#### อินเจคชันฟังก์ชันของไอออนหนักที่มีพลังงานสูงจากควงอาทิตย์

นางสาวฑิราณี ขำล้ำเลิศ

วิทยานิพนธ์นี้เป็นส่วนหนึ่งของการศึกษาตามหลักสูตรปริญญาวิทยาศาสตรคุษฎีบัณฑิต สาขาวิชาฟิสิกส์ ภาควิชาฟิสิกส์ คณะวิทยาศาสตร์ จุฬาลงกรณ์มหาวิทยาลัย

ปีการศึกษา 2544

ISBN 974-03-0893-7

ลิขสิทธิ์ของจุฬาลงกรณ์มหาวิทยาลัย

# INJECTION FUNCTION OF ENERGETIC HEAVY IONS FROM THE SUN

Miss Thiranee Khumlumlert

A Dissertation Submitted in Partial Fulfillment of the Requirements for the Degree of Doctor of Philosophy in Physics

Department of Physics

Faculty of Science.

Chulalongkorn University

Academic Year 2001

ISBN 974-03-0893-7

Dissertation Title	Injection Function of Energetic Heavy Ions from the Sun
Ву	Miss Thiranee Khumlumlert
Department	Physics
Thesis Advisor	Associate Professor David Ruffolo, Ph.D.
	**
Accepted	by the Faculty of Science, Chulalongkorn University in Partial
Fulfillment of the Requirer	nents for the Doctor's Degree.
Park K	area A.D.
	arnimeDeputy Dean for Administrative Affairs
(Associate Professor Pi	pat Karntiang, Ph.D) Acting Dean, Faculty of Science
DISSERTATION COMMIT	FEE // / / / / / / / / / / / / / / / / /
File	BALLE PALENCYMANCHIE. Chairman
(As	ssistant P <mark>rofessor Pisistha</mark> Ratanavararaksa, Ph.D.)
<u> </u>	David Ruffolo Thesis Advisor
	ssociate Professor David Ruffolo, Ph.D.)
<i>\.</i>	Mund Unditalian hat Member
(Al	npisit Ungkitchanukit, Ph.D.)
	0 1/4
จ พักล <sub>ะ</sub>	
(Ra	attachat Mongkolnavin, Ph.D.)
	N. Saugnawaž Member
****	

(Nuanwan Sanguansak, Ph.D.)

Dissertation Title

นางสาวฑิราณี ขำล้ำเลิศ : อินเจคชันฟังก์ชันของไอออนหนักที่มีพลังงานสูงจากดวงอาทิตย์ (INJECTION FUNCTION OF ENERGETIC HEAVY IONS FROM THE SUN)

อ. ที่ปรึกษา : รศ. ดร. เดวิด รูฟโฟโล, 139 หน้า. ISBN 974-03-0893-7.

