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## APPENDIX I

### INSTRUMENTATION

#### Equipments

(a) Static Strain Indicator Type SM-60D, Kyowa

Measuring range	:	-29,500 to + 30,500 × 10 <sup>-6</sup> strain
		Minimum reading 5 × 10 <sup>-6</sup> strain.
Meter scale	:	+ 500 × 10 <sup>-6</sup> strain, Scale length 123 mm. Minimum scale 10 × 10 <sup>-6</sup> strain
Gage resistance	:	60 to 500 ohms
Bridge voltage	:	1.6 V.DC.
Gage factor	:	2.00, constant
Accuracy	:	10 × 10 <sup>-6</sup> strain of least reading 1 % of each range
Operating temperature	:	-10°C to + 50°C

(b) Switching and Balancing Box Model SS-24R, Kyowa

Input Configurations

and Gage Compatibility	:	Quarter bridge 60, 120, 350 and 500 Ohms, 3-lead-wire arrangement Half bridge 60-1,000 ohms Full bridge 60, 120, 350 and 500 ohms
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**Resistive Bridge**

**Balance** : Screwdriver adjustment on built-in 10-turn potentiometers, up to 1.5 % of difference in gage resistances.

**Zero Drift due to**

**Switching** :  $2 \times 10^{-6}$  strain or less with Gage Factor setting at 2.00

**Bridge Co-ordinate** : 4 position 1, 2, 4 gage and Next

**Gage Resistance**

**Co-ordinate** : 4 positions : 60, 120, 350 and 500 ohms

**Bridge Balance**

**Change-over** : Toggle Switch NON-BAL/BAL, useful when no bridge balance is required

**(c) Strain Gage, Kyowa**

**Type** : KFC - 5 - D16 - 11

**Gage Resistance** :  $120.0 \pm 0.4$  ohms

**Gage Factor** :  $2.10 \pm 1$  %

**Thermal output** :  $\pm 1.8 \mu\epsilon/^\circ\text{C}$

**(d) Dial Gage, Mitutoyo**

**Range** : 20 mm.

**No.** : 2050 B

**Graduation** : 0.01 mm.

## APPENDIX II

### TABLES

This content is composed of the results obtained from the proposed solution and the experimental investigation. The results are shown in tabular form from table 1 through table 11.

Table 1 Measured points.

Point	Positions for Measuring Deflection		Positions for Measuring Strain	
	x (mm.)	y (mm.)	x (mm.)	y (mm.)
1	270	0	270	0
2	210	0	210	0
3	150	0	150	0
4	90	0	90	0
5	30	0	30	0
6	30	17	30	17
7	90	52	90	52
8	150	87	150	87
9	210	121	210	121
10	270	156	270	156
11	270	95	270	104
12	270	60	270	52

Table 2 Theoretical values of deflection for case 1.

Co-ordinate (x, y)	$wD/qa^4$	
	$\nu = 0.3$	$\nu = 0.1$
300, 0	0.0614	0.0596
250, 0	0.0813	0.0854
200, 0	0.1029	0.1111
150, 0	0.1223	0.1336
100, 0	0.1373	0.1506
50, 0	0.1466	0.1612
0, 0	0.1498	0.1648
50, 28.87	0.1456	0.16
100, 57.73	0.1331	0.1459
150, 86.6	0.1133	0.1231
200, 115.47	0.0852	0.0919
250, 144.34	0.0488	0.0517
300, 173.2	0	0

Table 3 Experimental deflections for case 1.

Point	$w \times 10^2$ (mm.)					
	490.5 (N/m <sup>2</sup> )	981 (N/m <sup>2</sup> )	1471.5 (N/m <sup>2</sup> )	1962 (N/m <sup>2</sup> )	2452.5 (N/m <sup>2</sup> )	2943 (N/m <sup>2</sup> )
Dial gauge rdg. No.						
1	10.5	14	21.5	27.5	34	40.5
2	13.3	21	31.5	41	52.5	63
3	15	19	42.5	56	72	85.5
4	16.2	34	51	68.5	85.5	101.5
5	17	37	57	76	96	113
6	11	35	52	69.5	87	104
7	19	30	44	59.5	73	87
8	25	22.5	32	44	55	65.5
9	29	13	18.5	25	31.5	37

Table 4 Theoretical values of moment for case 1.

Co-ordinate (x, y)	$M_x/qa^2$		$M_y/qa^2$	
	$\nu = 0.3$	$\nu = 0.1$	$\nu = 0.3$	$\nu = 0.1$
300 0	- 0.1288	- 0.139	0.3993	0.4329
250 0	0.0483	0.0391	0.3216	0.3388
200 0	0.1626	0.153	0.2885	0.2937
150 0	0.2324	0.2217	0.2819	0.2715
100 0	0.2721	0.2601	0.2873	0.2783
50 0	0.2919	0.2789	0.2946	0.284
0 0	0.2978	0.2844	0.2978	0.2844

Co-ordinate (x, y)	$M_\eta/qa^2$		$M_\xi/qa^2$	
	$\nu = 0.3$	$\nu = 0.1$	$\nu = 0.3$	$\nu = 0.1$
0 0	0.2978	0.2844	0.2978	0.2844
50 28.87	0.2904	0.2776	0.2931	0.2811
100 57.73	0.2721	0.2608	0.2753	0.2674
150 86.6	0.2535	0.2454	0.2337	0.2318
200 115.47	0.2529	0.2503	0.15	0.1556
250 144.34	0.2957	0.302	- 0.0011	0.0123
300 173.2	0.4144	0.4344	- 0.2522	- 0.2322



Table 5. Experimental strains for case 1.

Point	Strain x 10 <sup>6</sup>					
	490.5 (N/m <sup>2</sup> )	981 (N/m <sup>2</sup> )	1471.5 (N/m <sup>2</sup> )	1962 (N/m <sup>2</sup> )	2452.5 (N/m <sup>2</sup> )	2943 (N/m <sup>2</sup> )
1x	0	0	2	4	8	10
1y	0	10	20	22	36	43
2x	8	16	20	40	53	65
2y	10	20	34	44	58	71
3x	10	20	42	58	70	88
3y	16	30	44	60	76	92
4x	18	40	60	80	108	140
4y	16	30	50	70	79	82
5x	20	48	66	90	133	168
5y	16	40	56	90	112	132
6 $\eta$	20	40	62	80	105	133
6 $\xi$	20	40	54	70	98	128
7 $\eta$	20	38	54	66	98	132
7 $\xi$	20	36	42	66	94	121
8 $\eta$	18	34	50	60	79	94
8 $\xi$	10	20	30	40	52	68
9 $\eta$	16	32	40	56	75	92
9 $\xi$	8	16	24	36	52	64
10 $\eta$	2	2	10	20	22	29
10 $\xi$	0	2	2	6	9	10



Table 6 Experimental moments for case 1.

Point	Moment (N-m/m)			
	490.5 (N/m <sup>2</sup> )	981 (N/m <sup>2</sup> )	1471.5 (N/m <sup>2</sup> )	1962 (N/m <sup>2</sup> )
1x	0	0.4	4.51	5.99
1y	0	5.65	11.6	13.12
2x	6.21	12.42	17.06	30.1
2y	7	14	22.6	31.65
3x	8.37	16.4	31.2	42.96
3y	10.73	20.35	32	43.75
4x	12.88	27.7	42.4	46.81
4y	12.1	23.72	38.44	53.14
5x	14.02	33.9	46.81	66.1
5y	12.43	30.75	42.8	66.13
6η	14.7	29.4	44.2	57
6ξ	14.7	29.4	41.04	53.14
7η	14.7	27.6	39.34	48.5
7ξ	14.7	26.79	38.55	48.5
8η	11.86	22.6	33.35	40.7
8ξ	8.7	17.07	25.44	32.78
9η	10.4	20.8	26.7	37.7
9ξ	7.23	14.5	20.35	29.84
10η	1.13	1.5	6	12.3
10ξ	0.34	1.5	2.8	6.8

Table 7 Theoretical values of deflection for case 2.

Co-ordinate (x, y)		$wD/Pa^2$	
		$\nu = 0.3$	$\nu = 0.1$
300	0	0.021	0.0219
250	0	0.0312	0.0345
200	0	0.0421	0.0473
150	0	0.0526	0.0593
100	0	0.0618	0.0696
50	0	0.0688	0.0773
0	0	0.072	0.0808
50	28.87	0.0679	0.0763
100	57.73	0.0591	0.0666
150	86.6	0.0476	0.0537
200	115.47	0.0341	0.0383
250	144.34	0.0186	0.0207
300	173.2	0	0

Table 3 Experimental deflections for case 2.

Point	$w \times 10^2$ (mm.)				
	10 (kg)	20 (kg)	30 (kg)	40 (kg)	50 (kg)
Dial guage rdg. No.					
1	6	13	19.5	25.5	32
2	11.4	23.6	35.2	47.2	59
3	15.7	32	48.7	64	80.5
4	20.6	40.8	61	81.5	101
5	23.5	46.5	69.5	91	115
6	23.5	48	71.6	96	119.5
7	19.2	39	57.2	79	98
8	14.4	29.6	44	59.6	74.6
9	8.2	17	23.6	34.7	43

Table 9 Theoretical values of moment for case 2.

Co-ordinate (x, y)	$M_x/P$		$M_y/P$	
	$\nu = 0.3$	$\nu = 0.1$	$\nu = 0.3$	$\nu = 0.1$
300 0	- 0.0348	- 0.0438	0.1349	0.1553
250 0	0.013	0.0054	0.1199	0.135
200 0	0.0503	0.0422	0.1227	0.1336
150 0	0.0844	0.0741	0.1404	0.1473
100 0	0.1239	0.1096	0.1738	0.176
50 0	0.187	0.1653	0.2355	0.2302
0 0	$\infty$	$\infty$	$\infty$	$\infty$

Co-ordinate (x, y)	$M_\eta/P$		$M_\xi/P$	
	$\nu = 0.3$	$\nu = 0.1$	$\nu = 0.3$	$\nu = 0.1$
0 0	$\infty$	$\infty$	$\infty$	$\infty$
50 28.87	0.1741	0.154	0.2224	0.2186
100 57.73	0.113	0.1004	0.1588	0.1623
150 86.6	0.082	0.0743	0.1169	0.1242
200 115.47	0.0706	0.0677	0.0765	0.0853
250 144.34	0.0812	0.084	0.0257	0.0336
300 173.2	0.1206	0.1314	-0.0465	-0.0427

Table 10 Experimental strains for case 2.

Point	Strain x 10 <sup>6</sup>				
	10 (kg)	20 (kg)	30 (kg)	40 (kg)	50 (kg)
1x	0	0	0	0	0
1y	0	4	10	17	23
2x	6	16	19	31	38
2y	11	24	38	52	64
3x	30	35	49	64	82
3y	13	26	44	64	87
4x	27	50	80	112	144
4y	24	56	87	120	169
5x	40	89	132	178	233
5y	45	94	144	195	259
6 $\eta$	35	70	111	157	204
6 $\xi$	49	97	150	208	266
7 $\eta$	18	33	57	80	108
7 $\xi$	23	48	78	111	151
8 $\eta$	16	23	28	45	62
8 $\xi$	14	28	45	65	87
9 $\eta$	10	17	27	41	56
9 $\xi$	4	14	19	28	38
10 $\eta$	14	17	17	19	24
10 $\xi$	0	0	0	0	0

Table 11 Experimental moments for case 2.

Point	Moment (N - m/m)			
	10 (kg)	20 (kg)	30 (kg)	40 (kg)
1x	0	0.68	1.7	2.88
1y	0	2.26	5.65	9.61
2x	5.26	13.11	17.18	26.34
2y	7.23	16.28	24.70	34.65
3x	19.16	24.2	35.16	47.03
3y	12.44	20.63	33.18	47.03
4x	19.33	37.76	60	83.66
4y	18.15	40.13	62.75	86.83
5x	30.24	66.25	99	133.69
5y	32.22	68.23	203.78	140.41
6 $\eta$	28.09	56.02	88.18	124.02
6 $\xi$	33.63	66.70	103.61	144.2
7 $\eta$	14.07	26.79	45.45	64.04
7 $\xi$	16.05	22.73	53.76	76.31
8 $\eta$	11.41	17.75	23.46	36.46
8 $\xi$	10.63	19.73	30.19	44.37
9 $\eta$	6.33	11.98	18.48	27.92
9 $\xi$	3.96	10.8	15.32	22.78
10 $\eta$	7.91	9.61	9.61	10.74
10 $\xi$	2.37	2.88	2.88	3.22

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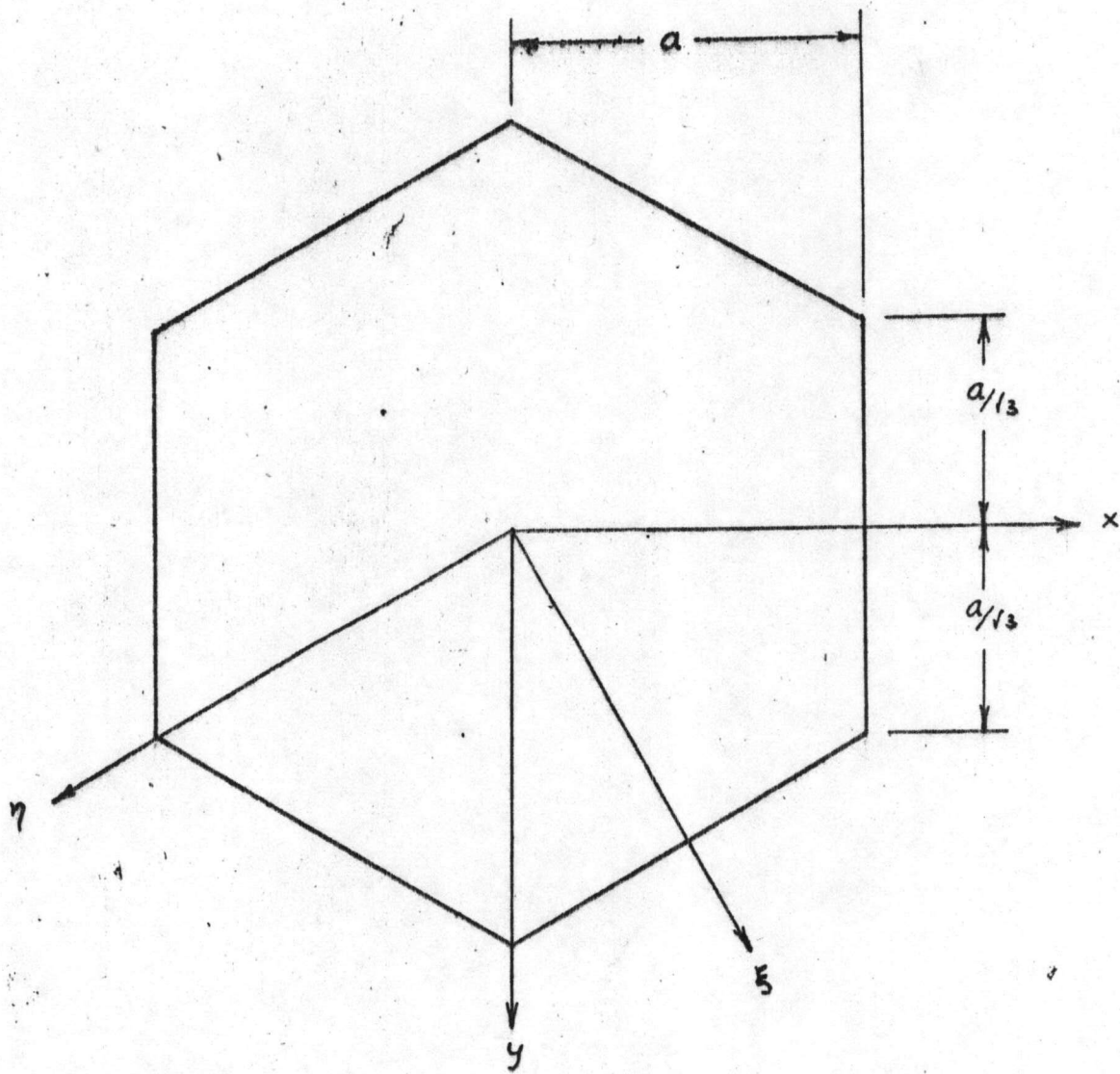


