



## Chapter 5

### Discussion and Conclusions

In this work, we have shown that the interlayer coupling plays an important role in providing a mechanism for enhancement of  $T_c$ . The "Josephson-like coupling between the layers which arises through interaction of electron in the neighbouring  $\text{CuO}_2$  planes enhances the transition temperature within the layer.

In our model we assume the existence of coupling due to direct interlayer hopping. As we have shown, such hopping is only a higher-order effect in oxide superconductors. Even though  $t$  is small, such small  $t$  can arise through phonon or plasmon assisted hopping, for example.

Also in our evaluation of  $T_c$ , we assume that coupling constants  $V_c$ ,  $V_d$  and  $V_{er}$  do not change significantly with the introduction of small dispersion along the  $z$  axis. To justify this assumption it would be necessary to calculate  $V_c$ ,  $V_d$  and  $V_{er}$ . Clearly, this is beyond the scope of this work. Therefore we proceed, keeping  $V_c$ ,  $V_d$  and  $V_{er}$  fixed.

From our calculation we have shown that, within the limits of our assumption, introducing the small hopping matrix element between layers reduces  $T_c$ . Finite  $t$  may also lead to a very anisotropic excitation spectrum. The anisotropy may be used to explain certain experimental data.

Finally we discuss the intralayer coupling. This coupling owes its strength to a quasi-two-dimensional nature of electronic states. We expect that the coupling constants will either not change or will decrease if the hopping between layers is allowed. The results of our calculation are consistent with such behavior, and one generally expects that in such a case an increased direct hopping between layers would be unfavorable for high- $T_c$  superconductivity, and the reduction in  $T_c$  due to direct hopping is offset by an increase of the coupling constants.

In conclusions, we have developed a model of layered high temperature superconductor. Specifically, we explored the implications of  $T_c$  mediated by bounding layers due to proximity effect.

Our formulas for  $T_c$  revealed that various layer couplings (coherent pair transitions and direct hopping between layers) play substantial roles in determining  $T_c$ . The bounding layer plays a role by renormalizing the interaction constants of the system.

Our major results and predictions in the framework of this system are as follows : the introduction of a small interlayer hopping matrix element always reduces  $T_c$ , the Josephson-like coupling between layers always enhances  $T_c$ . The possible proximity effect in the bounding neighbor layer plays an important role in the enhancement of  $T_c$ . These different mechanisms can coexist in principle and the competing effects can provide a way to understand the observed maximum  $T_c$  as a function of  $n$  (23). The actuality and relative importance in real materials have to be considered individually in correspondence with specific electronic

structures.  $T_c$  can be obtained by a judicious parametrization of all the relevant coupling constants appearing in the model. We note that the model proposed in the present work is much simplified, we hope our arguments provide a rationale for investigating the  $T_c$ 's in other multilayered structures.