3.877	2.67	1.906
$\lambda$	1.8110	1.1880	0.9313

Table 5.16 The collection efficiency raising factor  $\lambda$  for  $Pe=1000$

'N degraded  $\lambda$ . Figure 5.147 shows the effect of  $e'_N$  on  $\eta/\eta_0$  vs. dust load. Similarly,  $e'_N$  degraded  $\eta/\eta_0$ .

### 5.3.1.3 Effects of Pe

It is well known that the diffusivity and  $\eta_0$  is inversely proportional to Pe. Here the effects of Pe on the dendrite distribution, the average dendrite size, the total population of dendrites,  $\lambda$ , and  $\eta$  for  $R=0.1$  and the values of  $e_N$  and  $e'_N$  shown in Table 5.5. Figure 5.148 shows the effect of Pe on the dendrite distribution. As seen from the figure, the concentration of the smaller dendrites decreased when Pe increased. Figure 5.149 shows the effect of Pe on the average dendrite size. As seen from the figure, the average dendrite size increased slightly. Figure 5.150 shows the effect of Pe on the total population of dendrites. As seen from the figure, the population of dendrites becomes much smaller when Pe increases. Table 5.15 show the effect of Pe on  $\lambda$ .  $\lambda$  increased with increasing Pe because of decreasing  $\eta_0$ . Figure 5.151 shows the effect of Pe on  $\eta$ . As soon from the figure,  $\eta$  decreased with increasing Pe. Figure 5.152 shows the effect of Pe on  $\eta/\eta_0$  vs. dust-load.  $\eta/\eta_0$  increased faster as Pe increased.

### 5.3.1.4 Effects of R

The effect of R was investigated at  $Pe=1000$  using the values of the parameters  $e_N$  and  $e'_N$  shown in Table 5.5. When R increased, the particles were larger so more are captured on a fiber. Figure 5.153 shows the effect of R on the dendrite distribution. As seen from the figure, the dendrite concentration  $P_N$  was lower and decreased faster as  $N_{gen}$  increased. Since the particles were larger, the number of captured particles could be smaller. Figure 5.154 shows the effect of R on the average dendrite size. The average dendrite size increased faster when R was larger. Figure 5.155 shows the effect of R on the total population of dendrites. As seen from the figure, when  $N_{gen}$  is still small (less than 30), the total number of dendrites at a lower R is smaller than that at a higher R. However, as time passes, the population of dendrites at a higher R attains a larger asymptotic size. Table 5.16 shows  $\lambda$  the effect of R on  $\lambda$ .  $\lambda$  decreased with increasing R because of increased  $\eta_0$ . Figure 5.156



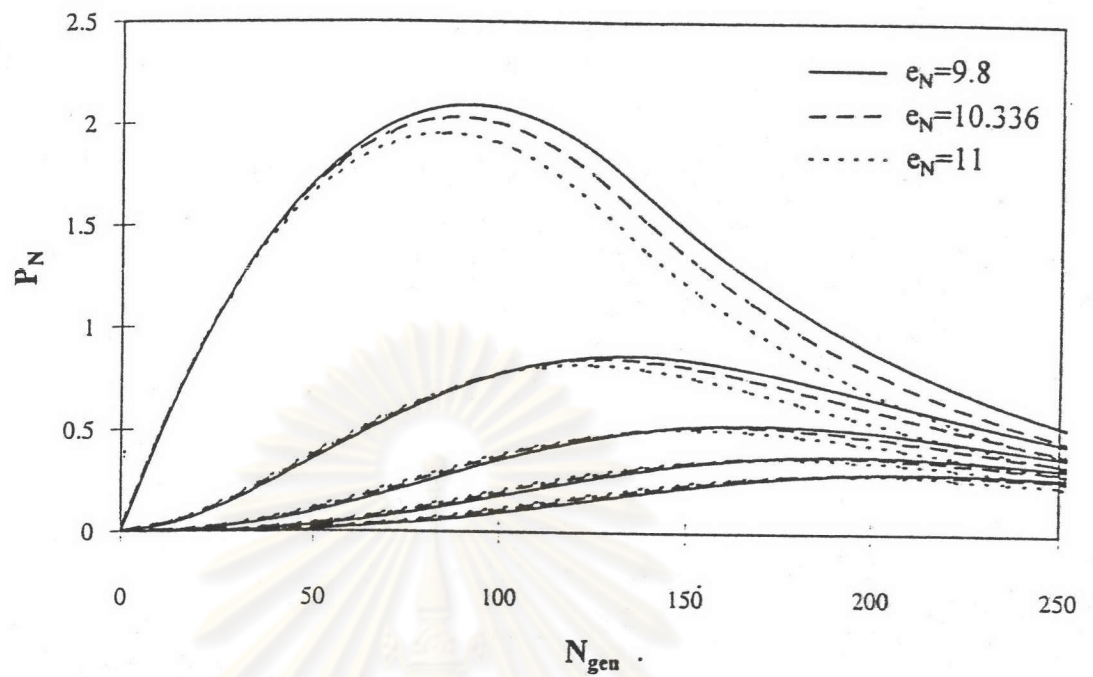


Figure 5.158 Dendrite distribution for inertial impaction of  $R=0.1$ ,  $St=1$ , and  $e'_N=5.01$

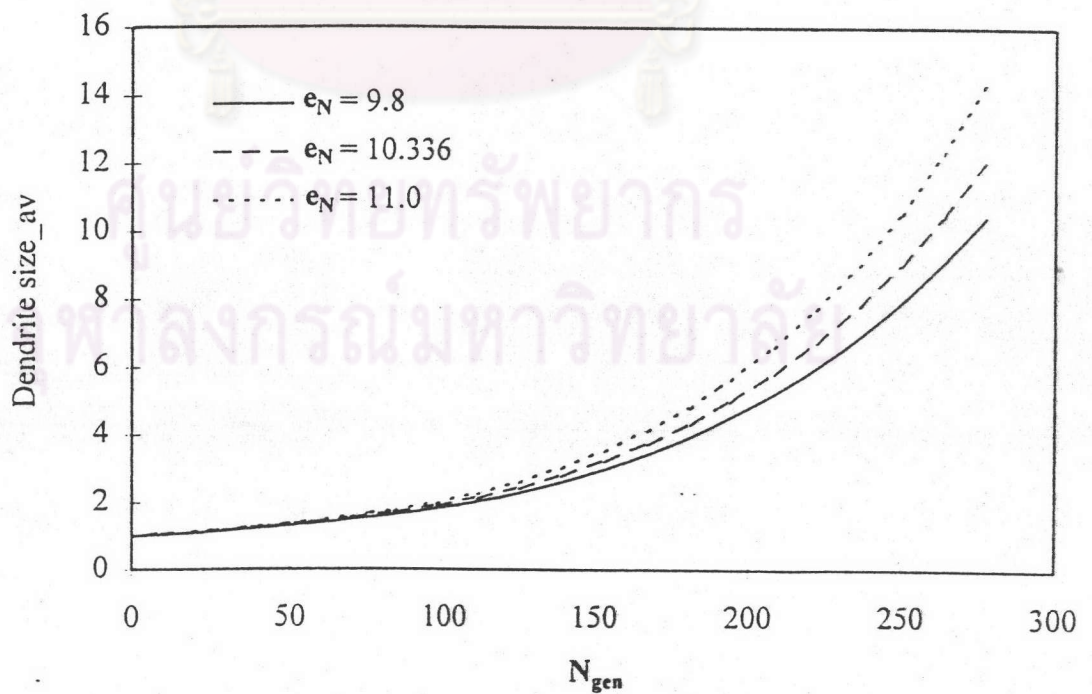


Figure 5.159 Dendrite average size for inertial impaction of  $R=0.1$ ,  $St=1$ , and  $e'_N=5.01$

