การหางนาคงองเครื่องกำเนิคไฟฟ้าแบบกระจายชนิคพลังงานแสงอาทิตย์ ในระบบจำหน่ายไฟฟ้า โคยพิจารณาสภาวะแสงอาทิตย์และความผิคเพี้ยนทางฮาร์มอนิก

นายวิชชากร เฮงศรีธวัช

วิทยานิพนธ์นี้เป็นส่วนหนึ่งของการศึกษาตามหลักสูตรปริญญาวิศวกรรมศาสตรคุษฎีบัณฑิต สาขาวิชาวิศวกรรมไฟฟ้า ภาควิชาวิศวกรรมไฟฟ้า คณะวิศวกรรมศาสตร์ จุฬาลงกรณ์มหาวิทยาลัย ปีการศึกษา 2554 ลิขสิทธิ์ของจุฬาลงกรณ์มหาวิทยาลัย

บทคัดย่อและแฟ้มข้อมูลฉบับเต็มของวิทยานิพนธ์ตั้งแต่ปีการศึกษา 2554 ที่ให้บริการในคลังปัญญาจุฬาฯ (CUIR) เป็นแฟ้มข้อมูลของนิสิตเจ้าของวิทยานิพนธ์ที่ส่งผ่านทางบัณฑิตวิทยาลัย

The abstract and full text of theses from the academic year 2011 in Chulalongkorn University Intellectual Repository(CUIR) are the thesis authors' files submitted through the Graduate School.

SIZING OF PHOTOVOLTAIC DISTRIBUTED GENERATORS IN A DISTRIBUTION SYSTEM WITH CONSIDERATION OF SOLAR RADIATION AND HARMONIC DISTORTION

Mr. Vichakorn Hengsritawat

A Dissertation Submitted in Partial Fulfillment of the Requirements for the Degree of Doctor of Philosophy Program in Electrical Engineering Department of Electrical Engineering Faculty of Engineering Chulalongkorn University Academic year 2011 Copyright of Chulalongkorn University

Thesis Title	SIZING OF PHOTOVOLTAIC DISTRIBUTED
	GENERATORS IN A DISTRIBUTION SYSTEM WITH
	CONSIDERATION OF SOLAR RADIATION AND
	HARMONIC DISTORTION
Ву	Mr. Vichakorn Hengsritawat
Field of Study	Electrical Engineering
Thesis Advisor	Assistant Professor Thavatchai Tayjasanant, Ph.D.

Accepted by the Faculty of Engineering, Chulalongkorn University in Partial Fulfillment of the Requirements for the Doctoral Degree

......Dean of the Faculty of Engineering (Associate Professor Boonsom Lerdhirunwong, Dr.Ing.)

THESIS COMMITTEE

...... Chairman

(Professor Bundhit Eua-arporn, Ph.D.)

...... Thesis Advisor

(Assistant Professor Thavatchai Tayjasanant, Ph.D.)

...... Examiner

(Assistant Professor Kulyos Audomvongseree, Ph.D.)

..... External Examiner

(Assistant Professor Natthaphob Nimpitiwan, Ph.D.)

...... External Examiner

(Pradit Fuangfoo, Ph.D.)

วิชชากร เฮงศรีธวัช : การหาขนาดของเครื่องกำเนิดไฟฟ้าแบบกระจายชนิดพลังงาน แสงอาทิตย์ในระบบจำหน่ายไฟฟ้า โดยพิจารณาสภาวะแสงอาทิตย์และความผิดเพี้ยน ทางฮาร์มอนิก (SIZING OF PHOTOVOLTAIC DISTRIBUTED GENERA-TORS IN A DISTRIBUTION SYSTEM WITH CONSIDERATION OF SOLAR R ADIATION AND HAR MONIC DISTORTION) อ.ที่ปรึกษา วิทยานิพนธ์หลัก: ผศ.คร.ธวัชชัย เตชัสอนันต์, 162 หน้า.

้วิทยานิพนธ์เล่มนี้นำเสนอวิธีทางกวามน่าจะเป็น เพื่อหางนาคที่เหมาะสมของเครื่อง ้ กำเนิดไฟฟ้าแบบกระจายชนิดพลังงานแสงอาทิตย์ในระบบจำหน่ายไฟฟ้า โดยพิจารณาถึง สภาวะการกระจายของแสงอาทิตย์และความผิดเพี้ยนทางฮาร์มอนิก ด้วยวิธีการดังกล่าว การ ้จำลองแบบมอนติการ์โลจะถูกนำมาใช้ในการสุ่มก่าการกระจายแสงอาทิตย์, อุณหภูมิแวคล้อม รวมถึงแรงคันที่สถานีไฟฟ้าย่อย และความต้องการของโหลคในระบบจำหน่ายไฟฟ้า โดยมี ้วัตถุประสงค์ เพื่อทำให้กำลังไฟฟ้าสุญเสีย จริงเฉลี่ยของระบบมีค่าต่ำสุด ในขณะ ที่เงื่อนไข บังคับทางค้านคุณภาพไฟฟ้า ซึ่งได้แก่ แรงคันไฟฟ้าที่โหนด ุกระแสฮาร์มอนิก ุค่าความ ้ผิดเพี้ยนแรงดันฮาร์มอนิกรวม และก่ากวามผิดเพี้ยนความต้องการฮาร์มอนิกรวม ยังกงอยู่ใน ้งอบเงตที่กำหนดตามมาตรฐาน IEC และ IEEE ทั้งนี้ยังได้รวมผลของฮาร์มอนิกที่มีอยู่เดิม ในระบบเพื่อ ประเมิน หาขนาดที่เหมาะสมของเครื่องกำเนิดไฟฟ้าแบบกระจายชนิดพลังง าน แสงอาทิตย์ด้วย วิทยานิพนธ์เล่มนี้ยังได้นำเสนอวิธีการวิเคราะห์ด้วยดัชนีเสถียรภาพแรงดัน เพื่อเลือก ตำแหน่งที่เหมาะสมในการติดตั้งเครื่องกำเนิดไฟฟ้าแบบกระจายชนิดพลังงาน แสงอาทิตย์ นอกจากนี้ ยังได้มีการศึกษาผลกระทบที่มีต่อการหางนาดที่เหมาะสมของเครื่อง ้กำเนิดไฟฟ้าแบบกระจายชนิดพลังงานแสงอาทิตย์ จากการใช้แบบจำลองของโหลดและการ ้ปรับค่าตัวประกอบกำลัง ในการทำงาน ที่แตกต่างกัน รวมถึง ศึกษาผลกระทบของแบบจำลอง ้ของอินเวอร์เตอร์ และ การพิจารณาถึง เครื่องกำเนิดไฟฟ้าแบบกระจายอื่นที่มีอย่เดิมในระบบ ้ จำหน่ายไฟฟ้า วิธีการที่พัฒนาขึ้นสามารถประยกต์ใช้ได้กับระบบจริง โดยได้ทำการทดสอบ กับระบบขนาค 33 บัส และระบบจำหน่ายไฟฟ้าแห่งหนึ่งของประเทศไทยขนาค 51 บัส

ภาควิชา	วิศวกรรมไฟฟ้า	ลายมือชื่อนิสิต
สาขาวิชา <u></u>	วิศวกรรมไฟฟ้า	ลายมือชื่อ อ.ที่ปรึกษาวิทยานิพนธ์หลัก
ปีการศึกษา	2554	

4971875421 : MAJOR ELECTRICAL ENGINEERING KEYWORDS: PHOTOVOLTAIC GENERATION / MONTE CARLO SIMULA-TION / PROBABILISTIC APPROACH / SOLAR RADIATION / HARMONIC DISTORTION

VICHAKORN HENGSRITAWAT: SIZING OF PHOTOVOLTAIC DIS-TRIBUTED GENERATORS I N A DI STRIBUTION S YSTEM W ITH CONSIDERATION OF SOLAR RADIATION AND HARMONIC DIS-TORTION. ADVISOR: ASST. PROF. THAVATCHAI TAYJASANANT, Ph. D., 162 pp.

This dissertation presents a probabilistic approach to calculate an optimal size of photovoltaic distributed generators (PV-DGs) in a distribution system with consideration of solar radiation and harmonic distortion. Monte Carlo simulation is applied to predict solar radiations, ambient temperatures, substation voltages and load de mands. The formulated objective f unction is t o m inimize ave rage r eal power loss, while power quality constraints i.e., node voltage, harmonic current, total harmonic distortion voltage and total de mand distortion are kept within the limits complied with IEC and IEEE standards. Existing background harmonics are included in an evaluation of the optimal size of PV-DG. In addition, static voltage stability ind ex a nalysis is proposed t o select a proper l ocation of P V-DG installation in a distribution system. Furthermore, impacts of static load models and power factor control on optimal PV-DG sizing as well as effects of PV inverter modeling and existing DGs in a distribution system are taken i nto account. The developed method can be applied to actual systems and was tested with a 33-Bus test system and an actual 51-Bus radial distribution system in Thailand.

Department : Electrical Engineering	Student's Signature
Field of Study : <u>Electrical Engineering</u>	Advisor's Signature
Academic Year : 2011	

ACKNOWLEDGEMENTS

First, I would like to give a special thank to my a dvisor, Assistant Professor Dr. Thavatchai Tayjasanant, for his advice, suggestions, encouragement and support throughout the development of this dissertation as well as my study program.

Second, I would like to thank chairman and examination committee for their va luable s uggestions a nd us eful r ecommendations. I would like also t hank Sripatum University (SPU) to award me a scholarship for entire my study as well as Dr. Jakpetch Matharatch from the Provincial Electricity Authority of Thailand (PEA) for the measurement data at PV farm of Solar Power Company.

Finally, my special thanks to my family, my wife and my daughter for their l ove, pa tience, i nspiration, s upport a nd understanding i n pa st years. T his research is dedicated to them.

Contents

Abstract in Thai	iv
Abstract in English	v
Acknowledgements	vi
Contents	vii
List of Tables	X
List of Figures	xi
Nomenclatures	xvii

CHAPTER

I.	Int	roduction	1
	1.1	Overview of World's PV Generation	1
	1.2	Solar PV Technologies Overview	4
		1.2.1 Solar Converting Directly Technology	4
		1.2.1.1 Crystalline Silicon	5
		1.2.1.2 Thin Film	6
		1.2.1.3 Concentrated Photovoltaic System (CPV)	8
		1.2.2 Solar Converting Indirectly Technology	8
		1.2.2.1 Trough Systems	9
		1.2.2.2 Power Tower Systems	9
		1.2.2.3 Dish Engine Systems	10
	1.3	PV Generation System in Thailand	11
	1.4	Motivation	16
		1.4.1 Harmonic Distortion	17
		1.4.2 Power Fluctuations	19
		1.4.3 Voltage Regulation	20
	1.5	Literature Reviews	22

D	٨	6	21	E
Г	A	L.	J.	Ľ

		1.5.1 Literature Reviews on Optimal DG Sizing and Location	22
		1.5.2 Literature Reviews on Optimal PV-DG Sizing	25
	1.6	Objectives and Scope of Works	27
	1.7	Synopsis of Chapters	29
II.	Moo	leling of System Components	30
	2.1	Grid-Connected Photovoltaic Systems	30
	2.2	Solar Radiation and Ambient Temperature Modeling	31
		2.2.1 Statistical Model of Solar Radiation	32
		2.2.2 Statistical Model of Ambient Temperature	33
	2.3	Photovoltaic Modeling	35
		2.3.1 PV Model Implementation in Matlab/Simulink	41
		2.3.2 PV Model Validation	44
		2.3.3 Maximum Power Point Tracking (MPPT)	50
	2.4	PV Inverter Modeling	51
	2.5	Substation and Load Modeling	56
		2.5.1 Probabilistic Load Models	56
		2.5.2 Probabilistic Substation Voltage Model	58
III.	A V	oltage Stability Index for Radial Distribution Networks	59
	3.1	Introduction	59
	3.2	Voltage Stability Index Methodology	59
	3.3	Test Results of Voltage Stability Index Calculation	65
IV.	Rad	ial Distribution System Power Flow and	
	Har	monic Calculation	70
	4.1	Introduction	70
	4.2	The Modified Newton Method	70
		4.2.1 Loss Equations From System Data	75
		4.2.2 The Modified Newton Method Calculation Steps	76

	4.3	Test Results of Radial Distribution System Power Flow	
		Calculation	79
	4.4	Harmonic Modeling	80
		4.4.1 Harmonic Load Modeling	80
		4.4.2 Harmonic Capacitor Modeling	82
		4.4.3 Harmonic Feeder Modeling	82
		4.4.4 Background Harmonic Modeling	82
	4.5	Harmonic Calculation in a Distribution System	83
V.	Algo	orithm of Optimal PV-DG Sizing Technique and	
V.	Algo Nun	orithm of Optimal PV-DG Sizing Technique and nerical Results	89
V.	Algo Nun 5.1	Derithm of Optimal PV-DG Sizing Technique and Inerical Results Introduction.	89 89
v.	Algo Nun 5.1 5.2	orithm of Optimal PV-DG Sizing Technique and nerical Results Introduction Problem Formulation.	89 89 89
V.	Algo Nun 5.1 5.2 5.3	orithm of Optimal PV-DG Sizing Technique and nerical Results. Introduction. Problem Formulation. The Algorithm of Optimal PV-DG Sizing Technique.	89 89 89 90
V.	Algo Num 5.1 5.2 5.3 5.4	orithm of Optimal PV-DG Sizing Technique and nerical Results. Introduction. Problem Formulation. The Algorithm of Optimal PV-DG Sizing Technique. Numerical Results and Discussion.	89 89 89 90 92
v.	Algo Num 5.1 5.2 5.3 5.4	Orithm of Optimal PV-DG Sizing Technique and merical Results.Introduction.Problem Formulation.The Algorithm of Optimal PV-DG Sizing Technique.Numerical Results and Discussion.5.4.1Scenario-1:	89 89 89 90 92 92
v.	Algo Num 5.1 5.2 5.3 5.4	orithm of Optimal PV-DG Sizing Technique andnerical Results.Introduction.Problem Formulation.The Algorithm of Optimal PV-DG Sizing Technique.Numerical Results and Discussion.5.4.1 Scenario-1:5.4.2 Scenario-2:	89 89 90 92 92 105

VI.	Con	clusions and Future Works	120
	6.1	Conclusions	120
	6.2	Future Works	121

REFERENCES	122
APPENDICES	131
BIOGRAPHY	162

PAGE

List of Tables

TABLE		PAGE
1.1	DG's category according to generation technologies	1
1.2	Some of renewable potential and target plan of Thailand	14
1.3	Adder rate for SPPs and VSPP using renewable energy of Thailand.	14
1.4	Summary of the methodologies for optimal DG sizing and	
	location	25
2.1	The key specifications of the Sharp 80 Wp PV module at STC	42
2.2	Summary of PV model parameters values	44
2.3	Solar radiation levels and the corresponded ambient temperatures	45
2.4	Output comparison between the simulation results and the	
	measurements on different solar radiation	46
2.5	Typical harmonic current in percent of fundamental corresponding	
	to solar radiation	55
3.1	Line data and load data of the 15-bus radial distribution system	65
3.2	Bus stability indices for different load models of 15-bus test system.	66
3.3	C ritical bus stability i ndex value f or different t ypes of l oad a nd	
	substation voltage	67
4.1	Power flow solution obtained for 15-bus radial distribution system	80
4.2	Characteristic AC line harmonic currents in multi-pulse systems	84
4.3	Current distortion limits in IEC 61727 standard	88
5.1	Critical bus stability index values of the test system	93
5.2	Summarize the optimal size of PV-DGs installation	103
5.3	Summarize the total number of PV modules and inverter units for	
	optimal PV-DGs sizes solutions	104
5.4	Multiple optimal PV-DGs sizes for various PF operations with	
	CP-model	112
5.5	Existing DGs locations, capacity and its operating conditions	117

List of Figures

FIGRUR	E	PAGE
1.1	Annual installed and cumulative amount of large-scale	
	grid-connected PV power plants in the period from 1995 to 2008	2
1.2	Amount of large-scale grid-connected PV power plants put into	
	service annually in the period from 1995 to 2008	3
1.3	Large-scale PV power plants – annual and cumulative installed	
	power output capacity worldwide in the period from 1995 to 2008	4
1.4	Monocrystalline silicon PV panel	5
1.5	Multicrystalline silicon PV panel	6
1.6	Cadmium Telluride PV panel	6
1.7	Amorphous Silicon PV panel	7
1.8	CIGS PV panel	7
1.9	Concentrated photovoltaic system	8
1.10	Schematic diagram of parabolic trough system	9
1.11	Schematic diagram of power tower system	10
1.12	Schematic diagram of solar dish engine system	10
1.13	Proportion of domestic and import energy of Thailand in 2010	11
1.14	Energy source portion of power generation of Thailand in 2010	12
1.15	Yearly average solar radiation potential of the areas in Thailand	12
1.16	Percentage of area classified by average solar radiation levels	
	of Thailand	13
1.17	PV installation capacity status since 1983-2010 of Thailand	15
1.18	Installation capacity status of solar application system since	
	1983-2010 of Thailand	15
1.19	Case of DG unit interfering with voltage regulation on a	
	distribution feeder	20
2.1	Principal components in a single phase grid-connected PV systems	31
2.2	Simplified schematic diagram of grid-connected PV systems	31
2.3	Hourly variations of solar radiation in Chiang Mai during	
	6.00 am-6.00 pm on Jan-Dec 2007	32