Fig 1. Hexagonal Plate



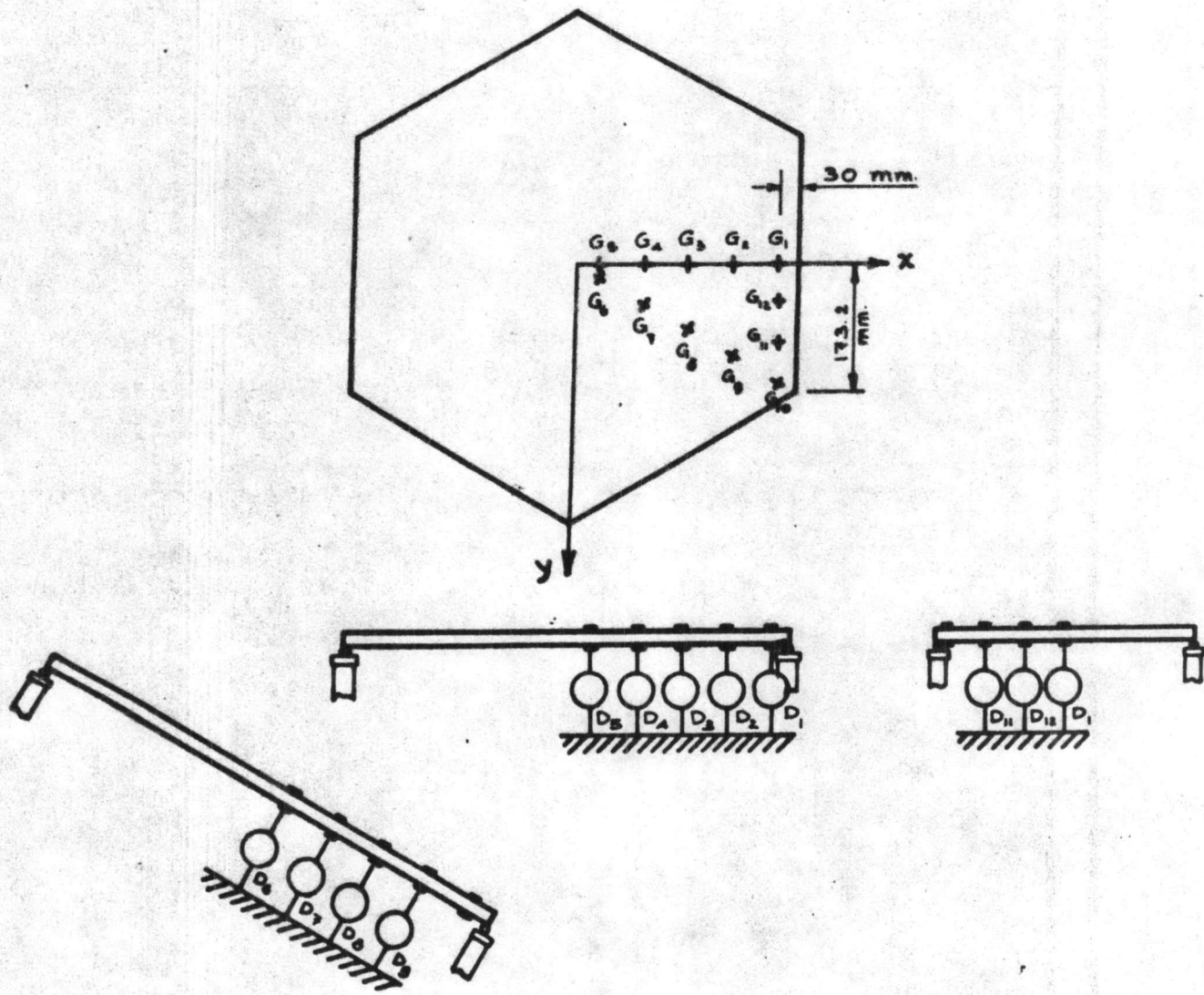


Fig. 2. Schematic Diagram of supports and instrumentations

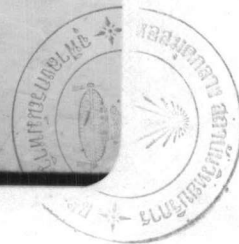
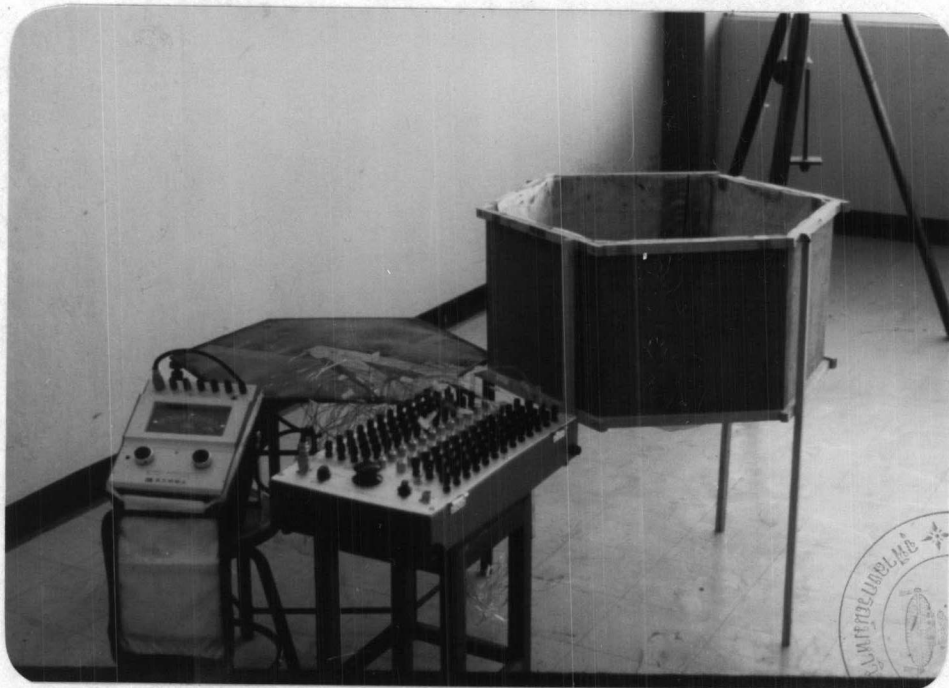


Fig. 3. Set up for the experimentation. Case 1.



Fig. 4 Set up for the experimentation. Case 2.