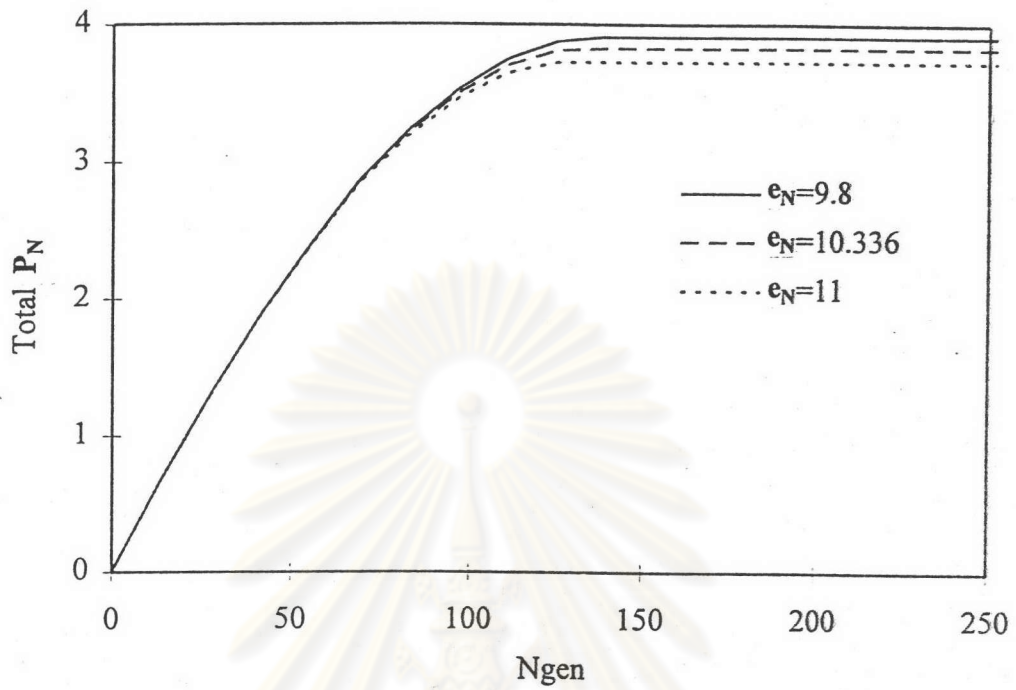


Figure 5.160 Total population of dendrites for inertial impaction  
( $R=0.1$ ,  $St=1$  and  $e'_N=5.01$ )

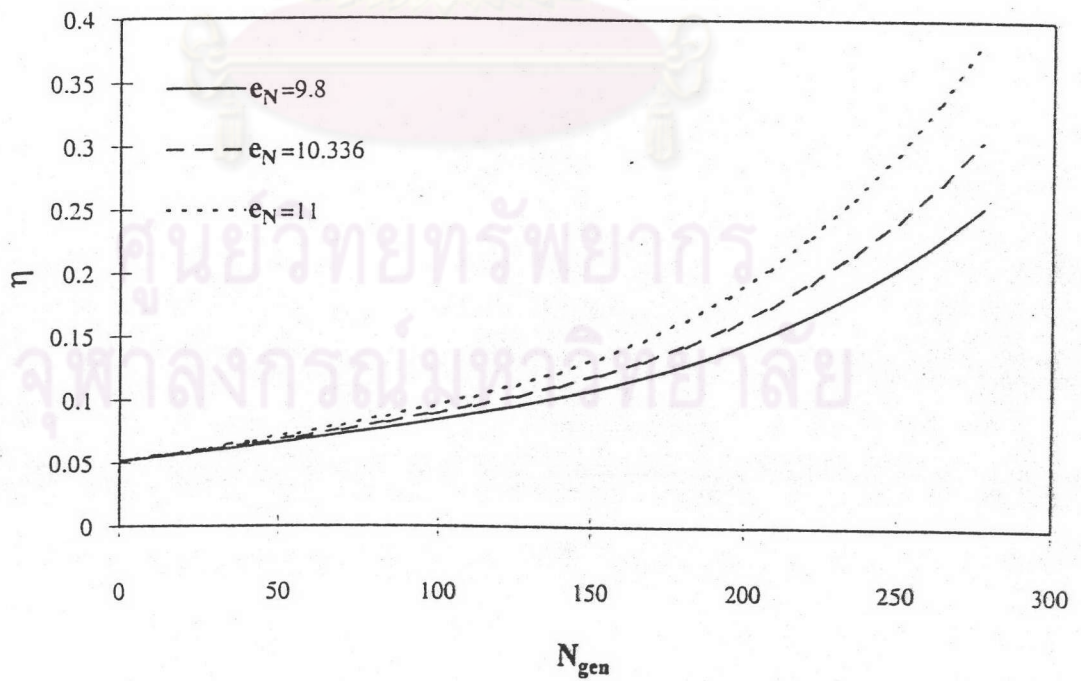


Figure 5.161 Collection efficiency for inertial impaction of  $R=0.1$ ,  $St=1$ ,  
and  $e'_N=5.01$

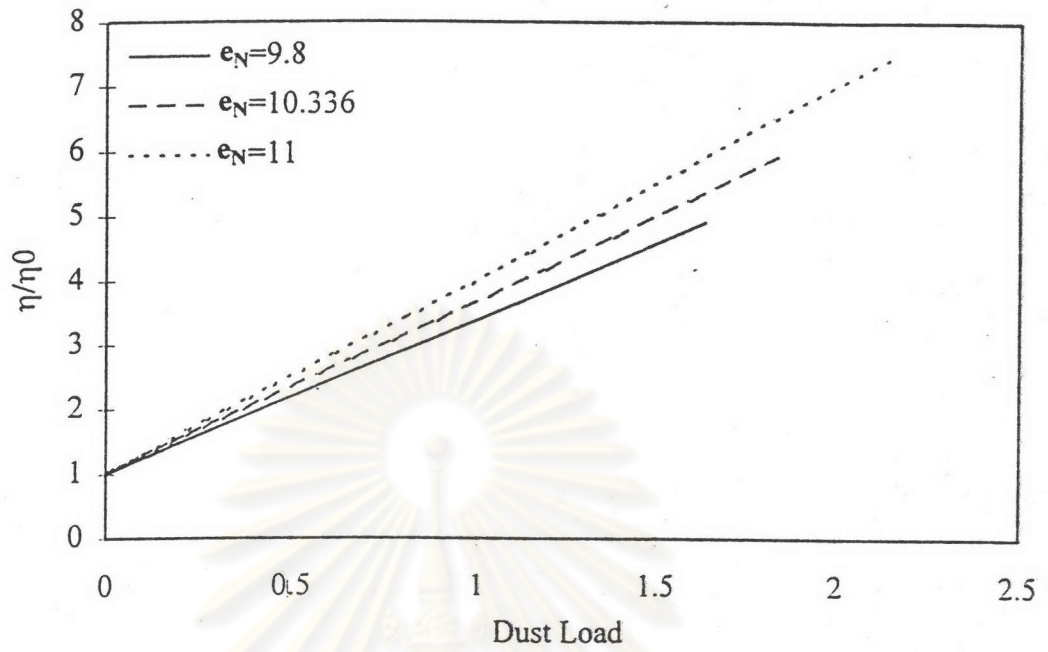


Figure 5.162 Normalized collection efficiency of dust load for  $R=0.1$ ,  $St=1$ , and  $e'_N=5.01$

