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## **Appendices**

## Appendix A: Matlab® Program

### An Example of the M-file Script Routines Used to Calculate the Electron and the Hole Wavefunctions for Multiple Quantum Dots by Solving the Schrödinger Equation Using the Different Effective Masses Approach

The whole calculation program is separated into four files:

1. **PD\_ALIGNED\_QDs.m** -- the main routine used to calculate polarization degree of aligned QDs
2. **Call-ELECTRICFIELD.m** -- the subroutine called to define the two-dimensional electric field system
3. **Call-ALIGNED\_QDs.m** -- the subroutine called to define the region of InAs and GaAs
4. **ALIGNED\_QDs\_eigenergy.m** -- the subroutine called to calculate the eigen-energies and eigen-functions of aligned QDs

List of the routines:

#### **PD\_ALIGNED\_QDs.m**

```

clc
clear
close all
clear all

x0 = 0; xf=200;           % starting and end points of x axis (in units of nanometers)
y0 = 0; yf=200;           % starting and end points of y axis (in units of nanometers)
Mx =100;                  % Number of sample points in x axis (in units of nanometers)
My =100;
n = XX;                   % size of quantum dot in x-direction
% to get the real dimension should multiply by 2)
A = XX;                   % size of QDs in Y direction
d = XX;                   % spacing between one QDs and another
% to get the real dimension, should calculated (d-1)x 2)
% XX stands for parameter, corresponding to QDs (by input value)

dotaddleft = XX;          % additional dots on left hand side
dotaddright = XX;          % additional dots on right hand side
numdots = dotaddleft+dotaddright; % total number of QDs, corresponding to
% numdots=dotaddleft+dotaddright

```

```

N = 50; %mid point of the mesh
dx = (xf - x0)/Mx;
dy = (yf - y0)/My;
x = (-xf/2:xf/Mx:xf/2); %position of sample points in x axis
y = (-yf/2:yf/Mx:yf/2)'; %position of sample points in y axis

% NUMERICAL CALCULATION of the Schroedinger equation implemented by using Finite
% Difference Method
% Developed by Chonlakorn Chiewpanich (modified corresponding to Nan Nan Thidar Chit
% Swe's original program)
% The maximum mesh size for the two-dimensional Schroedinger equation is 100*100.
% One mesh is equivalent to 2 nm.
% Changing the mesh points is available by modifying N, Mx, My, xf, and yf,
corresponding to the condition of N = Mx = My = (xf/2) = (yf/2)

%-----
%-----

% Calculate the electron wavefunction
disp( '%This program shows the wavefunctions obtained by solving the Schroedinger')
disp('equation for ALIGNED quantum dots. The size of the dot is fixed at XX nm.')
disp ('%')
disp( '%Calculating the electron wavefunction')
disp ('%')
disp(' %The value of the band offset V1 is XX eV.')
disp ('%')
disp('%The length in the x direction and the y direction each is XX nm.')
disp ('%')
disp('%The number of the mesh points in the x and y directions is XX each.')
disp ('%')
disp(' %This program calculates based on the interdot spacing between QDs.')
disp ('%')
disp('Distance between QDs: 2d' );
disp ('%')
d=input ('d=');
num_sol=input ('%number of solutions:      ');
disp ('%')
m1=input ('%mass of electron in GaAs:      ');
m2=input ('%mass of electron in InAs:      ');
disp ('%')
disp ('%')
Vp=input ('%band offset (eV):      ');

[phi,te,d,num_sol,V1,V]=ALIGNED_QDs_eigenergy(d,num_sol,Mx,My,Vp,m1,m2);

figure(1);

mesh(x,y,V1)
xlabel('Distance (nm)')
ylabel('Distance (nm)')
zlabel('Potential energy, (eV)')