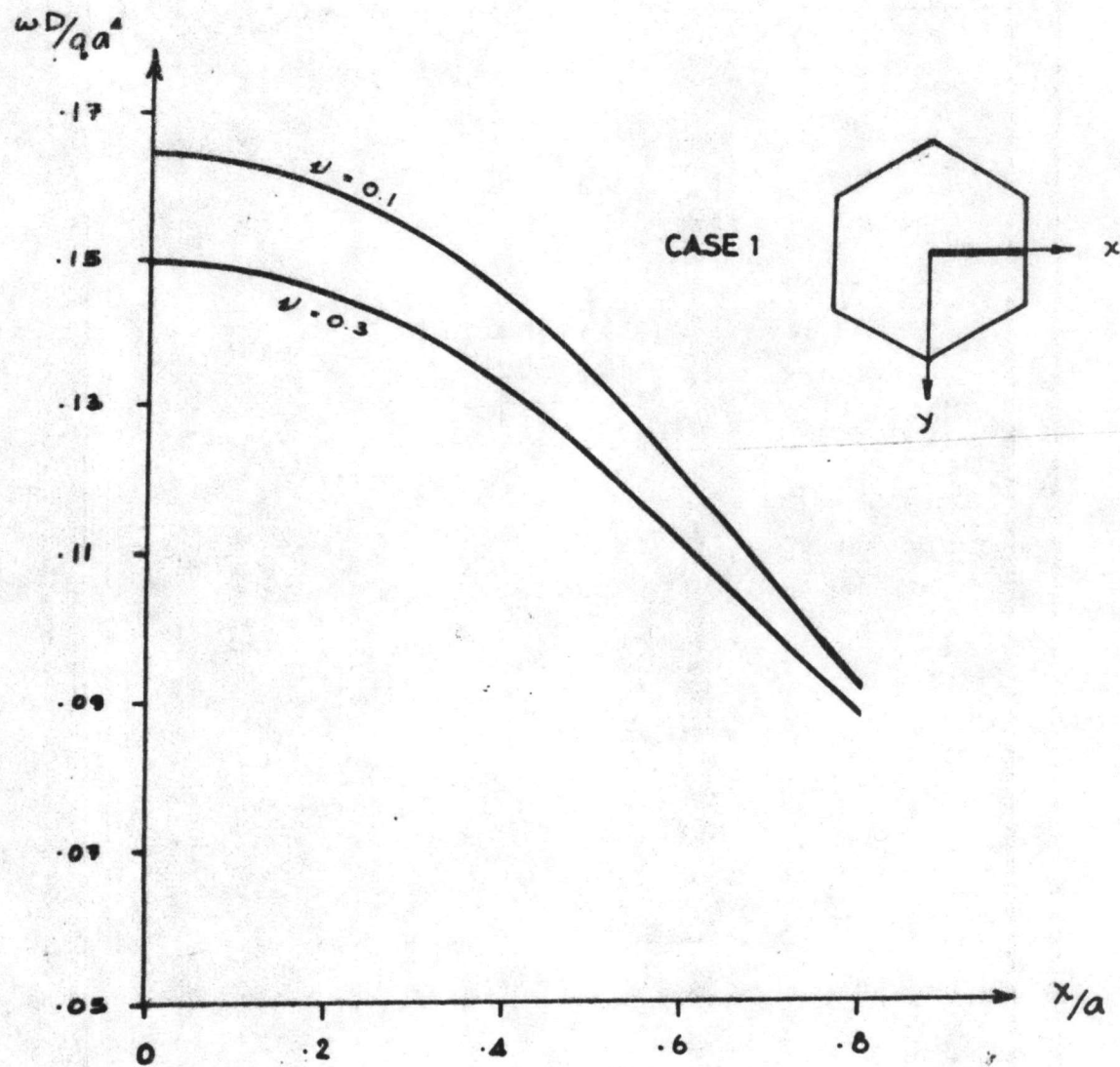


Fig. 5. Theoretical deflection v.s.  $x/a$ ,  $y/a = 0$

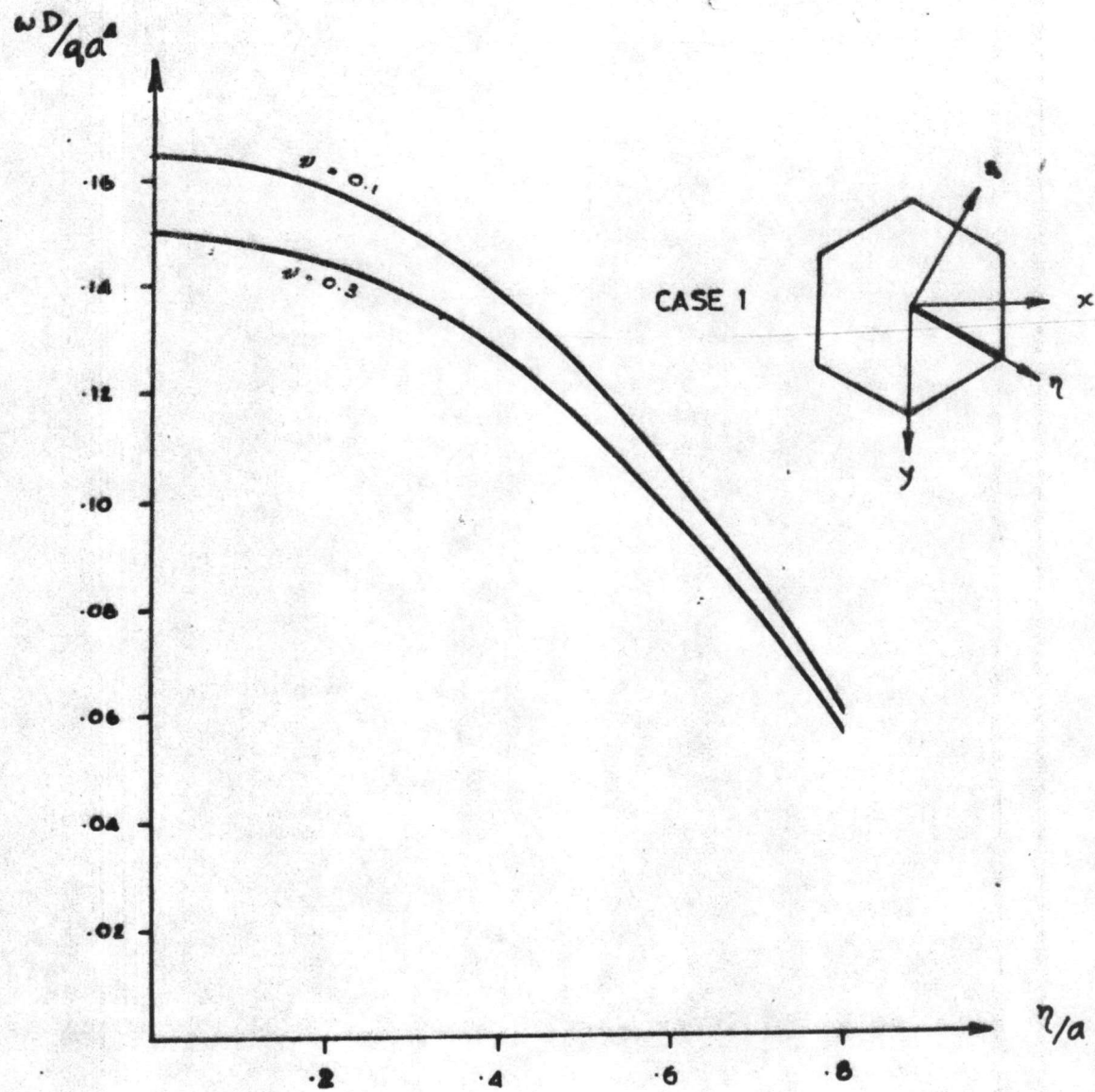


Fig. 6. Theoretical deflection v.s.  $\eta/a$ ,  $\epsilon/a = 0$

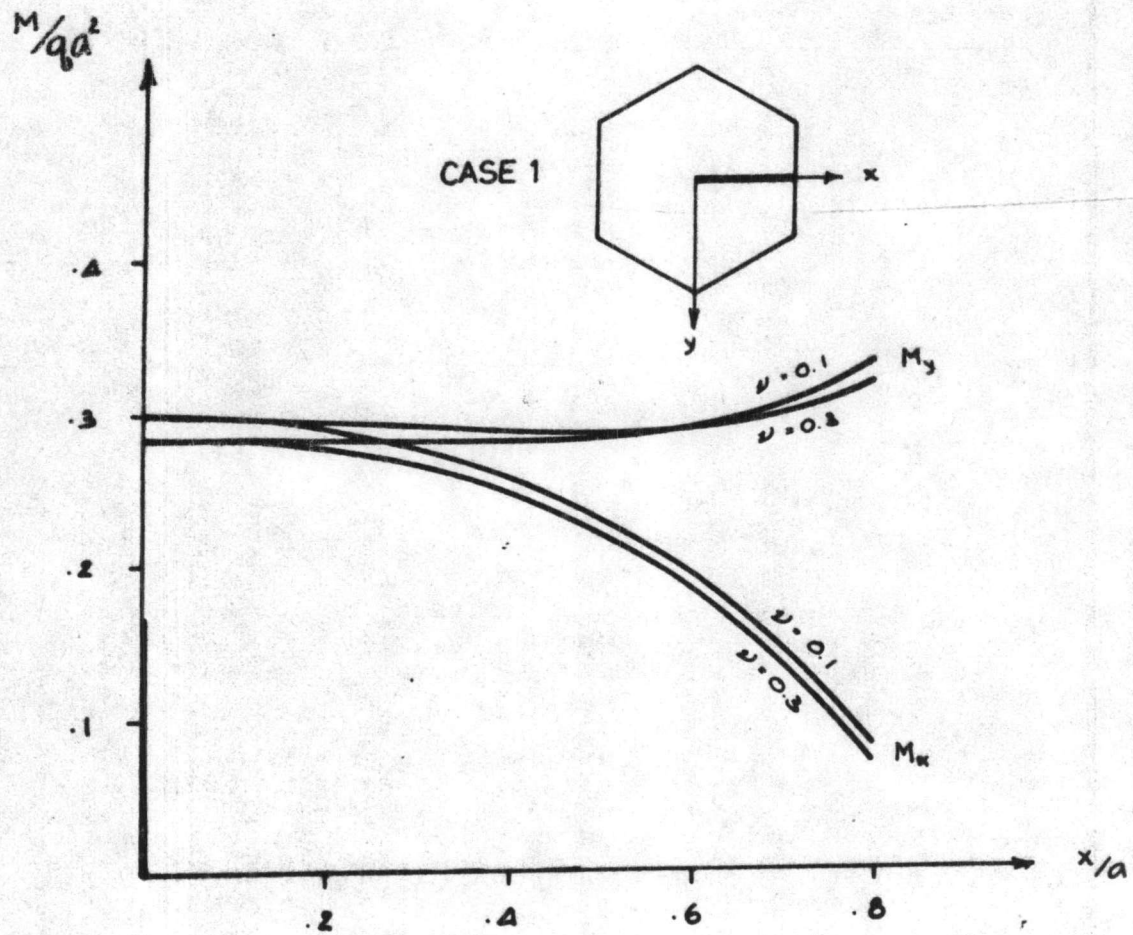


Fig. 7. Theoretical moment v.s.  $x/a$ ,  $y/a = 0$

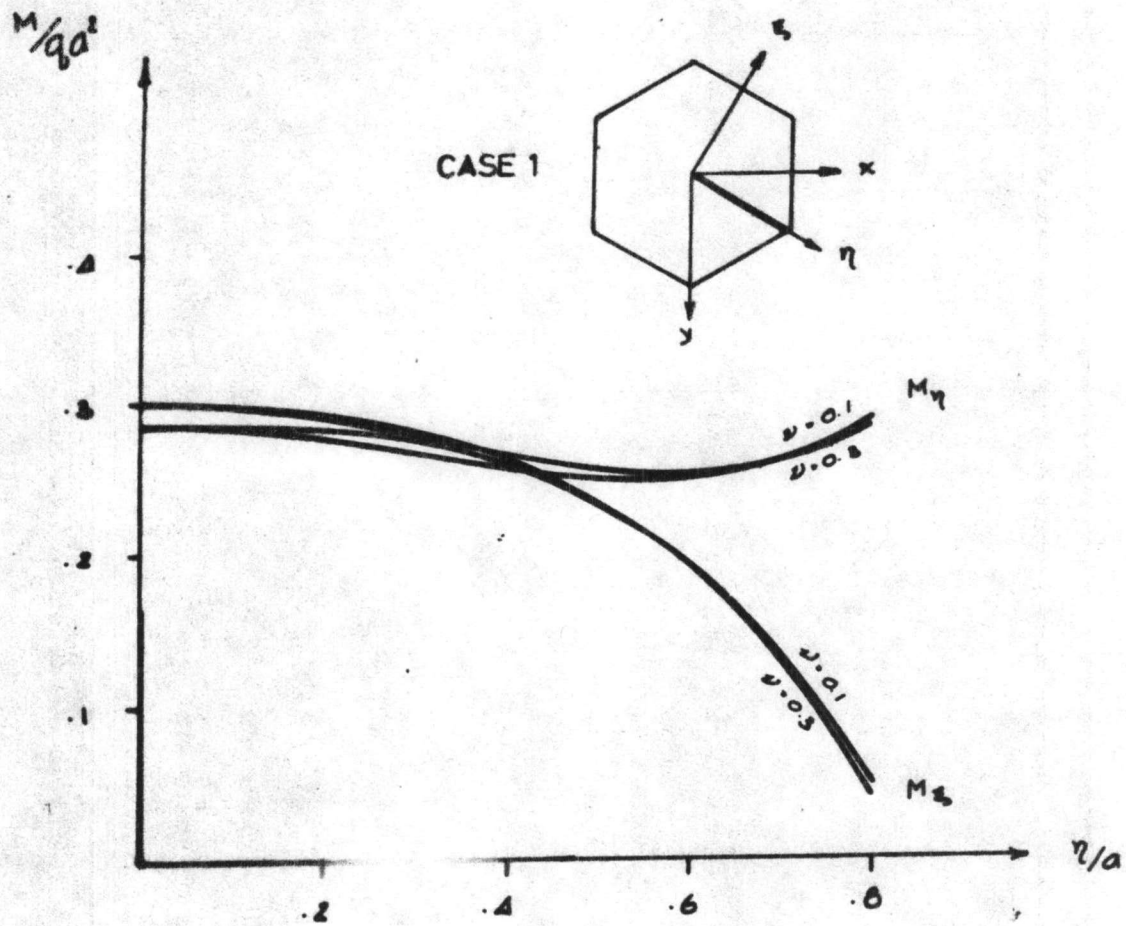


Fig. 8. Theoretical moment v.s.  $\eta/a$ ,  $\xi/a = 0$

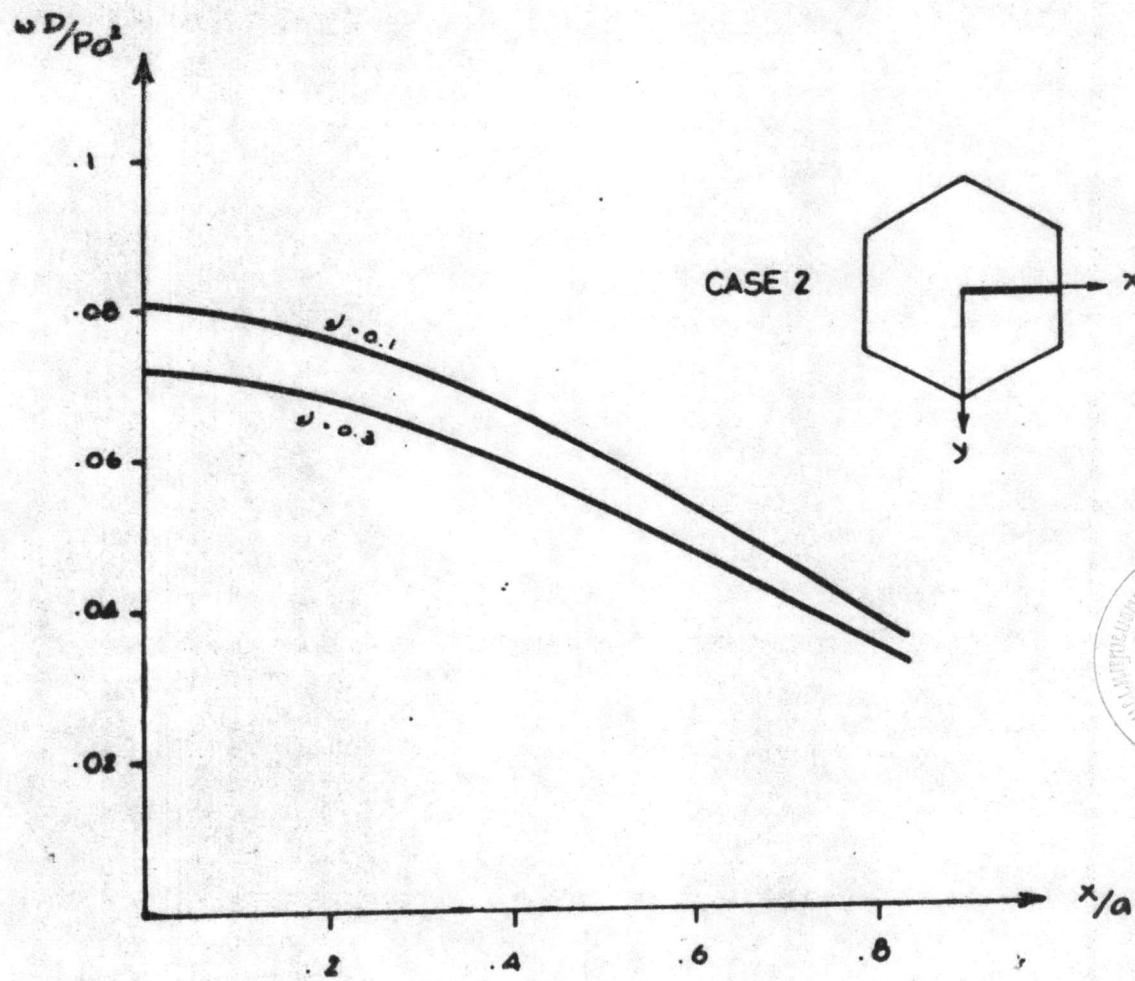