PAGE

xii

2.4	Probability density of solar radiation corresponding to Figure 2.3	33
2.5	Hourly variations of ambient temperature in Chiang Mai during	55
2.0	6.00 am-6.00 pm on Jan-Dec 2007.	34
2.6	Cumulative probability of ambient temperature corresponding	
	to Figure 2.5	35
2.7	Simplified equivalent circuit of the PV cell model	35
2.8	PV module consists of N_{pm} parallel branches, each of N_{sm} cells	
	in series	39
2.9	PV array consists of M_p parallel branches, each with M_s modules	
	in series	40
2.10	PV module model implementation in Simulink	41
2.11	Current and power versus voltage characteristics of Sharp 80Wp	
	PV module provided by manufacturer ($T_c = 25^{\circ}C$)	42
2.12	I-V characteristics of Sharp 80Wp PV module by simulation	
	$(T_c = 25^{\circ}C)$	43
2.13	P-V characteristics of Sharp 80Wp PV module by simulation	
	$(T_c = 25^{\circ}C)$	43
2.14	PV module tester (I-V Checker/MP-140)	44
2.15	Data measured in time series of the solar radiation	45
2.16	Data measured in time series of the ambient temperature	45
2.17	I-V characteristic curve from I-V checker at high solar radiation	47
2.18	I-V characteristic curve from simulation at high solar radiation	47
2.19	I-V characteristic curve from I-V checker at medium solar radiation	48
2.20	I-V characteristic curve from simulation at medium solar radiation	48
2.21	I-V characteristic curve from I-V checker at low solar radiation	49
2.22	I-V characteristic curve from simulation at low solar radiation	49
2.23	Flow chart of classic P&O technique	51
2.24	System schematic diagram of the PV farm	52
2.25	Maximum inverter output current and %THDi at various solar	
	radiations	52

2.26	Harmonic current spectrum at PCC of the PV farm corresponding	
	to 200 W/m ² solar radiation	53
2.27	Harmonic current spectrum at PCC of the PV farm corresponding	
	to 600 W/m ² solar radiation	54
2.28	Harmonic current spectrum at PCC of the PV farm corresponding	
	to 1000 W/m ² solar radiation	54
2.29	Probability density function of a load point with a normal	
	distribution	57
2.30	Probability density function of substation voltage with a normal	
	distribution	58
3.1	Simple two-node system	60
3.2	Flow chart of voltage stability index calculation	64
3.3	Single-line diagram of the 15-bus radial distribution system	65
3.4	Variation of critical bus stability index value with system load for	
	different static load models	68
3.5	Variation of critical minimum bus voltage with system load for	
	different static load models	68
3.6	Variation of critical bus stability index value with system load for	
	different substation voltages	69
3.7	Variation of critical minimum bus voltage with system load for	
	different substation voltages	69
4.1	A simple radial distribution system with 10-nodes and 9-branches	73
4.2	Flow chart of radial distribution system power flow calculation	78
4.3	Single-line diagram of the 15-bus radial distribution system with	
	nodes to branches ordering	79
4.4	Harmonic load model of CIGRE and R//L	81
4.5	Equivalent circuit of harmonic feeder modeling	82
4.6	A simplified distribution system for fundamental frequency analysis	83
4.7	A simplified distribution system for harmonic frequency analysis	84
5.1	Flow chart of the optimal PV-DG sizing technique	91

PAGE

xiv

5.2	Single-line diagram of 51-bus test system	93
5.3	Average system losses as a function of average PV-DG power	
	output in Case-1	94
5.4	Cumulative probability of voltage at PCC with and without PV-DG	
	in Case-1	95
5.5	Cumulative probability of THDv at PCC with and without	
	background harmonics in Case-1	95
5.6	Cumulative probability of TDD at PCC of inverter	96
5.7	Cumulative probability of I_h (even orders 2 to 8) at PCC of inverter.	97
5.8	Cumulative probability of I_h (odd orders 3 to 9) at PCC of inverter	97
5.9	Cumulative probability of I_h (odd orders 11 to 15) at PCC of	
	inverter	98
5.10	Cumulative probability of I_h (odd orders 17 to 21) at PCC of	
	inverter	98
5.11	Cumulative probability of I_h (odd orders 23 to 33) at PCC of	
	$r \sim r \sim r$	
	inverter	99
5.12	inverter. Average system losses as a function of PV-DGs size at buses 38	99
5.12	inverter. Average system losses as a function of PV-DGs size at buses 38 and 19.	99 100
5.12 5.13	inverter. Average system losses as a function of PV-DGs size at buses 38 and 19 Cumulative probability of voltage at buses 38 and 19 with and	99 100
5.12 5.13	inverter. Average system losses as a function of PV-DGs size at buses 38 and 19 Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A.	99 100 100
5.125.135.14	inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without	99 100 100
5.125.135.14	 inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. 	99100100101
5.125.135.145.15	 inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. Comparison of THDv at PCC between Case-2A and Case-2B with 	99100100101
5.125.135.145.15	 inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. Comparison of THDv at PCC between Case-2A and Case-2B with 35% of background harmonics. 	99100100101102
 5.12 5.13 5.14 5.15 5.16 	 inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. Comparison of THDv at PCC between Case-2A and Case-2B with 35% of background harmonics. Average system losses as a function of average PV-DG power 	99100100101102
 5.12 5.13 5.14 5.15 5.16 	 inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. Comparison of THDv at PCC between Case-2A and Case-2B with 35% of background harmonics. Average system losses as a function of average PV-DG power output with different load models. 	 99 100 100 101 102 106
 5.12 5.13 5.14 5.15 5.16 5.17 	 inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. Comparison of THDv at PCC between Case-2A and Case-2B with 35% of background harmonics. Average system losses as a function of average PV-DG power output with different load models. Cumulative probability of voltage at bus-19 with different load 	 99 100 100 101 102 106
 5.12 5.13 5.14 5.15 5.16 5.17 	inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. Comparison of THDv at PCC between Case-2A and Case-2B with 35% of background harmonics. Average system losses as a function of average PV-DG power output with different load models. Cumulative probability of voltage at bus-19 with different load models (PF = 1.0).	 99 100 100 101 102 106 106
 5.12 5.13 5.14 5.15 5.16 5.17 5.18 	inverter. Average system losses as a function of PV-DGs size at buses 38 and 19. Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A. Cumulative probability of THDv at PCC with and without background harmonics in Case-2A. Comparison of THDv at PCC between Case-2A and Case-2B with 35% of background harmonics. Average system losses as a function of average PV-DG power output with different load models. Cumulative probability of voltage at bus-19 with different load models (PF = 1.0). Cumulative probability of THDv at bus-19 with different load	 99 100 100 101 102 106 106

11	•

5.19	Average system losses as a function of average PV-DG power	
	output with different leading power factor (CP-model)	108
5.20	Average system losses as a function of average PV-DG power	
	output with different lagging power factor (CP-model)	108
5.21	Cumulative probability of voltage at bus-19 with different PV-DG	
	sizes corresponding to Figure 5.19	109
5.22	Cumulative probability of THDv at bus-19 with different PV-DG	
	sizes corresponding to Figure 5.19	109
5.23	Average system losses as a function of PV-DGs capacity at buses	
	10 and 19 with constant power load model (PF = 1.0)	110
5.24	Average system losses as a function of PV-DGs capacity at buses	
	10 and 19 with constant current load model (PF = 1.0)	110
5.25	Average system losses as a function of PV-DGs capacity at buses	
	10 and 19 with constant impedance load model ($PF = 1.0$)	111
5.26	Cumulative probability of voltage at buses 10 and 19 corresponding	
	to the result in Figure 5.23	111
5.27	Cumulative probability of THDv at buses 10 and 19 corresponding	
	to the result in Figure 5.23	112
5.28	Single-line diagram of 33-bus test system	114
5.29	Average system losses as a function of average PV-DG power	
	output without consideration of existing DGs	115
5.30	Cumulative probability of voltage at bus-10 without consideration	
	of existing DGs	116
5.31	Cumulative probability of THDv at bus-10 using different inverter	
	models without consideration of existing DGs	117
5.32	Average system losses as a function of average PV-DG power	
	output with consideration of existing DGs	118
5.33	Cumulative probability of voltage at bus-10 with consideration of	
	existing DGs	118

PAGE

FIGRURE	PAGE
5.34 Cumulative probability of THDv at bus-10 using different inver	ter
models with consideration of existing DGs	119

Nomenclatures

BH **Background Harmonic** CdTe Cadmium Tellluride CIGS Copper, Indium, Gallium and Selenide CPV Concentrated Photovoltaic System CSP **Concentrating Solar Power** CV Constant Voltage CP Constant Power Load CI Constant Current Load CZ Constant Impedance Load DEDE Department of Alternative Energy Development and Efficiency DG **Distributed Generation** DLF Deterministic Load Flow DNO Distribution Network Operator FF Fill Factor GA Genetic Algorithm GFCI Ground Fault Circuit Interrupter IC Incremental Conductance Method IEA International Energy Agency LDC Line Drop Compensator LTC Load-Tap-Changing MPPT Maximum Power Point Tracking NOCT Normal Operating Cell Temperature PCU Power Conditioning Unit PCC Point of Common Coupling PDP Power Development Plan PEA **Provincial Electricity Authority** PF Power Factor PLF Probabilistic Load Flow PWM Pulse Width Modulation PV Photovoltaic

PV-DG	Photovoltaic	Distributed	Generator
	1 notovonale	Distributed	Ocherator

- P&O Perturb and Observe
- RE Renewable Energy
- SPP Small Power Producer
- STC Standard Test Condition
- TDD Total Demand Distortion
- THD Total Harmonic Distortion
- THDi Total Harmonic Distortion Current
- THDv Total Harmonic Distortion Voltage
- VSI Voltage Stability Index
- VSPP Very Small Power Producer

CHAPTER I INTRODUCTION

1.1 Overview of World's PV Generation

At this time, fossil fuel is the main energy supplier of the worldwide economy. However, using in long time of it as being a major cause of environmental problems and it is necessary to look for alternative resources in power generation. Besides, the increasing demand for energy in a distribution system can create problems such as voltage drop, poor reliability, low power quality, losses increasing and grid instability, etc. Distributed generations (DGs) are a one way to solve this problem and it has continuously be enintroduced and promoted around the world. Presently, the necessity of producing more energy combined with the interest in clean technologies using renewable energy such as solar, wind, biomass and biogas, etc.

According to the IEEE standard 1547-2003 [1], DG is by definition that which is of limited size roughly 10 MVA or less. Generally, DG produces electricity close to customer loads and c an run on f ossil fuels, renewable energy resources or waste he at. DG can be cat egorized into three types ac cording to their g eneration technologies as shown in Table1.1. These technologies are entering a period of rapid expansion a nd c ommercialization. In f act, s tudies ha ve pr edicted t hat D G m ay account for up to 20% of all new generations going online by the year 2010 [2].

Among the renewable energy sources, hydropower and wind energy have the largest utilization. In countries with hydropower potential, small hydro turbines are used at the distribution level to sustain the utility network in dispersed or remote locations. The wind power potential in many countries around the world has led to a large interest and fast development of wind turbine technology [3].

Туре	Application	Operating Mode
Synchronous	Geothermal, Ocean, Internal combustion engine, Combined cycle, Combustion turbine	Capacitive PF
Induction	Wind turbine	Inductive PF
Inverter-based	Photovoltaic, Micro turbine, Fuel cells	Unity PF

Table 1.1 DG's category according to generation technologies

Another renewable energy technology that gains acceptance as a way of maintaining and improving living standard without harming the environment is the photovoltaic (PV) technology. The number of PV installations is mainly depending on the government policy and utility companies that support programs on grid-connected PV system [4-5].

From the studied information in [6], the International Energy Agency (IEA) says that there are a mbitious plans for the global development of the solar energy industry and the encouraging progress seen in 2009, over 90% of the world's 192 countries have yet to undertake large-scale deployment projects. However, just eight countries a counted for 89% of the world's total i nstalled PV g enerating capacity of 15 GW in 2008. The IEA has set 2020 targets of 200 G W of global installed capacity for PV and 148 GW for concentrated solar power (CSP), with both figures targeted to soar by 2030. The IEA suggests one key to progress towards a strong policy regime. However, it should be considering such regimes consist of Feed-in T ariffs (FiT) alone or s omething wider-reaching. Furthermore, be yond government policy, the other key areas for action must be addressed.

From the annual review in 2008 [7], which presents basic statistical data about the majority of large-scale photovoltaic power plants (>=200 kWp) worldwide currently in operation. It shows that the past y ear w as characterized by s everal projects of MW-range PV pow er plants, and it was a lso the year with the highest market growth r elated t o large-scale PV s ystems e ver. N ot onl y in S pain, where progress is a bundantly clear, but in some ot her c ountries the c umulative installed power increased significantly. In the E uropean Union progress w as, a mong ot hers, observed in Italy, the Czech R epublic and France; the G erman m arket de creased slightly, but due to the market explosion in Spain the installed power from 2008 still reached the level of the previous year.

This r eport's da tabase i ncludes m ore t han 1,90 0 l arge-scale P V pow er plants (put into service in 2008 or earlier), each with peak power of 200 kWp or more as s hown in F igure 1.1. The a mount of l arge-scale P V pl ants s orted b y c ountry is shown in F igure 1.2. More than 500 l arge-scale P V pl ants are located in Germany, more than 370 are in USA and more than 750 are in Spain. The cumulative power of all these PV power plants is more than 3.6 G Wp and average plant power output is slightly more than 1.8 MWp as shown in Figure 1.3.



Figure 1.1 Annual installed and cumulative amount of large-scale grid-connected PV power plants in the period from 1995 to 2008



Figure 1.2 Amount of large-scale grid-connected PV power plants put into service annually in the period from 1995 to 2008 (sort by country)



Figure 1.3 Large-scale PV power plants – annual and cumulative installed power output capacity worldwide in the period from 1995 to 2008

In 2008, m ore than 1,000 large-scale PV plants were constructed and put into service worldwide. In Spain more than 590 large-scale PV plants were put into service, more than 120 for each Germany and the USA. Among other countries it is worth m entioning B elgium a nd C zech R epublic w here s everal l arge-scale r oofmounted (Belgium) a nd gr ound-mounted (Czech R epublic) P V p lants w ere constructed. Regarding large-scale PV power plants K orea took on a leading role in Asia. Several M W-range pow er pl ants w ere p ut i nto s ervice i n Korea l ast year. Europe is by far the most advanced region with more than 800 large-scale PV plants put into service in 2008. In Europe more than 1500 large-scale PV power plants are currently operating, followed by the USA with about 400 PV plants.

1.2 Solar PV Technologies Overview

There are two major solar PV technologies convert from sunlight directly and indirectly into electricity energy.

1.2.1 Solar Converting Directly Technology [8]

This solar PV technology converts solar energy into useful energy forms by directly absorbing solar photons, particles of light that act as individual units of energy, and either converting part of the energy to electricity (as in a PV cell) or storing part of the energy in a chemical reaction. In the world of this PV solar power technology, there are several types of semiconductor technologies currently in use for PV solar panels. However, two types based on t he thickness of the semiconductor have become the most widely adopted namely crystalline silicon and thin film [9]. Conventional crystalline silicon solar cell is relatively speaking very thick of 200-500 μ m where "thin" means something like 1-10 μ m.

1.2.1.1 Crystalline Silicon

Crystalline silicon panels are constructed by first putting a single slice of silicon through a series of processing steps, creating one solar cell. These cells are then assembled together in multiples to make a solar panel. Crystalline silicon, also called wafer silicon, is the oldest and the most widely used material in commercial solar panels. There are two main types of crystalline silicon panels as follows:

Monocrystalline Silicon

Monocrystalline (also called single crystal) panels use solar cells that are cut from a piece of silicon grown from a single, uniform crystal as shown in Figure 1.4. Monocrystalline panels are among the most efficient yet most expensive on the market. They require the highest purity silicon and the most involved manufacturing processes.



Figure 1.4 Monocrystalline silicon PV panel

• Multicrystalline Silicon

Multicrystalline (also called polycrystalline) panels use solar cells that are cut from multifaceted silicon crystals as shown in Figure 1.5. They are less uniform in appearance than monocrystalline cells, resembling pieces of shattered glass. These are the most common solar panels on the market, being less expensive than monocrystalline silicon. They are also less efficient, though the performance gap has begun to close in recent years.



Figure 1.5 Multicrystalline silicon PV panel

1.2.1.2 Thin Film

Thin film solar panels are made by placing thin layers of semiconductor material ont o v arious s urfaces, us ually on glass. The t erm *thin film* refers t o the amount of s emiconductor m aterial us ed. It is applied in a t hin film t o a s urface structure, such as a sheet of glass. Contrary to popular belief, most thin film panels are not flexible. Overall, thin film solar panels offer the lowest manufacturing costs and are becoming more prevalent in the industry. There are three main types of thin film used.

• Cadmium Telluride (CdTe)

CdTe is a semiconductor compound formed from cadmium and tellurium. CdTe solar panels are manufactured on glass as shown in Figure 1.6. They are the most common type of thin film solar panel on the market and the most cost-effective to manufacture. CdTe panels perform significantly better in high temperatures and in low-light conditions.



Figure 1.6 Cadmium Telluride PV panel

Amorphous Silicon

Amorphous silicon is the non-crystalline form of silicon and was the first thin film material to yield a commercial product, first used in consumer items such as calculators. It can be deposited in thin layers on to a variety of surfaces and of fers lower costs than traditional crystalline silicon, though it is less efficient at converting sunlight into electricity. Amorphous silicon PV panel is shown in Figure 1.7.



Figure 1.7 Amorphous Silicon PV panel

• Copper, Indium, Gallium and Selenide (CIGS)

CIGS is a c ompound s emiconductor t hat can be deposited ont o m any different m aterials. CIGS has only r ecently be come available for s mall commercial applications and is considered a developing PV technology. CIGS PV panel is shown in Figure 1.8.



Figure 1.8 CIGS PV panel

At present, C dTe s olar panels technology are chose come first for s olar application because of its s uperior ene rgy out put cha racteristic a cross r eal-world conditions, its low c ost volume production be nefits a nd its s uperior environmental performance. CdTe has lower temperature-related loss than crystalline silicon due to a lower temperature coefficient. It also provides superior energy output in low, indirect and diffuse light conditions, producing more electricity on cloudy days.