```



```

Phi = Phihole.*Phielectron;      % e-h overlapping
Phiee= Phielectron.*Phielectron; % e-e overlapping
Phihh= Phihole.*Phihole;        % h-h overlapping

% Central overlap
Centralee=sum(sum(Phiee(N-A/2:N+A/2, (N-d/2+1):(N+d/2+1))));

Centralhh=sum(sum(Phihh(N-A/2:N+A/2, (N-d/2+1):(N+d/2+1))));

Centraleh=sum(sum(Phi(N-A/2:N+A/2, (N-d/2+1):(N+d/2+1))));

sumCentral=Centralee+Centralhh-2*Centraleh;

if NU == 1    %half number of total QDs. Note that for Bi-QDs, the program is operating
% only this logic

Area=(A*d);

Overlapped=sumCentral/Area

else

for i=1:NU-1 %In case of number of QDs is greater than

%Left overlap
Leftee(i)=sum(sum(Phiee(N-n/2:N+n/2, ((N-(2*i+1)*d/2)-(2*i-1)*n+1)):((N-(2*i-1)*d/2)-
(2*i-1)*n+1))));

Lefthh(i)=sum(sum(Phihh(N-n/2:N+n/2, ((N-(2*i+1)*d/2)-(2*i-1)*n+1)):((N-(2*i-1)*d/2)-
(2*i-1)*n+1))));

Lefteh(i)=sum(sum(Phi(N-n/2:N+n/2, ((N-(2*i+1)*d/2)-(2*i-1)*n+1)):((N-(2*i-1)*d/2)-
(2*i-1)*n+1))));

%Right overlap
Rightee(i)=sum(sum(Phiee(N-n/2:N+n/2, ((N+((2*i-1)*d/2)+(i*n)+1)):((N+(2*i+1)*d/2)-
(i*n)+1))));

Righthh(i)=sum(sum(Phihh(N-n/2:N+n/2, ((N+((2*i-1)*d/2)+(i*n)+1)):((N+(2*i+1)*d/2)-
(i*n)+1))));

Righteh(i)=sum(sum(Phi(N-n/2:N+n/2, ((N+((2*i-1)*d/2)+(i*n)+1)):((N+(2*i+1)*d/2)-
(i*n)+1))));

end

sumeehh = sum(Leftee)+sum(Lefthh)+sum(Rightee)+sum(Righthh);
sumeh   = sum(Lefteh)+sum(Righteh);

```

```

Area=(A*d);

Overlapped=(sumCentral+sumeehh-2*sumeh)/Area

end

%-----
%
```

---

```

% Calculate the Linear Polarization Degree (PD)
[X,Y]=meshgrid(x,y);
D1=abs(Phielectron.*X.* Phihole);
D2=abs(Phielectron.*Y.* Phihole);
AA =sum (sum(D1));
BB =sum (sum(D2));
RAWPD = abs((AA-BB)/(AA+BB)) % PD of single QD
Cgridarea=abs(Overlapped*((AA-BB) / (AA+BB))) % PD of aligned QDs

```

---

**Call-ELECTRICFIELD.m**

```

function[elecx,elecy]=Call_ELECTRICFIELD(voltx,voltz);

voltx = input ('%voltage applied along the x direction:      ');
voltz = input ('%voltage applied along the y direction:      ');

% Calculation of specification matrix

M = 99*99; % M is dimension of specification matrix, corresponding to number of node
% in electric field system = (xf-1)*(xf-1) because we neglect the row and column that
% refer to ground voltage

% Ex. 3*3 voltage node V11 V12 V13
%                  V21 V22 V23
%                  V31 V32 V33
% The corresponding potential matrix is X = V11      and its dimension is sqrt(M)*1
%                  V12
%                  V13
%                  V21      9*1 matrix
%                  V22
%                  V23
%                  V31
%                  V32
%                  V33

r=sparse(sparse(diag(-4+zeros(M,1),0))+sparse(diag(ones(M-
sqrt(M),1),sqrt(M)))+sparse(diag(ones(M-sqrt(M),1),-sqrt(M))));
```

```

% Specification matrix of 3*3 voltage node
%
% -4   1   0   1   0   0   0   0   0
%  1  -4   1   0   1   0   0   0   0
%  0   1  -4   0   0   1   0   0   0
%  1   0   0  -4   1   0   1   0   0
%  0   1   0   1  -4   1   0   1   0
%  0   0   1   0   1  -4   0   0   1
%  0   0   0   1   0   0  -4   1   0
%  0   0   0   0   1   0   1  -4   1
%  0   0   0   0   0   1   0   1  -4

% Specify "1" at the position i=j+1
% At the position j=i+1. "1" is specified that equals to (dimension of nodes - 1)
% Ex. 3*3 voltage node → 1 1 0 1 1 0 1 1 0
% Ex. 4*4 voltage node → 1 1 1 0 1 1 1 0 1 1 1 0 1 1 1 0

for i=1:M
    for j=1:M

        if i == j+1
            r(i,j)=1;
            if i == j+1 && mod(j,sqrt(M))== 0 %Specify "0" at the position i=j+1 and
mod(j, dimension of nodes)=0
                r(i,j)=0;
            end
        elseif j == i+1
            r(i,j)=1;
            if j == i+1 && mod(i,sqrt(M))== 0 %Specify "0" at the position j=i+1 and
mod(i, dimension of nodes)=0
                r(i,j)=0;
            end
        end
    end
end
end

%-----
%-----
```