Fig. 9. Theoretical deflection v.s.  $x/a$ .  $y/a = 0$



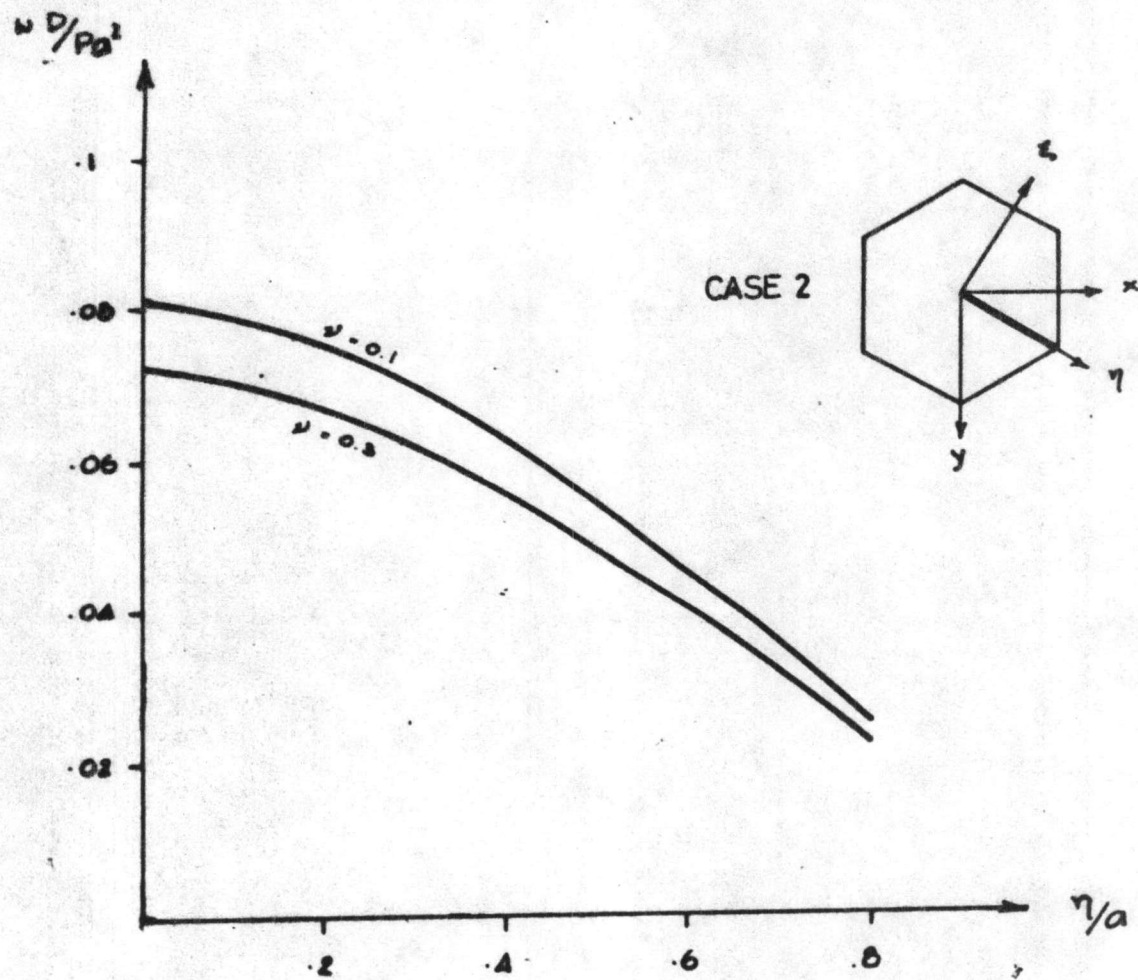


Fig. 10. Theoretical deflection v.s.  $\eta/a$ ,  $\xi/a = 0$

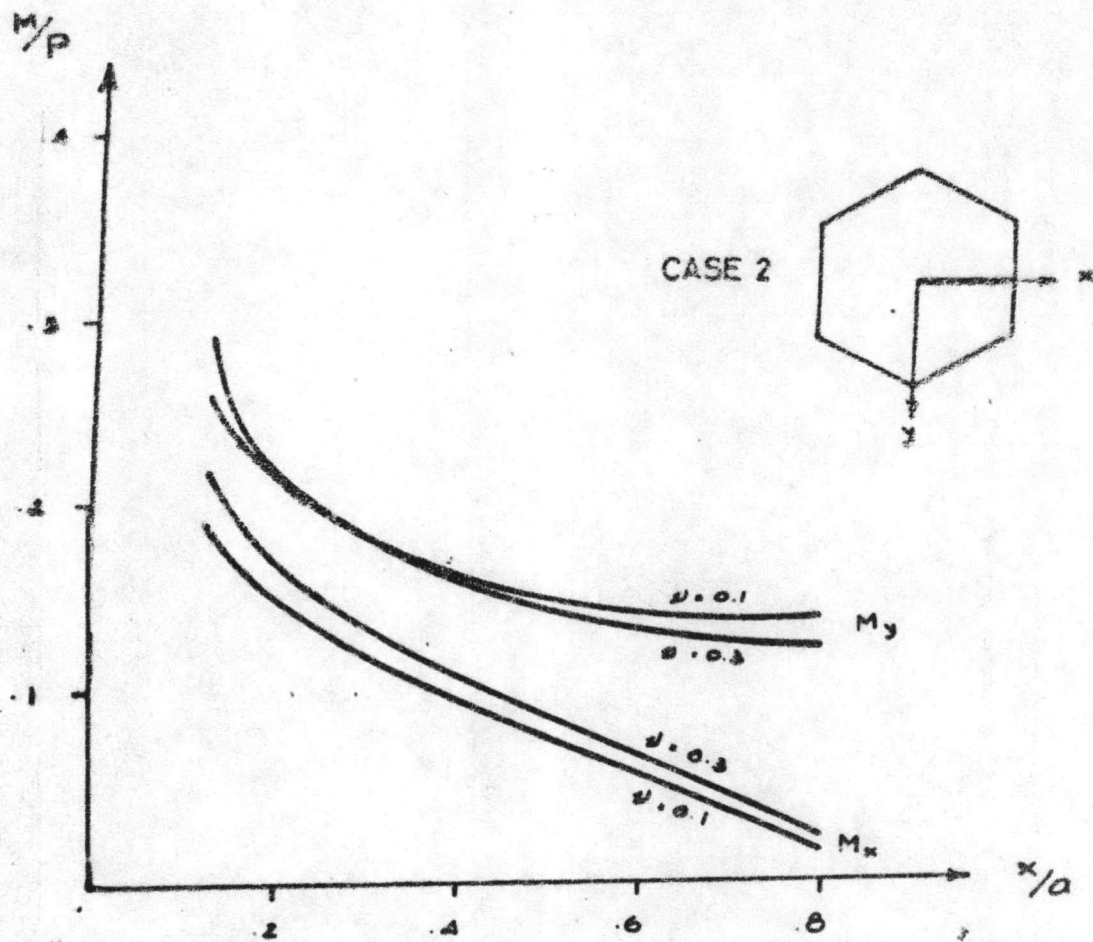


Fig II. Theoretical moment v.s.  $x/a$ ,  $y/a=0$

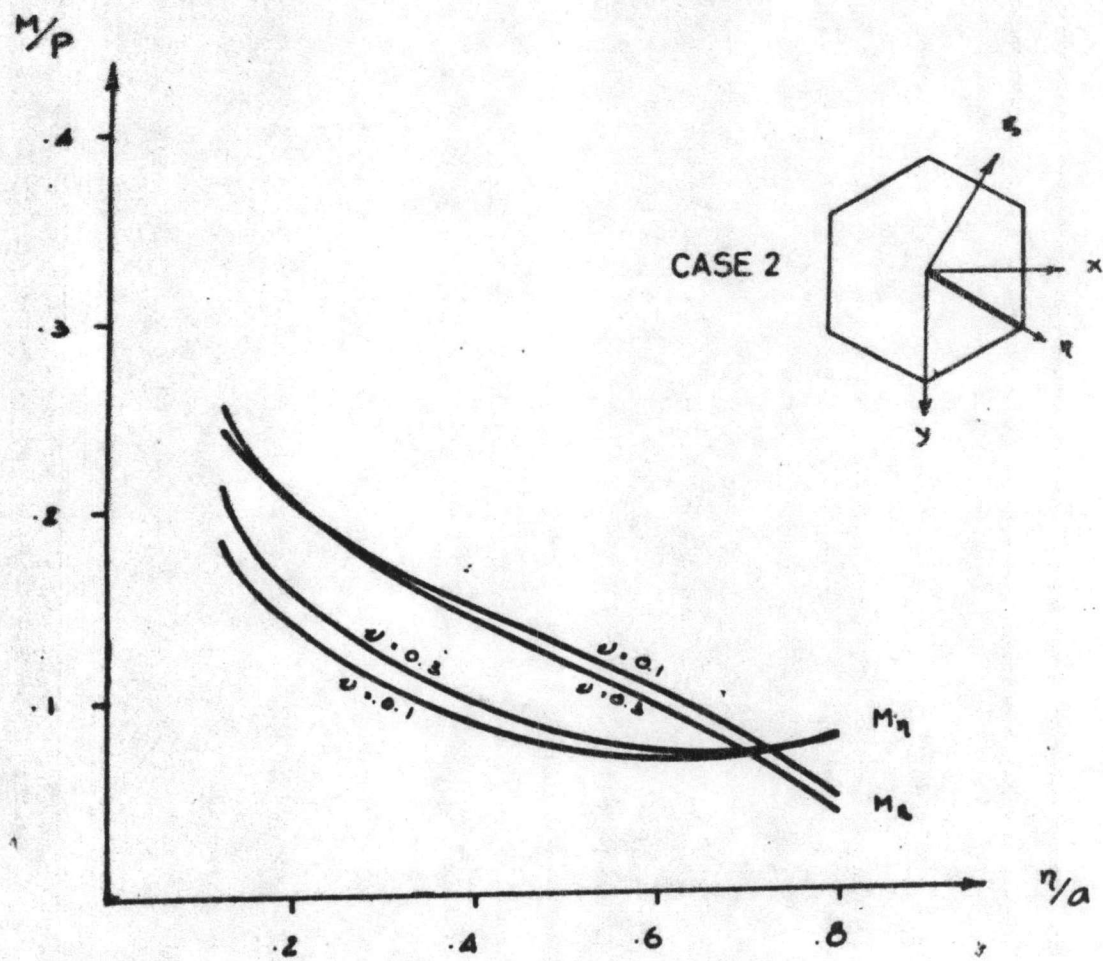


Fig. 12. Theoretical moment v.s.  $\eta/a$ ,  $\xi/a=0$

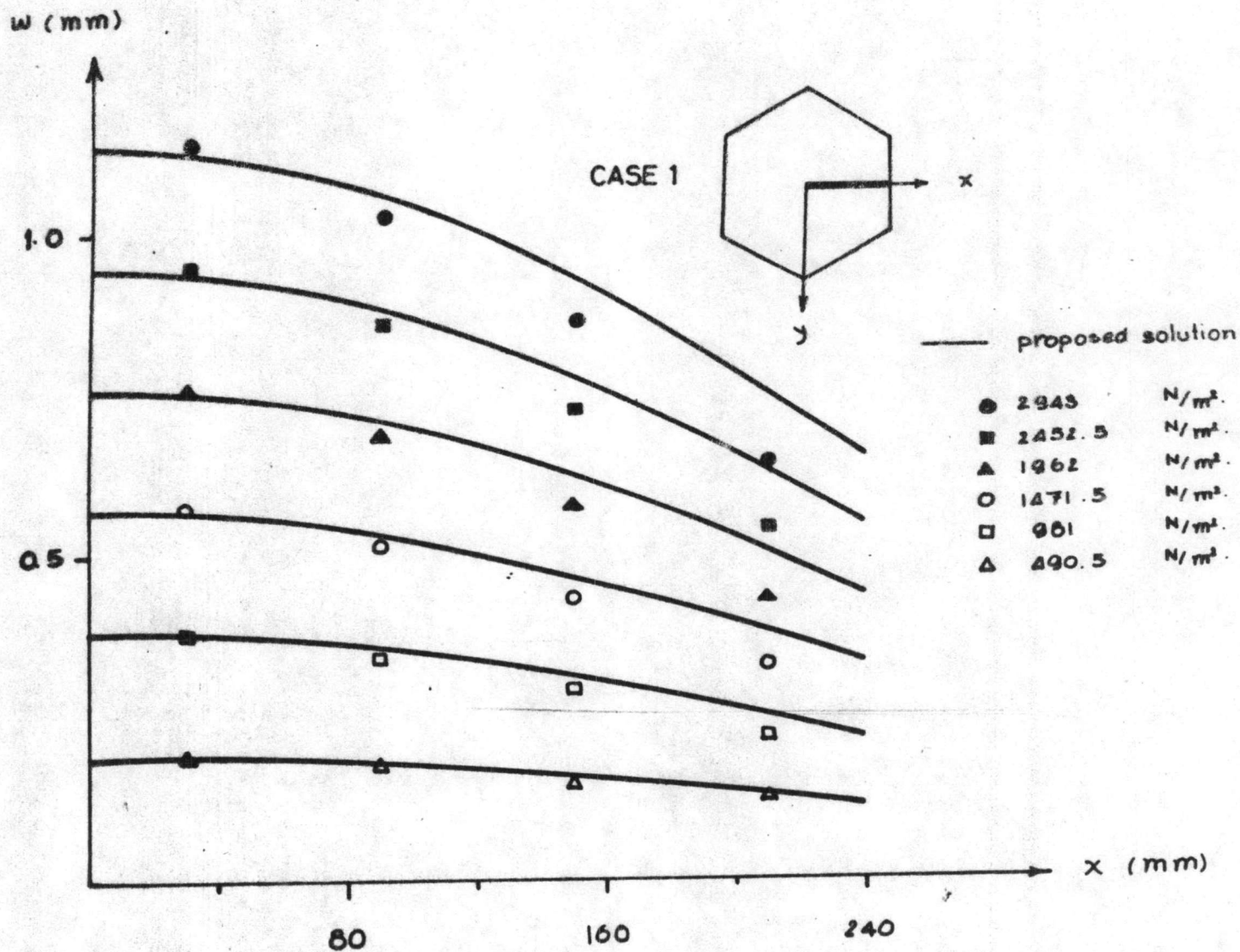


Fig. 13. Experimental deflection v.s.  $x$ ,  $y=0$

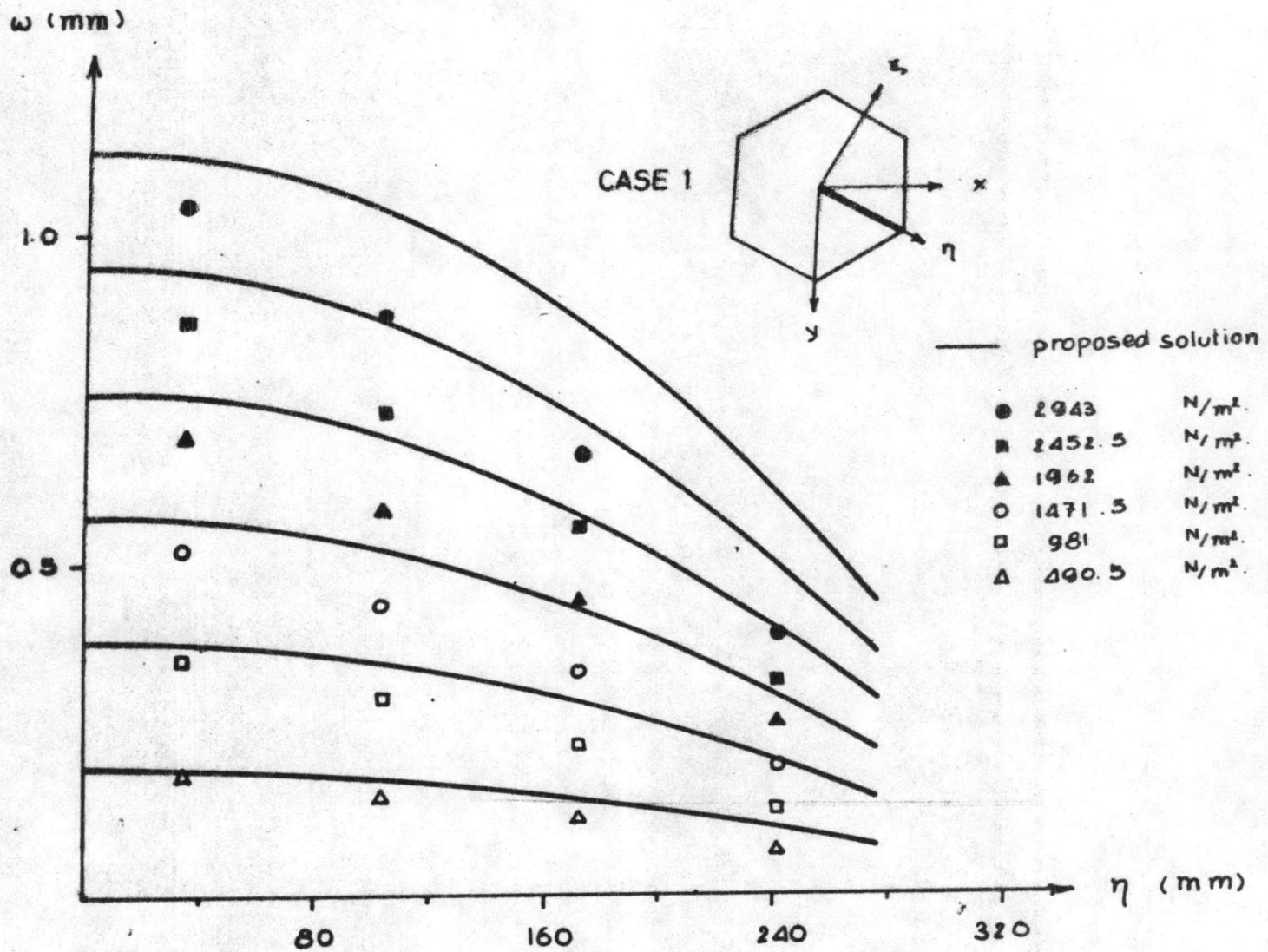