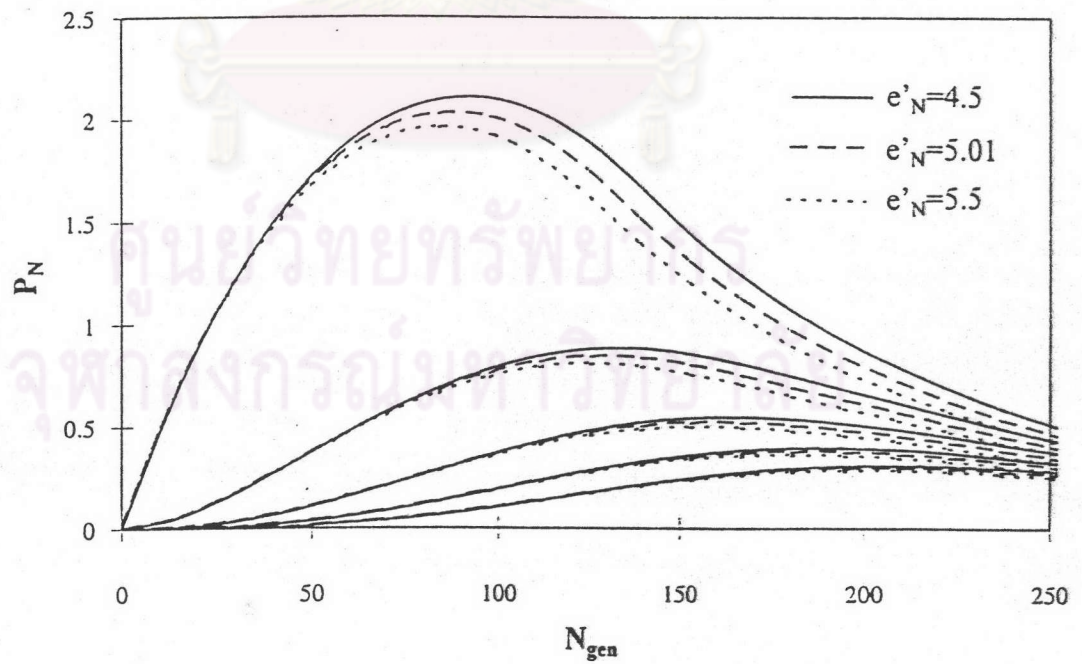


Figure 5.163 Dendrite distribution for inertial impaction of  $R=0.1$ ,  $St=1$ , and  $e'_N=10.336$



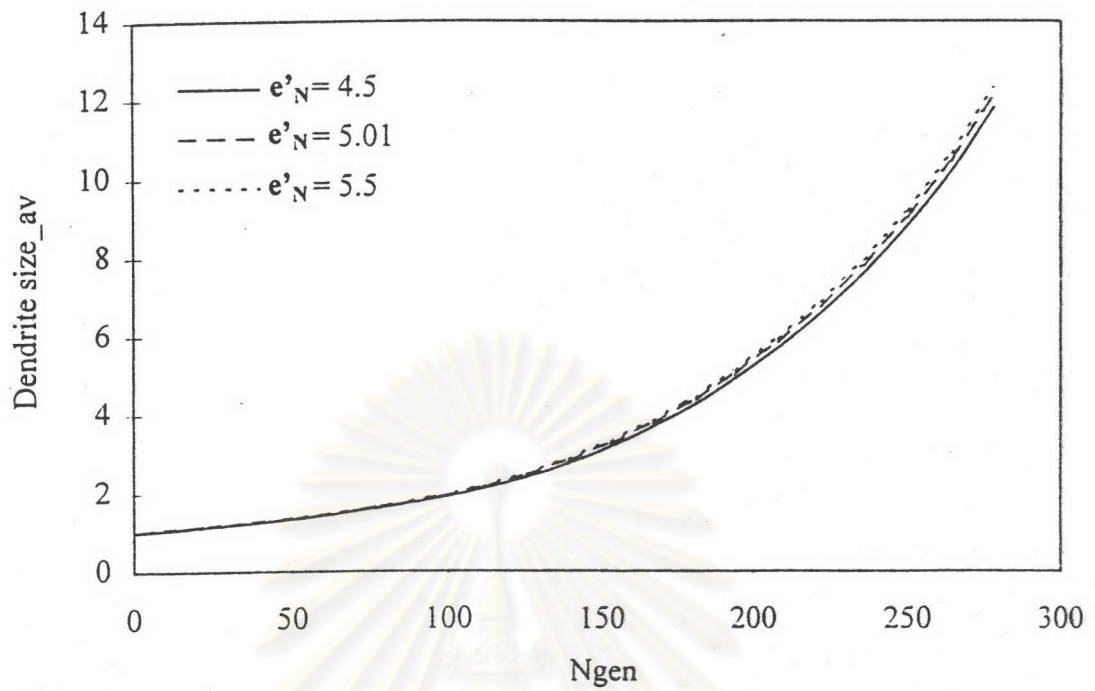


Figure 5.164 Dendrite average size for inertial impaction of  $R=0.1$ ,  $St=1$ , and  $e_N=10.336$

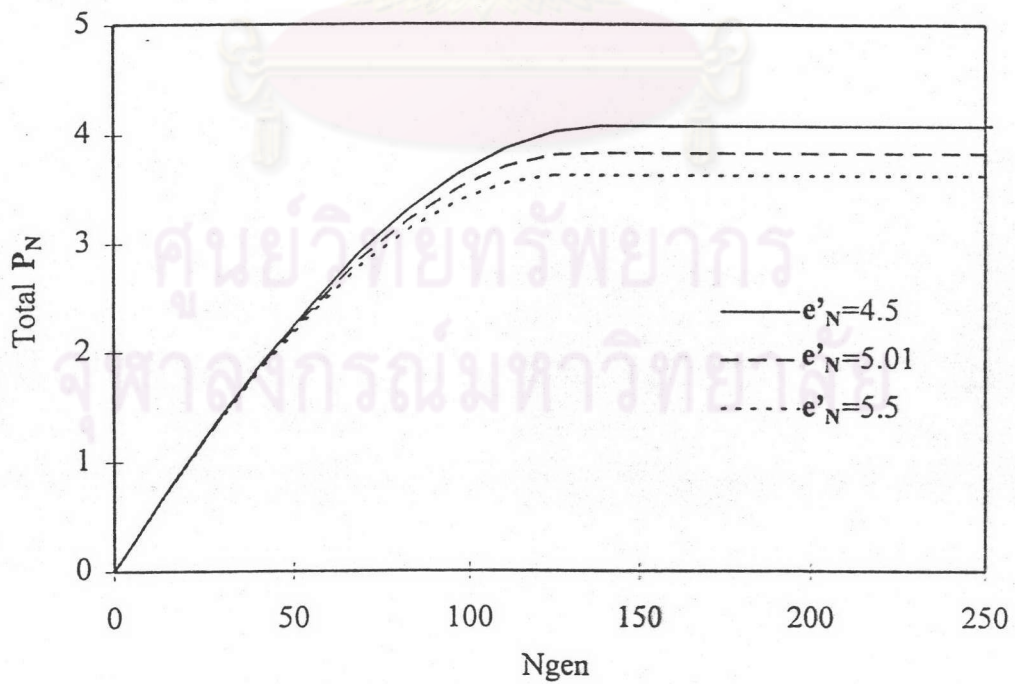


Figure 5.165 Total population of dendrites for inertial impaction ( $R=0.1$ ,  $St=1$  and  $e_N=10.336$ )