1.2.1.3 Concentrated Photovoltaic System (CPV) [10]

Concentrated PV system is a technology to increase the efficiency of the cells by concentrate sunlight on solar cells. The PV cells in a CPV system are built into concentrating collectors that use a lens or mirrors to focus the sunlight onto the cells as s hown in Figure 1.9. CPV systems must track the s un to ke ep the light focused on the PV cells. The primary advantages of CPV system are high efficiency, low system cost and low capital investment to facilitate rapid scale-up, it means that the systems can use less expensive semiconducting PV material to achieve a specified electrical out put. However, reliability is a n important te chnical challenge for thi s emerging technological approach. Because of the systems are generally require highly sophisticated tracking devices.



Figure 1.9 Concentrated photovoltaic system

1.2.2 Solar Converting Indirectly Technology [11]

This technology uses mirrors t o c oncentrate the s unlight e nergy and convert it into thermal energy to create steam to drive a turbine of the generator that generates el ectrical pow er. This t echnology i s well know n a s C oncentrating S olar Power (CSP) technology.

Generally, CSP pl ants g enerate el ectric pow er b y us ing m irrors t o concentrate the sun's energy and convert it into high temperature heat. That heat is then channeled through a conventional generator. The plants consist of two parts, one

that collects solar energy and converts it to heat and then another that converts the heat energy to electricity. C SP te chnology ut ilizes three a lternative te chnological approaches such as trough systems, power tower systems and di sh/engine systems. All C SP technological a pproaches r equire l arge areas for solar r adiation collection when used to produce electricity at commercial area.

1.2.2.1 Trough Systems

Trough s ystems us e l arge U -shaped (parabolic) r eflectors (focusing mirrors) t hat ha ve oi l f illed pi pes r unning a long t heir center or f ocal point. The mirrored reflectors are tilted toward the sun and focus sunlight on the pipes to heat the oil inside to as much as 750°F. The hot oil is then used to boil water, which makes steam to run conventional steam turbines and generators. The schematic diagram and parabolic trough system are shown in Figure 1.10.





Figure 1.10 Schematic diagram of parabolic trough system

1.2.2.2 Power Tower Systems

Power t ower s ystems al so called central r eceivers, use m any l arge, flat heliostats (mirrors) to track the sun and focus its rays onto a receiver. As shown in Figure 1.11, the r eceiver s its on t op of a tall tower in which c oncentrated s unlight heats a fluid as hot as 1,050°F. The hot fluid can be used immediately to make steam for el ectricity generation or s tored for l ater us e. That m eans el ectricity can be produced during periods of pe ak needed on c loudy days or even several hours a fter sunset.



Figure 1.11 Schematic diagram of power tower system

1.2.2.3 Dish Engine Systems

Dish engine systems use mirrored dishes to focus and concentrate sunlight onto a receiver. As shown in Figure 1.12, the receiver is mounted at the focal point of the dish. To capture the maximum amount of solar energy, the dish assembly tracks the s un across t he s ky. T he r eceiver i s i ntegrated into a hi gh efficiency external combustion engine. The engine has thin tubes containing hydrogen or helium gas that runs along t he out side of t he e ngine's f our piston c ylinders and op en i nto t he cylinders. As concentrated sunlight falls on the receiver, it heats the gas in the tubes to very hi gh temperatures, w hich causes ho t g as t o e xpand i nside t he c ylinders. T he expanding gas d rives t he pi stons. T he pi stons t urn a crankshaft, w hich dr ives a n electric generator. The receiver, engine and generator com prise a s ingle, integrated assembly mounted at the focus of the mirrored dish.





Figure 1.12 Schematic diagram of solar dish engine system

1.3 PV Generation System in Thailand

From Thailand's e nergy s ituation in 2010 r eport [12], i t s hows t hat Thailand imports variety forms of energy which worth many millions Baths as shown in Figure 1.13. Actually, Thailand's consumption of energy has been increasing every year in forms of gas, oil, coal and electricity. The energy crisis in the past few years has caused energy price rising up a nd affected e conomic development countrywide. Therefore, in order to lower an import of some energy, the Ministry of Energy h as come up with a policy to develop the renewable energy (RE) for a fifteen years period (2008-2022) by the Thailand P ower D evelopment P lan 2010 (PDP 2010) [13]. The objective of the plan is to increase the portfolio of renewable energy to 20.3% of the final energy consumption in 2022. At the end of the plan, the portion of renewable energy in pow er ge neration s hall be 2.4% or 5,608 M W from 1.4% at pr esent a s shown in Figure 1.14.



Figure 1.13 Proportion of domestic and import energy of Thailand in 2010



Figure 1.14 Energy source portion of power generation of Thailand in 2010

Furthermore, from the study of Silapakorn University and Department of Alternative Energy Development and Efficiency (DEDE) found that the average solar radiation potential of Thailand is about 18.2 MJ/m²-day or 5.06 kWh/m²-day, which is a very good potential. However, the solar radiation potential of the areas in Thailand (as shown in Figure 1.15) can be classified into three groups as follows [14]:

- <u>The high potential area</u>: ave rage s olar radiation a bout 19 -20 M J/m²-day o r 5.28-5.56 kWh/m²-day which covers 14.3% of the total area
- <u>The medium potential area</u>: a verage s olar r adiation a bout 18-19 M J/m²-day or 5-5.28 kWh/m²-day which covers 50.2% of the total area
- <u>The low potential area</u>: average s olar r adiation l ess t han 18 M J/m²-day o r 5 kWh/m²-day which covers 35.5% of the total area



Figure 1.15 Yearly average solar radiation potential of the areas in Thailand

From Figure 1.15, the highest average solar radiation zone is on the north eastern area and some a rea of the central of Thailand. The percentage of the area which classified by average solar radiation levels is shown in Figure 1.16, while the yearly average solar radiation of the whole country is 18 MJ/m²-day.



Figure 1.16 Percentage of area classified by average solar radiation levels of Thailand

Therefore, f rom thi s in formation, it s hows that the s olar pot ential in Thailand is very important. And it should not be overlooked because the solar energy resource in Thailand is enough for the future. Table 1.2 shows the renewable potential and t arget pl an of T hailand. Note from T able 1.2 that the solar energy potential to produce electricity energy is 50,000 M W, which is the highest compared with other energy resources. However, the existing electricity power produced by solar energy is just only 32 MW. This is because the capital investment cost of PV technology is still expensive com pared with ot her t echnologies, although PV t echnology has be en continually reduced at the present.

However, i n order t o e neourage t o pr oduce more electricity po wer b y solar ene rgy, the M inistry of E nergy of T hailand has pr omoted the ad der r ate of 8 Bth/kWh for small power producers (SPPs) or very small power producers (VSPPs). This rate is also using solar energy technology (called the concentrating solar power, CSP) t o pr oduce t he t hermal ene rgy and then to produce t he electricity power as shown in Table 1.3.

Electricity Power	Potential	Existing	2008-2011	2012-2016	2017-2022
Produced by	(MW)	(MW)	(MW)	(MW)	(MW)
Solar	50,000	32	55	95	500
Wind Energy	1,600	1	115	375	800
Hydro Power	700	56	165	281	324
Biomass	4,400	1,610	2,800	3,220	3,700
Biogas	190	46	60	90	120
Municipal Solid Waste	400	5	78	130	160
Hydrogen	-	-	0	0	3.5
Total	57,290	1,750	3,273	4,191	5,608

Table1.2 Some of renewable potential and target plan of Thailand

Table1.3 Adder rate for SPPs and VSPPs using renewable energy of Thailand

Type of power source of power plant	Old adder	New adder	Adder special plus	Adder special plus for Yala, Pattani, Naratiwas	Given adder duration
	(Bth/kWh)	(Bth/kWh)	(Bth/kWh)	(Bth/kWh)	(years)
1.Biomass					
-Installed capacity <= 1 MW	0.30	0.50	1.00	1.00	7
-Installed capacity > 1 MW	0.30	0.30	1.00	1.00	7
2.Biogas					
-Installed capacity <= 1 MW	0.30	0.50	1.00	1.00	7
-Installed capacity > 1 MW	0.30	0.30	1.00	1.00	7
3.Waste					
-AD and Land fill	2.50	2.50	1.00	1.00	7
-Thermal process	2.50	3.50	1.00	1.00	7
4.Wind energy					
-Installed capacity <= 50 kW	3.50	4.50	1.50	1.50	10
-Installed capacity > 50 kW	3.50	3.50	1.50	1.50	10
5.Micro water turbine					
-Installed capacity 50kW-<200kW	0.40	0.80	1.00	1.00	7
-Installed capacity < 50kW	0.80	1.50	1.00	1.00	7
6.Solar energy (PV,CSP, etc.)	8.00	8.00	1.50	1.50	10

From the PV capacity installation report of Thailand [15], the DEDE has PV pr ojects a round t he c ountry with c apacity 3,510.5 kW s ince 1983 t o 2010.

However, the PV generation system that was installed in Thailand can be separated into a stand-alone system (off-grid) and grid-connected system. The total capacity of the PV generation system of Thailand in 2010 is 49.21 MW as shown in Figure 1.17, which are 29.65 MW of stand-alone and 19.56 MW of grid-connected system. This installed capacity c an classify b y the solar a pplication system a s shown in F igure 1.18. It s hows t hat t he s olar e nergy i s t he m ost a pplied s ource t o p roduce t he electricity as 26.8 MW or 54.4% of total capacity.



Figure 1.17 PV installation capacity since 1983-2010 of Thailand



Solar application system

Figure 1.18 Installation capacity of solar application system since 1983-2010 of Thailand

1.4 Motivation

Generally, distribution systems are the radial type systems, which can be found in r ural or s uburban a reas, are normally de signed t o ope rate w ithout a ny generation sources connected to the grid. The interconnection of any generation sources on the distribution system can be variously impact on the power flow, voltage regulations at customer load and utility equipments. These impacts may be caused the system ope ration in either positively or ne gatively de pending on t he di stribution system ope rating ch aracteristics and the DG characteristics [2]. There are s ome positive impacts which are the system benefits as follows:

- Voltage support and improved power quality.
- Loss reduction in some cases [16].
- Peak shaving.
- Transmission and distribution capacity release.
- Deferment of new or upgraded T&D infrastructure.
- Improved utility system reliability.

Achieving the above benefits is in practice much more difficult than often realized. DG s ources m ust be r eliable, dispatchable of t he pr oper s ize, and at t he proper l ocations. T herefore, w ithout pr oper pl anning a nd a nalysis, D Gs c an ha ve negative impacts to the distribution system as follows:

- Large pe netration level of D G m ay de teriorate s ystem ope ration, system security and system dynamic performance.
- Conventional distribution systems need adequate protection in order to accommodate exchange of power.
- Signaling for dispatch of resources becomes extremely complicated.
- Connection and revenue contracts are difficult to establish.
- Safety concerns with energy generated from multiple sources.

Since DGs have a dvantages and disadvantages as mentioned above a lso many DGs will not be utility owned or will be variable energy sources such as solar and wind. There is no guarantee that these conditions will be satisfied and that the full system support benefits will be realized. Thus, DG interconnection policy should take into account how to maximize the desired benefits.

The PV generation is one type of inverter-based DGs that will be come more widespread at this time and the future due to anticipated cost reductions in PV technology and installation. PV systems are expected to play a p romising role as a clean power electricity s ource in meeting future electricity d emands. However, the integration of PV systems into power networks can cause both benefits and drawbacks depending on l ocations, operating modes and allowable sizes [17-19]. Since, the PV system is int erfaced to the di stribution s ystem t hrough a pul se width modulated (PWM) inverter, which is the main source of harmonic current. They may create the associated i njection of ha rmonic c urrents i nto t he di stribution s ystem l ead t o malfunction of harmonic-sensitive equipment if the injection of harmonic currents is allowed to reach excessive l evels [20]. Therefore, with the growing pe netration of inverter-based DGs especially phot ovoltaic distributed generation (PV-DG). T here should be m ore c oncerns about technical c onstrains and e xisting r egulation by the Distribution Network Operators (DNO) in order to assess the impact of PV system on the electric power quality and limit their integration.

In system planning and design aspect, there are some of the issue concerns of utilities when PV-DGs are interconnected to the grid as follows:

- Harmonic distortion
- Power fluctuation
- Voltage regulation
- 1.4.1 Harmonic distortion [21]

From a harmonic modeling standpoint, i nverter-based D G units c an b e viewed as a nonlinear load injecting harmonic current into the distribution feeder [22]. This could result in an unacceptable level of total harmonic distortion (THD).

THD can be applying to both current and voltage which are defined as the ratio of the rms value of harmonics and the rms value of the fundamental. THD of currents (THDi) varies from a few percent to more than 100%. THD of vol tage (THDv) is usually less than 5%. However, THDv below 5% is widely considered to

be acceptable, but values above 10% are unacceptable and will cause problems for sensitive equipment and loads.

It is widely r ecognized t hat t he pr esence of n onlinear c omponents o f power s ystems m anifests i n the appe arance of ha rmonics [23]. T he presence of harmonics in a power system is undesirable for a number of reasons, some of which are:

- Harmonics increase power losses in both utility and customer equipment.
- Sometimes harmonics may provoke malfunctioning of sensitive load or control equipment.
- Harmonics ha ving s ignificant m agnitudes can caus e a r eduction of lifetime of m otors, t ransformers, capacitor banks a nd s ome ot her equipment.
- A harmonic resonance problem with shunt capacitor can be occurred in some condition. And it produces large spikes of current and voltage on the system which cause the operation of protective devices or the failure of equipment.

Power electronic devices, as used for PV inverter, may cause a harmonic's problems. T he m agnitude a nd t he or der o f h armonic c urrents i njected b y dc/ac inverters de pend on t he t echnology of the inverter and m ode of i ts op eration. For example, a forced-commutated inverter with pulse-width-modulation operated in the linear range, will introduce only harmonics in the range of high frequencies, i.e., at and/or around multiples of the carrier frequency [24].

Many p apers s tudied power qua lity pr oblems i n ha rmonic a spect associated with a large num ber of distributed grid-connected PV s ystem on a distribution network [25-29]. The main objective of these papers is to analyze the observed phenomena of harmonic interference of large populations of these inverters. From the results of these papers, it indicates that the increasing of grid-connected PV systems c an c ause the harmonic di stortion pr oblem due t o hi gh pe netration of PV system.
1.4.2 Power fluctuations

At a large s cale, the uncertainty characteristic of power output of PV systems can affect the power quality and reliability. Since, the power generated from PV s ystems will be f luctuating a ll the time depending on climate conditions and geographic location. In the future, if a large number of PV systems are connected to the grids, the fluctuation of PV power output may cause the problems such as voltage fluctuation and large frequency deviation in electric power system operation [30-35]. Therefore, for the high penetration of PV systems interconnection to the grids without reduction of the r eliability and pow er quality of ut ility pow er s ystems, suitable measures should be applied to the PV systems side.

Battery s torage is the one device which c an be us ed t o r educe t he P V power out put fluctuation. There are s everal s tudies which investigations a imed at improving the performance of PV systems equipped with batteries [36-41]. However, using the energy storage device increases the capital cost, as it needs maintenance.

Therefore, in order to assess the power quality of a distribution system under nor mal op erating c onditions with high penetration of PV-DGs and without batteries, electrical characteristics of the current injection into the distribution network are ne cessary to be un derstood t horoughly. Generally, the power s ystem analysis under normal operation is based on a deterministic load flow calculation. However, the solar energy sources of PV-DG units are often uncontrollable and thus introduce uncertain factors i nto t he di stribution s ystem. As a result, t he PV ou tput power injection into the distribution system is fluctuating throughout the year [34].

As mentioned above, the combination of many uncertain factors may be make the difficulty and complicated to assess a distribution system performance under normal ope rating c onditions through a de terministic approach. Therefore, a probabilistic approach is necessary in order to assess the system power quality, which these uncertain factors are taking into account, e.g. power losses, voltage regulation, power fluctuation and harmonic distortion.

1.4.3 Voltage regulation

Generally, load-tap-changing (LTC) tr ansformers a t s ubstations, supplementary line regulators on feeders, and switched capacitors on feeders are used to regulate the voltage of a radial distribution system. Through the application of these devices, the voltages at a customer load point are kept within the acceptable limit. In practice, the v oltage r egulation is normally based on r adial pow er flows from the substation to the load points. Interconnection of DG introduces meshed power flows, which may be interfering with the system voltage regulation. The following regulation problems may occur [2]:

• Low voltage caused by DG just downstream of a regulator with line-drop compensation

If a DG i s connected to downstream of a vol tage r egulator or LTC transformer, which is using considerable line drop compensation as shown in Figure 1.19. Then the regulation controls will be unable to properly measure feeder demand. Fig.1.19 demonstrates that the improper voltage profiles may occur under with and without DG. In case of with DG, the voltage is reduced because the DG decreases the observed load at the line drop compensator (LDC) control. In this case, the regulator confuses into setting a voltage low er than is required to maintain adequate s ervice levels at the end of the feeder.



Fig. 1.19 Case of DG unit interfering with voltage regulation on a distribution feeder

• *High voltage due to DG*

DG may also result in high voltage at some electric customers. It can be seen that high penetration of DGs may cause reverse power flow to the substation. For this case, the vol tage can increase along the feeder. In some locations where the primary voltage is already high and the load is low, the rise in voltage can be enough to push the voltage over the acceptable limit [21].

Furthermore, the problem of high voltage may occur from the uncertainty of power fluctuation due to both PV-DG as mentioned above and load demand. If PV-DG does not operate i n c oordinate with t he l ocal l oad, t hey m ight i ncrease t he variations be tween the maximum a nd minimum vol tage le vel. As the mini mum voltage level could remain in a high load with a low PV-DG power situation, but the maximum voltage level could increase in low load with full PV-DG production.