Fig. 14. Experimental deflection v.s  $\eta$ .  $\xi = 0$

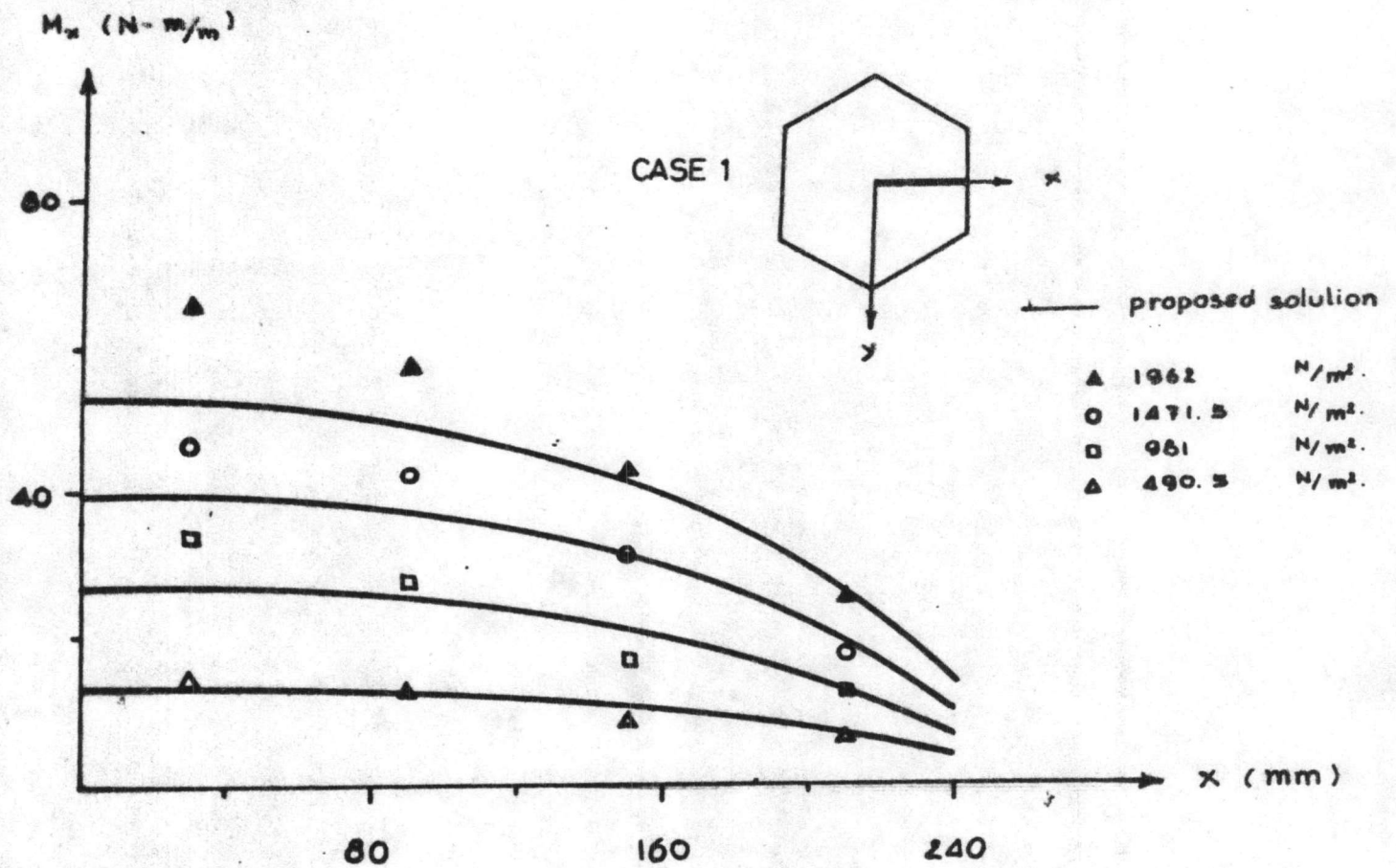


Fig.15. Experimental moment ( $M_x$ ) v.s.  $x$ ,  $y=0$

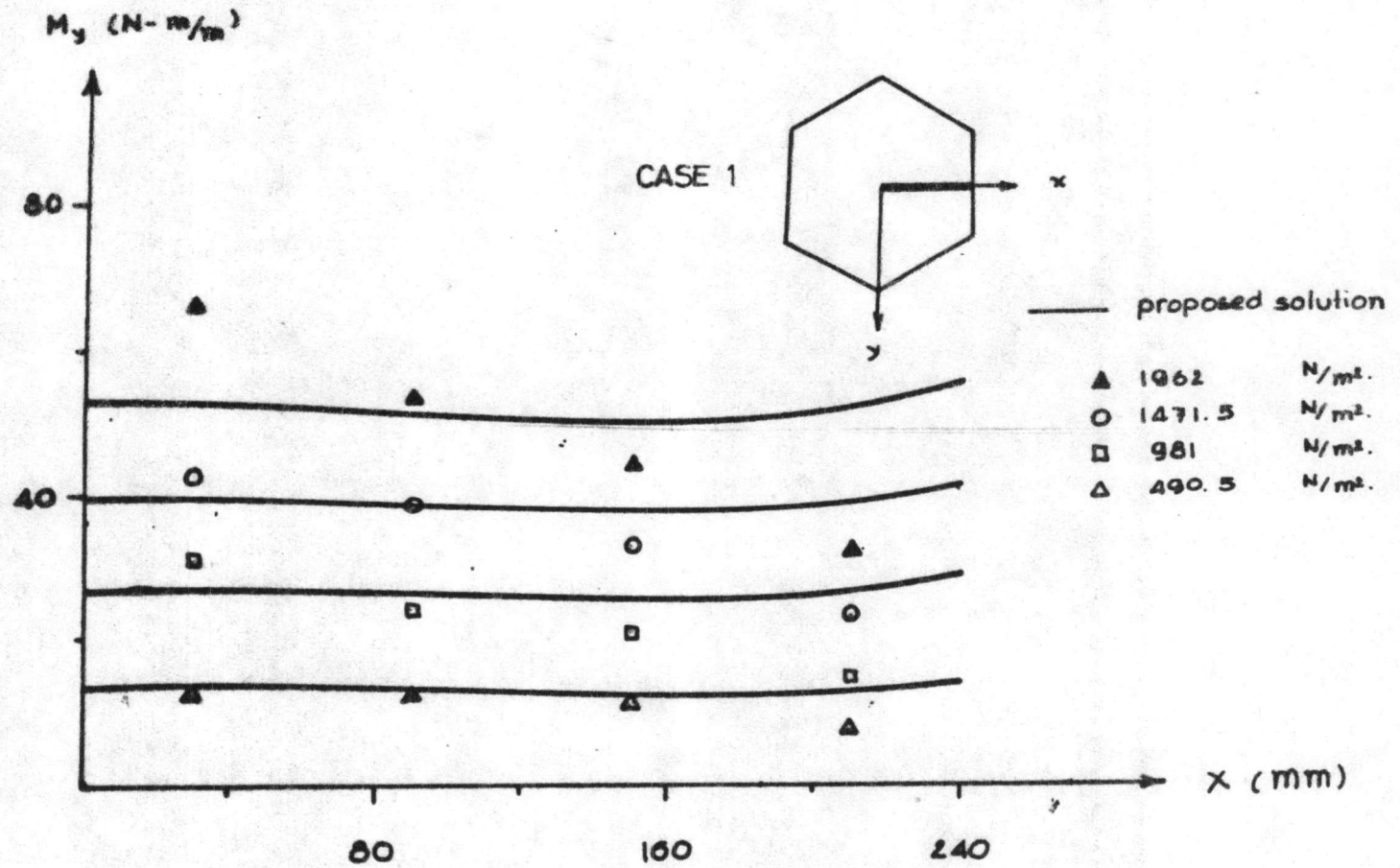


Fig. 16. Experimental moment ( $M_y$ ) v.s.  $x$ ,  $y=0$

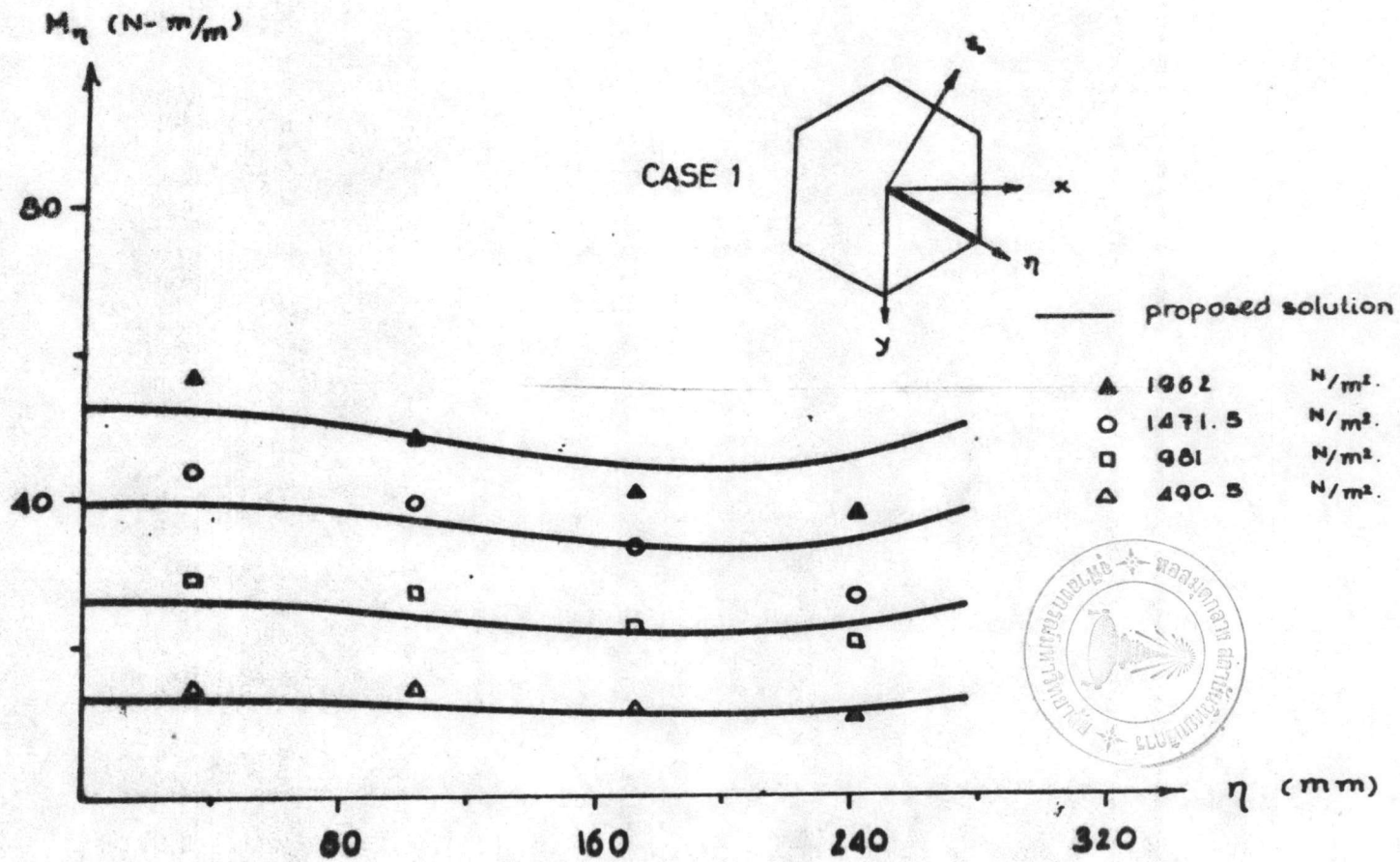


Fig.17. Experimental moment ( $M_\eta$ ) v.s.  $\eta$ ,  $\epsilon = 0$



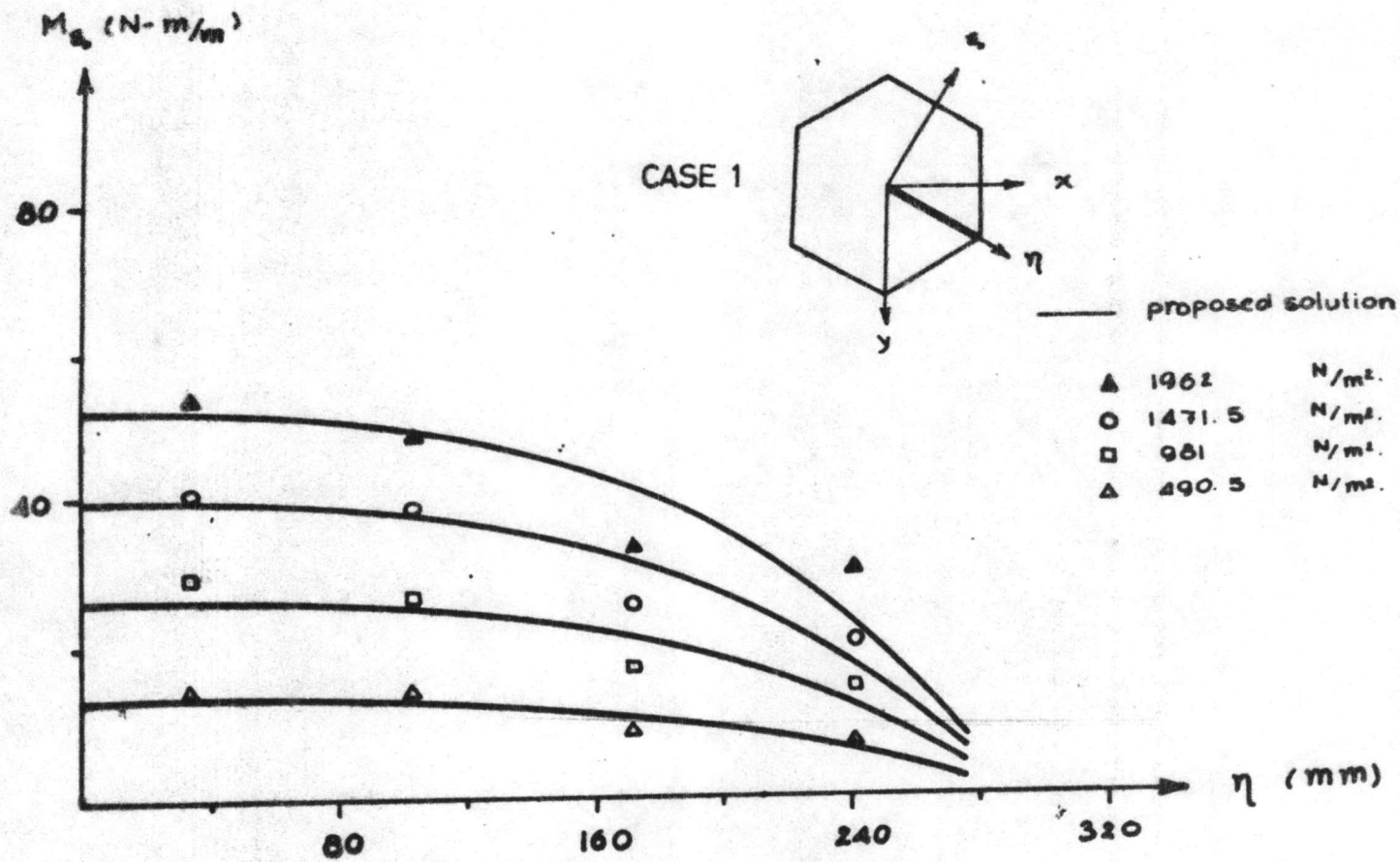


Fig. 18. Experimental moment ( $M_x$ ) v.s.  $\eta$ .  $z=0$