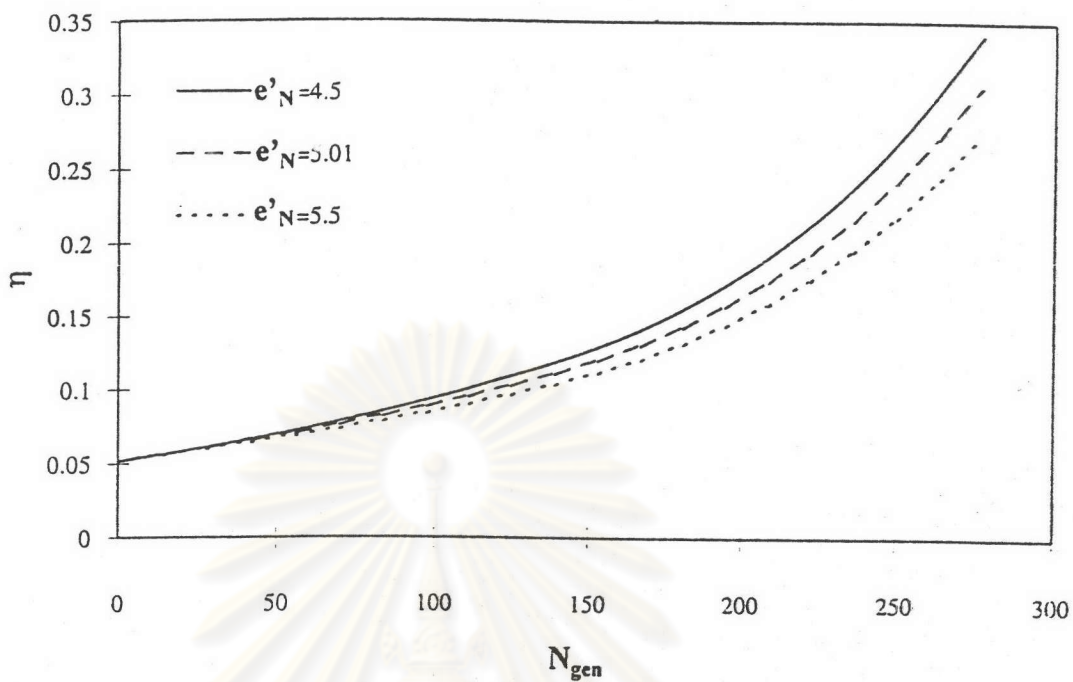


Figure 5.166 Collection efficiency for inertial impaction of  $R=0.1$ ,  $St=1$ , and  $e_N=10.336$

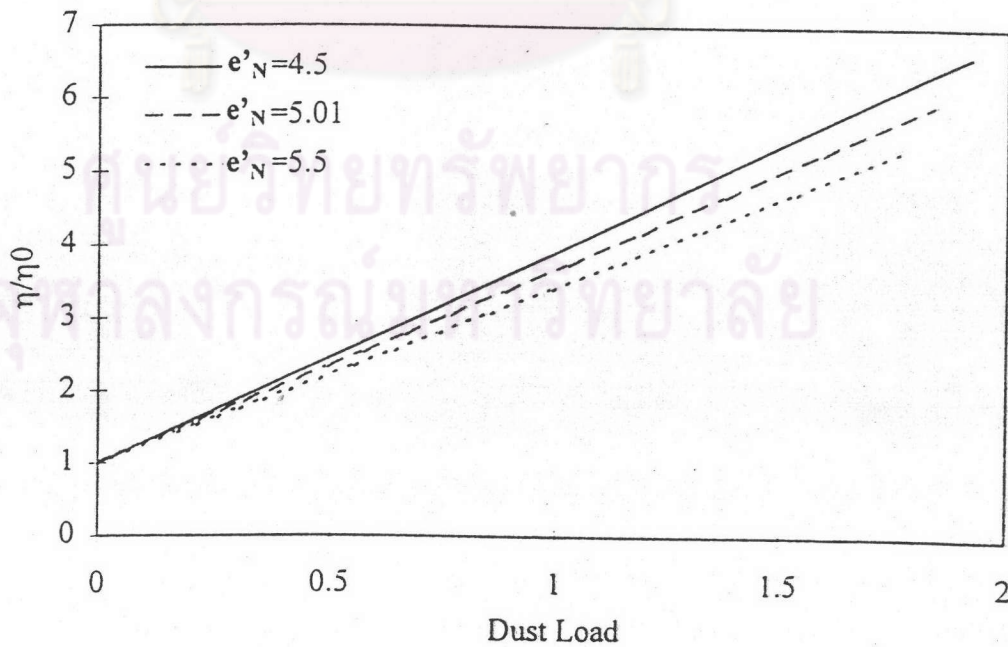


Figure 5.167 Normalized collection efficiency of dust load for  $R=0.1$ ,  $St=1$ , and  $e_N=10.336$

shows the effect of  $R$  on  $\eta$ . As seen from the figure,  $\eta$  increased with increasing  $R$ . Because the particles were bigger, they were captured more easily. Figure 5.157 shows the effect of  $R$  on  $\eta/\eta_0$  vs. dust-load. Similarly,  $\eta/\eta_0$  increase more slowly as  $R$  increased.

### 5.3.2 Inertial impaction

The dendritic growth was investigated for inertial impaction, the effects of the parameters  $e_N$  and  $e'_N$ , the Stokes number  $St$ , and  $R$  on the dendrite distribution, the average dendrite size, the total population of dendrites,  $\lambda$  and  $\eta$ . In this section the effects of the parameters  $e_N$  and  $e'_N$  for  $R=0.1$  and  $St=1.0$ , the effect of  $St$  for  $R=0.1$ , and the effect of  $R$  for  $St=1.0$ , were investigated.

#### 5.3.2.1 Effects of $e_N$

When  $e_N$  increases, so does the effective capture area. The effect of  $e_N$  on the dendrite distribution, the average dendrite size, the total population of dendrites,  $\lambda$  and  $\eta$  were investigated at  $R=0.1$ ,  $St=1.0$  and  $e'_N=5.01$ . Figure 5.158 shows its effect on the dendrite distribution. As seen from the figure, when  $e_N$  increased, the dendrite concentration  $P_N$  initially increased but subsequently decreased faster. Figure 5.159 shows the effect of  $e_N$  on the average dendrite size which increased more rapidly when  $e_N$  increased. Figure 5.160 shows the comparative effect of  $e_N$  on the total population of dendrites. As seen from the figure, the population number of dendrites becomes smaller when  $e_N$  increases. Table 5.17 shows the positive effect of  $e_N$  on  $\lambda$ . Figure 5.161 shows its effect on  $\eta$ . As seen from the figure,  $\eta$  increased when  $e_N$  increased because its effective capture area increased. Figure 5.162 shows the effect of  $e_N$  on  $\eta/\eta_0$  vs. dust-load. As seen from the figure,  $\eta/\eta_0$  vs. dust load increased also with increasing  $e_N$ .

