

## REFERENCES

- Apirathvorakij, V. and Karasudhi, P. 1980. Quasi-static bending of a cylindrical elastic bar partially embedded in a saturated elastic half space. Int. J. Solids and Struct 16 : 625-644.
- Apsel, R. J. and Luco, J. E. 1987. Impedance functions for foundations embedded in a layered medium: an integral equation approach. Earthquake Engng. and Struct. Dyn 15 : 213-231.
- Beck, J. V. and Arnold, K. J. 1977. Parameter estimation in engineering and science. John Wiley & Sons, Inc.
- Biot, M. A. 1941. General theory of three-dimensional consolidation. J. Appl. Physics 12 : 155-164.
- Biot, M. A. 1956. Theory of propagation of elastic waves in a fluid-saturated porous solid. I. Low-frequency range. J. Acoust. Soc. Am 28(2) : 168-178.
- Biot, M. A. (1962) Mechanics of deformation and acoustic propagation in porous media. J.Appl. Physics 33 : 1482-1498.
- Cheng A. H.-D., and Detournay E. 1998. On singular integral equations and fundamental solutions of poroelasticity. Int. J. Solids Structures 35 : 4521-4555
- Fowler, G. F., and Sinclair, G. B. 1978. The longitudinal harmonic excitation of a circular bar embedded in an elastic half-space. Int. J. Solids and Struct 14 : 999-1012.
- Karasudhi, P. 1990. Fundation of solid mechanics. Kluwer, Dordrecht, The Netherlands.
- Karasudhi, P., Rajapakse, R. K. N. D. and Hwang, B. Y. 1984. Torsion of a long cylindrical elastic bar partially embedded in layered elastic half space. Int. J. Solids and Struct 20 : 1-11.

- Keer, L. M and Freeman, N. J. 1967. Torsion of a cylindrical rod welded to an elastic half space. J. Appl. Mech. 34 : 687-692.
- Luk, V. K. and Keer, L. M. 1979. Stress analysis for an elastic half space containing an axially loaded rigid cylindrical rod. Int. J. Solids and Struct 15 : 805-827.
- Luk, V. K. and Keer, L. M. 1980. Stress analysis of a deep rigid axially-loaded cylindrical anchor in an elastic medium. Int. J. Numer. anal. Meth. Geomech 4 : 215-232.
- Luco, J. E. 1976. Torsion of a rigid cylinder embedded in an elastic half space. J. appl. Mech. ASME 43 : 419.
- Luco, J. E. and Wong, H. L. 1986. Response of hemispherical foundation embedded in half-space. J. Engng Mech ASCE 112(12) : 1363-1374
- Muki, R. and Sternberg, E. 1969. On the diffusion of an axial load from an infinite cylindrical bar embedded in an elastic medium. Int. J. Solids and Struct 5 : 587-606.
- Muki, R. and Sternberg, E. 1970. Elastostatic load transfer to a half space from a partially embedded axially loaded rod. Int. J. Solids and Struct 6 : 69-90.
- Niumpardit, B. and Karasudhi, P. 1981. Load transfer from an elastic pile to a saturated porous elastic soil. Int. J. Numer. Anal. Meth. Geomech 5 : 115-138.
- Ohsaki, Y. 1973. On movement of a rigid body in semi-infinite elastic medium. Proc. Japan Earthquake Engineering Symp. Tokyo : 245-252
- Piessens, R., E. deDoncker-Kapenga, C.W. Uberhuber, and D.K. Kahaner 1983. QUADPACK. Springer-Verlag. New York
- Poulos, H. G. and Davis, E. H. 1968. The settlement behavior of a single axially loaded incompressible piles and piers. Geotechnique 18 : 351.
- Rajapakse, R. K. N. D. 1988. A note on the elastodynamic load transfer problem. Int. J. Solids and Struct 24 : 963-972.