• Interaction with regulating equipment

Some D Gs us e f eedback t o c ontrol vol tage, b ut th is w ay int eracts negatively to the utility regulation equipment. There may be undesirable cycling of regulation de vices a nd not iceable pow er qua lity i mpacts unde r s uch c onditions. In case of intermittent power output of PV-DG, this may change the system voltage or current flows enough to cause a regulator tap change or an operation of a switched capacitor [21].

As mentioned all above, it can be seen that there is some interesting issues concern with PV-DG included harmonic distortion, power fluctuation and difficulty of voltage regulation. The installation of PV-DG into a distribution system can cause both benefits and drawbacks depending on locations, operating modes and allowable sizes.

Therefore, this dissertation proposes the sizing of photovoltaic distributed generators in a distribution system with consideration of solar radiation and harmonic distortion. The objective is to maximize the power produced by PV-DG installation and minimize system losses, while the voltage profile as well as harmonic current, total harmonic voltage distortion (THDv) and total demand distortion (TDD) at the point of common coupling (PCC) are kept at an acceptable limit.

The pr obabilistic a pproach i s a pplied t o solve t he pr oblem because distribution utilities de liver electric energy to their customers within an appropriate range to maximize customer satisfaction and to reduce system losses. In the presence of PV-DG, it is difficult to regulate voltage since the PV system is a type of random generation. That is de pendent of t he environmental c onditions na mely the vol tage variation of PV-DG at the PCC as a function of solar radiation level [42-43]. So, it is impossible to a chieve a realistic evaluation of where and when an overvoltage can happen in a distribution system during an investigate a period of time by simply using a de terministic l oad f low (DLF) analysis, which i s ba sed on t he m ean values or expected values of customer loads and generations as inputs to solve a problem. For this reason, a probabilistic load flow (PLF) analysis is employed to ensure that the solution will be effective for the acceptable voltage deviation.

1.5 Literature Reviews

1.5.1 Literature Review on Optimal DG Sizing and Location

Generally, DG i s an electric pow er s ource c onnected directly t o a distribution ne twork or c ustomer site. Since DG c an be installed c lose to anyplace, which is required the advantages of DG in terms of efficiency and losses, investment, reliability and pow er q uality. However, interconnection of D G can create some technical problems such as difficulty of voltage regulation, over a thermal limit a nd exceeded harmonic di stortion, etc. The severity of t his pr oblem d epends on s ize, location, number and operating mode of DG. Therefore, several papers studied how to determine optimal size and location of DG, which is based on the synchronous type, in a di stribution ne twork w ith c onsideration of t echnical c onstraints a s m entioned above.

Authors in [44] and [45] proposed technique to minimize power losses in a distribution feeder by optimizing DG model in terms of size, location and operating point of D G. S ensitivity analysis f or po wer losses in terms of DG s ize and D G operating point was also performed in these papers. The proposed technique has been developed with c onsidering the load cha racteristic w ith constant i mpedance and constant c urrent models. Test r esults indicated that r eal pow er loss can be r educed with a DG of optimal size, located at an optimal place in the feeder. DGs in [46] are treated as mobile reactive compensators, which can be connected as a kind of reactive compensation equipment to improve voltage stability. A quantitative index is proposed to evaluate the voltage stability of load nodes to decide the opt imal D G location. The opt imal p enetration level of D G at opt imal location is the n calculated by P rimal-Dual Interior P oint M ethod. T he opt imal calculation realizes the highest voltage e ligible ratio and minimum pow er loss by adjusting the reactive power output of DG in a precondition of system security. The simulation results show the b est location and p enetration level of D G for voltage stability in the test system.

A multi-objective approach for optimal location and sizing to maximize the penetration of DG in a distribution network is proposed in [47]. The proposed optimization procedure is a nevolutionary multi-objective a lgorithm based on t he genetic algorithm (GA) with the ε -constrained t echnique. The goal of this methodology is to maximize the benefits of the presence of DGs and limit the network performance deterioration because DG is not connected at optimal locations.

Reference [48] pr oposed A nt C olony O ptimization (ACO) ba sed algorithm for DG sources allocation and sizing in distribution systems. The objective is de fined a s m inimization of D G i nvestment c ost a nd t otal ope ration c ost of t he system subject to a set of constraints such as capacity of feeder, voltage limit and total DG capacity limitation.

The optimal D G num ber a nd s izing f ormulated a s a NonLinear Programming (NLP) pr oblem has been proposed in [49]. The major objective is improving the voltage profiles of distribution networks using multiple DG s ources. The constraints of this paper are the nodal complex voltage and DG power factors. Further, the s tatic l oad m odels a s c onstant power, c onstant current a nd c onstant impedance are investigated.

In [50], the optimization of DG units and shunt capacitors for economic operation of di stribution s ystems was proposed. T he m inimization of ove rall investment cost with the integration of DG units and shunt capacitors is assessed with the c onsideration of s upply qua lity, r eliability a nd e nergy l oss. A n ew pl anning methodology by using Particle S warm Optimization (PSO) is proposed to minimize the overall cost for optimal sizing and location of DG units and shunt capacitors.

The effect of the variation of loads with voltage and frequency for optimal allocation of DG in terms of location and size is addressed in [51]. The objective is to minimize the real power loss and to maintain the voltage within specified limits at buses using genetic algorithms in a distribution network. However, an evaluation of frequency on analysis under certain assumptions regarding frequency has been made within the permissible range 0.98 pu to 1.02 pu.

The paper in [52] presents an approach by using the genetic algorithm for optimal a llocation of s ingle a nd multiple D Gs in terms of loc ation and size to minimize an average of locational charges for unit active power at buses. It means that the bus with maximum locational charge may be chosen as optimal location. The voltage at buses within specified limits is considered as the constraint. The static load models as constant power, constant current and constant impedance were considered.

The paper in [53] proposed the selection of optimal location and size of multiple DGs by using Kalman filter algorithm. The selection of optimal locations of multiple D Gs was considered from tot al pow er los s in a s teady-state ope ration. Thereafter, the optimal sizes are determined by using the Kalman filter algorithm. The objective is to minimize the total power loss of system. The merit of this algorithm is that it took the only few samples from a large-scale pow er s ystem with many data samples and therefore, it reduced the computational requirement dramatically during the optimization process.

The opt imal D G s izing pr oblem i n [54] i s t ackled b y t he S equential Quadratic Programming deterministic technique. The DG modeling is separated into two types, which a re t reated a s a P V bus and PQ bus. The objective function i s minimizing real power losses with consideration of the thermal network restrictions and t he bus c omplex vo ltage c onstraints. F urthermore, t he i mpact of bot h t he D G modeling a nd t he s tatic l oad r esponse t o vol tage upon t he opt imal D G s ize were studied.

A multi-objective placement and penetration level of DGs were examined in [55]. By concerning both technical and economical parameters of a power system using genetic algorithm combined with Multi-Attribute Decision Making (MADM) method. The technical parameter including total losses, bus es vol tage profile, l ine capacity limits and total reactive power flow were considered. The approach consists of GA for determining the best generation configurations of system by considering technical parameters that are included in the fitness function, and MADM techniques for ranking the selected plans regard to technical and economical attributes.

A combination of genetic algorithm and simulated annealing is presented in [56] f or opt imal D G a llocation i n di stribution ne tworks. The obj ective i s t o minimize di stribution po wer losses for a fixed number of D Gs and a specific t otal capacity of D Gs. The constraints a re bus es v oltage m agnitude and l ine c urrent capacity limits. Through this algorithm, a significant improvement in the optimization goal is achieved.

From [44-56], methods, objective function, parameter constraints and load models for optimal sizing and location of DG based on the synchronous type in a distribution system can be summarized as shown in Table 1.4. Among the methods for optimal DG sizing and location, the genetic algorithm is the most popular method.

Methodologies	Objective functions	Constraints	Load models
 Genetic algorithm (GA) Nonlinear programming Sequential quadratic programming Particle swarm optimization Ant colony optimization Combination of GA and Simulated annealing Combination of GA and MADM Kalman filter algorithm 	 min (real power loss) min (voltage variation) min (investment and operating cost) 	Bus voltagesThermal limitsDG capacity	 Constant power Constant current Constant impedance

Table 1.4 Summary of the methodologies for optimal DG sizing and location

1.5.2 Literature Review on Optimal PV-DG Sizing

The methodologies as shown in Table 1.4, how ever, are used for optimal synchronous-based DG s izing a nd l ocation, which all are based on a deterministic approach. There a re m any t echniques presented in bot h s tand-alone a nd g rid-connected systems through de terministic a nd p robabilistic a pproaches. In o rder to determine a PV-DG size and assess a distribution system performance under normal operating conditions.

In order to determine PV-DG size based on a probabilistic approach, an analysis of a stand-alone PV system on output of PV systems and load demands were studied in [57]. Reliability indices in terms of 1 oss of 1 oad hours (LOLH), e nergy losses and t otal c ost of investment are the main factors for evaluating the optimal operation of stand-alone PV scheme. Solar radiation and load demand in [57] were modeled as s tochastic va riables us ing hi storical da ta a nd experimentation, respectively.

In [58], authors presented several techniques to design a stand-alone PV system. Three probabilistic methods (i.e., fixed days of battery backup and recharge, loss of load probability (LOLP) and Markov Chain modeling) were proposed. The LOLP t echnique has been suggested as the most reliable be cause it provided a detailed view of the system performance to design the PV system among all proposed techniques.

In [59], a uthors proposed the sizing procedure for stand-alone and gridconnected PV systems. It was based on an analytical method and sized not only PV arrays but a lso ba tteries a nd i nverters. T he analytical s izing m ethod could be categorized into three types, which are based on loads and irradiation, available areas and LOLP. The objective was not to minimize system c ost m athematically, but to give an optimal design at the practical level on the basis of experimental knowledge.

In [60], a uthors pr oposed a pr obabilistic a pproach t o d esign a gridconnected P V s ystem in l ow vol tage f eeder. T he pr oposed m ethod de termined the optimum PV rating with a voltage constraint at the specified connecting point.

At present, inverter-based DG can perform functions other than supplying real power. The innovation and improvements in electronic devices allow using DG to improve power quality in the grid [61]. For this reason, specific planning tools for optimal placement and sizing of DG should be adopted to consider the multiple and contrasting goals that the DNO strives to achieve [62].

Furthermore, in case of PV-DG, the uncontrollable of solar energy sources can introduce uncertain factors into a distribution system such as voltage fluctuation as mentioned in section 1.4. Therefore, it is necessary to obtain an effective method for optimal PV-DG sizing and location. To cope with this, a probabilistic approach is an alternative for solving the problem.

However, most research works related to optimal PV-DG sizing normally do not consider the power quality constraints i.e., harmonic currents from PV-DG, total harmonic distortion due to PV-DG as well as background harmonic condition. Furthermore, the PV model in relevant papers is mostly using an approximate model which ac power output of PV system is assumed to be linearly proportional to solar radiation. And they do not mention about optimal location of PV-DG installation.

1.6 Objectives and Scope of Works

Objectives of this dissertation can be described as follows:

- To obtain an optimal size of single and multiple PV-DGs in a distribution system with consideration of solar radiation and harmonic distortion.
- To propose the steady state voltage stability index method for determining the proper locations of PV-DG as utility planning and design aspect.
- To compare PV-DG sizing between consideration with and without system background harmonics.
- To assess power quality impacts on a distribution system under nor mal operating conditions with installation of PV-DG units.
- To study an impact of static load models and power factor control on the optimal sizing of PV-DG.
- To study an effect of PV inverter models and existing DGs in a distribution system on the optimal PV-DG sizing.

Scope of the research can be summarized as follows:

- The proposed technique is based on a probabilistic approach, i.e., Monte Carlo simulation.
- The PV model in this research is based on Sharp 80Wp, NE-80E2E solar module, which is pol ycrystalline s ilicon material t ype. T he ma ximum power (80W) is defined a t 1000 W /m² solar r adiation and 25°C cell temperature under standard test conditions (STC).

- The PV model is integrated with the simplified perturb and observe (P&O) maximum pow er point tracking (MPPT) technique to automatically find the maximum pow er out put unde r a given s olar r adiation and a mbient temperature, which are based on real statistical data.
- The substation vol tage a nd l oad de mand are assumed t o be a random variable with a normal distribution function.
- The protection coordination is not considered in this research.
- The c oordination of vol tage r egulation e quipments with P V-DGs is not considered.
- PV-DGs are considered without batteries storage.
- A distribution system is assumed to be balanced.
- The ba ckground ha rmonics a re t aking i nto a ccount to determine the optimal size of PV-DG.
- Other types of DGs, such as synchronous and induction generation, are allowed with various locations, operating modes and sizes to incorporate with the optimal PV-DG sizing.
- In order to evaluate the harmonic distortion levels in a distribution system, the PV-DG is modeled as a harmonic current source based on statistical harmonic current spectra from measurements of a PV farm.
- The steady state voltage stability index (VSI) method is used to determine the proper locations for placing a PV-DG.
- The objective function of the proposed method is to:
 - Minimize average system real power loss

Subjected to the technical constraints as follows:

- Node voltage limited as $1 \pm 0.05 \ pu$

or 0.95 $pu \le V_i \le 1.05 pu$

- Harmonic currents at each order (up to 33rd) should not exceed the limits, which are based on IEC 61727 standard [63].
- Total ha rmonic vol tage di stortion (THD_v) at P CC should not exceed 5%, which is based on IEEE 519-1992 standard [64].

- Total de mand di stortion (TDD) at P CC s hould not e xceed 5%, which is based on IEC 61727 standard.
- An actual PEA 51-bus radial distribution system in Thailand and a 33-bus system are used for test cases of the proposed method.

1.7 Synopsis of Chapters

The material in this dissertation is organized as follows:

Chapter 1 pr esents world's P V ge neration ove rview, s olar P V technologies and PV generation in Thailand. The literature reviews of related research are also addressed. The motivation, objective, scope of work and research approach are also mentioned.

Chapter 2 presents models of grid-connected PV system components. The statistical mode ls of s olar r adiation and ambient t emperature a re pr oposed. The probabilistic load model, PV model, MPPT and PV inverter model are also addressed.

Chapter 3 presents the s teady s tate vol tage s tability inde x me thod to determine the proper PV-DG installation location.

Chapter 4 pr esents the modified Newton method to calculate power flow in a radial distribution system. The ha rmonic modeling and calculation are also presented.

Chapter 5 proposes the algorithm of PV-DG sizing technique and problem formulation. The numerical results of several study cases are also investigated.

Chapter 6 presents contributions of the dissertation, conclusion and future works.

CHAPTER II MODELING OF SYSTEM COMPONENTS

2.1 Grid-Connected Photovoltaic Systems

PV power s ystems have made a successful transition from small standalone sites to large grid-connected systems. The utility interconnection brings a new dimension to the renewable power e conomy by pooling the temporal excess or the shortfall in the renewable power with the connecting grid that generates base-load power using conventional fuels. Generally, the grid supplies power to the site loads when needed or absorbs the excess power from the site when available. A kilowatthour meter is used to measure the power delivered to the grid and another is used to measure the power drawn from the grid.

As shown in Figure 2.1 [9], the principal components in a single phase grid-connected, PV system side consists of the array itself with two leads from each string sent to a combiner box that includes blocking diodes, individual fuses for each string and usually a lightning surge arrestor. Two wires from the combiner box deliver dc power to a fused array disconnected switch, which allows the PVs to be completely isolated from the system. The inverter sends ac power through a breaker to the utility service panel. A dditional components not shown include the maximum power point tracker (MPPT), a ground-fault circuit interrupter (GFCI) that shuts the system down if any currents flow to ground and circuitry to disconnect the PV system from the grid if the utility loses power. The inverter, some of the fuses and switches, the MPPT, GFCI and other power management devices are usually integrated into a single power conditioning unit (PCU). Figure 2.2 shows the simplified schematic di agram of the grid-connected PV systems included PV generator, PCU and step-up transformer.



Figure 2.1 Principal components in a single phase grid-connected PV systems



Figure 2.2 Simplified schematic diagram of grid-connected PV systems

For large-scale grid-connected PV systems, a PV generator consists of a typical connection group of PV s trings, of which t he type of connection is not considered in this dissertation. The MPPT is integrated into the PCU which sends the maximum power through a step-up transformer to the grid. In power quality aspect, a large a mount of c onverted pow er f rom DC t o AC s ide c an c ause t he ha rmonic problem. T his depends on typical i nverter t opologies a nd op erating po int, w hich depends on power produced by PV generator under a solar radiation condition.

2.2 Solar Radiation and Ambient Temperature Modeling

To analyze PV systems, we need to know how much sunlight is available. A fairly straightforward set of equations can be used to predict where the sun is in the sky at a ny time of a day for an y location on earth as well as solar intensity (or insolation which incident solar radiation) on a clear day. To determine average daily solar radiation under the combination of clear and cloudy conditions that exist at any site long-term measurements of sunlight hitting a horizontal surface is required.

2.2.1 Statistical Model of Solar Radiation

In this dissertation, hourly solar radiation is modeled as a statistical model based on data measured from a study area. Hourly variations of solar radiation were collected in one year. Figure 2.3 s hows the example of hour ly v ariations of s olar radiation in Chiang Mai during 6.00 am to 6.00 pm on January to December 2007 (see Appendix A for complete data). The SI unit for s olar radiation is watt per s quare meter (W/m^2).



Figure 2.3 Hourly variations of solar radiation in Chiang Mai during 6.00 am-6.00 pm on Jan-Dec 2007

From t he m easurements, i n t his c ase, t he pr obability de nsity of s olar radiation may not be able to accurately model as a conventional distribution function e.g., W eibull, Gamma, Exponential, etc. H ence t he s olar r adiation i s modeled a s a stochastic variable from historical measurement data, as shown in Figure 2.4.