#### 5.3.2.2 Effect of $e'_N$

Increasing  $e'_N$  increases the effective shadow area, so more vacant sites on the fiber surface was shielded. The effects of  $e'_N$  on the dendrite distribution, the average dendrite size, the total population of dendrites,  $\lambda$  and  $\eta$  were investigated at  $R=0.1$ ,  $St=1.0$  and  $e_N=7.499$ . Figure 5.163 shows its effect on the dendrite



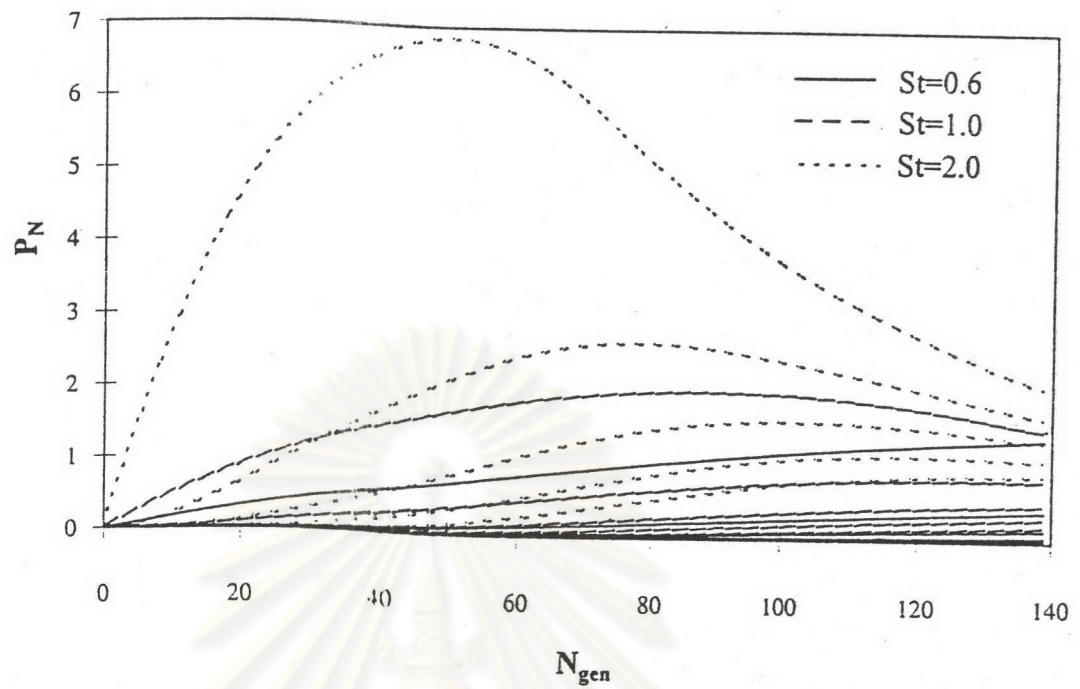


Figure 5.168 Dendrite distribution of inertial impaction with  $St$  as parameter for  $R=0.1$

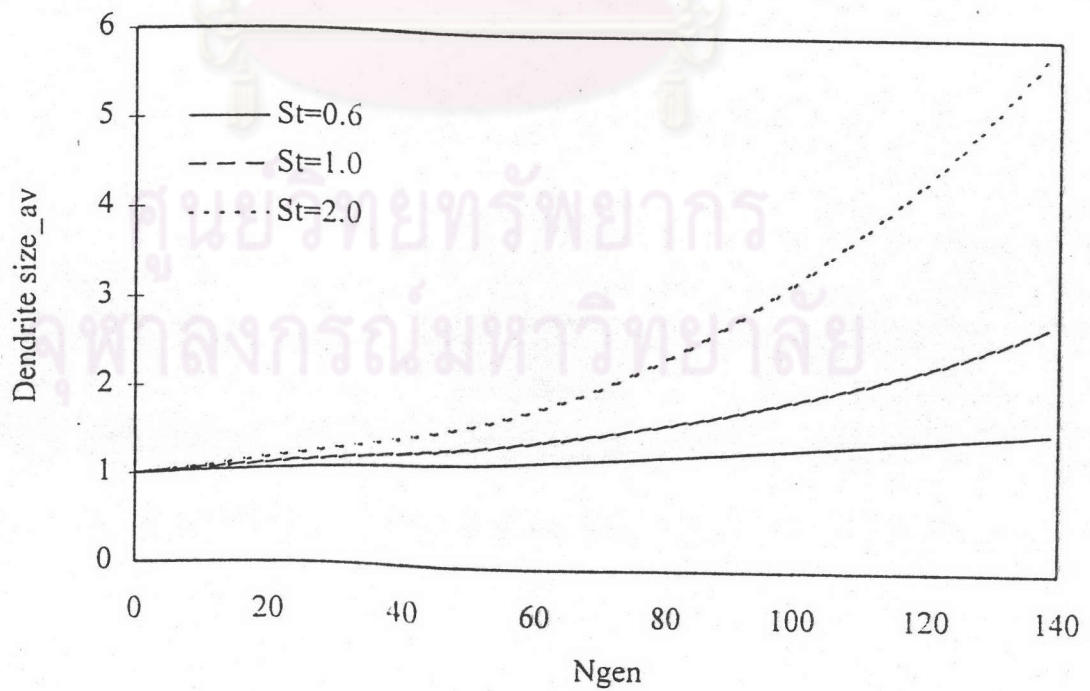


Figure 5.169 Dendrite average size of inertial impaction with  $St$  as parameter for  $R=0.1$

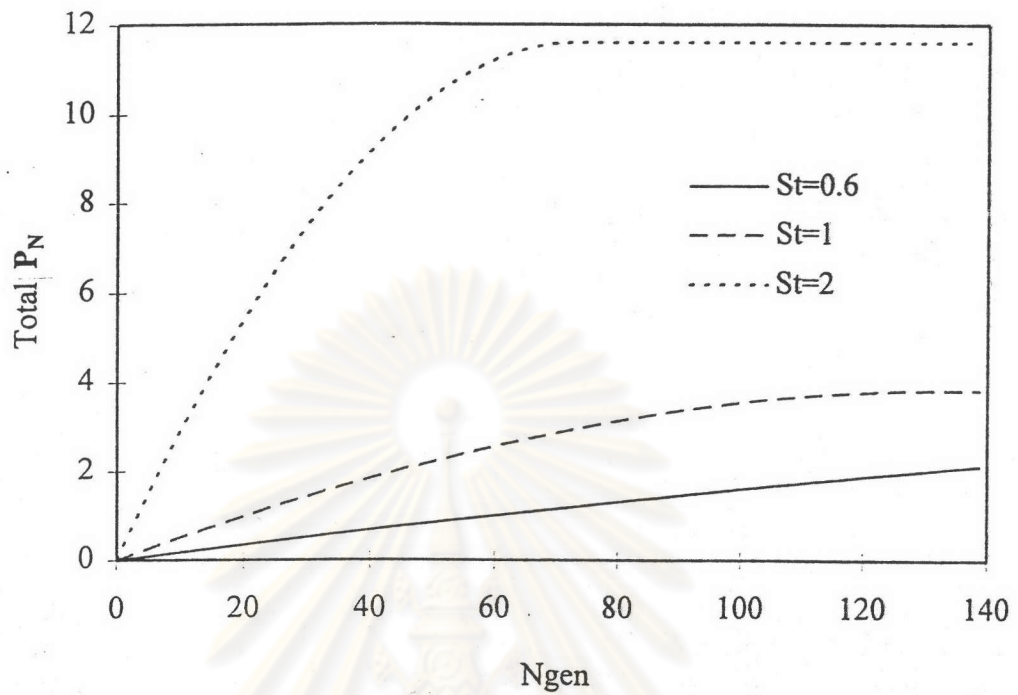


Figure 5.170 Total population of dendrites for inertial impaction ( $R=0.1$ )