- Rajapakse, R. K. N. D. and Shah, A. H. 1987. On the longitudinal harmonic motion of an elastic bar embedded in an elastic half-space. Int. J. Solids and Struct 23 : 267-285.
- Rajapakse, R. K. N. D. and Senjuntichai, T. 1995. An indirect boundary integral equation method for poroelasticity. Int. for Numer. and Anal. Meth. In Geomech 19 : 587-614.
- Senjuntichai, T., and Rajapakse, R. K. N. D. 1994. Dynamic green's functions of homogeneous poroelastic half-plane. J. Eng. Mech. Div 120(11) : 2381-2404
- Sneddon, I. N. (1951). Fourier Transforms. McGraw-Hill, New York.
- Suriyamongkol, S., Karasudhi, P., and Lee, S. L. 1973. Axially loaded rigid cylindrical body embedded in a half space. Proc. 13<sup>th</sup> Midwestern Mechanics Conf p.333, University of Pittsburgh.
- Wang, Y. and Rajapakse, R. K. N. D. 1990. Asymmetric boundary-value problems for a transversely isotropic elastic medium. Int. J. Solids Struct 26 : 833-849
- Zeng, X., and Rajapakse, R. K. N. D. 1999a. Vertical vibrations of a rigid disk embedded in a poroelastic medium. Int. for Numer. and Anal. Meth. In Geomech 23(15) : 2075-2095.
- Zeng, X., and Rajapakse, R. K. N. D. 1999b. Dynamic axial load transfer from elastic bar to poroelastic medium. J. Engng Mech ASCE 125(9) : 1048-1055.



## **APPENDIX**

ศูนย์วิทยทรัพยากร  
จุฬาลงกรณ์มหาวิทยาลัย

This appendix is given the non-zero arbitrary functions appearing in the general solutions given by equation (3.40)-(3.46) corresponding to different type of loads.

### A.1 Arbitrary Functions for vertical loading

$$A_1 = \frac{\eta_2 e^{-\gamma_1 z'}}{2\mu N_1} \bar{T}_z(\xi) \quad (\text{A.1})$$

$$B_1 = \frac{\eta_2 (v_5 e^{-\gamma_1 z'} + 2\xi^2 v_3 e^{-\gamma_2 z'} - 4\xi^2 S_1 v_1 e^{-\gamma_3 z'})}{2\mu N_1 R} \bar{T}_z(\xi) \quad (\text{A.2})$$

$$C_1 = -\frac{\eta_1 e^{-\gamma_2 z'}}{2\mu N_1} \bar{T}_z(\xi) \quad (\text{A.3})$$

$$D_1 = \frac{\eta_1 (2\xi^2 v_4 e^{-\gamma_1 z'} - v_6 e^{-\gamma_2 z'} + 4\xi^2 S_1 v_1 e^{-\gamma_3 z'})}{2\mu N_1 R} \bar{T}_z(\xi) \quad (\text{A.4})$$

$$E_1 = \frac{\xi v_1 e^{-\gamma_3 z'}}{2\mu \gamma_3 N_1} \bar{T}_z(\xi) \quad (\text{A.5})$$

$$F_1 = \frac{\xi v_2 (v_4 e^{-\gamma_1 z'} - v_3 e^{-\gamma_2 z'}) + \xi v_1 v_7 e^{-\gamma_3 z'}}{2\mu \gamma_3 N_1 R} \bar{T}_z(\xi) \quad (\text{A.6})$$

$$B_2 = B_1 - A_1 e^{2\gamma_1 z'} \quad (\text{A.7})$$

$$D_2 = D_1 - C_1 e^{2\gamma_2 z'} \quad (\text{A.8})$$

$$F_2 = F_1 + E_1 e^{2\gamma_3 z'} \quad (\text{A.9})$$

where

$$v_1 = \eta_1 - \eta_2 \quad (\text{A.10})$$

$$v_2 = \eta_1 \beta_2 - \eta_2 \beta_1 \quad (\text{A.11})$$

$$\nu_3 = 4\eta_1\gamma_2\gamma_3 \quad (\text{A.12})$$

$$\nu_4 = 4\eta_2\gamma_3\gamma_1 \quad (\text{A.13})$$

$$\nu_5 = S_1\nu_2 - \xi^2(\nu_3 + \nu_4) \quad (\text{A.14})$$

$$\nu_6 = S_1\nu_2 + \xi^2(\nu_3 + \nu_4) \quad (\text{A.15})$$

$$\nu_7 = S_1\nu_2 + \xi^2(\nu_3 - \nu_4) \quad (\text{A.16})$$

and

$$N_1 = 2\xi^2\nu_1 - \nu_2 \quad (\text{A.17})$$

$$R = -S_1\nu_2 + \xi^2(\nu_3 - \nu_4) \quad (\text{A.18})$$

In the above equations,  $\bar{T}_z(\xi) = sJ_0(\xi s)$  is the zeroth-order Hankel transform of the applied axisymmetric vertical ring load of radius  $s$  at  $z = z'$ .