Figure 2.4 Probability density of solar radiation corresponding to Figure 2.3

2.2.2 Statistical Model of Ambient Temperature

Generally, the operating t emperature is not c onsidered i n P V s ystem analyzing. Because the temperature has a few effect on the PV system output power. Thus, in PV model, the power output of PV system is approximately proportional to solar radiation. However, the power output of PV system can be changed around 10% (constant solar radiation) when the ambient temperature is varied from the minimum to m aximum values, based on m easurement data, by simulation. Therefore, in this dissertation, the temperature effect is included in the PV model.

Similarly to solar radiation, hourly variations of ambient temperature are modeled as a statistical model based on data measured from the same area and time (see Appendix A for c omplete da ta). Figure 2.5 s hows t he hou rly variations of ambient temperature (degree) in Chiang Mai during 6.00 am to 6.00 pm on January to December 2007.



Figure 2.5 Hourly variations of ambient temperature in Chiang Mai during 6.00 am-6.00 pm on Jan-Dec 2007

From Figure 2.5, the ambient temperature can be modeled as a Weibull distribution function, as shown in Figure 2.6. The probability density function of a Weibull random variable x is [65]

$$f(x) = \frac{\beta}{\alpha^{\beta}} x^{\beta-1} \exp\left[-\left(\frac{x}{\alpha}\right)^{\beta}\right]$$
(2.1)

where $0 \le x < \infty$, $\beta > 0$ is the *shape parameter* and $\alpha > 0$ is the *scale parameter* of the distribution. The cumulative probability distribution function is

$$F(x) = 1 - \exp\left[-\left(\frac{x}{\alpha}\right)^{\beta}\right]$$
(2.2)

By the inverse transform method

give
$$U = F(x) = 1 - \exp\left[-\left(\frac{x}{\alpha}\right)^{\beta}\right]$$
 (2.3)

so
$$X = \alpha [-\ln(1-U)]^{1/\beta}$$
 (2.4)

where U is a uniformly distributed random variate between [0,1]. Since 1-U is also a uniformly distributed random variate between [0,1], Equation (2.4) becomes

$$X = \alpha (-\ln U)^{1/\beta} \tag{2.5}$$

where the values of α is 29.2763 and β is 6.5052 from the curve fitting.



Figure 2.6 Cumulative probability of ambient temperature corresponding to Figure 2.5

2.3 Photovoltaic Modeling

For this research work, a model of moderate complexity was used [66]. The PV model included temperature dependence of the photo-current (I_{ph}) and the saturation current of the diode (I_0) . A series resistance (R_s) was included, but not a shunt resistance. A single shunt diode was used with the diode quality factor set to achieve the best curve match. This model is a simplified version of the two diode model presented by Gow and Manning [67]. The simplified equivalent circuit of a PV cell is shown in Figure 2.7.



Figure 2.7 Simplified equivalent circuit of the PV cell model

Furthermore, PV model in this dissertation is integrated with maximum power point tracker as will be described in next section. Accuracy and complexity can be introduced to the model by adding in turn

- Temperature dependence of the diode saturation current I_0
- Temperature dependence of the photo current I_{ph}
- Series r esistance R_s , which gives a m ore accurate s hape be tween the maximum power point and the open circuit voltage
- Either allowing the diode quality factor to become a variable parameter, instead of being fixed at either 1 or 2

From t he c orresponding s tatistical m odel, r andom s olar r adiation (G_a) and ambient temperature (T_a) are generated by Monte C arlo simulation. These data are required to evaluate the I-V characteristic of PV model. The voltage output of the PV cell is represented by Equation (2.6), which is a function of the p hotocurrent mainly determined by load current and depended on the solar irradiation level and cell temperature during the operation.

$$V_{pv} = (AkT_c / q) \ln(I_{ph} + I_0 - I_{pv} / I_0) - I_{pv}R_s$$
(2.6)

Equation (2.6) can be rewritten as

$$I_{pv} = I_{ph} - I_0 \left(e^{\frac{q(V_{pv} + I_{pv}R_s)}{AkT_c}} - 1 \right)$$
(2.7)

The equations which describe the I-V characteristic of PV model are as follows:

$$I_{ph} = I_{ph(T_1)} \left[1 + K_0 \left(T_c - T_1 \right) \right]$$
(2.8)

$$I_{ph(T_1)} = G_a \left(I_{sc(stc)} / G_{a(stc)} \right)$$
(2.9)

$$K_0 = \left(I_{sc(T_2)} - I_{sc(T_1)} \right) / (T_2 - T_1)$$
(2.10)

$$I_{0} = I_{0(T_{1})} \left(\frac{T_{c}}{T_{1}}\right)^{3/A} \times e^{-\frac{qV_{s}}{Ak} \left(\frac{1}{T_{c}} - \frac{1}{T_{1}}\right)}$$
(2.11)

$$I_{0(T_1)} = I_{sc(T_1)} / (e^{\frac{qV_{oc(T_1)}}{AkT_1}} - 1)$$
(2.12)

where I_{ph} is temperature dependence of the photo-current (A)

 I_0 is temperature dependence of the diode saturation current (A)

 I_{pv} is cell output current (A)

 V_{pv} is cell output voltage (V)

 V_{oc} is cell open circuit voltage (V)

 V_q is band gap voltage (V)

 R_s is series resistance of cell (Ω)

- q is electron charge (coulomb)
- k is Boltzmann constant (J/K)
- *A* is diode quality factor
- T_c is cell operating temperature (°C)
- G_a is operating solar radiation (W/m²)

 $G_{a(stc)}$ is solar radiation at Standard Test Condition, STC, (1000 W/m²)

- T_1 is reference cell temperature at condition-1, normally refer at STC (25°C)
- T_2 is reference cell temperature at condition-2 (°C)
- $I_{sc(stc)}$ is short circuit current per cell at STC (A)
- $I_{sc(T_2)}$ is short circuit current per cell at T_2 (A)

The photo-current is directly proportional to solar radiation. When short circuit oc curs in the c ell, negligible current can flows in the di ode. Hence, the proportionality constant in Equation (2.9) is set so the rated short circuit current is delivered under rated solar radiation. The relationship between the photo-current and temperature is linear as shown in Equation (2.8) and is deduced by noting the change of photo-current with the change of temperature as follow by Equation (2.10).

When the c ell is not i lluminated, the r elationship between the c ell's terminal voltage and current is given by the Shockley equation. When the cell is open circuited and illuminated, the photo-current flows entirely in the diode. The I-V curve is offset from the origin by the photo generated current as follow by Equation (2.7). For t he value of t he s aturation current at 25 °C is calculated using the open-circuit voltage and short-circuit current at this temperature as follow by Equation (2.12). The relationship of di ode s aturation c urrent t o t emperature i s m ore c omplex, but fortunately it contains no variables requiring evaluation as follow by Equation (2.11).

The value of di ode quality factor is depending on the material type of photovoltaic cell, it takes a value between 1 and 2. Generally, the value of di ode quality factor A = 2 for crystalline silicon and A < 2 for amorphous silicon PV cell.

Therefore, the value of 2 i s used a st ypical i n nor mal ope ration of the m odel validation for the Sharp 80Wp PV module, which is a crystalline silicon material.

For the series resistance (R_s) of PV cell, it can be obtained using the only manufacturer supplied data for the PV modules at Standard Test Conditions (STC), such as open-circuit voltage, short-circuit current and maximum power. The equations which used to evaluate the value of the series resistance are given by the expression [68-69]:

$$R_{s} = \left[1 - \frac{FF}{FF_{0}}\right] \times \left[\frac{V_{oc(stc)}}{I_{sc(stc)}}\right]$$
(2.13)

$$FF = P_{\max}^{C} / \left[V_{oc(stc)} \times I_{sc(stc)} \right]$$
(2.14)

$$FF_0 = \left[V_{oc(nom)} - \ln(V_{oc(nom)} + 0.72)\right] / \left[V_{oc(nom)} + 1\right]$$
(2.15)

$$V_{oc(nom)} = V_{oc(stc)} / V_t$$
(2.16)

$$V_t = AkT_c/q \tag{2.17}$$

$$P_{\max}^{C} = P_{\max(stc)}^{M} / (N_{sm} \times N_{pm})$$
(2.18)

$$V_{oc(stc)} = V_{oc(stc)}^{M} / N_{sm}$$
(2.19)

$$I_{sc(stc)} = I_{sc(stc)}^{M} / N_{pm}$$
(2.20)

where $V_{oc(stc)}$ is cell open circuit voltage at STC (V)

- $V_{oc(stc)}^{M}$ is module open circuit voltage at STC (V)
 - V_t is cell thermal voltage (V)
- $I_{sc(stc)}^{M}$ is module short circuit current at STC (A)
 - P_{max}^{C} is cell maximum power (W)
- P_{\max}^{M} is module maximum power at STC (W)
 - FF is fill factor
 - N_{sm} is number of series cells in each cell parallel branches
 - N_{pm} is number of cell parallel branches in module

Normally, cells are grouped in to "modules", which are encapsulated with various materials to protect the c ells and the electrical c onnectors f rom the environment. T he manufacturers s upply P V c ells i n modules, c onsisting of N_{pm} parallel branches, each with N_{sm} solar cells in series, as shown in Figure 2.8 [69].



Figure 2.8 PV module consists of N_{pm} parallel branches, each of N_{sm} cells in series

In order to develop the model of PV module, the cell output voltage (V_{pv}) is then multiplied by the number of the cells connected in series N_{sm} to calculate the full module voltage (V^M) , they all have the same voltage in each parallel branches. In the s ame w ay, t he c ell out put c urrent (I_{pv}) is t hen multiplied by t he num ber of branches c onnected in parallel N_{pm} to obtain the full module c urrent (I^M) , they all carry the same current in series each branches.

The modules in a PV system are typically connected in "arrays". Figure 2.9 illustrates the case of an array with M_p parallel branches each with M_s modules in series [69]. The applied voltage at the array's terminal is denoted by V^A , while the total c urrent of the array is denoted by E quation (2.21). If it is a ssumed that the modules are identical and the ambient solar radiation is the same on all the modules, then the array's current is Equation (2.22).

$$I^{A} = \sum_{i=1}^{M_{p}} I_{i}$$
 (2.21)

$$I^{A} = M_{p} \times I^{M} \tag{2.22}$$



Figure 2.9 PV array consists of M_p parallel branches, each with M_s modules in series

In t his di ssertation, t he P V a rrays a re m odeled based on a c onnection group of Sharp 80Wp PV modules to obtain the rated size of PV-DG. The rated power of PV-DG is defined as peak power output, when solar radiation is 1000 W/m^2 and cell t emperature i s 25° C. H owever, a t ype of c onnection of P V m odules i s not considered in this work.

Since the working temperature of the PV cells (T_c) depends exclusively on t he s olar r adiation (G_a) and on t he ambient t emperature (T_a). To he lp t he researcher account for changes in cell performance with temperature, manufacturers often provide an indicator called the NOCT, which stands for Normal Operating Cell Temperature. The NOCT is cell temperature in a module when ambient is 20°C, solar radiation is 800 W /m² and wind speed is 1 m /s. T he value of NOCT for modules currently on the market varies from about 42 to 46 °C. However, in this dissertation, the value of NOCT is 42°C from testing. To account for other ambient conditions, the following expression may be used [68]:

$$T_{c} = T_{a} + G_{a} \left[\frac{NOCT - 20^{\circ}C}{800 \ W/m^{2}} \right]$$
 (2.23)

where T_c is cell temperature (°C)

 T_a is ambient temperature (°C)

 G_a is solar radiation (W/m²)

2.3.1 PV Model Implementation in Matlab/Simulink

This section shows how the mathematical model of PV module described in section 2.3 works by implemented in Matlab/Simulink. The mathematical model of PV module can be represented in Simulink implementation as shown in Figure 2.10. The input of PV module is an operating solar radiation G_a and ambient temperature T_a . The ma jor pa rt of structure is M atlab function bl ocks, w hich e ach c ontains necessary e quations l isted i n pr evious s ection, as follows from Equations (2.7) t o (2.20), to calculate the cell current I_{pv} . Then I-V and P-V curve can be established by changing the terminal output cell voltage V_{pv} .



Figure 2.10 PV module model implementation in Simulink

A P V m odule of S harp 80W p i s us ed t o examine on P V m odel implementation. The electrical characteristics of Sharp 80Wp under STC ($T_c = 25^{\circ}C$, $G_a = 1000 \text{ W/m}^2$) as given in Table 2.1, which the specification sheet can be found in Appendix B. The c urrent a nd pow er v ersus v oltage o f P V m odule p rovided b y manufacturer is shown in Figure 2.11.

Electrical Char	acteristic	
Open-circuit voltage	(V_{oc})	21.3 V
Short-circuit current	(<i>Isc</i>)	5.31 A
Voltage at max power	(V_m)	17.1 V
Current at max power	(I_m)	4.67 A
Maximum power	(P_m)	80 W

Table 2.1 The key specifications of the Sharp 80 Wp PV module at STC (1000 W/m² solar radiation, 25°C cell temperature)



Figure 2.11 Current and power versus voltage characteristics of Sharp 80Wp PV module provided by manufacturer ($T_c = 25^{\circ}C$)

In or der to compare s imulation results with the electrical characteristic provided b y m anufacturer. T he out put c urrent a nd pow er r elated to voltage are simulated for various s olar radiation levels as 600, 800 a nd 1000 W/m², while cell temperature i s f ixed a t 25°C. T he s imulation r esults of c urrent a nd pow er ve rsus voltage characteristics are shown in Figures 2.12 and 2.13 respectively.



Figure 2.12 I-V characteristics of Sharp 80Wp PV module by simulation ($T_c = 25^{\circ}C$)



Figure 2.13 P-V characteristics of Sharp 80Wp PV module by simulation ($T_c = 25^{\circ}C$)

Note from Figures 2. 12 and 2.1 3 that t he r esults s how good correspondence to the model. Table 2.2 summarizes the values of various parameters used in PV model.

Parameters	Values
Band gap voltage, V_g	1.12 V (for crystalline silicon)
Electron charge, q	$1.6e^{-19}$ Coulomb
Boltzmann constant , k	1.38 <i>e</i> ⁻²³ J/K
Diode quality factor, A	2 (for crystalline silicon)
Cell temperature at STC , T_1	25°C
Cell temperature at condition-2, T_2	75°C
Short circuit current at STC , $I_{sc(stc)}$	5.31 A (T ₁)
Short circuit current at T_2 , $I_{sc(T_2)}$	5.47 A (3% increase of $I_{sc(stc)}$)
Series resistance , R_s	0.0132 Ω/cell
Number of series cells, N_{sm}	36
Number of parallel branches , N_{pm}	1
NOCT	42°C

Table 2.2 Summary of PV model parameters values

2.3.2 PV Model Validation

This s ection s hows the r esults of Sharp 80 Wp PV m odule m odel validation using r eal data from me asurement of s olar r adiation. Pyranometer was directly connected to the portable PV module tester (I-V checker/MP-140), as shown in Figure 2.14. Ambient temperature was r ecorded by a thermocouple s ensor. The data m easured of solar r adiation and ambient temperature is shown in Figures 2.15 and 2.16 respectively. All of this is measured in one of a cloudy day on 21 October 2008.



Figure 2.14 PV module tester (I-V Checker/MP-140), EKO Instruments Co., Ltd.



Figure 2.15 Data measured in time series of the solar radiation



Figure 2.16 Data measured in time series of the ambient temperature

The m odel va lidation i s done b y c omparing between results which obtained by I-V checker and simulation results obtained by Matlab/Simulink. In order to validate the model, three different levels of solar radiation are considered. Table 2.3 shows t he s pecified values of hi gh, m edium a nd l ow solar r adiation levels and ambient temperatures corresponding to a certain solar radiation.

Level	Solar radiation (W/m ²)	Ambient temperature (°C)	Time (hr)
High	1025.3	36.04	11.50
Medium	600.6	30.91	09.20
Low	205.1	33.80	14.00

Table 2.3 Solar radiation levels and corresponded ambient temperatures

Various out puts such as I_{sc} , V_{oc} , P_m , etc., are compared between the simulation results and the measurements on three levels of solar radiation, as shown in Table 2.4. A good agreement of the results can be seen although it has a small error. From Table 2.4, it indicates that the error of the fill factor (FF) is less than 5% for all solar radiation levels. Furthermore, it shows that the error of all parameters is less than 5% except at low solar radiation. The I-V curve which obtained by I-V checker and simulation on high, medium and low solar radiation are shown in Figures 2.17 to 2.22 respectively.

Level	Ηiξ	zh solar radiati	noi	Mediu	ım solar radia	tion	Low) solar radiatic	uo
Output	Measured	Simulated	% Error	Measured	Simulated	% Error	Measured	Simulated	% Erroi
I_{sc} (A)	5.619	5.572	0.83	3.149	3.232	2.64	1.101	1.099	0.23
V_{oc} (V)	19.18	18.51	3.49	19.51	18.66	4.36	17.50	17.18	1.83
P _m (W)	69.66	67.38	3.27	42.55	40.52	4.77	13.50	12.58	6.81
$I_m \ (A)$	4.979	4.847	2.65	2.842	2.834	0.29	0.969	096.0	0.93
V_{m} (A)	13.99	13.90	0.64	14.97	14.30	4.48	13.93	13.10	5.96
FF	0.6465	0.6533	1.05	0.6925	0.6718	2.99	0.7011	0.666	4.96

in Equation (2.14) navig $v_{oc} as$ the product of Isc and m and nue 5 ratto FIU Jactor (FF) IS The IVULE.