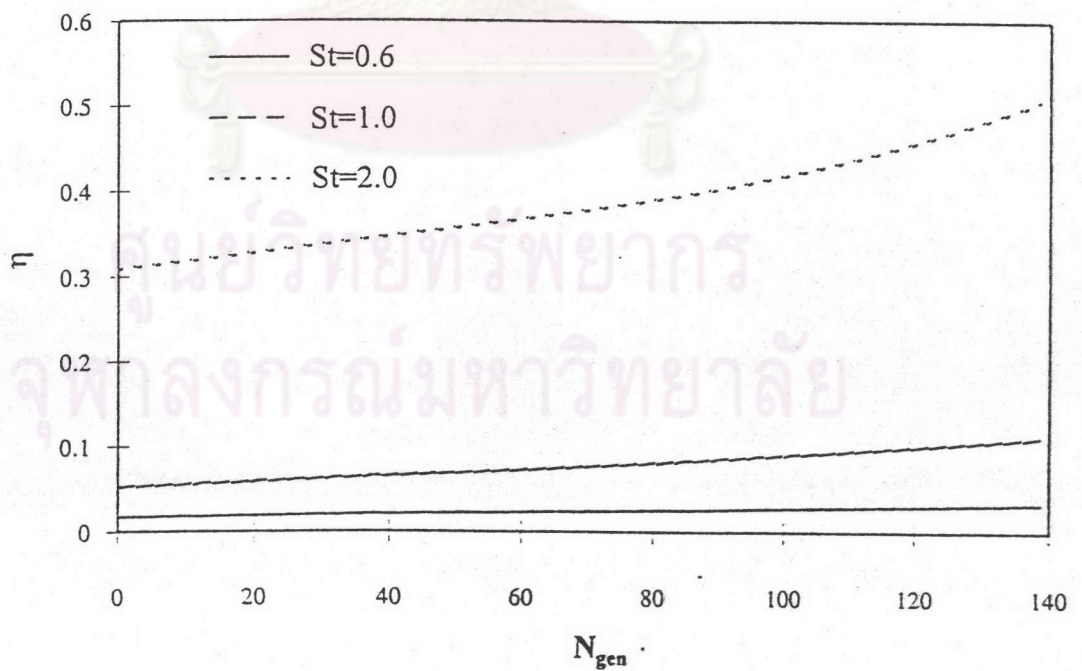


Figure 5.171 Collection efficiency of inertial impaction with  $St$  as parameter for  $R=0.1$

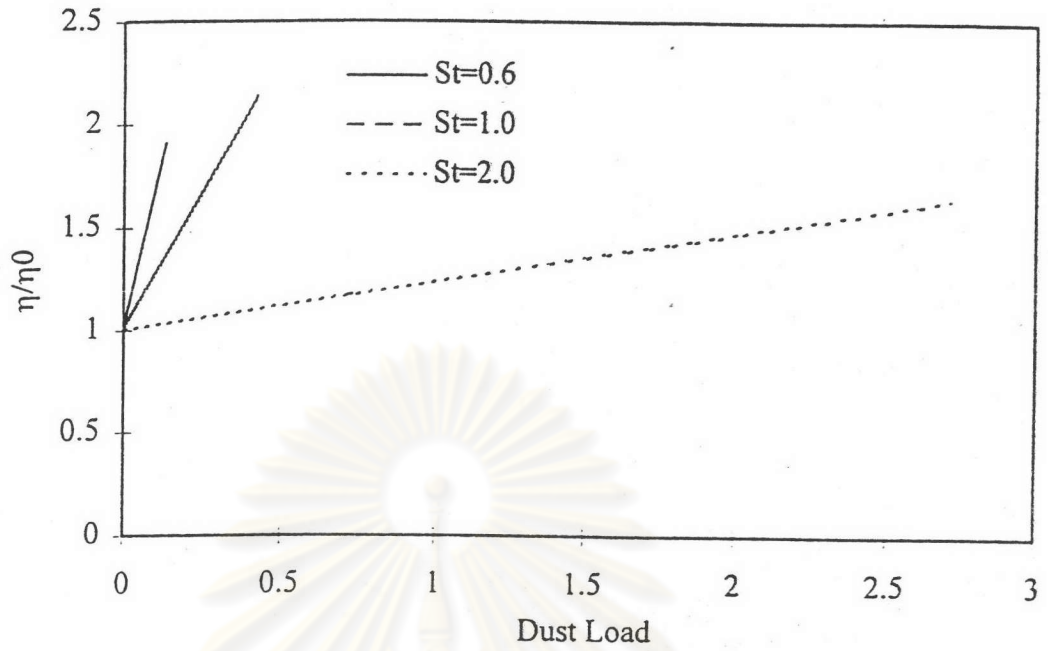


Figure 5.172 Normalized collection efficiency of dust load with St as parameter for R=0.1

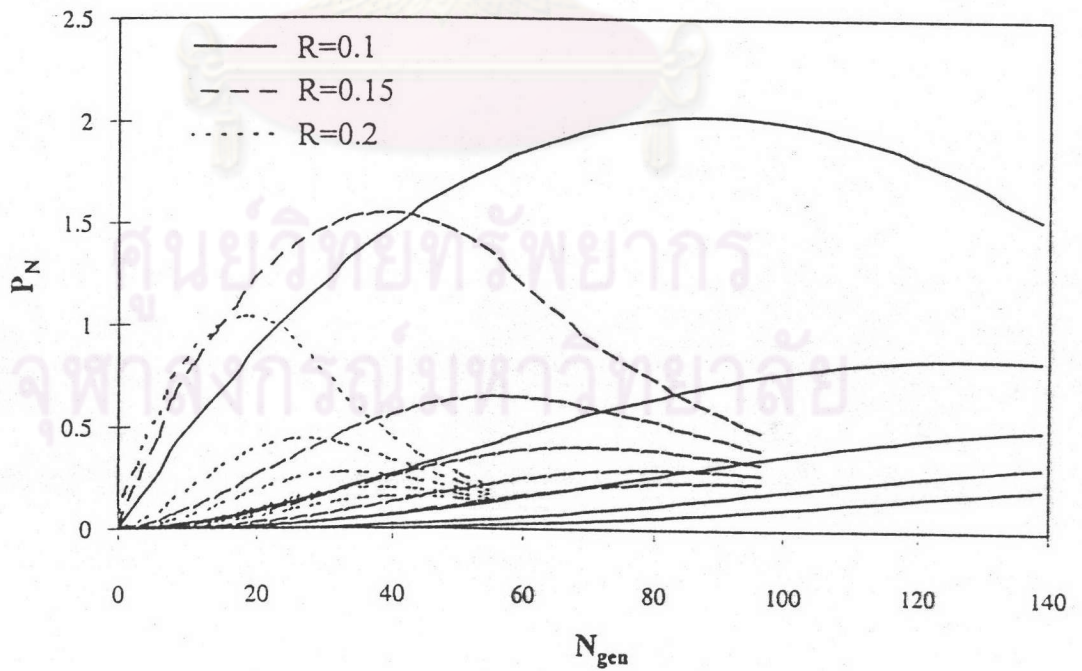


Figure 5.173 Dendrite distribution of inertial impaction with R as parameter for St=1