## A.2 Arbitrary functions for radial loading

$$A_1 = \frac{\xi\eta_2 e^{-\gamma_1 z'}}{2\mu\gamma_1 N_2} \bar{T}_r(\xi) \quad (\text{A.19})$$

$$B_1 = \frac{\xi(\eta_2\nu_5 e^{-\gamma_1 z'} + 2\xi^2\eta_1\nu_4 e^{-\gamma_2 z'} - S_1\nu_1\nu_4 e^{-\gamma_3 z'})}{2\mu\gamma_1 N_2 R} \bar{T}_r(\xi) \quad (\text{A.20})$$

$$C_1 = -\frac{\xi\eta_1 e^{-\gamma_2 z'}}{2\mu\gamma_2 N_2} \bar{T}_r(\xi) \quad (\text{A.21})$$

$$D_1 = \frac{\xi(2\xi^2\eta_2\nu_3 e^{-\gamma_1 z'} - \eta_1\nu_6 e^{-\gamma_2 z'} + S_1\nu_1\nu_3 e^{-\gamma_3 z'})}{2\mu\gamma_2 N_2 R} \bar{T}_r(\xi) \quad (\text{A.22})$$

$$E_1 = \frac{\nu_1 e^{-\gamma_3 z'}}{2\mu N_2} \bar{T}_r(\xi) \quad (\text{A.23})$$

$$F_1 = \frac{4\xi^2 v_2 (\eta_2 e^{-\gamma_1 z'} - \eta_1 e^{-\gamma_2 z'}) + v_1 v_7 e^{-\gamma_3 z'}}{2\mu N_2 R} \bar{T}_r(\xi) \quad (\text{A.24})$$

$$B_2 = B_1 + A_1 e^{2\gamma_1 z'} \quad (\text{A.25})$$

$$D_2 = D_1 + C_1 e^{2\gamma_2 z'} \quad (\text{A.26})$$

$$F_2 = F_1 - E_1 e^{2\gamma_3 z'} \quad (\text{A.27})$$

where

$$N_2 = v_1 (\xi^2 - \gamma_3^2) \quad (\text{A.28})$$

In the above equations,  $\bar{T}_r(\xi) = s J_1(\xi s)$  is the first-order Hankel transform of the applied axisymmetric radial ring load of radius  $s$  at  $z = z'$ .

### A.3 Arbitrary functions for fluid source

$$A_1 = \frac{e^{-\gamma_1 z'}}{2\delta(\chi_1 - \chi_2)\gamma_1} i \sqrt{\frac{\rho}{\mu}} \bar{Q}(\xi) \quad (\text{A.29})$$

$$B_1 = \frac{v_5 e^{-\gamma_1 z'} + 2\xi^2 v_4 e^{-\gamma_2 z'}}{2\delta(\chi_1 - \chi_2)\gamma_1 R} i \sqrt{\frac{\rho}{\mu}} \bar{Q}(\xi) \quad (\text{A.30})$$

$$C_1 = \frac{e^{-\gamma_2 z'}}{2\delta(\chi_2 - \chi_1)\gamma_2} i \sqrt{\frac{\rho}{\mu}} \bar{Q}(\xi) \quad (\text{A.31})$$

$$D_1 = \frac{2\xi^2 v_3 e^{-\gamma_1 z'} - v_6 e^{-\gamma_2 z'}}{2\delta(\chi_1 - \chi_2)\gamma_2 R} i \sqrt{\frac{\rho}{\mu}} \bar{Q}(\xi) \quad (\text{A.32})$$

$$E_1 = 0 \quad (\text{A.33})$$

$$F_1 = -\frac{2\xi v_2 (e^{-\gamma_1 z'} - e^{-\gamma_2 z'})}{\delta(\chi_2 - \chi_1)R} i \sqrt{\frac{\rho}{\mu}} \bar{Q}(\xi) \quad (\text{A.32})$$

$$B_2 = B_1 + A_1 e^{2\gamma_1 z'} \quad (\text{A.33})$$

$$D_2 = D_1 + C_1 e^{2\gamma_2 z'} \quad (\text{A.34})$$

$$F_2 = F_1 \quad (\text{A.35})$$

In the above equations,  $\bar{Q}(\xi) = sJ_0(\xi s)$  is the zeroth-order Hankel transform of the applied ring fluid source of radius  $s$  at  $z = z'$ .

ศูนย์วิทยทรัพยากร  
จุฬาลงกรณ์มหาวิทยาลัย

## BIOGRAPHY

Mr. Sikarn Mani was born in Bangkok 1978. He graduated from Faculty of Engineering, Mahidol University in 1998. He continued his study for Master Degree in Civil Engineering at Chulalongkorn in 2000.



ศูนย์วิทยทรัพยากร  
จุฬาลงกรณ์มหาวิทยาลัย