การปะทุที่ดวงอาทิตย์คือการระเบิดบนผิวของดวงอาทิตย์ ที่อาจเกี่ยวข้องกับการปล่อยก้อนมวลจากโค โรนา (CME) เข้าไปในตัวกลางระหว่างดาวเคราะห**์ ทั้งการร**ะเบิดและการปล่อยก้อนมวลจากโคโรนานี้สามารถ ปลดปล่อยอนุภาคพลังงานสูงจากดวงอาทิตย์และส่งผลที่สำคัญต่อโลกได้แก่ การรบกวนระบบสื่อสารทางวิทยุ หรือเป็นสาเหตุของการเกิดกระแสไฟฟ้าขัดข้อง เราใช้สมการการขนส่งของ รูฟโฟโล (1995) เพื่อศึกษาการเคลื่อน ที่ของอนุภาคพลังงานสูงจากดวงอาทิตย์ที่เคลื่อนที่เข้าไปในตัวกลางระหว่างดาวเคราะห์ในสถานการณ์ต่างๆ ได้ แก่ เหตุการณ์ ณ วันที่ 9 กรกฎาคม 2539 สำหรับโปรตอนที่มีพลังงานต่ำ, เหตุการณ์ ณ วันที่ 6 พฤศจิกายน 2540 สำหรับไอออนพลังงานปานกลางของธาตุต่างๆ หลายช่วงพลังงาน และการรวมผลของเส้นสนามแม่เหล็ก แบบคอขวดสำหรับเหตุการณ์บนดวงอาทิตย์ ณ วันที่ 14 กรกฎาคม 2543 เราได้ทำการพัฒนาวิธีการใหม่สำหรับ การวิเคราะห์ข้อมูลที่ได้จากยานอวกาศหรือข้อมูลที่ตรวจวัดได้บนพื้นโลกสำหรับอนุภาคประเภทต่างๆ ในช่วงพลัง งานต่างๆ โดยการรวมการแปรปรวนที่ไม่ใช่การแป<del>รปรวนเชิงสถิติ เราใช้การฟิตข้อมูล</del>แบบกำลังสองน้อยที่สุดเชิง เส้น (linear least squares fitting) และการตัดอย่างอัตโนมัติเพื่อให้ได้ค่าที่ดีที่สุดของฟังก์ชันเชิงเส้นแบบ สามเหลี่ยมเพื่อฟิตข้อมูลได้ตามวัตถุประสงค์โดยขึ้นกับค่าต่ำสุดของผลต่างกำลังสอง ( $\chi^2$ ) เราพบว่าการเร่งของ อนุภาคพลังงานสูงจากดวงอาทิตย์สามารถเกิดขึ้นใกล้ดวงอาทิตย์และพิจารณาผลของการเคลื่อนที่ของคลื่น กระแทกที่เกิดจากการปล่อยก้อนมวลจากโคโรนา การเร่งที่เกิดจากการปล่อยก้อนมวลจากโคโรนามีค่ามากที่สุด เมื่อ CMEs เคลื่อนที่ใกล้ดวงอาทิตย์ และ CMEs จะสูญเสียประสิทธิภาพของการเร่งหลังจากเคลื่อนที่ออกจาก ดวงอาทิตย์ และความสามารถที่จะเร่งอนุภาคที่มีพลังงานสูงกว่าจะลดลงอย่างเร็วมากกว่าในกรณีของอนุภาคที่ มีพลังงานต่ำกว่า ยิ่งไปกว่านั้นในงานนี้ยังแสดงหลักฐานที่สำคัญของการสะท้อนในคอขวดสนามแม่เหล็กที่เกิด ในบริเวณที่ไกลกว่าโลกด้วย

ภาควิชา ฟิสิกส์ สาขาวิชา ฟิสิกส์ ปีการศึกษา 2544 ลายมือชื่อนิสิต ที่ธาณ ราค้าเส้น

ลายมือชื่ออาจารย์ที่ปรึกษา ....เฉวิฉ รุฟโฟโล....

##4173831423

: MAJOR PHYSICS

KEY WORD: SOLAR FLARE / SOLAR ENERGETIC PARTICLES / SOLAR WIND / ACCELERATION / MIRRORING THIRANEEE KHUMLUMLERT: THESIS TITLE. (INJECTION FUNCTION OF ENERGETIC HEAVY IONS FROM THE SUN) THESIS ADVISOR: ASSOC.PROF. DAVID RUFFOLO, PhD.,

139 pp. ISBN 974-03-0893-7.

A solar flare is an explosion on the surface of the Sun, which may be associated with a coronal mass ejection (CME) into the interplanetary medium, both of which can release energetic particles and have important effects on the Earth, such as disrupting radio communications or causing electric power failures. We treat the solar energetic particle propagation through the interplanetary medium using a transport equation (Ruffolo 1995) in different situations, such as for the low energy protons of the solar event on July 9, 1996, the medium energy ions of many species and energy bands from the solar event on November 6, 1997, and adding the effect of bottleneck magnetic field lines for the solar event on July 14, 2000. We have developed a new technique for analyzing spacecraft or ground-based data for various types of particles and energy bands, taking nonstatistical fluctuations into account. We used the linear least squares fitting and the optimized automatic truncation of the piecewise linear function to fit the data objectively, relying on  $\chi^2$ minimization. We found that the acceleration of the solar energetic particles can happen near the Sun, and include the effect of the motion of CME-driven shock. The acceleration by CMEs is greatest when CMEs propagate near the Sun, CMEs lose efficiency of the acceleration after they propagate outward from the Sun, and furthermore the ability to accelerate higher energy particles decreases more quickly than for lower energy particles. Furthermore, this work provides important evidence of mirroring in a magnetic bottleneck beyond the Earth.