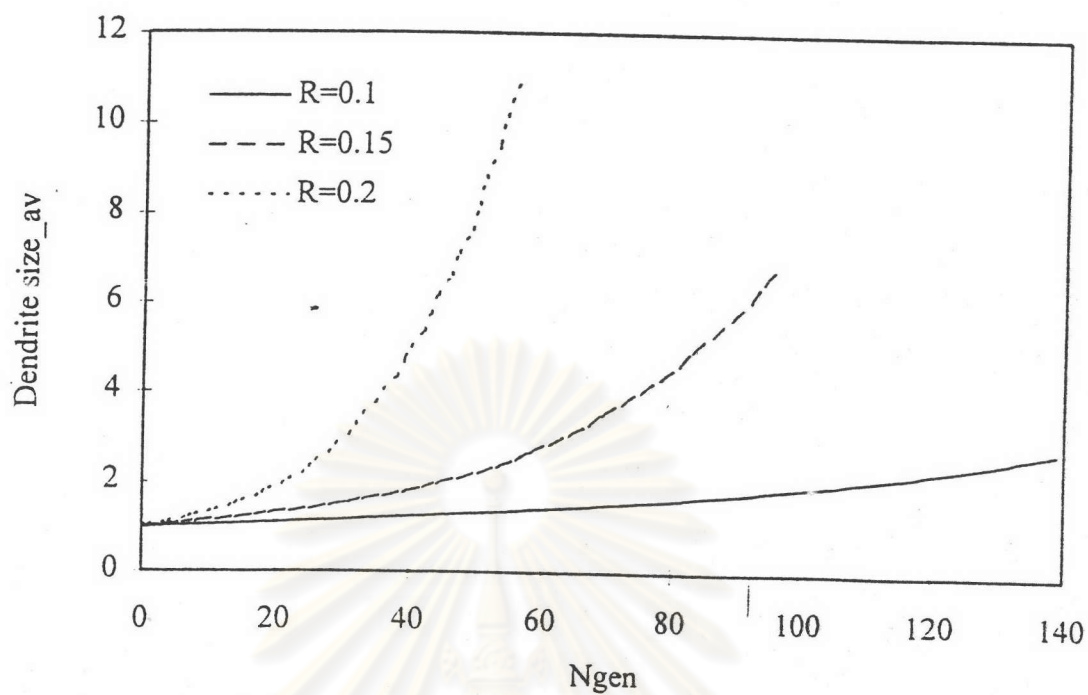


Figure 5.174 Dendrite average size of inertial impaction with  $R$  as parameter for  $St=1$

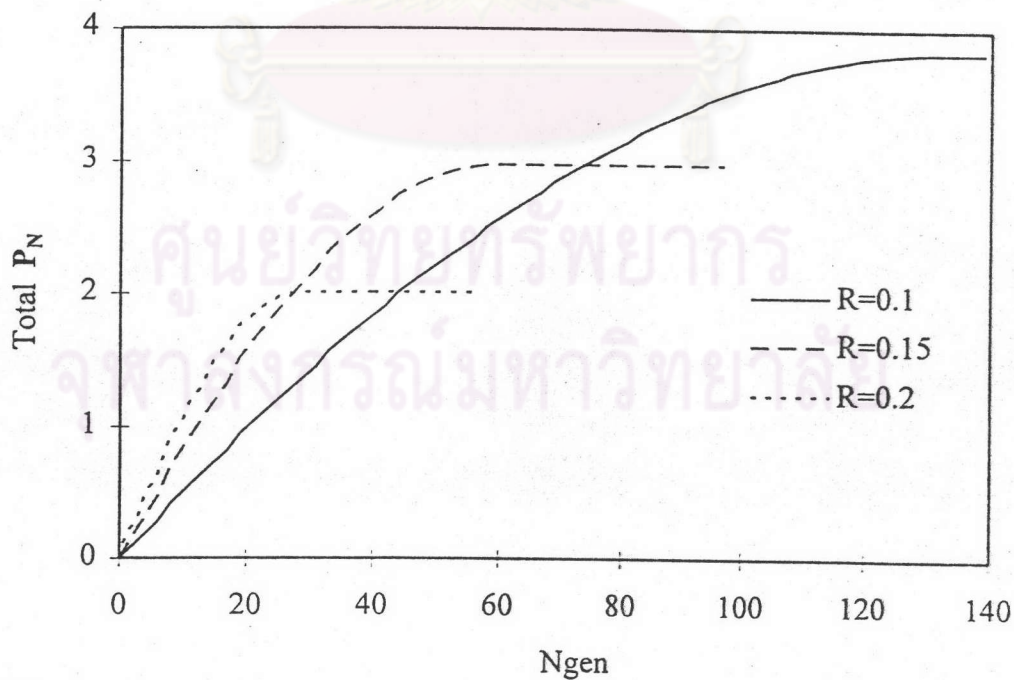


Figure 5.175 Total population of dendrites for inertial impaction ( $St=1$ )

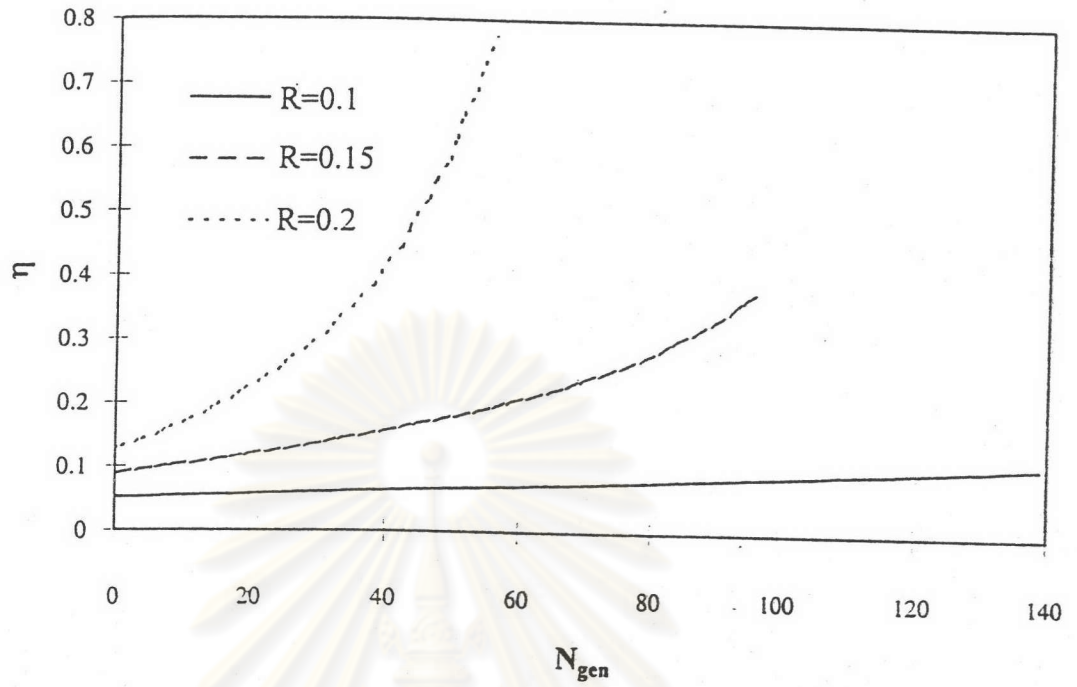


Figure 5.176 Collection efficiency of inertial impaction with  $R$  as parameter for  $St=1$