% Boundary condition at the interface of different medium

```

% Ex. 2 QDs
%
%          |     e1     |     |
%          |           |     |
%          | ----- |     | ----- |
%          |   |   e2   |     |     |     |
%          |   |           |     |     |     |
%          | ----- |     | ----- |
%          |           |     |
%          |           |     |
%          |-----|-----|-----|
```

```

s=sqrt(M);
dielec0=8.854187*(10^-12);
dielec1=12.9*dielec0; %dielectric constant of GaAs (e1)
dielec2=15.15*dielec0; %dielectric constant of InAs (e2)

% Continuity at the interface, D1=D2
% Ex. 3*3 voltage node           v11 v12 v13      Interface nodes are v12,v22,v32
%
%                                     v21 v22 v23
%
%                                     v31 v32 v33

% From D1=D2 --> e1E1=e2E2
%
% At V12, e1(V12-V11)=e2(V13-V12) --> (e1+e2)V12 = e1V11 + e2V13
% At V22, e1(V22-V21)=e2(V23-V22) --> (e1+e2)V22 = e1V21 + e2V23
% At V32, e1(V32-V31)=e2(V33-V32) --> (e1+e2)V32 = e1V31 + e2V33
%
% Compared to previously specified voltage
%
%                                     v12 = (1/4)(v11+v13+volty+v22)
%
%                                     v22 = (1/4)(v21+v23+v12+v32)
%
%                                     v32 = (1/4)(v31+v33py+v22)
%
%
% Ex. 3*3 voltage node   [-4    1    0    1    0    0    0    0    0    0] [v11
%
%                         1    -4   -1    0    1    0    0    0    0    0] [v12
%
%                         0    1    -4   -1    0    1    0    0    0    0] [v13
%
%                         1    0    0    -4   -1    0    1    0    0    0] [v21
%
%                         0    1    0    1    -4   -1    0    1    0    0] [v22
%
%                         0    0    1    0    1    -4   -1    0    0    1] [v23
%
%                         0    0    0    1    0    0    -4   -1    0    0] [v31
%
%                         0    0    0    0    1    0    1    -4   -1    0] [v32
%
%                         0    0    0    0    0    1    0    1    -4   -1] [v33]
%
%
% At V12,V22,V32 the values change to
%
%
%                         -e1   e1+e2   e2   0    0    0    0    0    0    0] [v12
%
%                         0    0    0    -e1   e1+e2   -e2   0    0    0    0] [v22
%
%                         0    0    0    0    0    0    -e1   e1+e2   -e2   0] [v32]

%
% Boundary condition at the QDs's edge

F=s;

%
% Position of four edges of all QDs
for dot = -(numdots-1)*(d/2):d:(numdots-1)*(d/2)
%
% Ex. number of dot = 2 → numdots = 2 → dot = -(d/2):d:(d/2)

%
% Top edge

for i=((((F*F)+1)/2) - (A*F)/2 +dot -n)+1 : (((((F*F)+1)/2) - (A*F)/2 +dot)-1
%
r(i,1:s*s)= 0;
%
end

