# MELT FRACTURE AND WALL SLIP CHARACTERISTICS OF HDPE AND LLDPE

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#### ABSTRACT

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KEY WORDS : Wall Slip / Stick-Slip Transition / Melt Fracture / Extrapolation Length

Methavee Kwaengsobha : Melt Fracture and Wall Slip Characteristics of HDPE and LLDPE. Thesis Advisors: Prof. Ronald G. Larson and Assoc. Prof. Anuvat Sirivat, 170 pp. ISBN 974-638-478-3

We investigated the wall slip characteristics of HDPE and LLDPE polymer melts from the capillary extrusion. The wall slip magnitude of HDPE and LLDPE was found to increase with temperature but to decrease with molecular weight. The slip velocity depends on the wall shear stress according to the power law  $V_s = A\tau_w^m$ , where A depends on temperature, molecular structure, and molecular weight. The scaling exponent m depends only on molecular structure and molecular weight.

The extrapolation length was used to characterize the slip velocity following the theory of Brochard and de Gennes. Our results indicate that at low temperature and with a high molecular weight, the entanglement state was observed because the grafted chains which are attached to the wall surface effectively entangle with the mobile chains. On the other hand, at high temperature, the marginal state was observed because some grafted chains have been fully extended resulting in a smaller entanglement loci density. The extrapolation length obeys the linear law b =  $CV_s$  where C depends slightly on temperature but strongly on molecular weight. C was found to be equal to  $\eta'_0/\tau^*$  where  $\eta'_0$  is the zero shear rate viscosity and  $\tau^*$  is onset shear stress for slip, consistent with the theory of Brochard and de Gennes in the marginal regime. No rouse regime was observed in this experiment.

# บทคัดย่อ

เมธาวี แขวงโสภา: การศึกษาผิวขรุขระของพลาสติกและอัตราการใหลลื่นที่ไม่สม่ำ เสมอบนชิ้นส่วนของพลาสติกที่ถูกรีดจากท่อกลมของพอลิเอทธิลีนชนิดความหนาแน่นสูงและ พอ ลิเอทธิลีนชนิดความหนาแน่นเชิงเส้นต่ำ (Melt Fracture and Wall Slip Characteristics of HDPE and LLDPE) อ.ที่ปรึกษา : Prof. Ronald G. Larson และ รศ. คร. อนุวัฒน์ ศิริวัฒน์ 170 หน้า ISBN 974-638-478-3

วิทยานิพนธ์นี้ เสนอการค้นคว้าเกี่ยวกับการเกิดผิวขรุขระ และอัตราการลื่นไหลที่ ไม่สม่ำเสมอบนชิ้นส่วนพลาสติกที่เกิดจากกระบวนการรีดจากท่อกลม จากการทดลองพบว่า อัตรา การไหลลื่นที่ไม่สม่ำเสมอของสารโพลิเมอร์ จะเพิ่มขึ้นตามอุณหภูมิ แต่จะลดลงตามน้ำหนัก โมเลกุลของโพลิเมอร์ นอกจากนี้ ยังขึ้นอยู่กับค่าความเค้นยกกำลังด้วย

การลากระยะทางของอัตราการลื่นไหลที่ไม่สม่ำเสมอจากผิวท่อกลมไปเป็นศูนย์ ได้นำมาใช้ในการศึกษาลักษณะเฉพาะของอัตราการลื่นไหล ตามทฤษฎีของ Brochard และ de Gennes ซึ่งจากการทคลองพบว่า ที่อุณหภูมิต่ำ และพอลิเมอร์มีน้ำหนักโมเลกุลสูง จะสังเกตพบ สภาวะที่สายโซ่พอลิเมอร์มีการพันกัน เนื่องจากสายโซ่พอลิเมอร์ที่ติดอยู่กับผนังท่อสามารถที่จะ พันกันกับสายโซ่พอลิเมอร์ ที่เคลื่อนที่ได้ นอกจากนี้ ยังพบว่าที่อุณหภูมิสูง จะสังเกตพบสภาวะที่ อัตราการลื่นไหลที่ไม่สม่ำเสมอของพอลิเมอร์ จะมีความสัมพันธ์เชิงเส้นกับการลากระยะทางของ อัตราการลื่นไหลที่ไม่สม่ำเสมอของพอลิเมอร์ เนื่องจากสายโซ่พอลิเมอร์บางส่วนที่ติดกับผนังท่อมี การยึดตัวออกทำให้ความหนาแน่นในการพันกันของพอลิเมอร์ลคลง และยังมีความสันพันธ์กับ ความหนืดของพอลิเมอร์ ที่ความเร็วเป็นศูนย์ และความเก้นเริ่มด้นของการเกิดอัตราการลื่นไหล อย่างไรก็ดีในการทดลองนี้ไม่พบสภาวะที่พอลิเมอร์มีการเคลื่อนที่อย่างอิสระ

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