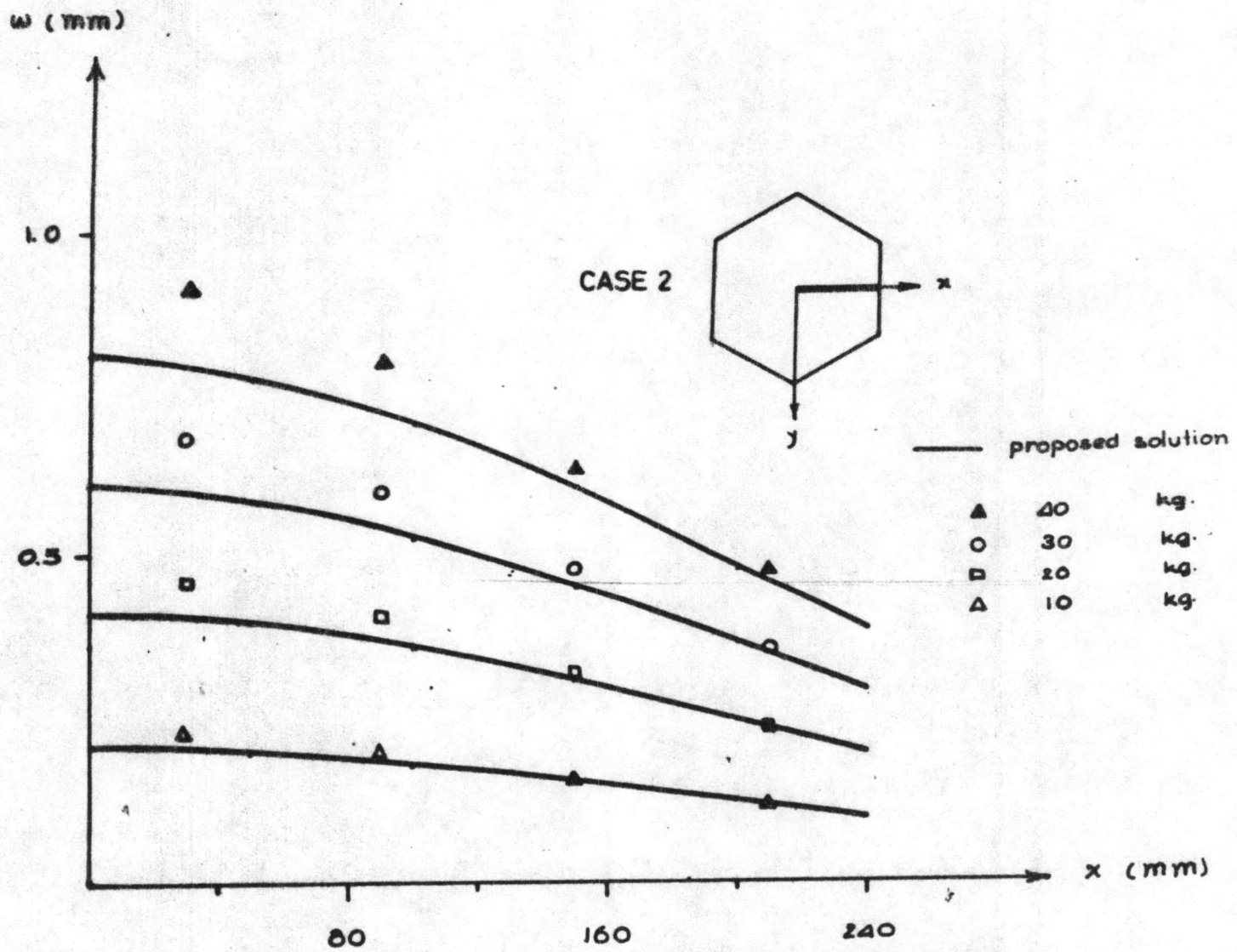


Fig. 19. Experimental deflection v.s.  $x$ ,  $y = 0$

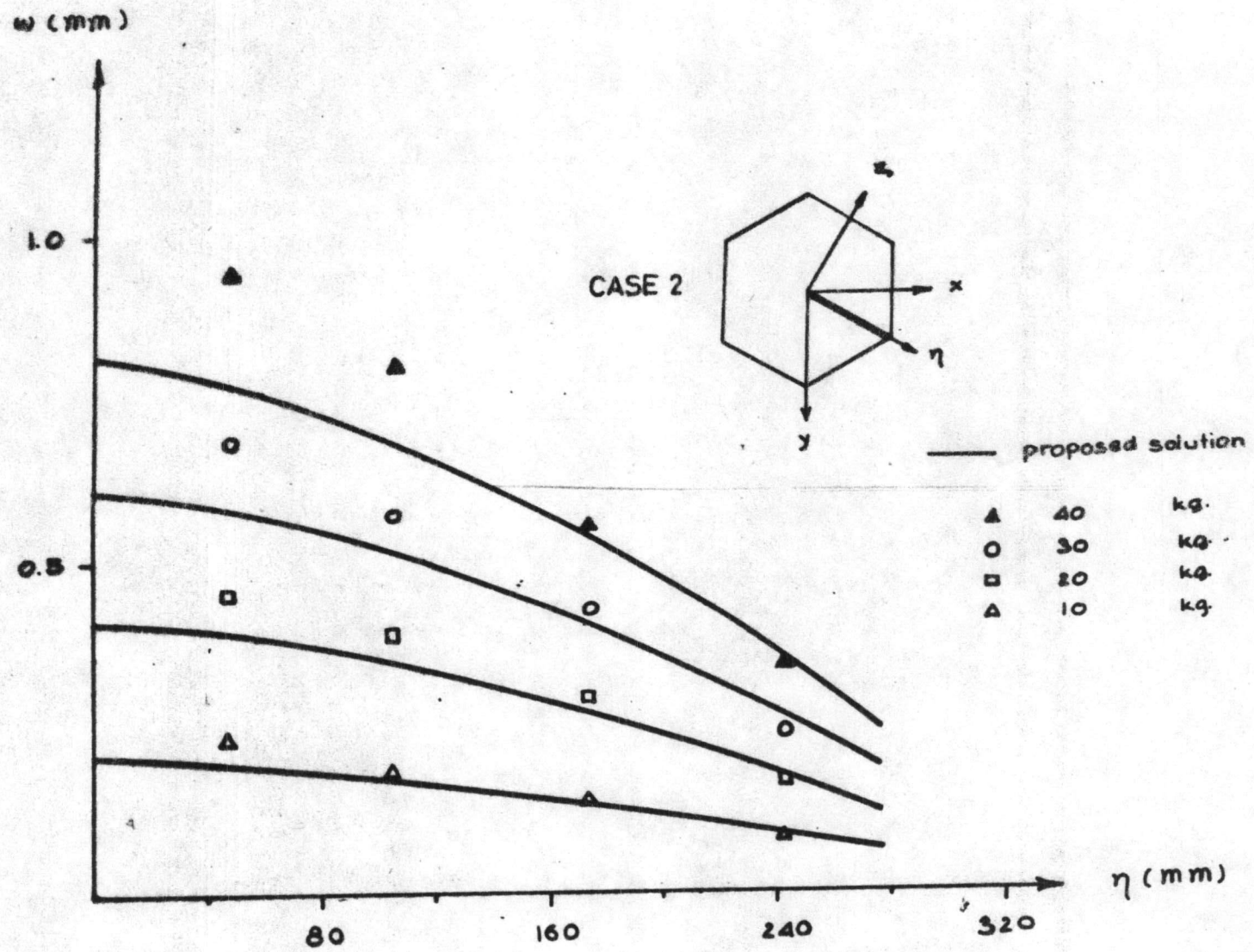


Fig. 20. Experimental deflection v.s  $\eta$ ,  $\xi = 0$

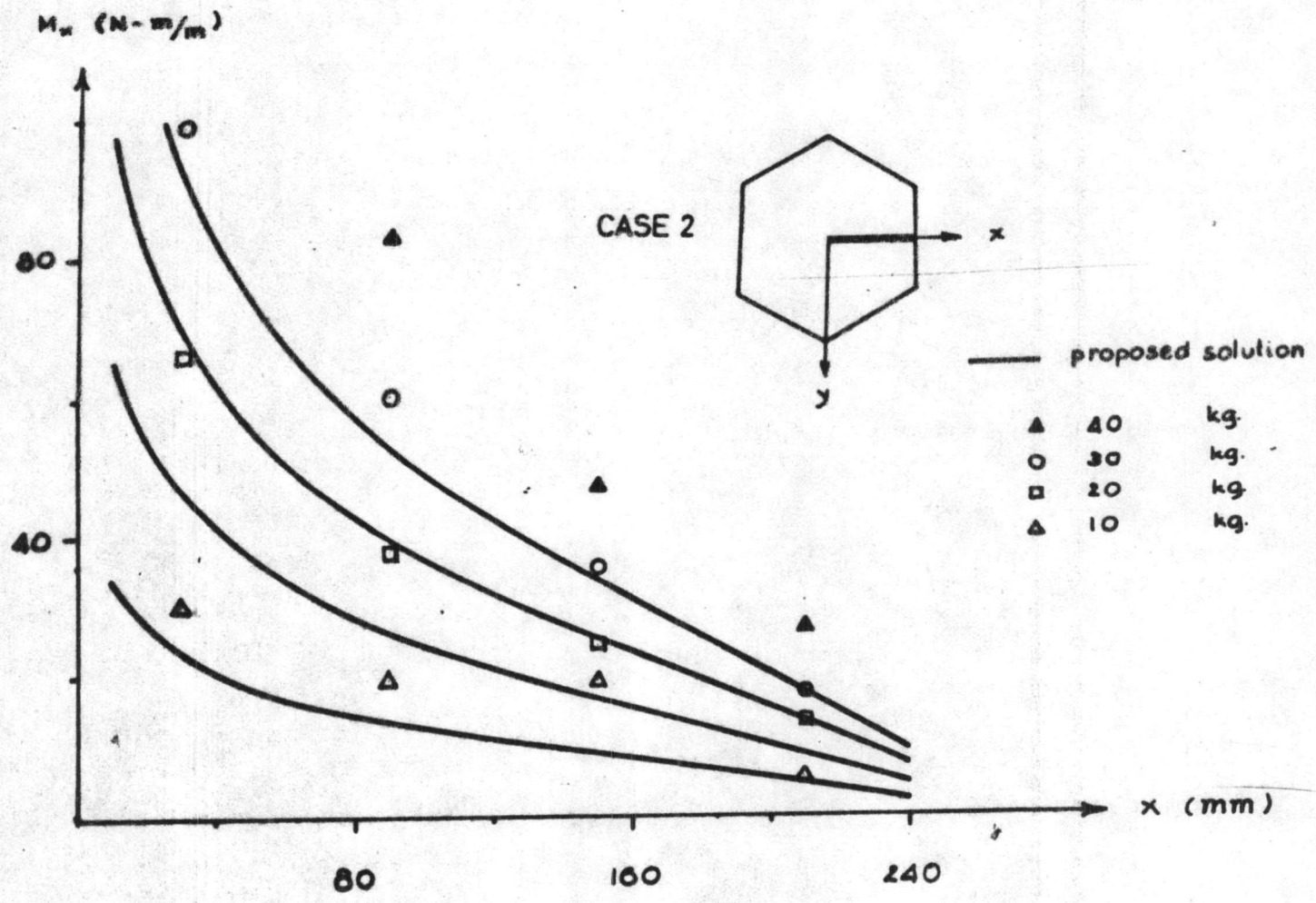


Fig. 21. Experimental moment ( $M_x$ ) v.s.  $x$ ,  $y=0$

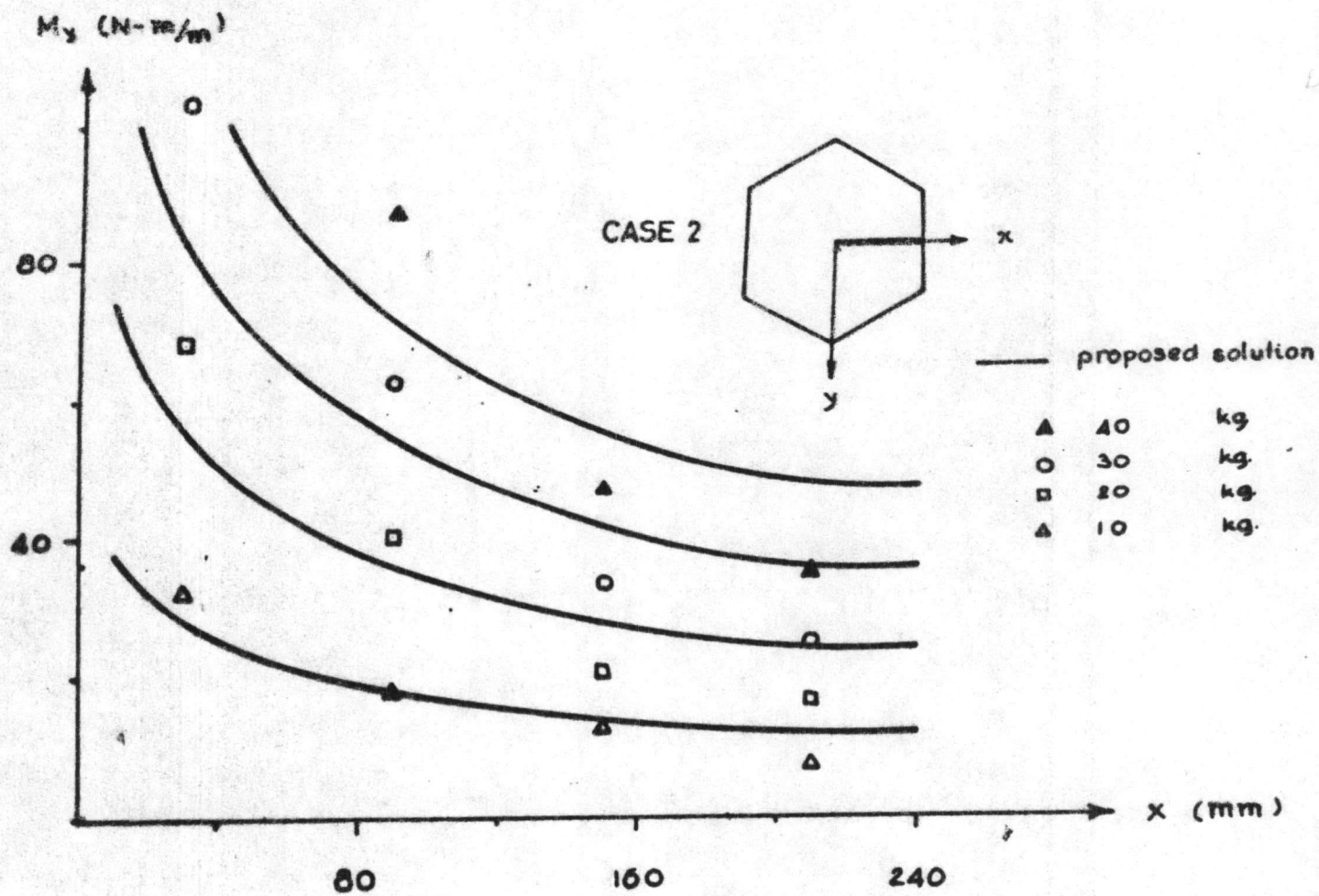


Fig. 22. Experimental moment ( $M_y$ ) v.s.  $x$ ,  $y=0$

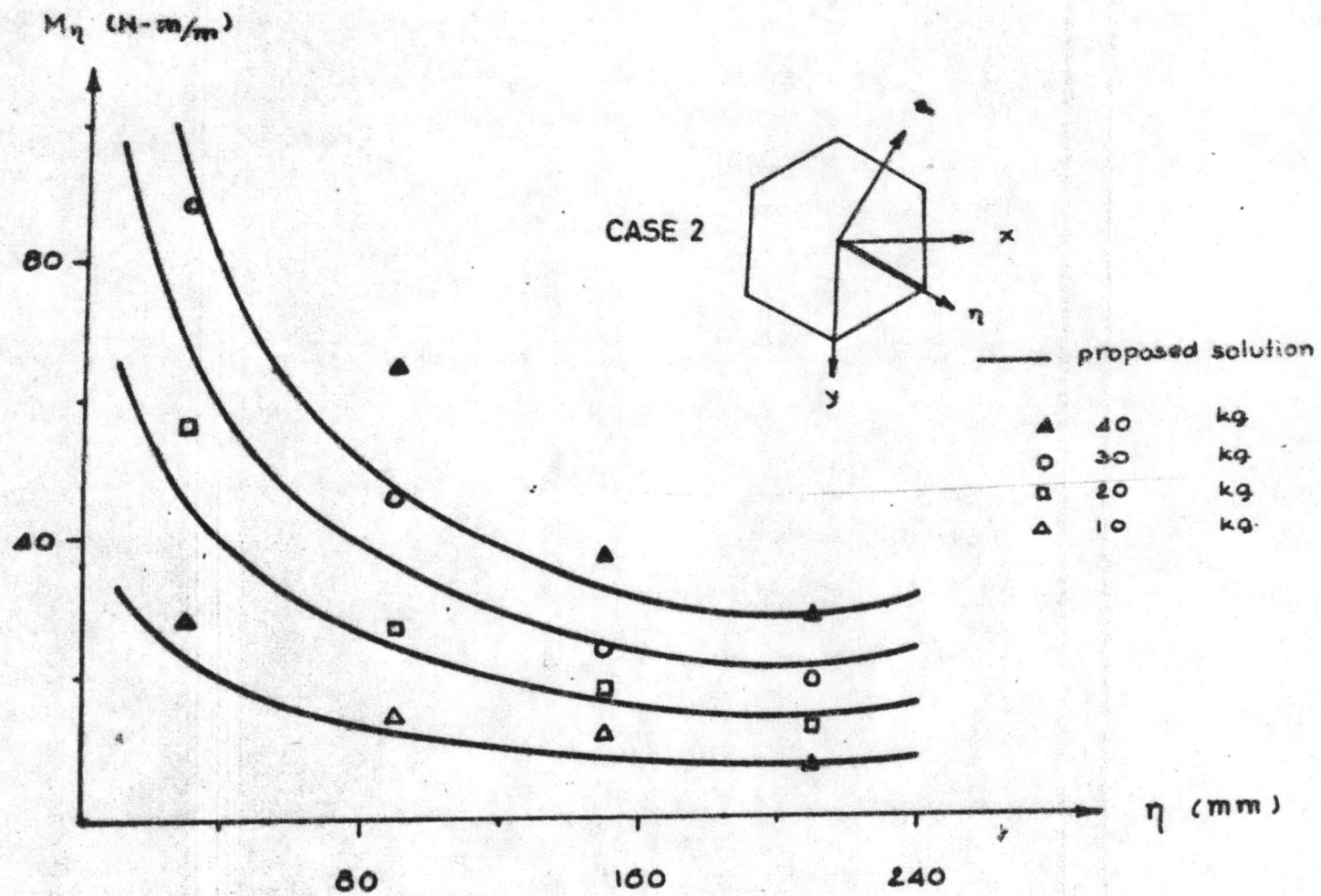