```

```

for i=(((F*F)+1)/2) - (A*F)/2 +dot -n)+1 : (((F*F)+1)/2) - (A*F)/2 +dot)-1

r(i,i)= dielec1+dielec2;
r(i,i-s)= -dielec1;
r(i,i+s)= -dielec2;

end

% Bottom edge

for i=(((F*F)+1)/2) - (A*F)/2 +dot -n + (A*F))+1:((((F*F)+1)/2) - (A*F)/2 +dot +
(A*F))-1

r(i,1:s*s)= 0;

end

for i=(((F*F)+1)/2) - (A*F)/2 +dot -n + (A*F))+1:((((F*F)+1)/2) - (A*F)/2 +dot +
(A*F))-1

r(i,i)= dielec1+dielec2;
r(i,i-s)= -dielec2;
r(i,i+s)= -dielec1;

end

% Left edge

for i=(((F*F)+1)/2) - (A*F)/2 +dot -n)+1 :F:((((F*F)+1)/2) - (A*F)/2 +dot -n +
(A*F))-1

r(i,1:s*s)= 0;

end

for i=(((F*F)+1)/2) - (A*F)/2 +dot -n)+1 :F:((((F*F)+1)/2) - (A*F)/2 +dot -n +
(A*F))-1

r(i,i)= dielec1+dielec2;
r(i,i-1)= -dielec1;
r(i,i+1)= -dielec2;

end

```

```

% Right edge

for i=(((F*F)+1)/2) - (A*F)/2 +dot)+1 :F: (((F*F)+1)/2) - (A*F)/2 +dot + (A*F))-1

r(i,1:s*s)= 0;%ເພື່ອກຳໄຂມີບັນດາສະແດງ

end

for i=(((F*F)+1)/2) - (A*F)/2 +dot)+1 :F: (((F*F)+1)/2) - (A*F)/2 +dot + (A*F))-1

r(i,i)= dielec1+dielec2;
r(i,i-1)= -dielec2;
r(i,i+1)= -dielec1;

end

end

%-----%
%-----%

% Boundary condition of applied voltage
%
% volty (voltage applied along the y direction)
%
%-----%
%
% px | | | voltz (voltage applied along the z direction)
%
% | | | |
% | | | |
% px | | | voltz (voltage applied along the x direction)
%
% | | | |
%-----%
%
% py | | | |
%
px=0;%ground
py=0;%ground

k=sqrt(M);

% Calculation of boundary matrix (matrix B)
%
% Ex. 3*3 voltage node
%
% B = -(summation of branch connected to V11) 9*1 matrix
%     -(summation of branch connected to V12)
%     -(summation of branch connected to V13)
%     -(summation of branch connected to V21)
%     -(summation of branch connected to V22)
%     -(summation of branch connected to V23)
%     -(summation of branch connected to V31)
%     -(summation of branch connected to V32)
%     -(summation of branch connected to V33)

```

```

%Four corners ((1,1)(1,j)(i,1)(i,j))
b(1)= -(px+volty);
b(k)= -(volty+voltx);
b(((k-1)*k)+1)=- (px+py);
b(k*k)=- (voltx+py)';

%Top edge      (from (1,2) to (1,j-1))
b(2:k-1)= -volty;
%Bottom edge   (from (i,2) to (i,j-1))
b(((k-1)*k)+2:(k*k)-1)=-py;

%Left boundary (from (2,1) to (i-1,1))
b(k+1:k:(k-1)*(k-1))=-px;
%Right boundary (from (2,j) to (i-1,j))
b(2*k:k:(k-1)*k)=-voltx;

%For free nodes, their values are "0"

%-----%
%-----%

% Solving for potential matrix

b=b';

TEM=r\b; % Solving matrix X by X= (A)\b(B)

%
% Ex. 3*3 voltage node
%
%          X @ X= V11  9*1 matriz
%
%                  V12
%
%                  V13
%
%                  V21
%
%                  V22
%
%                  V23
%
%                  V31
%
%                  V32
%
%                  V33
%
% Re-arranged from 9*1 matrix to 3*3 matrix, that is,      V11 V12 V13
%
%                                         V21 V22 V23
%
%                                         V31 V32 V33

for f=1:s*s
i=ceil(f/s);
j=mod(f,s);

if j==0
j=s;
end