Figure 2.17 I-V characteristic curve from I-V checker at high solar radiation



Figure 2.18 I-V characteristic curve from simulation at high solar radiation



Figure 2.19 I-V characteristic curve from I-V checker at medium solar radiation



Figure 2.20 I-V characteristic curve from simulation at medium solar radiation



Figure 2.21 I-V characteristic curve from I-V checker at low solar radiation



Figure 2.22 I-V characteristic curve from simulation at low solar radiation

2.3.3 Maximum Power Point Tracking (MPPT)

The maximum power point tracking of a PV array is usually an essential part of a PV system to draw peak power from the solar array in order to maximize the produced energy to DC-DC converter, as a part of PCU in Figure 2.2. Many MPPT methods have be en developed and implemented. The methods vary in complexity, sensors r equired, c onvergence s peed, c ost, r ange of e ffectiveness, i mplementation hardware, popularity, and in other respects. They range from the almost obvious (but not necessarily ineffective) to the most creative (not necessarily most effective).

In fact, so many methods have been developed like, Perturb and Observe Method (P&O), Incremental C onductance M ethod (IC), S liding M ode C ontrol Method that are widely used for MPPT system in PV, and other method like, Constant Voltage (CV), S hort-current P ulse M ethod, O pen V oltage M ethod, Fuzzy Logic Control, Neutral Network, and other unpopular method is also used in different field of MPPT [70-72].

Therefore, it has become difficult to adequately determine which method, newly proposed or existing is most appropriate for a given PV system. However, the simplified P&O MPPT technique is used in this dissertation.

The P&O algorithms operate by periodically perturbing (i.e. incrementing or decrementing) the array terminal voltage and comparing the PV output power with that of the previous perturbation cycle. If the PV array operating voltage changes and power increases (dP/dV > 0), the control system moves the PV array operating point in that direction; otherwise the operating point is moved in the opposite direction. In the next perturbation cycle the algorithm continues in the same way [70].

Generally, classic P&O method is widely us ed, the perturbations of the PV ope rating point have a fixed magnitude. In an analysis, the magnitude of perturbation is 0.37% of V_{oc} of PV array. The algorithm of the classic P&O is shown in Figure 2.23.



Figure 2.23 Flow chart of classic P&O technique

2.4 PV Inverter Modeling

Since, PV systems are interfaced to a distribution system through a PWMbased inverter, which is one of the main harmonic sources. These harmonic sources may c reate pr oblems t o vi cinity equipment de pending on t heir harmonic or der, amplitudes and system characteristic. Unfortunately, there is no s tandard harmonic waveform of inverter-based DG since the harmonic injection from inverter-based DG depends on the design of individual manufacture.

Therefore, the P V-DG is modeled as a harmonic current source at the point of common coupling (PCC). The harmonic current spectra of P V-DG were collected from m easurements of a 6 MWp PV f arm on M ay 2010 in N akhon Ratchasima province, north-eastern r egion of T hailand. The system s chematic diagram of the PV farm is shown in Figure 2.24.



Figure 2.24 System schematic diagram of the PV farm

Harmonic current measurements are based on 540 units of 11 kW Sunny Mini C entral S MC-11000TL g rid-connected i nverter. Maximum i nverter out put current and total harmonic current distortion (THDi) at various solar radiation levels are shown in Figure 2.25.



Figure 2.25 Maximum inverter output current and %THDi at various solar radiations

From Figure 2.25, it in dicates that the T HDi and output current of the inverter varied proportionally t ot hes olar radiation. F urthermore, from t he relationship of %THDi and solar radiation, nonlinearity of the inverter becomes large at low solar radiation. Under such conditions, the large amount of harmonics will be injected to a distribution system. Although, the magnitudes of harmonic currents are small at low s olar radiation, but the % THDi is la rge. This may de teriorate the electrical power quality of systems, if the large number of PV-DGs is interconnected to a distribution system. In this dissertation, only harmonic current magnitudes are considered for worse-case study.

Figures 2.26 to 2.28 show some of harmonic spectrum up to 33^{rd} order at PCC of the PV farm corresponding to solar radiation at 200, 600 and 1000 W/m², respectively. The typical harmonic current in percent of fundamental (50 Hz) can be seen in Table 2.5.



Figure 2.26 Harmonic current spectrum at PCC of the PV farm corresponding to 200 W/m^2 solar radiation



Figure 2.27 Harmonic current spectrum at PCC of the PV farm corresponding to 600 W/m^2 solar radiation



Figure 2.28 Harmonic current spectrum at PCC of the PV farm corresponding to 1000 W/m^2 solar radiation
Harmonic	Typical harmonic current in percent of fundamental (%)					
order	200 W/m ²	600 W/m ²	1000 W/m ²			
2	0.976	0.301	0.211			
3	6.829	1.506	1.057			
4	1.951	0.452	0.317			
5	12.195	4.066	2.748			
6	0.976	0.301	0.211			
7	2.439	0.753	0.317			
8	0.488	0.301	0.106			
9	0.976	0.301	0.211			
10	0.976	0.301	0.211			
11	2.439	0.602	0.423			
12	0.976	0.301	0.211			
13	0.976	0.301	0.211			
14	0.976	0.301	0.211			
15	0.976	0.301	0.211			
16	0.976	0.301	0.211			
17	0.976	0.151	0.211			
18	0.488	0.151	0.106			
19	0.976	0.151	0.106			
20	0.488	0.151	0.106			
21	0.976	0.151	0.106			
22	0.976	0.301	0.211			
23	0.976	0.301	0.211			
24	0.488	0.151	0.106			
25	0.976	0.151	0.106			
26	0.488	0.151	0.106			
27	0.488	0.151	0.106			
28	0.488	0.151	0.106			
29	0.488	0.151	0.106			
30	0.488	0.151	0.106			
31	0.976	0.151	0.106			
32	0.488	0.151	0.106			
33	0.976	0.151	0.106			

 Table 2.5 Typical harmonic current in percent of fundamental corresponding to solar radiation

In practical, interconnections of small PV-DGs may not result in violation of the power quality standard. However, with the existent of background harmonics and the increase of penetration level, PV-DGs may create harmonic currents which bring to excessive levels of tot al harmonic voltage di stortion (THDv) at P CC. Therefore, prior to interconnect PV-DGs, utilities should consider several technical constraints to avoid the power quality impacts from PV-DGs. Background harmonics modeling will be mentioned in Chapter 4 on harmonic calculations section.

2.5 Substation and Load Modeling

Since, in or der to f ind t he opt imal s ize of P V-DG w ithout c onsidering uncertainties of 1 oad a nd s ubstation vol tage may be que stionable. Therefore, i n probabilistic load flows process, load demand and substation voltage are assumed to be a random variable with a normal distribution.

2.5.1 Probabilistic Load Models

In t his w ork, a ll l oads a re c orrelated a nd f ollow the s ame probability density function of load demands (L_d) as given by:

$$f(L_d) = \frac{1}{\sigma\sqrt{2\pi}} \exp{-\frac{(L_d - \bar{L}_d)^2}{2\sigma^2}}$$
(2.24)

where \overline{L}_d is the mean value of load demand

 σ is the standard deviation, which set to 10% in this dissertation

Generally, the classical constant pow er load model is typically us ed in power flow studies of a distribution system. However, the actual load of a distribution system cannot j ust be modeled us ing constant pow er model. The use of constant current, constant impedance or a composite of all these load models are required to accurately represent the load. Therefore, three static load models are investigated to study the impact of load model on optimal PV-DG sizing. Probability density function of all static load models follows normal distribution in Equation (2.24). These types of loads are typically categorized as follows [73]:

• Constant Power Load Model (CP) :

The active and reactive powers do not vary with voltage magnitude changes.

• Constant Current Load Model (CI) :

The a ctive and r eactive pow ers are di rectly pr oportional t o t he v oltage magnitude.

• Constant Impedance Load Model (CZ) :

The act ive and reactive pow ers a re pr oportional t o t he s quare of v oltage magnitude.

The active and reactive power characteristics of three static load models are given by:

$$P = P_0 \left[a_p + b_p \left(\frac{|V|}{|V_0|} \right) + c_p \left(\frac{|V|}{|V_0|} \right)^2 \right]$$
(2.25)

$$Q = Q_0 \left[a_q + b_q \left(\frac{|V|}{|V_0|} \right) + c_q \left(\frac{|V|}{|V_0|} \right)^2 \right]$$
(2.26)

where P_0 and Q_0 are active and reactive powers consumed at a reference voltage V_0 , respectively. C onstant coefficients de pend on t het ype of l oad t hat i s be ing represented, e.g.,

for CP model $a_p = a_q = 1$, $b_p = b_q = c_p = c_q = 0$ for CI model $b_p = b_q = 1$, $a_p = a_q = c_p = c_q = 0$ for CZ model $c_p = c_q = 1$, $a_p = a_q = b_p = b_q = 0$

Figure 2.29 illustrates an example of act ive pow er probability d ensity function at a load point with a normal distribution, which \bar{L}_d is 145 kW, and σ is 10%.



Figure 2.29 Probability density function of a load point with a normal distribution

2.5.2 Probabilistic Substation Voltage Model

Similarly to load models, substation voltage (V_s) is a ssumed t o be a random variable with nor mal distribution. B ut the standard d eviation of substation voltage is set to 1.5% to cover in 0.95 pu to 1.05 pu range of mean value (\bar{V}_s) , which is a ssumed t o be 1.0 p u. T he pr obability d ensity f unction of s ubstation vol tage illustrates in Figure 2.30 and it can be expressed mathematically as follow:

$$f(V_{s}) = \frac{1}{\sigma\sqrt{2\pi}} \exp{-\frac{(V_{s} - \overline{V}_{s})^{2}}{2\sigma^{2}}}$$
(2.27)

where $\overline{V_s}$ is the mean value of substation voltage

 σ is the standard deviation, which set to 1.5% in this dissertation



Figure 2.30 Probability density function of substation voltage with a normal distribution

CHAPTER III A VOLTAGE STABILITY INDEX FOR RADIAL DISTRIBUTION NETWORKS

3.1 Introduction

In practice, utilities cannot assign the PV-DGs installation location to be connected to the feeder because it mainly depends on c ustomers who own the PV systems. However, for planning aspect, this chapter presents a voltage stability index (VSI) for identifying the most s ensitive bus to the vol tage collapse in a r adial distribution network for selecting the proper PV-DG located.

With an increased l oading a nd e xploitation of t he e xisting pow er structure, the probability of occurrence of voltage collapse is significantly greater than before and the identification of the nodes which are prone to the voltage fluctuations has attracted more attention for the transmission and as well as the distribution systems. The main causes of voltage instability are as follows:

- The load on transmission line is too high
- The voltage sources are too far from the load centers
- The voltage sources are too low
- There is insufficient load reactive compensation

For operating a power system in a safe and secure manner, all insecure operating states must be identified well in advance to facilitate corrective measures to overcome the threat of possible voltage collapse [74].

3.2 Voltage Stability Index Methodology [75]

For deriving the voltage stability index of radial distribution networks, we need to consider a simple two-node system as shown in Figure 3.1.



Figure 3.1 Simple two-node system

From Figure 3.1, the following equations can be written:

$$I_{l} = \frac{|V_{n1}| \angle \delta_{n1} - |V_{n2}| \angle \delta_{n2}}{R_{l} + jX_{l}}$$
(3.1)

 $I_{l} = \frac{P_{n2} - jQ_{n2}}{V_{n2}^{*}}$ (3.2)

where l is branch number

- n_1 is branch end node
- n_2 is receiving end node
- I_l is current of branch l
- V_{n1} is voltage of node n_1
- V_{n2} is voltage of node n_2
- P_{n_2} is total active power load fed through node n_2
- Q_{n2} is total reactive power load fed through node n_2

From Equations (3.1) and (3.2), we obtain:

$$\frac{|V_{n1}| \angle \delta_{n1} - |V_{n2}| \angle \delta_{n2}}{R_l + jX_l} = \frac{P_{n2} - jQ_{n2}}{V_{n2}^*}$$
(3.3)

therefore
$$|V_{n1}||V_{n2}| \angle (\delta_{n1} - \delta_{n2}) - |V_{n2}|^2 = (P_{n2} - jQ_{n2})(R_l + jX_l)$$
 (3.4)

and

$$\begin{aligned} |V_{n1}| |V_{n2}| \cos(\delta_{n1} - \delta_{n2}) - |V_{n2}|^2 + j |V_{n1}| |V_{n2}| \sin(\delta_{n1} - \delta_{n2}) \\ &= (P_{n2}R_l + Q_{n2}X_l) + j(P_{n2}X_l - Q_{n2}R_l) \end{aligned}$$
(3.5)

Separating real and imaginary parts of Equation (3.5), we obtain:

$$\left|V_{n1}\right|\left|V_{n2}\right|\cos(\delta_{n1} - \delta_{n2}) - \left|V_{n2}\right|^{2} = P_{n2}R_{l} + Q_{n2}X_{l}$$
(3.6)

therefore

$$|V_{n1}||V_{n2}|\cos(\delta_{n1} - \delta_{n2}) = |V_{n2}|^2 + P_{n2}R_1 + Q_{n2}X_1$$
(3.7)

and

$$|V_{n1}||V_{n2}|\sin(\delta_{n1} - \delta_{n2}) = P_{n2}X_1 - Q_{n2}R_1$$
(3.8)

Squaring and adding Equations (3.7) and (3.8), we obtain:

$$|V_{n1}|^{2}|V_{n2}|^{2} = \left(|V_{n2}|^{2} + P_{n2}R_{l} + Q_{n2}X_{l}\right)^{2} + \left(P_{n2}X_{l} - Q_{n2}R_{l}\right)^{2}$$
(3.9)

From algebraic formula:

$$(a+b+c)^{2} = a^{2} + b^{2} + c^{2} + 2(ab+bc+ac)$$
(3.10)

We can rearrange Equation (3.9) to

$$\left|V_{n2}\right|^{4} + 2\left(P_{n2}R_{l} + Q_{n2}X_{l} - 0.5\left|V_{n1}\right|^{2}\right)\left|V_{n2}\right|^{2} + \left(R_{l}^{2} + X_{l}^{2}\right)\left(P_{n2}^{2} + Q_{n2}^{2}\right) = 0$$
(3.11)

or $|V_{n2}|^4 - (|V_{n1}|^2 - 2P_{n2}R_l - 2Q_{n2}X_l)V_{n2}|^2 + (P_{n2}^2 + Q_{n2}^2)(R_l^2 + X_l^2) = 0$ (3.12)

Equation (3.12) has a straightforward solution and does not depend on the phase angle, which simplifies the problem formulation. In a distribution system, the voltage angle is not s o important be cause the variation of vol tage angle from the substation to the tail-end of a distribution feeder is only few degrees [76].

Let
$$b_l = \left(\left| V_{n1} \right|^2 - 2P_{n2}R_l - 2Q_{n2}X_l \right)$$
 (3.13)

$$c_{l} = \left(P_{n2}^{2} + Q_{n2}^{2}\right)\left(R_{l}^{2} + X_{l}^{2}\right)$$
(3.14)

From Equations (3.12) to (3.14), we get

$$\left|V_{n2}\right|^{4} - b_{l}\left|V_{n2}\right|^{2} + c_{l} = 0$$
(3.15)

From Equation (3.15), it is seen that the receiving end voltage $|V_{n2}|$ has four solutions follow to a given formulation:

$$|V_{n2}| = \pm \sqrt{\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}}$$
 (3.16)

and these solutions are:

1.
$$0.707\sqrt{b_l - \sqrt{b_l^2 - 4c_l}}$$

2. $-0.707\sqrt{b_l - \sqrt{b_l^2 - 4c_l}}$
3. $-0.707\sqrt{b_l + \sqrt{b_l^2 - 4c_l}}$
4. $0.707\sqrt{b_l + \sqrt{b_l^2 - 4c_l}}$

Now, for realistic data, when *P*, *Q*, *R*, *X* and *V* are expressed in per unit, b_l is always positive because the term $2\{P_{n2}R_l + Q_{n2}X_l\}$ is very small as compared to $|V_{n1}|^2$ and also the term $4c_l$ is very small as compared to b_l^2 . Therefore, $\sqrt{b_l^2 - 4c_l}$ is nearly equal to b_l and hence the first two solutions of $|V_{n2}|$ are nearly equal to zero and not feasible. The third solution is negative and so not feasible. The fourth solution of $|V_{n2}|$ is positive and feasible. Therefore, the solution of Equation (3.15) is unique.

That is
$$|V_{n2}| = 0.707 \sqrt{b_l + \sqrt{b_l^2 - 4c_l}}$$
 (3.17)

From Equation (3.17), it is seen that a feasible load flow solution of radial distribution networks will exist if:

$$b_l^2 - 4c_l \ge 0 \tag{3.18}$$

Thus, from Equations (3.13), (3.14) and (3.18), we get

$$\left(\left| V_{n1} \right|^2 - 2P_{n2}R_l - 2Q_{n2}X_l \right)^2 - 4\left(P_{n2}^2 + Q_{n2}^2 \right) \left(R_l^2 + X_l^2 \right) \ge 0$$
(3.19)

After simplification we get

$$|V_{n1}|^{4} - 4(P_{n2}X_{l} - Q_{n2}R_{l})^{2} - 4(P_{n2}R_{l} + Q_{n2}X_{l})|V_{n1}|^{2} \ge 0$$
(3.20)

Let

$$VSI(n_2) = |V_{n1}|^4 - 4(P_{n2}X_1 - Q_{n2}R_1)^2 - 4(P_{n2}R_1 + Q_{n2}X_1)|V_{n1}|^2$$
(3.21)

where $VSI(n_2)$ is voltage stability index of node n_2 , for stable operation of the radial distribution networks, $VSI(n_2) \ge 0$ for $n_2 = 2,3,...,N_b$

By using this voltage stability index, one can measure the level of stability of r adial di stribution ne tworks and t hereby a ppropriate a ction m ay be t aken if t he index indicates a poor level of stability.

Actually, P_{n2} and Q_{n2} are sum of the active and reactive power loads of all the nodes beyond node n_2 plus the active and reactive power load of node n_2 itself plus the sum of the active and reactive power losses of all the branches beyond node n_2 .