Fig. 23. Experimental moment ( $M_\eta$ ) v.s.  $\eta$ ,  $\alpha = 0$

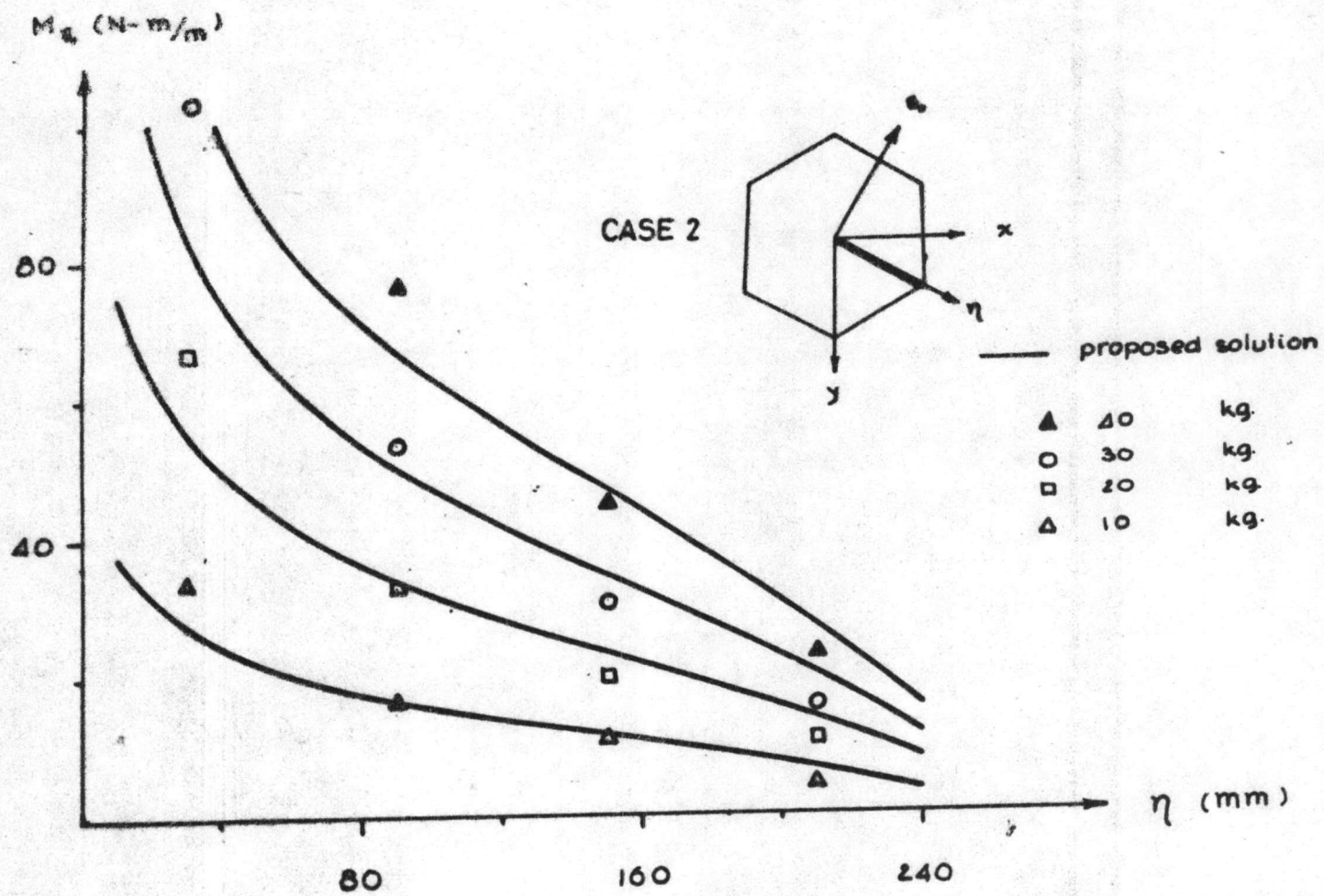


Fig.24. Experimental moment ( $M_s$ ) v.s.  $\eta$ ,  $\epsilon = 0$

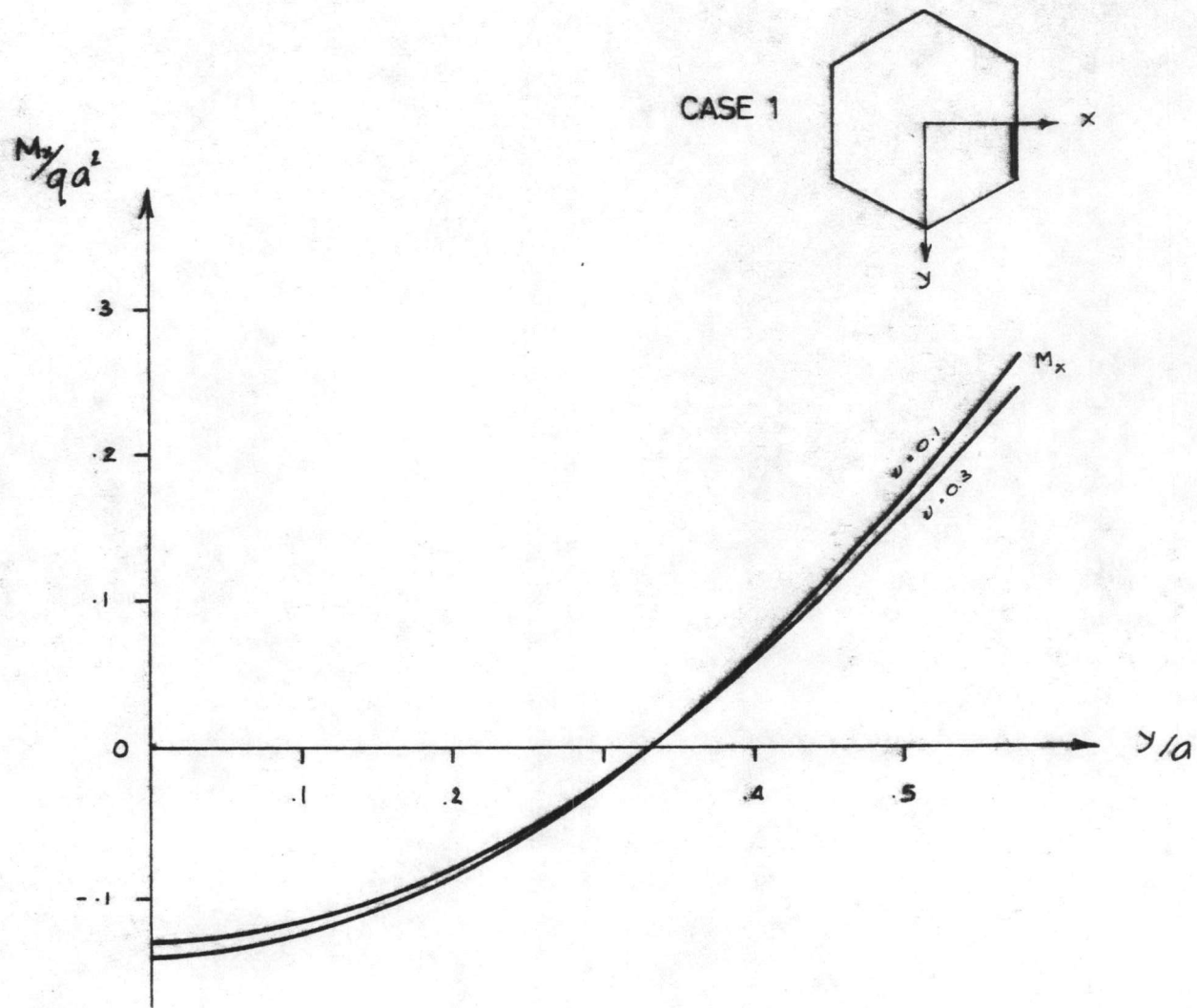


Fig. 25. Theoretical moment v.s.  $y/a$ ,  $x/a = 1$



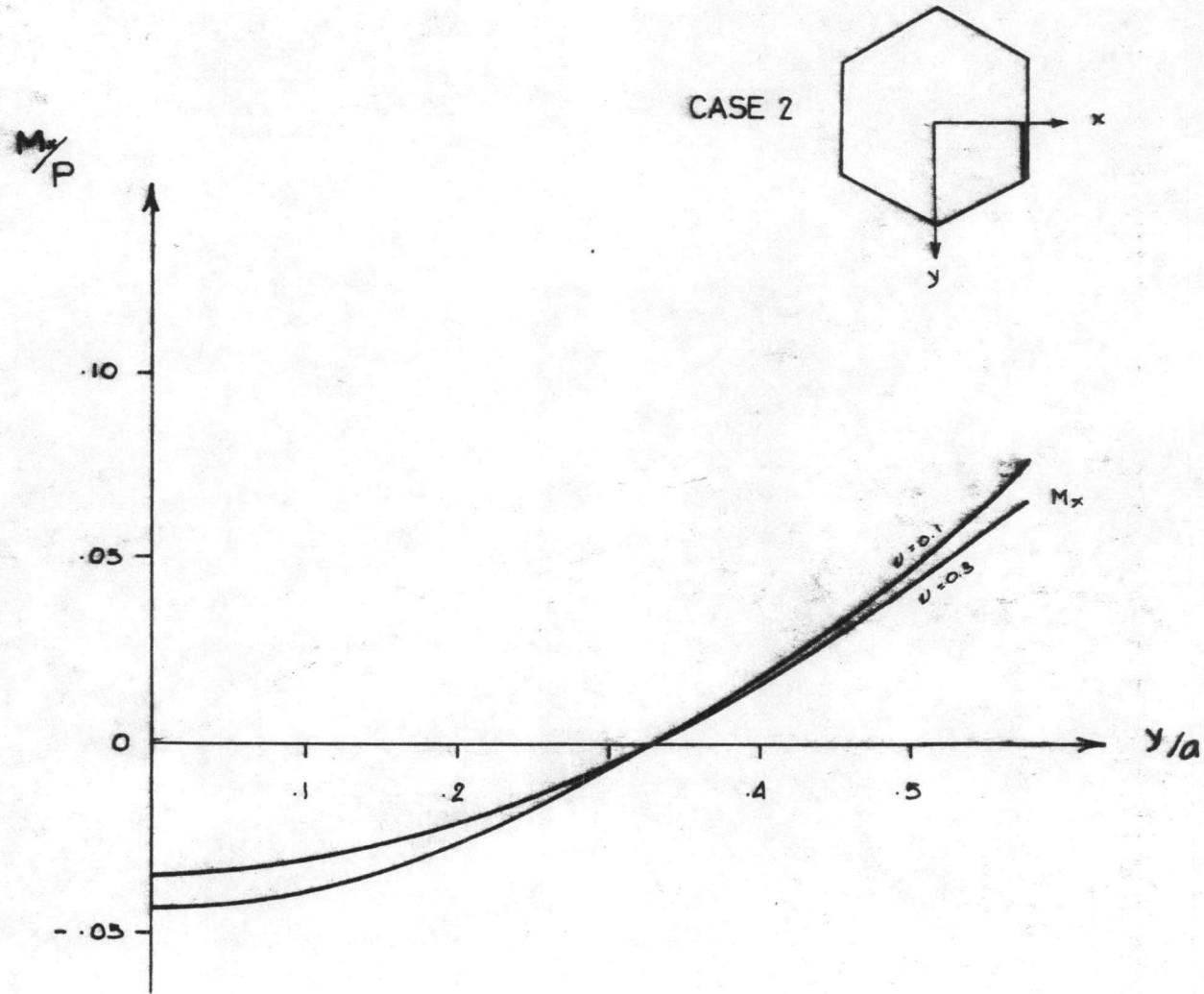


Fig. 26. Theoretical moment v.s.  $y/a$ ,  $x/a = 1$

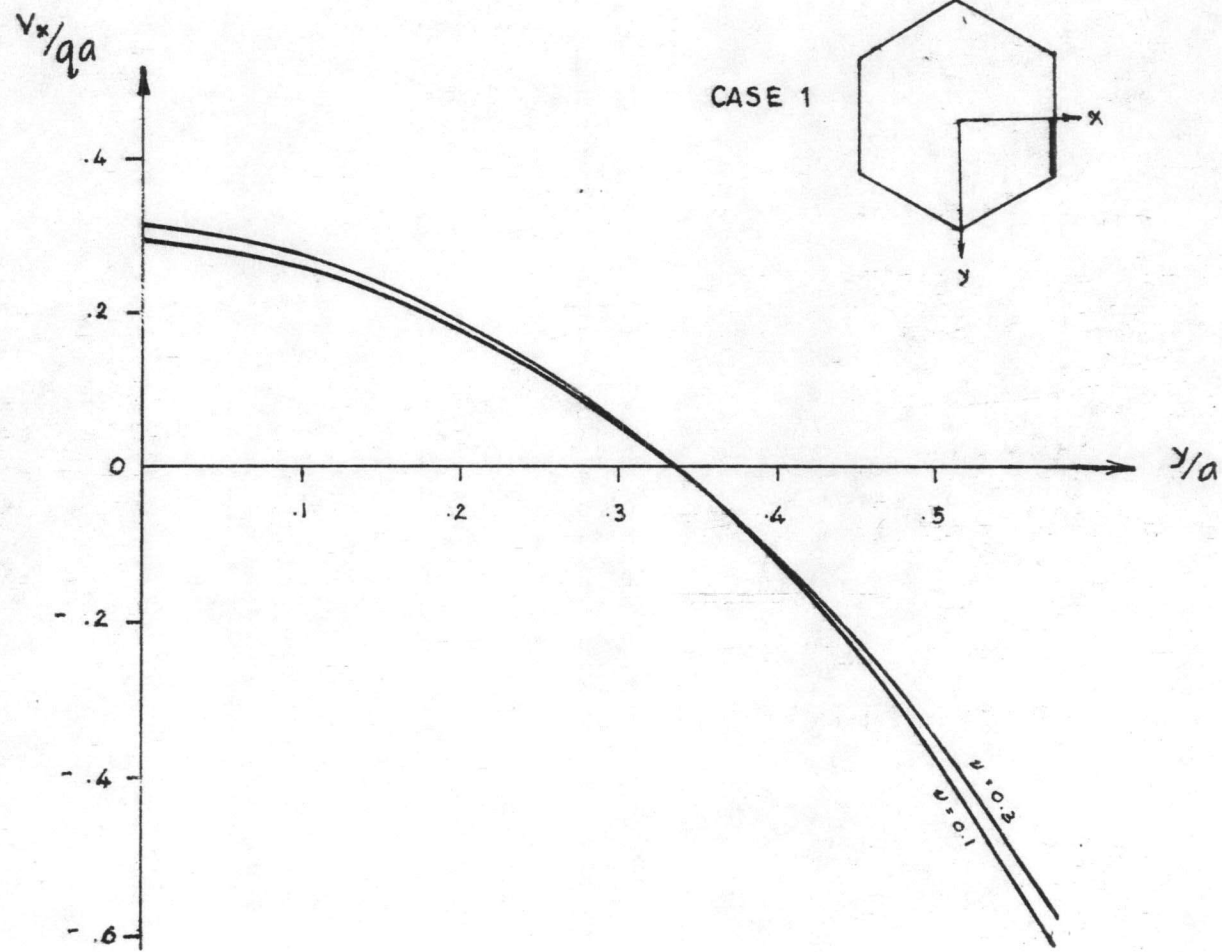


Fig. 27. Theoretical shear force v.s.  $y/a$ ,  $x/a = 1$