```

```

VOLT(i,j)=TEM(f); % Potential distribution of the system

end

%-----
%-----

% Investigation of electric field distribution

deltaxx=2; % One mesh is equivalent to 2 nm
deltayy=2;

% Ex(x,y) = (V(x+delta,y)-V(x,y))/delta
% Ey(x,y) = (V(x,y+delta)-V(x,y))/delta
%
% Ex. 3*3 voltage node V11 V12 V13
%                  V21 V22 V23
%                  V31 V32 V33
%
%          volty
%
%          -----
%
%          |           |
%          |           |
%          px |           |   voltz
%
%          |           |
%          |           |
%          |           |
%
%          -----
%
%          py
%
% Since px,py are ground, so Ex(i,j)=(V(i,j+1)-V(i,j))/delta
% Ex. Ex(1,2)=V(1,3)-V(1,2)
% Ey(i,j) =(V(i-1,j)-V(i,j))/delta
% Ex. Ey(2,2)=V(1,2)-V(2,2)

for i=1:s
    for j=1:s

        if i-1 == 0
            h=volty;
            elecy(i,j)=(h-VOLT(i,j))./deltayy; %uu
        else
            elecy(i,j)=(VOLT(i-1,j)-VOLT(i,j))./deltayy;
        end
        if j+1 == s+1

```

```

l=voltx;

elecx(i,j)=(l-VOLT(i,j))./deltaxx;%m1

else

elecx(i,j)=(VOLT(i,j+1)-VOLT(i,j))./deltaxx;

end

end

% Contour plot of potential distribution
X1 = 1:sqrt(99*99);
Y1 = 1:sqrt(99*99);
figure(6)
mesh(Y1,X1,VOLT)

```

---

**Call-ALIGNED\_QDs.m**

```

function[mass,V1,V,const]=Call_ALIGNED_QDs(d,Vp,m1,m2,Mx,My);

x0 = 0; xf=200; % starting and end points of x axis (in nanometers)
y0 = 0; yf=200; % starting and end points of y axis (in nanometers)

dx = (xf - x0)/Mx; % increment in x direction = length(nm)/Mx
x = x0 + [0:Mx]*dx; % position of sample points in x direction
dy = (yf - y0)/My; % increment in x direction= length(nm) /Mx

y = y0+[0:My].'*dy; % position of sample points in y direction

h=1.0545715968; % Planck's constant ( x 10^-34 unit in Js)
hbar2=h^2;

echarge=1.6021764628; % electron charge ( x 10^-19 C)

baremass=9.10938188; % bare electron mass (x 10^31 kg)

m1=m1*baremass; % effective mass of carrier in GaAs
m2=m2*baremass; % effective mass of carrier in InAs
const=hbar2/echarge;
deltax=xf/Mx; % x-increment = length(nm)/n
deltax2=deltax^2;
const=const/deltax2;
mass=m1*ones(Mx+1,My+1); % define the GaAs effective mass region

```

```

% GaAs region

for i =1:My-1;
    for j = 1:My-1

        V(i,j)      =bandoffsetelectron-Vb+echarge*VOLT(i,j);
        % Ratio between bandoffset of electron and hole is 0.7:0.3

    end
end

% dots on left hand side

for g = 1:dotaddleleft

    for i = N-A/2:N+A/2;                      % position of InAs mass and barrier
        for j = ((N-((2*g)-1)*(d/2)))-((g)*n):((N-((2*g)-1)*(d/2)))-((g-1)*n)

            V(i,j)      =0+echarge*VOLT(i,j);
            mass(i,j)   =me2;

        end
    end
end

% dots on right hand side

for g = 1:dotaddright

    for i = N-A/2:N+A/2;                      % position of InAs mass and barrier
        for j = ((N+((2*g)-1)*(d/2)))+((g-1)*n):((N+((2*g)-1)*(d/2)))+((g)*n)

            V(i,j)      =0+echarge*VOLT(i,j); %Original
            mass(i,j)   =me2;

        end
    end
end

```

---

**ALIGNED\_QDs\_eigenergy.m**

```

function[phi,te,d,num_sol,V1,V]=ALIGNED_QDs_eigenergy(d,num_sol,Mx,My,Vp,m1,m2);

% Call the function to define the region of QDs

[mass,V1,V,const]=Call_ALIGNED_QD(d,Vp,m1,m2,Mx,My);

for i=2:Mx-1;
    for j=2:My-1;