Department of Physics

Field of study: Physics

Academic year 2001

Student's signature. David Ruffelo...

#### Acknowledgements

I would like to extend my sincere thanks to my advisor, Assoc. Prof. David Ruffolo, who suggested this topic and has provided guidance, assistance and insights throughout my time under his thesis advisor. He has given the opportunities to perform research with other researchers. I have gained much from my association with him.

I am very grateful to Dr. Glenn Mason, Dr. Joseph Dwyer, Dr. Mihir Desai, and everybody at the Department of Physics, University of Maryland, USA. for suggestions and help while I stayed there for 7 months. I appreciate this very much.

I am also grateful to the thesis committee for their reading and offering suggestions for this dissertation. I would like to thank everybody in the computational astrophysics research lab for their friendly help and will-power to me. Finally, I would like to dedicate this thesis to my father and my family for everything they have given to me.

This work was also supported by the Thailand Research Fund and Naresuan University.

#### Contents

Abstract in Thaiiv
Abstract in Englishv
Acknowledgementsvi
Contents vii
List of Figures ix
List of Tablesxviii
Chapter 1 Introduction 1
1.1 The Objective2
1.2 Procedure and Outline
1.3 Usefulness of This Work
Chapter 2 Theoretical Background and
Transport Equation 4
2.1 Irregular Magnetic Field from the Sun4
2.2 Transport of Particles: Fokker-Planck Equation
2.3 Transport Equation for Solar Energetic Particles in
Interplanetary Space
Chapter 3 Methodology of Fitting
3.1 Simulation of the Interplanetary Transport of Solar
Energetic Particles17
3.2 Least Squares Fitting
3.3 Piecewise Linear Injection Function
3.4 Automatic Truncation of the Injection Function and Variation
of Joint Times25
3.5 Procedure for the Fitting

## Contents (cont.)

Chapter 4 Preparing Spacecraft or	
Ground-Based Data for Fitting.	31
4.1 Data Selection	31
4.2 Additional Information about Events of Interest	33
4.3 Uncertainty of the Spacecraft Data: Taking Interplanetary	
Fluctuation into Account	34
4.4 Sources of Data	37
Chapter 5 Results and Discussion	40
5.1 The Solar Event on July 9, 1996	41
5.2 The Solar Event on July 14, 2000	46
5.3 The Solar Event on November 6, 1997	54
5.4 Comparison of Results for Three Solar Events	67
Chapter 6 Conclusions	70
References	73
Appendices	
Appendix A Uncertainty of Interplanetary Fluctuations	76
Appendix B The Minimum $\chi^2$ Point	80
Appendix C Fitting Results for November 6, 1997	82
Appendix D Data That Could Not Be Fitted Well	103
Appendix E Wind Program for Simulation	111
Vitae	122

#### List of Figures

Figure	Page
Figure 2.1	Solar wind and the interplanetary magnetic field
Figure 2.2	The propagation of magnetic flux through a closed contour, $L6$
Figure 2.3	Particle orbits in a uniform magnetic field for various pitch angles8
Figure 2.4	The adiabatic focusing and pitch-angle scattering in the fixed frame (a)
	and the solar wind frame (b)
Figure 2.5	Illustration of the Archimedean spiral field and $\psi(z)$
Figure 3.1	The deconvolution technique for a piecewise linear injection function
	near the Sun: a) shows the triangular injection profiles, b) shows the
	response functions, which result from the convolution of the Green's
	function with each triangular injection profile from a), c) is the
	best-fit piecewise linear injection profile, and d) is the linear
	combination (solid line) of response functions (dashed lines) 24
Figure 3.2	Example of joint times of the injection function, determined by $\varepsilon$
	and $\delta$
Figure 3.3	Flow chart of the fitting method
Figure 4.1	An example of spacecraft data for oxygen with the statistical
	uncertainties
Figure 4.2	The spacecraft data for oxygen with the new uncertainties
Figure 5.1	Solar wind parameters from the WIND spacecraft on July 2-29, 1996.
	The event of interest is on July 9, or day of year $(doy) = 191$ .
	Downloaded from http://web.mit.edu/space/www/wind
Figure 5.2	The X-ray flux profile on July 7-9, 1996, downloaded from
	http://solar.sec.noaa.gov/ftpmenu/plots.html