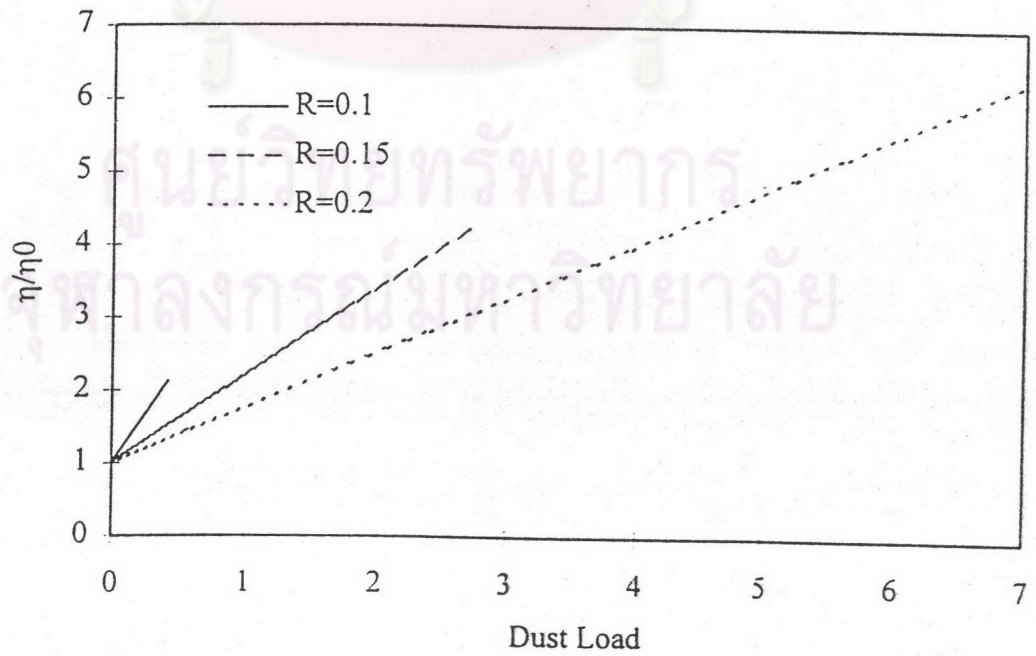


Figure 5.177 Normalized collection efficiency of dust load with  $R$  as parameter for  $St=1$

$e_N$	9.8	10.336	11
$\lambda$	2.395	2.663	2.995

Table 5.17 The collection efficiency raising factor  $\lambda$  for  $R=0.1$   $St=1$  and  $e'n=5.01$

$e'_N$	4.5	5.01	5.5
$\lambda$	2.918	2.663	2.418

Table 5.18 The collection efficiency raising factor  $\lambda$  for  $R=0.1$   $St=1$  and  $en=10.336$

$St$	0.6	1	2
$e_N$	17.453	10.336	2.475
$e'_N$	3.849	5.01	2.006
$\lambda$	6.8020	2.6630	0.2345

Table 5.19 The collection efficiency raising factor  $\lambda$  for  $R=0.1$

$R$	0.1	0.15	0.2
$e_N$	10.336	6.299	5.288
$e'_N$	5.01	2.739	2.287
$\lambda$	2.6630	1.1867	0.7503

Table 5.20 The collection efficiency raising factor  $\lambda$  for  $St=1$



distribution. As seen from the figure, the dendrite concentration  $P_N$  increase a little initially but subsequently decreased faster. Figure 5.164 shows the effect of  $e'_N$  on the average dendrite size. The average dendrite size increased a little faster with increasing  $e'_N$ . Figure 5.165 shows the comparative effect of  $e'_N$  on the total population of dendrites. As seen from the figure, the population of dendrites also becomes smaller when  $e'_N$  increases. Table 5.18 shows the negative effect of  $e'_N$  on  $\lambda$ . Figure 5.166 shows the effect of  $e'_N$  on  $\eta$ . As seen from the figure,  $\eta$  increased more slowly with increasing  $e'_N$ . Figure 5.167 shows the effect of  $e'_N$  on  $\eta/\eta_0$  vs. dust-load. As seen from the figure,  $\eta/\eta_0$  increase more slowly as  $e'_N$  increased

### 5.3.2.3 Effects of St

The effects of St was investigated for  $R=0.1$  and the parameters  $e_N$  and  $e'_N$  shown in Table 5.6. Figure 5.168 shows the effect of St on the dendrite distribution. The dendrite concentration  $P_N$  increased faster as St increased. Figure 5.169 shows effect of St on the average dendrite size. As seen from the figure, the average dendrite size increased a little faster with increasing St. Figure 5.170 shows the effect of St on the total population of dendrites. As seen from the figure, the population of dendrites becomes much larger when St increases. Table 5.19 shows the effect of St on  $\lambda$ .  $\lambda$  decreased because  $\eta_0$  increased with increasing St. Figure 5.171 shows the effect of St on  $\eta$ . As seen from the figure,  $\eta$  increased faster with increasing St because the particles were captured more easily. Figure 5.172 shows the effect of St on  $\eta/\eta_0$  vs. dust-load. As seen from the figure,  $\eta/\eta_0$  increased with increasing St.

### 5.3.2.4 Effect of R on the model

As in the case of convective diffusion, increase in R increased the particle collection efficiency. The effect of R was investigated for  $St=1.0$  and the parameters  $e_N$  and  $e'_N$  shown in Table 5.6. Figure 5.173 shows the effect of R on the dendrite distribution. As seen from the figure, the dendrite distribution curves packed sooner but lower because it was sufficient to capture lies particles when R was large. Figure 5.174 shows the effect of R on the average dendrite size. The average dendrite

size increased faster when  $R$  increased. Figure 5.175 shows the effect of  $R$  on the total population of dendrites. As seen from the figure, when  $N_{gen}$  is small (less than 20), the total population of dendrites at a lower  $R$  is smaller than that at a higher  $R$ . However, as times passes, the total population of dendrites at a larger  $R$  attains a larger asymptotic size. However, in Table 5.20,  $\lambda$  decreased with increasing  $R$ . Figure 5.176 shows the effect of  $R$  on  $\eta$ . As seen from the figure,  $\eta$  increased significantly with increasing  $R$  because large particles were captured more easily. Figure 5.177 shows the effect of  $R$  on  $\eta/\eta_0$  vs. dust-load. As seen from the figure,  $\eta/\eta_0$  increased faster with increasing  $R$ .



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