```

```

d(i,j)=(((1/(mass(i1,j)+mass(i,j))+1/(mass(i+1,j)+mass(i,j)))+
(1/(mass(i,j-1)+mass(i,j))+1/(mass(i,j+1)+mass(i,j))))*const+ v(i,j));

% diagonal matrix element

offd1(i,j)=[(1/(mass(i-1,j)+mass(i,j))) *const;

% off-diagonal matrix element

offd3(i,j)=[(1/(mass(i,j-1)+mass(i,j))) *const;

end

for i=1:Mx-1;

    for j=1:My-1;

        offd2(i,j)=[(1/(mass(i+1,j)+mass(i,j))) *const;
        offd4(i,j)=[(1/(mass(i,j+1)+mass(i,j))) *const;

        end
    end

offd2(end,:)=zeros(1,My-1);
offd4(:,end)=zeros(My-1,1);

for i=2:Mx-1;

    for j=1:1;

        d(i,j)=(((1/(mass(i1,j)+mass(i,j))+1/(mass(i+1,j)+mass(i,j))
+(1/(mass(i,j)+mass(i,j))+1/(mass(i,j+1)+mass(i,j))))*const+ v(i,j));
        offd1(i,j)=[(1/(mass(i-1,j)+mass(i,j))) *const;

        end
    end

for i=1:1;

    for j=2:Mx-1;

        d(i,j) =-(((1/(mass(i,j)+mass(i,j))+1/(mass(i+1,j)+mass(i,j))
+(1/(mass(i,j-1)+mass(i,j))+1/(mass(i,j+1)+mass(i,j))))*const+
v(i,j));

        % diagonal matrix element

        offd3(i,j)=[(1/(mass(i,j-1)+mass(i,j))) *const;

        end
    end

    d(1,1) = -(((1/(mass(1,1)+mass(1,1))+1/(mass(2,1)+mass(1,1))+
(1/(mass(1,1)+mass(1,1))+1/(mass(1,2)+mass(1,1))))*const+ v(i,j));

    H=-(d(:))'; % diagonal matrix element
    offd1=(offd1(:))'; % off-diagonal element 1
    offd2=(offd2(:))'; % off-diagonal element 2