Figure 5.3	The intensity fitting results of protons at 123 keV from the WIND
	spacecraft. Diamonds indicate the data with uncertainties, and the
	line indicates the fit
Figure 5.4	The anisotropy fitting results of protons at 123 keV from the WIND
	spacecraft on July 9, 1996. Diamonds indicate the data with
	uncertainties, and the line indicates the fit45
Figure 5.5	The injection function of protons at 123 keV of solar event on July 9,
	1996 at $\lambda_r$ =0.42 AU, in which the injection time is 274 min from
	point A to B
Figure 5.6	The X-ray flux profile on July 13-15, 2000
Figure 5.7	Solar wind parameters measured near Earth by the WIND spacecraft on
	July 14 to August 10, 2000. The event of interest is on July 14, or
	day of year $(doy) = 196$
Figure 5.8	The intensity fitting results for protons on July 14, 2000 before adding
	the bottleneck configuration. Points indicate data, with uncertainties,
	and the line represents the fit49
Figure 5.9	The anisotropy fitting results for protons on July 14, 2000 before adding
	the bottleneck configuration
Figure 5.10	The configuration of magnetic field lines from the Sun to the Earth,
	with the bottleneck
Figure 5.1	1 The intensity fitting results for protons on July 14, 2000 after adding
	the bottleneck configuration for $\lambda$ = 0.18 AU
Figure 5.13	2 The anisotropy fitting results for protons on July 14, 2000 after adding
	the bottleneck configuration for $\lambda$ = 0.18 AU
Figure 5.1	3 The injection profile with FWHM of 7 min for the solar event on July

	14, 2000
Figure 5.14	The hourly averaged oxygen intensity from $60~\mathrm{keV/n}$ to $50~\mathrm{MeV/n}$ from
	the ACE spacecraft due to the Nov. 4 and 6, 1997 events, where F
	is a flare time, S is a shock arrival time. (Mason et al. 1999a) 55
Figure 5.15	The X-ray flux profile on November 6, 199757
Figure 5.16	The solar wind parameters from the WIND spacecraft on November
£	5 to December 2, 1997. The event of interest is on November 6,
	or day of year $(doy) = 310$
Figure 5.17	The intensity fitting result of oxygen at 15.6-21.0 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997. The
	diamond symbols indicate data with their uncertainties, and
	the line represents the fit60
Figure 5.18	The injection function of oxygen at 15.6-21.0 MeV/n of the solar event
	on November 6, 1997 at the best-fit $\lambda$ = 0.054 AU60
Figure 5.19	The intensity fitting result of neon at 17.6-23.6 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199761
Figure 5.20	The injection function of neon at 17.6-23.6 MeV/n of the solar event
	on November 6, 1997 at the best-fit $\lambda = 0.054 \text{ AU} \dots 61$
Figure 5.21	The intensity fitting result of magnesium at 16.0-19.3 MeV/n from the
	SIS instrument on the ACE spacecraft on November 6, 199762
Figure 5.22	The injection function of magnesium at 16.0-19.3 MeV/n of the solar
	event on November 6, 1997 at three best-fit $\lambda$ = 0.041 AU62
Figure 5.23	The intensity fitting result of silicon at 13.0-17.3 MeV/n from the
	SIS instrument on the ACE spacecraft on November 6, 199763
Figure 5.24	The injection function of silicon at 13.0-17.3 MeV/n of the solar event
	on November 6, 1997 at the best-fit $\lambda = 0.042 \text{ AU} \dots 63$