After load flow calculation, when the load was increased gradually, the voltages of all nodes are known, the branch currents are known. Therefore, P_{n2} and Q_{n2} for $n_2 = 2,3,...,N_b$ can easily be calculated using Equation (3.2) and hence one can easily calculate the voltage stability index of each node. The node at which the value of the stability index is minimum, is more sensitive to the voltage collapse and more candidate to install PV-DG.

In this dissertation, load flow a nalysis was a chieved by using the load flow algorithm given in Chapter 4 in which each nodes power is multiplied by a load factor as [74]:

$$S = \lambda S_b \tag{3.22}$$

where λ is load factor and S_b is base load

The c ritical bus id entified by e valuating bus v oltage m agnitudes jus t before the load flow diverges. Divergence is assumed when the iteration number of the load flow a lgorithm r eaches t o 200. T he a lgorithm of vol tage s tability i ndex calculation can be summarized as seen the flow chart in Figure 3.2.



Figure 3.2 Flow chart of voltage stability index calculation

3.3 Test Results of Voltage Stability Index Calculation

To demonstrate the methodology of the voltage stability index (VSI), this section presents a 15-bus radial distribution system from [77] for VSI calculation. The single-line diagram of the 15-bus test system is shown in Figure 3.3. Line and load data of this system are given in Table 3.1.



Figure 3.3 Single-line diagram of the 15-bus radial distribution system

Duanah	Line imped	ance (ohm)	Load deman	d (kW/kVar)
Dranch	R	X	P_L	Q_L
1 – 2	1.35309	1.32349	44.10	44.99
2 - 3	1.17024	1.14464	70.00	71.41
3 - 4	0.84111	0.82271	140.00	142.82
4 - 5	1.52348	1.02760	44.10	44.99
4 - 6	1.19702	0.80740	140.00	142.82
4 - 7	2.23081	1.50470	70.00	71.41
3 – 8	1.79553	1.21110	140.00	142.82
8 – 9	2.44845	1.65150	70.00	71.41
9-10	2.01317	1.35790	44.10	44.99
2 - 11	2.01317	1.35790	70.00	71.41
11-12	1.68671	1.13770	44.10	44.99
2 - 13	2.55727	1.72490	140.00	142.82
13 - 14	1.08820	0.73400	140.00	142.82
13 – 15	1.25143	0.84410	70.00	71.41

Table 3.1 Line data and load data of the 15-bus radial distribution system

Total base load = 1.226 MW, 1.251 MVar

For this simulation, a different magnitude substation voltages $(|V_s|)$ and different static load models of constant power (CP), constant current (CI) and constant impedance (CZ) a re c onsidered. T able 3.2 s hows bus s tability indi ces and i ts minimum bus voltage for different load models and substation voltage 1.0 pu of the 15-bus test system.

D N.	CP model		CI	model	CZ model	
BUS NO.	VSI	V _{min} pu	VSI	V _{min} pu	VSI	V _{min} pu
2	0.2042	0.7259	0.3259	0.7854	0.4841	0.8479
3	0.0936	0.5737	0.1991	0.6768	0.3505	0.7731
4	0.0679	0.5140	0.1600	0.6339	0.3048	0.7436
5	0.0644	0.5038	0.1541	0.6266	0.2975	0.7385
6	0.0563	0.4879	0.1434	0.6156	0.2855	0.7311
7	0.0572	0.4897	0.1446	0.6169	0.2868	0.7319
8	0.0600	0.5004	0.1523	0.6268	0.2971	0.7391
9	0.0411	0.4528	0.1257	0.5963	0.2663	0.7187
10	0.0365	0.4374	0.1183	0.5866	0.2572	0.7122
11	0.2407	0.7009	0.3334	0.7603	0.4707	0.8285
12	0.2302	0.6927	0.3200	0.7522	0.4572	0.8223
13	0.1310	0.6126	0.2139	0.6873	0.3590	0.7774
14	0.1234	0.5930	0.2021	0.6707	0.3431	0.7655
15	0.1308	0.6015	0.2109	0.6778	0.3523	0.7705

Table 3.2 Bus stability indices for different load models of the 15-bus test system

	0.1200	0.0010	0.2109	0.0770	0.2022	0.7700
	г т 11	2 2 1 4	1 1 1	1	1 11	1 (1 (1
	From I able	3.2, when t	he load 1s 11	icreased gra	adually, it fo	ounds that the
	1 0 1				10.0 11	
minimum v	value of volta	ge stability	index is occ	curring at bi	is-10 for all	types of load

 $(|V_s| = 1.0 \ pu)$

models. It is also observed that bus 10 has the minimum voltage.

Table 3.3 shows critical bus index value and its bus voltage of the 15-bus test s ystem for di fferent s ubstation vol tage a nd different static loa d mode ls. The system loads are increased from zero to the critical loading point by multiplying each node active and reactive power by a load factor lambda (λ) as 0.01 t imes of its previous value in each step for all loads. Note from Table 3.3 that, for all loading conditions, minimum stability index value is observed of the bus 10.

T	Substation	Critical loading condition			
Loaa model	voltage (pu)	$VSI_{min} = VSI_{10}$	$ V_{min} $ pu		
	0.95	0.0296	0.4152		
СР	1.00	0.0365	0.4374		
_	1.05	0.0433	0.4566		
	0.95	0.1151	0.5825		
CI	1.00	0.1183	0.5866		
_	1.05	0.1730	0.6450		
	0.95	0.2104	0.6773		
CZ	1.00	0.2582	0.7129		
	1.05	0.3139	0.7485		

 Table 3.3 Critical bus stability index value for different types of load and substation voltage

Figures 3.4 and 3.5 show the variations of the critical bus index value at bus-10 and its bus voltages with the increase of the system loads for different load models, substation voltage 1.0 pu. Points A, B and C indicate the critical loading point beyond which a small increment of load causes the voltage collapse.

From Figures 3. 4 and 3.5, it is seen that the critical bus inde x value decrease with the increase of the system load, and it closes to zero when system's total power closes to the critical loading point. From the each loading conditions, it is observed that the critical bus indices are always at the minimum. Moreover, it is also observed that the different load models cause only different stability index value and bus voltage magnitudes, it does not affect the critical bus number of the test system.



Figure 3.4 Variation of critical bus stability index value with system load for different static load models



Figure 3.5 Variation of critical minimum bus voltage with system load for different static load models

Similarly, Figures 3.6 and 3.7 show the variations of the critical bus index value at bus-10 and its bus voltages with the increase of the system loads for different substation voltage, constant power load model. Points A, B and C indicate the critical loading point beyond which a small increment of load causes the voltage collapse.



Figure 3.6 Variation of critical bus stability index value with system load for different substation voltages



Figure 3.7 Variation of critical minimum bus voltage with system load for different substation voltages

From simulation results, in this case, it can summarize that the stability index a nd c onsequently, the vol tage a re m inimum f or c onstant pow er l oad a nd maximum f or c onstant i mpedance l oad a nd t hat f or c onstant c urrent l oad i s i n between these two, as seen in Table 3.3.

Finally, if we have a planning to install PV-DG in this system, the most candidate bus is bus-10 based on the voltage stability index.

CHAPTER IV

RADIAL DISTRIBUTION SYSTEM POWER FLOW AND HARMONIC CALCULATION

4.1 Introduction

In pr actical, c onfigurations of a distribution s ystem have been high r/x ratio (ill-condition) which deteriorates the diagonal dominance of the Jacobian matrix. Therefore, the conventional Newton's power flow method may be divergence in some case. Therefore, this chapter presents a modified Newton method from [78] to solve the pr oblem. Furthermore, ha rmonic m odeling a nd ha rmonic c alculation i n a distribution system are mentioned.

A modified Newton method is utilized to solve the power flow for a radial distribution system without reducing the problem size, yet still capable of achieving robust convergence and high efficiency. This method is derived a Newton formulation where the Jacobian matrix is in UDU^T form, where U is a constant upper triangular matrix de pending s olely on s ystem t opology and D is a bl ock di agonal m atrix resulting from the radial structure and special properties of the distribution system.

With this formulation, the conventional Newton algorithm of forming the Jacobian matrix, LU factorization and forward back substitution can be replaced by back/forward sweeps on radial feeders with equivalent impedances.

4.2 The Modified Newton Method

In conventional N ewton method [79], the equation to solve power flow problem for $\Delta\theta$ and ΔV is expressed in Equation (4.1).

$$\begin{bmatrix} H & N \\ J & L \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta V / V \end{bmatrix} = \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix}$$
(4.1)

where

$$H_{ij} = -V_i V_j \Big(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \Big) \qquad j \neq i$$
(4.2)

$$H_{ii} = V_i \sum_{j \in i, j \neq i} V_j \Big(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \Big)$$
(4.3)

$$N_{ij} = -V_i V_j \Big(G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \Big) \qquad j \neq i$$
(4.4)

$$N_{ii} = -V_i \sum_{j \in i, j \neq i} V_j \Big(G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \Big) - 2V_i^2 G_{ii}$$
(4.5)

$$J_{ij} = V_i V_j \Big(G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \Big) \qquad j \neq i$$
(4.6)

$$J_{ii} = -V_i \sum_{j \in i, j \neq i} V_j \Big(G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \Big)$$
(4.7)

$$L_{ij} = -V_i V_j \Big(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \Big) \qquad j \neq i$$
(4.8)

$$L_{ii} = -V_i \sum_{j \in i, j \neq i} V_j \Big(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \Big) + 2V_i^2 B_{ii}$$
(4.9)

Term $G_{ij} + jB_{ij}$ is the entry of nodal admittance matrix. Under assumption the voltage difference between two adjacent nodes is small $(\sin \theta_{ij} \approx 0)$ as well as term $G_{ii} + jB_{ii} = -\sum_{j \in i, j \neq i} (G_{ij} + jB_{ij})$. Thus the Jacobian matrix can be approximated as:

$$H_{ij} \approx V_i V_j B_{ij} \cos \theta_{ij} \qquad j \neq i$$
(4.10)

$$H_{ii} \approx -V_i \sum_{j \in i, j \neq i} V_j B_{ij} \cos \theta_{ij}$$
(4.11)

$$N_{ij} \approx -V_i V_j G_{ij} \cos \theta_{ij} \qquad j \neq i$$
(4.12)

$$N_{ii} \approx V_i \sum_{j \in i, j \neq i} V_j G_{ij} \cos \theta_{ij}$$
(4.13)

$$J_{ij} \approx V_i V_j G_{ij} \cos \theta_{ij} \qquad j \neq i$$
(4.14)

$$J_{ii} \approx -V_i \sum_{j \in i, j \neq i} V_j G_{ij} \cos \theta_{ij}$$
(4.15)

$$L_{ij} \approx V_i V_j B_{ij} \cos \theta_{ij} \qquad j \neq i$$
(4.16)

$$L_{ii} \approx -V_i \sum_{j \in i, j \neq i} V_j B_{ij} \cos \theta_{ij}$$
(4.17)

Equations (4.10) to (4.17) show that matrices H, N, J and L all have the same properties (symmetry, sparsity pattern) as the Nodal Admittance Matrix, hence they can be formed as:

$$H = L = A_{n-1} D_B A_{n-1}^T \tag{4.18}$$

$$J = -N = A_{n-1}D_G A_{n-1}^T (4.19)$$

where D_B and D_G are diagonal matrices with diagonal entries to be:

$$D_B = V_i V_j B_{ij} \cos\theta_{ij} \tag{4.20}$$

$$D_G = V_i V_j G_{ij} \cos \theta_{ij} \tag{4.21}$$

and A_{n-1} is node to branch incidence matrix, defined as:

$$A_{ij} = \begin{cases} 1, & \text{if brance } j \text{ is directed away from node } i \\ -1, & \text{if brance } j \text{ is directed towards node } i \\ 0, & \text{if brance } j \text{ is not incident to node } i \end{cases}$$

For a radial distribution system with n nodes and without shunt branches, the num ber of branches is n -1. Also by know ing the nodal vol tage at one node, assuming it is the first node for convenience. Hence, there are remaining n-1 unknown nodal voltages and we obtain matrix A_{n-1} is a square matrix, which its dimension is $(n-1) \times (n-1)$.

Furthermore, if nodes and branches are ordered appropriately, A_{n-1} is an upper triangular matrix with all diagonal entries to be 1 and all non-zero off-diagonal entries to be -1. One way to achieve such an A_{n-1} is ordering branches by layers away from t he r oot node (source node or r efference node) as s een in Figure 4.1. T he direction of each branch is towards the r oot node. The node or dering is proceeded simultaneously with the branch ordering. Note from Figure 4.1 t hat the branch from side node number is the same as the branch number. And the node to branch incident matrix of it is given in Equation (4.22).



Figure 4.1 A simple radial distribution system with 10-nodes and 9-branches

$$A_{n-1} = \begin{bmatrix} 1 & 0 & -1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & -1 & -1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0$$

From Equations (4.18) and (4.19), thus Equation (4.1) can be rewritten as:

$$\begin{bmatrix} A_{n-1} \\ A_{n-1} \end{bmatrix} \begin{bmatrix} D_B & -D_G \\ D_G & D_B \end{bmatrix} \begin{bmatrix} A_{n-1}^T \\ A_{n-1}^T \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta V/V \end{bmatrix} = \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix}$$
(4.23)

 ΔP and ΔQ are vector of r eal and reactive node power m ismatches respectively, which can be expressed as:

$$\Delta P_{i} = P_{i(scheduled)} - P_{i(cal)} \qquad i \neq reference \ node \qquad (4.24)$$
$$= [P_{i(gen)} - P_{i(load)}] - P_{i(cal)}$$
$$\Delta Q_{i} = Q_{i(scheduled)} - Q_{i(cal)} \qquad i \neq reference \ node \qquad (4.25)$$
$$= [Q_{i(gen)} - Q_{i(load)}] - Q_{i(cal)}$$

where

 ΔP_i and ΔQ_i are vector of real and reactive node power mismatches at node *i* $P_{i(gen)}$ and $Q_{i(gen)}$ are real and reactive node power generation at node *i* $P_{i(load)}$ and $Q_{i(load)}$ are real and reactive node power load at node *i* $P_{i(cal)}$ and $Q_{i(cal)}$ are net real and reactive node power load at node *i*

The expression for the net real and reactive node power, $P_{i(cal)}$ and $Q_{i(cal)}$ are

$$P_{i(cal)} = V_{i} \sum_{j=1}^{n} V_{j} \Big[G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \Big]$$
(4.26)

$$Q_{i(cal)} = V_{i} \sum_{j=1}^{n} V_{j} \Big[G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \Big]$$
(4.27)

where

$$V_i$$
, V_j are voltage magnitude at node *i* and *j*
 θ_i , θ_j are voltage phase angle at node *i* and *j*
 G_{ij} , B_{ij} are elements of bus admittance matrix $[Y_{bus}]$
 $\theta_{ij} = \theta_i - \theta_j$
 $Y_{ij} = G_{ij} + jB_{ij}$

It has been shown that the Jacobian matrix can be formed as the product of three square matrices in Equations (4.23). Next will showing the Equation (4.23) can be solved by back/forward sweeps. Let's define:

$$E = \Delta \theta + j \,\Delta V / V \tag{4.28}$$

$$S = \Delta P + j \Delta Q \tag{4.29}$$

$$W = D_B + jD_G \tag{4.30}$$

then equation (4.23) can be written as

$$A_{n-1} W A_{n-1}^T E = S (4.31)$$

or

$$A_{n-1} S_L = S (4.32)$$

$$W A_{n-1}^T E = S_L \tag{4.33}$$

where Equation (4.32) is the back sweep and Equation (4.33) is the forward sweep.

To solve *E* in Equation (4.33) in forward sweep $(A_{n-1}^T E = W^{-1}S_L)$, the diagonal matrix *W* can be inverted for each line. The diagonal in W^{-1} is denoted as the equivalent line impedance:

$$Z_{eq,ij} = R_{eq,ij} + jX_{eq,ij}$$
(4.34)

where

$$R_{eq,ij} = \frac{X_{ij}}{V_i V_j \cos \theta_{ij}}$$
(4.35)

$$X_{eq,ij} = \frac{R_{ij}}{V_i V_j \cos \theta_{ij}}$$
(4.36)

 R_{ij} and X_{ij} are resistance and reactance of line *i-j* respectively. The Diagonal matrix W^{-1} is a square matrix, which its dimension is (n-1) × (n-1).