```

```

offd3=(offd3(:))' % off-diagonal element 3;
offd4=(offd4(:))'; % off-diagonal element 4;
Mx1=((Mx-1)*(My-1));

for i=1:Mx1
    d(i)=H(i);
    offd1(i)=offd1(i);
    offd2(i)=offd2(i);
    offd3(i)=offd3(i);
    offd4(i)=offd4(i);
end

t = d(1:Mx1);
t1 = -offd1(2:Mx1);
t2 = -offd2(1:Mx1-1);
t3 = -offd3(Mx:Mx1);
t4 = -offd4(1:Mx1-(Mx-1));

Hmatrix2=sparse(diag(t,0)+diag(t1,-1)+diag(t2,1)+diag(t3,-(Mx-1))+diag(t3,(Mx-1)));
% Hamiltonian matrix

[phi,te]=eigs(Hmatrix2,num_sol,'SM'); % Use Matlab function "eigs" to find
% "num_sol" eigenfunctions and eigenvalues

for i=1:size(phi,1)
    if (phi(i)<0)
        phi(i)=(-1)*phi(i);
    elseif (phi(i)>=0)
        phi(i)=(1)*phi(i);
    end
end

AA= max(max(phi)); % Finding the maximum value of the wavefunction
phi = phi./AA; % Finding the normalized amplitude of the wavefunction

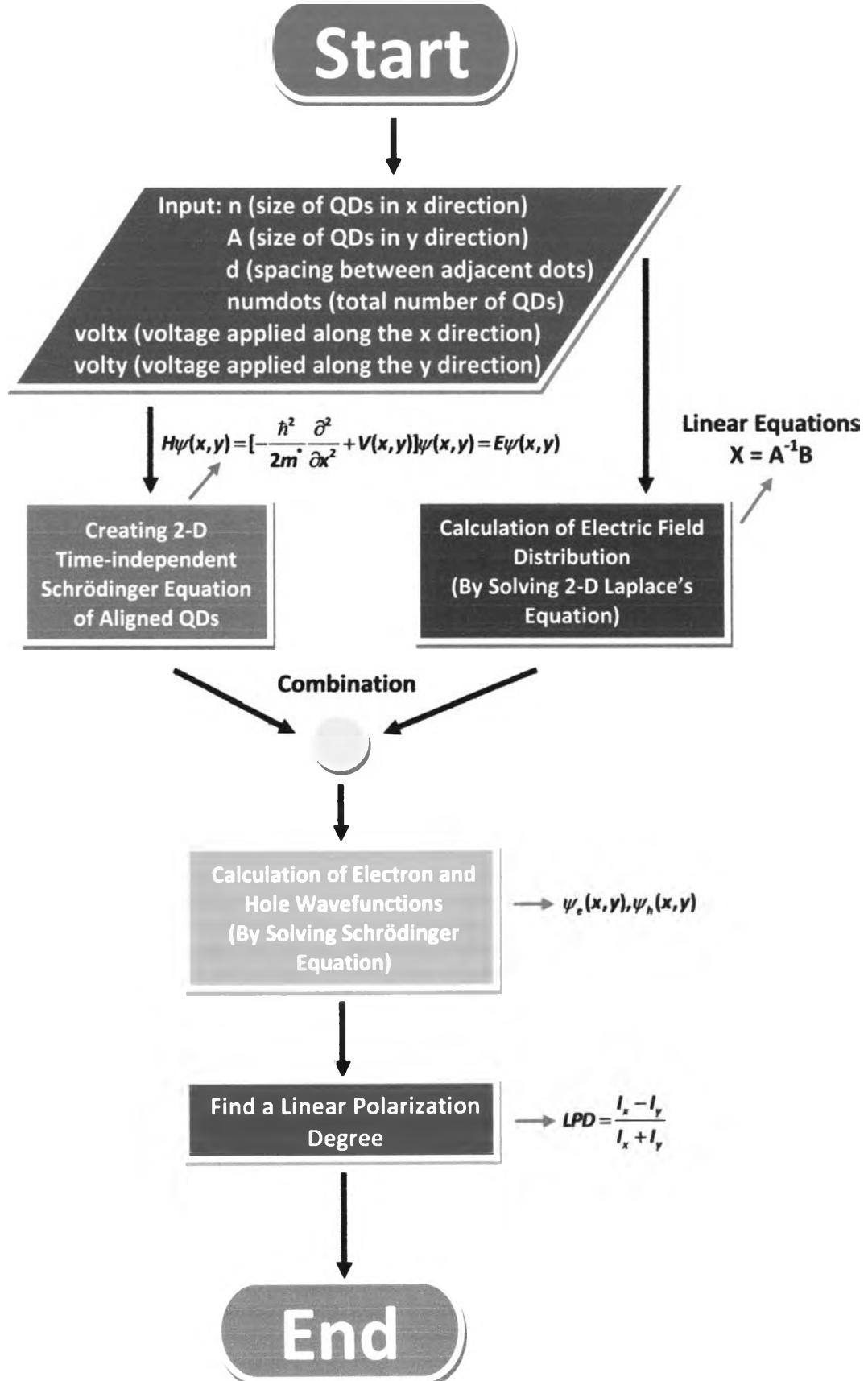
K= reshape(phi,Mx-1,My-1);
Phi=zeros(Mx+1,My+1);
Phi(2:Mx,2:end-1)=K(1:end,1:end);

return

```

---

## Calculation Flowchart



## Appendix B: List of Publications

### National Conference

1. Chonlakorn Chiewpanich , Chanin Wissawinthanon, and Somsak Panyakeow, "Comparison between two techniques for the growth of self-assembled laterally-aligned quantum dots: the superlattice template and the InGaAs induction layer", *Proceedings of the 32<sup>th</sup> Thailand's National Electrical Engineering Conference*, Vol.II, pp.915-918, October 2009.

### International Conference

1. N. Chit Swe, C. Chiewpanich, S. Suraprapapich, S. Panyakeow, and C. Wissawinthanon, "Temperature-dependent optical polarization property of self-assembled laterally-aligned quantum dots", *Proceedings of the International Conference on System on Chip Design Challenges*, Manila, Philippines, pp.141-144, September 2010.

## Vitae

**Chonlakorn Chiewpanich** was born in Bangkok, Thailand, on September 18<sup>th</sup>, 1985. He graduated from Nawamintrachinuthit Triamudomsuksanomkla school in March 2003. In June 2003, He entered Chulalongkorn University and received the Bachelor of Engineering in field of Electrical Engineering with GPAX 2.61 in May 2007. She was further his study in June 2007, as a master student of the Semiconductor Device Research Laboratory (SDRL). His interests are nanotechnology for III-V compound semiconductors, especially in nanophotonics devices.