Figure 5.25	The intensity fitting result of iron at 23.6-36.3 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199764
Figure 5.26	The injection function of iron at 23.6-36.3 MeV/n of the solar event on
	November 6, 1997 at the best-fit $\lambda$ = 0.033 AU
Figure 5.27	The summary results of the mean free path vs. energy per nucleon for
	each element for various energy values on November 6, 1997.
4	Diamonds, circles, triangles, crosses, and squares indicate magnesium,
	iron, oxygen, silicon, and neon, respectively
Figure 5.28	The injection function vs. kinetic energy of particles on November
	6, 1997. Diamonds, squares, triangles, and circles indicate oxygen,
	neon, magnesium, silicon, and iron, respectively
Figure A.1	Sample of the intensity of particles with $\sigma_{\rm stat}$ only. Note that the actual
	fluctuations are much greater than the error bars
Figure A.2	Sample of the intensity of particles with combined uncertainties
	$(\sqrt{\sigma_{stat}^2 + \sigma_{IPF}^2})$ . Now the error bars better represent the actual
	fluctuations
Figure B.1	Example of the $\chi^2$ value at various $\lambda$
Figure B.2	Example of the minimum point from a parabolic graph
Figure C.1	The intensity fitting results of oxygen at 7.1-10.0 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997 82
Figure C.2	The intensity fitting results of oxygen at 10.0-13.1 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997 83
Figure C.3	The intensity fitting results of oxygen at 13.1-15.6 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997 83
Figure C.4	The intensity fitting results of oxygen at 21.0-29.4 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997 84

Figure C.5	The intensity fitting results of oxygen at 29.4-38.9 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997 84
Figure C.6	The intensity fitting results of neon at $7.8\text{-}11.1~\text{MeV/n}$ from the SIS
	instrument on the ACE spacecraft on November 6, 1997 85
Figure C.7	The intensity fitting results of neon at 11.1-14.6 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997
Figure C.8	The intensity fitting results of neon at 14.6-17.6 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997
Figure C.9	The intensity fitting results of neon at 23.6-33.2 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 1997
Figure C.10	The intensity fitting results of neon at 33.2-44.0 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199787
Figure C.11	The intensity fitting results of magnesium at 8.5-12.2 MeV/n from the
	SIS instrument on the ACE spacecraft on November 6, 199787
Figure C.12	The intensity fitting results of magnesium at 12.2-16.0 MeV/n from
	the SIS instrument on the ACE spacecraft on November 6, 199788
Figure C.13	3 The intensity fitting results of magnesium at 19.0-26.0 MeV/n from
	the SIS instrument on the ACE spacecraft on November 6, 199788
Figure C.14	The intensity fitting results of silicon at 9.0-13.0 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199789
Figure C.18	The intensity fitting results of silicon at 17.3-20.8 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199789
Figure C.10	The intensity fitting results of silicon at 20.8-28.1 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199790
Figure C.1'	7 The intensity fitting results of silicon at 28.1-39.8 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199790

Figure C.18	The intensity fitting result of iron at 10.5-15.8 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199791
Figure C.19	The intensity fitting results of iron at 15.8-21.5 MeV/n from the SIS $$
	instrument on the ACE spacecraft on November 6, 199791
Figure C.20	The intensity fitting results of iron at 21.5-26.3 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199792
Figure C.21	The intensity fitting results of iron at 36.3-52.2 MeV/n from the SIS
	instrument on the ACE spacecraft on November 6, 199792
Figure C.22	The injection function of oxygen at 7.1-10.0, 10.0-13.1, and 13.1-15.6
	MeV/n, respectively, of the solar event on November 6, 1997 93
Figure C.23	The injection function of oxygen at 15.6-21.0, 21.0-29.4, and 29.4-38.9
	MeV/n, respectively, of the solar event on November 6, 1997 94
Figure C.24	The injection function of neon at 7.8-11.1, 11.1-14.6, and 14.6-17.6
	MeV/n, respectively, of the solar event on November 6, 1997 95
Figure C.25	The injection function of neon at 17.6-23.6 and 23.6-33.2 MeV/n,
	respectively, of the solar event on November 6, 199796
Figure C.26	The injection function of magnesium at 8.5-12.2, 12.2-16.0, and 16.0
	-19.3 MeV/n, respectively, of the solar event on November 6, 1997.97
Figure C.27	The injection function of magnesium at 19.3-26.0 MeV/n of the solar $$
	event on November 6, 199798
Figure C.28	The injection function of silicon at 9.0-13.0, 13.0-17.3, and 17.3-20.8
	MeV/n, respectively, of the solar event on November 6, 1997 99
Figure C.29	The injection function of silicon at 20.8-28.1 and 28.1-39.8 MeV/n,
	respectively, of the solar event on November 6, 1997100
Figure C.30	The injection function of iron at 10.5-15.8, 15.8-21.5, and 21.5-26.3
	MeV/n, respectively, of the solar event on November 6, 1997 101