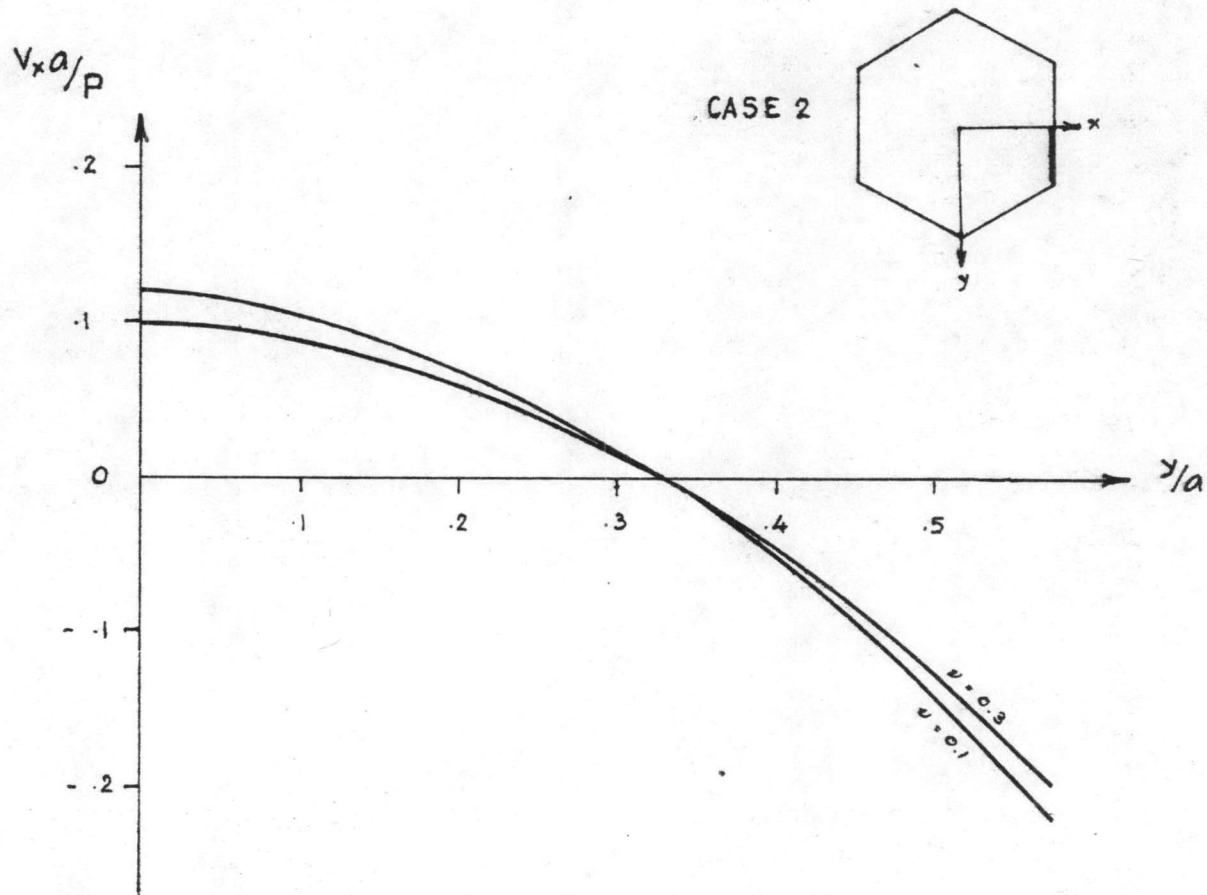


Fig. 28. Theoretical shear force v.s.  $y/a$ ,  $x/a = 1$

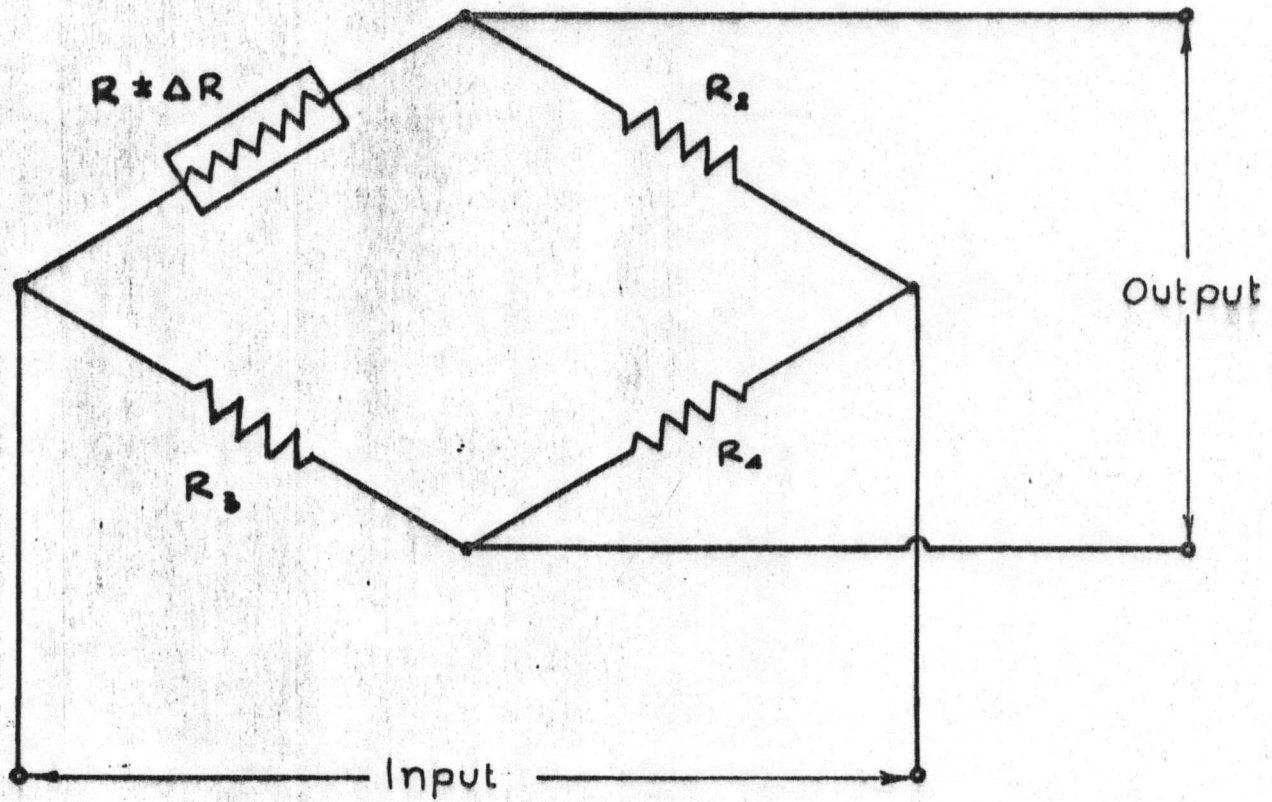


Fig. 29. Wheatstone bridge circuit

VITA



Mr. Prasong Ingsuwan was born on August 1950. He received the Bachelor's degree in Mechanical Engineering from Kasetsart University in the academic year of 1973. He is now working as lecturer at the Department of Mechanical Engineering, Chiang Mai University.