Figure C.31	The injection function of iron at $26.3-36.3$ and $36.3-52.2$ MeV/n,
	respectively, of the solar event on November 6, 1997102
Figure D.1	The intensity data with their uncertainties of oxygen at $38.9\text{-}63.8~\text{MeV}/$
	nucleon from the SIS instrument on the ACE spacecraft on November
	6, 1997. These data could not be fitted because there was more than
	one minimum in $\chi^2$ vs. $\lambda$
Figure D.2	The intensity data with their uncertainties of oxygen at $63.8\text{-}89.8~\text{MeV}/$
	nucleon from the SIS instrument on the ACE spacecraft on November
	6, 1997. These data could not be fitted because there was more than
	one minimum in $\chi^2$ vs. $\lambda$
Figure D.3	The intensity data with their uncertainties of neon at 44.0-72.2 MeV/
	nucleon from the SIS instrument on the ACE spacecraft on November
	6, 1997. These data could not be fitted because there was more than
	one minimum in $\chi^2$ vs. $\lambda$
Figure D.4	The intensity data with their uncertainties of neon at 72.2-101.8 MeV/
	nucleon from the SIS instrument on the ACE spacecraft on November
	6, 1997. These data could not be fitted because the fluctuations in
	the data were too great105
Figure D.5	The intensity data with their uncertainties of magnesium at 26.0-36.6
	MeV/nucleon from the SIS instrument on the ACE spacecraft on
	November 6, 1997. These data could not be fitted because there was
	more than one minimum in $\chi^2$ vs. $\lambda$
Figure D.6	The intensity data with their uncertainties of magnesium at 36.6-48.6
	MeV/nucleon from the SIS instrument on the ACE spacecraft on
	November 6, 1997. These data could not be fitted because there was
	more than one minimum in $\chi^2$ vs. $\lambda$

Figure D.7	The intensity data with their uncertainties of magnesium at 48.6-80.0
	MeV/nucleon from the SIS instrument on the ACE spacecraft on
	November 6, 1997. These data could not be fitted because there was
	more than one minimum in $\chi^2$ vs. $\lambda$
Figure D.8	The intensity data with their uncertainties of magnesium at 80.0-112.9
	MeV/nucleon from the SIS instrument on the ACE spacecraft on
	November 6, 1997. These data could not be fitted because the
	fluctuations in the data were too great
Figure D.9	The intensity data with their uncertainties of silicon at $39.8-52.9 \text{ MeV}/$
	nucleon from the SIS instrument on the ACE spacecraft on
	November 6, 1997. These data could not be fitted because the
4.	fluctuations in the data were too great
Figure D.10	The intensity data with their uncertainties of silicon at 52.9-87.1
	MeV/nucleon from the SIS instrument on the ACE spacecraft on
	November 6, 1997. These data could not be fitted because there was
- Nau-	more than one minimum in $\chi^2$ vs. $\lambda$
Figure D.11	The intensity data with their uncertainties of silicon at 87.1-123.2
	MeV/nucleon from the SIS instrument on the ACE spacecraft on
	November 6, 1997. These data could not be fitted because the
	fluctuations in the data were too great
Figure D.12	2 The intensity data with their uncertainties of iron at 52.2-70.2 MeV/
	nucleon from the SIS instrument on the ACE spacecraft on November
	6, 1997. These data could not be fitted because there was more
	than one minimum in $\chi^2$ vs. $\lambda$
Figure D.13	3 The intensity data with their uncertainties of iron at 70.2-117.5 MeV/
	nucleon from the SIS instrument on the ACE spacecraft on November

	6, 1997. These data could not be fitted because the fluctuations	
	in the data were too great	109
Figure D.14	The intensity data with their uncertainties of iron at 117.5-167.7	
	MeV/nucleon from the SIS instrument on the ACE spacecraft on	
	November 6, 1997. These data could not be fitted because the	
	fluctuations in the data were too great	110



#### List of Tables

able	age
e 5.1 Fitting results for November 6, 1997	. 66
e 5.2 Comparison of results for three solar events	. 69
e A.1 Table of uncertainty estimation. Times 1230-1530 min represent the d	ata
of interest, used to estimate the IPF uncertainty	.77