In order t o find the power flow s olution, the power flow p rocess h as finished w hen power mismatch of bot h r eal a nd r eactive pow er should be corresponding to:

$$\max \left| \Delta P^{k} \right| \ and \ \max \left| \Delta Q^{k} \right| \le \varepsilon \tag{4.37}$$

where

 $\max |\Delta P^{k}| \text{ is maximum real power mismatch for any iteration } k$ $\max |\Delta Q^{k}| \text{ is maximum reactive power mismatch for any iteration } k$ $\varepsilon \text{ is power mismatch tolerance which set to } 10^{-5}$

4.2.1 Loss Equations From System Data

Generally, the system real and reactive power loss can be derived into two sets of loss equations i.e., loss equations in terms of Y_{bus} and I_{bus} , and loss equations in terms of Z_{bus} and V_{bus} . The following two sets of loss equations are derived in exactly the same manner, which results in the identical forms for partial derivative equations. In t his di ssertation, loss e quations in term of Z_{bus} and V_{bus} is us ed to obtain system real power loss in probabilistic power flow calculation. However, the derivation of two sets of loss e quations can be found in [80]. The loss e quations in term of Z_{bus} and V_{bus} can be expressed by:

$$P_{L} = \sum_{i=1}^{N_{b}} \sum_{k=1}^{N_{b}} \left[(P_{i}P_{k} + Q_{i}Q_{k})\alpha_{ik} + (P_{i}Q_{k} - Q_{i}P_{k})\beta_{ik} \right]$$
(4.38)

$$Q_{L} = \sum_{i=1}^{N_{b}} \sum_{k=1}^{N_{b}} \left[(P_{i}P_{k} + Q_{i}Q_{k})\tau_{ik} + (P_{i}Q_{k} - Q_{i}P_{k})\theta_{ik} \right]$$
(4.39)

by defined

$$\alpha_{ik} = \frac{R_{ik}}{V_i V_k} \cos \delta_{ik} \tag{4.40}$$

$$\beta_{ik} = \frac{-R_{ik}}{V_i V_k} \sin \delta_{ik} \tag{4.41}$$

$$\tau_{ik} = \frac{X_{ik}}{V_i V_k} \cos \delta_{ik} \tag{4.42}$$

$$\theta_{ik} = \frac{-X_{ik}}{V_i V_k} \sin \delta_{ik} \tag{4.43}$$

where P_L, Q_L are system real and reactive power losses

 P_i, Q_i are real and reactive power load at bus *i*

- R_{ik} , X_{ik} are resistance and reactance of branch i k
 - V_i is voltage magnitude at bus *i*
 - δ_{ik} is different in voltage phase angle of bus *i*, *k* and $\delta_{ik} = \delta_i \delta_k$
 - N_b is total number of buses

4.2.2 The Modified Newton Method Calculation Steps

The flow c hart of radial di stribution s ystem p ower f low algorithm is shown in Figure 4.2. And the calculation step of modified Newton method based on backward and forward sweeps can be summarized as follows:

- (1) Read the radial system data and form bus admittance matrix $[Y_{bus}]$.
- (2) Order branches by layers away from the reference node to construct the node to branch incidence matrix $[A_{n-1}]$.
- (3) Initialize all node voltage and set iteration k = 0
- (4) Calculate net real and reactive nod e power load $P_{i(cal)}$ and $Q_{i(cal)}$ from Equations (4.26) and (4.27).
- (5) Calculate power mismatch ΔP_i and ΔQ_i from Equations (4.24) and (4.25).
- (6) Test for convergence from Equation (4.37). If power flow converge, the solution is obtained but if not go to step (7).
- (7) Calculate S_L in backward sweep from Equation (4.32).
- (8) Calculate equivalent line impedance $Z_{eq,ij}$ from Equation (4.34).
- (9) Calculate *E* in forward sweep from Equation (4.33) to find out $\Delta\theta$ and ΔV
- (10) Update the adopted node voltage to

$$\begin{aligned} \theta_i^{(k+1)} &= \theta_i^{(k)} + real(E_i) \\ V_i^{(k+1)} &= V_i^{(k)} + [imag(E_i) \times V_i^{(k)}] \end{aligned}$$

(11) Set new ite ration k = k + 1 and r epeat t o s tep (4) b y u sing new node voltage.



Figure 4.2 Flow chart of radial distribution system power flow calculation

4.3 Test Results of Radial Distribution System Power Flow Calculation

To demonstrate the methodology of the radial distribution system power flow calculation. The 15-bus radial distribution system from Chapter 3 is used again. Figure 4.3 shows the ordering of nodes and branches of the 15-bus radial distribution system, which node 1 is the reference node.



Figure 4.3 Single-line diagram of the 15-bus radial distribution system with nodes to branches ordering

From Figure 4.3, the node to branch incident matrix A_{n-1} has a dimension of (14×14) and it is given as:

For t his t est, t he pow er f low r esults a re c ompared with t he s olution obtained b y a c onventional N ewton m ethod a s s hown i n T able 4.1. T his t able indicates that the modified Newton method offers the same solution as that obtained by the conventional Newton method, which validates its solution accuracy.

Madawa	Modified Ne	wton method	Conventional Newton method		
Noae no.	V (pu)	δ (deg)	V (pu)	δ (deg)	
1	1.00000	0.00000	1.00000	0.00000	
2	0.97130	0.03194	0.97129	0.03193	
3	0.95669	0.04929	0.95668	0.04928	
4	0.95093	0.05645	0.95091	0.05644	
5	0.94994	0.06862	0.94993	0.06861	
6	0.94846	0.08685	0.94845	0.08685	
7	0.94863	0.08477	0.94862	0.08477	
8	0.94997	0.13142	0.94996	0.13144	
9	0.94585	0.18229	0.94584	0.18233	
10	0.94454	0.19855	0.94453	0.19859	
11	0.96798	0.07191	0.96797	0.07191	
12	0.96691	0.08492	0.96690	0.08492	
13	0.95825	0.18928	0.95824	0.18931	
14	0.95603	0.21649	0.95601	0.21653	
15	0.95697	0.20491	0.95696	0.20495	
P_{loss} , Q_{loss}	61.74 kW ,	57.25 kVar	61.78 kW ,	57.28 kVar	

Table 4.1 Power flow solution obtained for the 15-bus radial distribution system

4.4 Harmonic Modeling

For harmonic calculation, in this dissertation, the electrical equipments in a distribution system are modeled based on C IGRE model [81], which is a balance system. Therefore, the impedance values of each model are represented in all per phase.

4.4.1 Harmonic Load Modeling

Generally, a harmonic load model is represented as a simple model for harmonic study. This model includes a connection in series or parallel of resistance (R) and inductance (L), which some physical of load is neglected. C onsequence, harmonic voltage and harmonic current calculations may be incorrect.

Therefore, an effective harmonic load model is used in this dissertation. This harmonic load model c an be divided into t wo types (CIGRE and R //L) for a different harmonic order consideration, as seen in Figure 4.4.



Figure 4.4 Harmonic load model of CIGRE and R//L

From Figure 4.4, the C IGRE load model is used to study for harmonic frequency order 5th to 20th. This model consists of a series reactance (X_s) , a parallel reactance (X_p) and a resistance (R). The other is R//L load model, which consists of a resistance (R) and a reactance (X) in parallel connection. The R//L lode model is used to study f or harmonic frequency in order m ore than 20th. The parameters in each model can be expressed as follows:

$$R = \frac{U_{n,net}^2}{P_1} \tag{4.44}$$

$$X_s = (0.0073) \times h \times R \tag{4.45}$$

$$X_{p} = \frac{h \times R}{(6.7)\tan\theta_{1} - 0.74}$$
(4.46)

$$X = h \times \frac{U_{n,net}^2}{Q_1} \tag{4.47}$$

where $U_{n.net}$ is normal system voltage

- P_1 is real power load at fundamental frequency under $U_{n,net}$
- Q_1 is reactive power load at fundamental frequency under $U_{n,net}$
- *h* is harmonic order

$$\tan\theta_1 = Q_1/P_1$$

4.4.2 Harmonic Capacitor Modeling

For harmonic calculation, the capacitor modeling can be represented by capacitance which depends on harmonic frequency as:

$$X_{c}^{h} = -j \frac{1}{h2\pi} \frac{1}{f_{1}C}$$
(4.48)

$$y_{c}^{h} = -\frac{1}{X_{c}^{h}}$$
(4.49)

and

where X_c^h is capacitive reactance at harmonic frequency order h

 y_c^h is capacitive admittance at harmonic frequency order h

- *C* is capacitance of capacitor
- f_1 is fundamental frequency

4.4.3 Harmonic Feeder Modeling

The equivalent circuit of feeder can be represented by a series connection of feeder resistance and reactance, which depends on harmonic frequency as shown in Figure 4.5. And its expression is given in Equation (4.50).

•
$$R_{line}$$
 jhX_{line}

Figure 4.5 Equivalent circuit of harmonic feeder modeling

$$y_{line}^{h} = \frac{1}{R_{line} + jhX_{line}}$$
(4.50)

where R_{line} is line resistance

 X_{line} is line reactance at fundamental frequency

 y_{line}^{h} is line admittance at harmonic frequency order h

4.4.4 Background Harmonic Modeling

In t his di ssertation, e xisting ba ckground ha rmonic c onditions i n a distribution s ystem ar e taken i nto a ccount f or opt imal PV-DG s izing. Actually, background harmonics may occur from several nonlinear equipments such as 6-pulse

and 12 -pulse r ectifier, arc furnaces, adjustable s peed drives, etc. However, 6-pulse converters are the main harmonic sources which generate background harmonics in this s tudy. And the background harmonics are treated as a percentage of nonlinear loads at all load buses except PV-DG buses.

4.5 Harmonic Calculation in a Distribution System

This s ection pr esents ha rmonic vol tage a nd c urrent c alculations i n a distribution system. Also total ha rmonic di stortion of voltage a nd c urrent a re mentioned.



Figure 4.6 A simplified distribution system for fundamental frequency analysis

Figure 4. 6 shows a s implified di stribution s ystem for fundamental frequency a nalysis. In this f igure, 6 -pulse con verters are t reated as background harmonic sources of the system and it can be represented by harmonic current source with the typical harmonic current spectra (I_{BH}) as shown in Table 4.2 [82]. For the PV-DGs are interconnected at any bus, they are treated as harmonic current sources with the typical harmonic current spectra based on measurements at a PV farm (I_{PV}) as m entioned in Chapter 2. The other parameter in Figure 4.6 can be defined as follows:

- y_{ii}^{T} is line admittance at fundamental frequency of branch *i j*
- y_{ci}^{l} is capacitive admittance at fundamental frequency at bus *i*
- P_{li} is real power load at bus *i*
- Q_{ii} is reactive power load at bus *i*

Harmonic	Rectifier system pulse number			Harmonic current Harmonic fundamen		current in Indamental	
	б	12	18	24	irequency	Theoretical	Typical
5	х				300	20.00	19.20
7	х				420	14.20	13.20
11	х	х			660	9.09	7.30
13	х	х			780	7.69	5.70
17	х		х		1020	5.88	3.50
19	х		х		1140	5.26	2.70
23	х	х		х	1380	4.36	2.00
25	х	х		х	1500	4.00	1.60
29	х				1740	3.45	1.40
31	х				1860	3.23	1.20
35	х		х		2100	2.86	1.10
37	х		х		2220	2.70	1.00
NOTE—The theoretical values are given for a 6-pulse converter with ideal characteristics (i.e., square current waves with 120° conduction). The last column gives typical values based on a commutating impedance of 0.12 pu and a firing angle of 30° and infinite dc reactor (IEEE Std 519-1992, Table 13.1). These values are on the basis of one 6-pulse converter or all converters, assuming that the harmonics are additive. Since some harmonics will be canceled, but not entirely, a small percentage value may be assumed, as explained earlier in this subclause. Note that if the dc reactor is not large, some of the harmonics can be greater than typical (or theoretical) and some smaller.							

Table 4.2 Characteristic AC line harmonic currents in multi-pulse systems

The equivalent circuit for harmonic frequency analysis corresponding to the simplified system in Figure 4.6 is shown in Figure 4.7. Note from this figure that the 6-pulse converters and the PV-DGs are modeled as harmonic current sources to inject harmonic currents into the connected bus. The load de mand, shunt capacitor and feeder line are modeled as admittance of each components.



Figure 4.7 A simplified distribution system for harmonic frequency analysis where the parameters in Figure 4.7 can be defined as follows:

 y_{ij}^{h} is line admittance at harmonic frequency order *h* of branch *i* - *j* y_{ci}^{h} is capacitive admittance at harmonic frequency order *h* at bus *i* y_{li}^{h} is load admittance at harmonic frequency order *h* at bus *i*

- y_s^h is source admittance at harmonic frequency order *h*
- V_i^h is voltage at harmonic frequency order h at bus i
- I_i^h is current source at harmonic frequency order h at bus i

The source impedance (Z_s) c an be obtained from the given source data such as transformer voltage ratio, R/X ratio and MVA short circuit. The example for source impedance calculation can be expressed by the given source data as:

- Transformer ratio $(V_{high}/V_{low}) = 22kV/416V$
- R/X ratio = 10
- MVA short circuit = 100

From source data, we can calculate the short circuit current (I_{sc}) as:

$$I_{sc} = \frac{MVA_{sc} \times 10^6}{\sqrt{3} \times V_{low}} = \frac{(100 \times 10^6)}{\sqrt{3} \times 416} = 138.79 \ kA$$

And we can calculate the source impedance magnitude $(/Z_s)$ as:

$$|Z_s| = \frac{(V_{low}/\sqrt{3})}{I_{sc}} = \frac{(416/\sqrt{3})}{138.79 \ kA} = 0.00173 \ \Omega$$

Thus, we get a source resistance (R_s) and reactance (X_s) as:

$$R_{s} = \frac{|Z_{s}|}{\sqrt{(R/X \ ratio)^{2} + 1}} = \frac{(0.00173)}{\sqrt{10^{2} + 1}} = 0.000172 \ \Omega$$
$$X_{s} = (R/X \ ratio) \times R_{s} = 10 \times 0.000172 = 0.00172 \ \Omega$$

Therefore, we can find the source impedance and source admittance as:

$$Z_{s} = R_{s} + jX_{s} = 0.000172 + j0.00172 \quad \Omega$$
$$y_{s} = \frac{1}{Z_{s}} = \frac{1}{0.000172 + j0.00172} = 57.563 - j575.639 \quad mho$$

From Figure 4. 7, we can form bus admittance matrix at ha rmonic frequency or der *h* directly from the admittance of each component in a distribution system as mentioned ab ove. The harmonic bus admittance matrix $[Y_{bus}^h]$ of system with *m* nodes is a square matrix which its dimension is (m×m) as given by:

$$\begin{bmatrix} Y_{bus}^{h} \end{bmatrix} = \begin{bmatrix} Y_{11}^{h} & Y_{12}^{h} & 0 & & 0 \\ Y_{21}^{h} & Y_{22}^{h} & \cdot & & \\ 0 & \cdot & \cdot & & \\ & & \cdot & \cdot & 0 \\ & & & \cdot & Y_{m-1,m-1}^{h} & Y_{m-1,m}^{h} \\ 0 & & 0 & Y_{m,m-1}^{h} & Y_{mm}^{h} \end{bmatrix}$$
(4.51)

where

 $Y_{ij}^{h} = \begin{cases} -y_{ij}^{h} & \text{if } j \neq i \\ y_{i-1,i}^{h} + y_{i,i+1}^{h} + y_{li}^{h} + y_{ci}^{h} & \text{if } j = i \neq 1 \\ y_{12}^{h} + y_{s}^{h} & \text{if } j = i = 1 \end{cases}$ (4.52)

By know ing t he harmonic c urrent s ource at a ny bus $[I_i^h]$ and a lot the harmonic bus admittance $[Y_{bus}^h]$, we can obtain the harmonic voltage at any bus $[V_i^h]$ from Equation (4.53).

$$\begin{bmatrix} I_i^h \end{bmatrix} = \begin{bmatrix} Y_{bus}^h \end{bmatrix} \begin{bmatrix} V_i^h \end{bmatrix}$$
(4.53)

and we get

$$\begin{bmatrix} V_{1}^{h} \\ V_{2}^{h} \\ \cdot \\ \cdot \\ V_{m-1}^{h} \\ V_{m}^{h} \end{bmatrix} = \begin{bmatrix} Y_{11}^{h} & Y_{12}^{h} & 0 & & 0 \\ Y_{21}^{h} & Y_{22}^{h} & \cdot & & \\ 0 & \cdot & \cdot & & \\ 0 & \cdot & \cdot & & \\ & & \cdot & Y_{m-1,m-1}^{h} & Y_{m-1,m}^{h} \\ 0 & & 0 & Y_{m,m-1}^{h} & Y_{mm}^{h} \end{bmatrix}^{-1} \begin{bmatrix} I_{1}^{h} \\ I_{2}^{h} \\ \cdot \\ \cdot \\ I_{m-1}^{h} \\ I_{m}^{h} \end{bmatrix}$$
(4.54)

In optimal P V-DGs s izing pr ocess, t he ha rmonic c onstraints i .e., total harmonic voltage distortion (THDv), and total demand distortion (TDD) at a point of common coupling (PCC) are taken into accounted. The THDv and TDD are defined with harmonic frequency from order 2^{nd} to 33^{rd} as given by:

$$THD_{v,i} = \frac{\sqrt{\sum_{h=2}^{33} \left| V_i^h \right|^2}}{\left| V_i^1 \right|} \times 100 \%$$
(4.55)

$$TDD_{i} = \frac{\sqrt{\sum_{h=2}^{33} \left| I_{i}^{h} \right|^{2}}}{\left| I_{m,i}^{1} \right|} \times 100 \%$$
(4.56)

where V_i^1 is fundamental voltage at bus *i*

 V_i^h is harmonic voltage order h at bus i

 THD_{V_i} is total harmonic distortion voltage at bus *i*

 I_i^1 is fundamental current flow through bus *i*

 I_i^h is harmonic current order h flow through bus i

 $I_{m,i}^1$ is fundamental maximum load current flow through bus *i*

 TDD_i is total demand distortion at bus *i*

From IE C 61727 s tandard in P hotovoltaic s ystems-Characteristic of the utility interface, low levels of current and voltage harmonics at a connection point of PV-DG are desirable. Acceptable levels of harmonic voltage and current depend upon distribution system c haracteristic, type of s ervice, connected loads/apparatus and established utility practice. The P V-DG out put s hould have low c urrent di stortion levels to ensure that no adverse effects are caused to other equipment connected to the utility system.

To comply with IEC 61727 standard, the total harmonic current distortion shall be less than 5% at rated inverter output. Hence, in order to calculate the TDD at the connection point of P V-DG, the maximum load current in Equation (4.56) is replaced by rated current of PV inverter. And each individual harmonic current from PV inverter shall be limited to the percentages listed in Table 4.3.

Odd harmonics	Distortion limit
3 rd through 9 th	\leq 4.0 %
11 th through 15 th	$\leq~2.0~\%$
17 th through 21 st	\leq 1.5 %
23 rd through 33 rd	$\leq~0.6~\%$
Even harmonics	Distortion limit
2 nd through 8 th	≤ 1.0 %
10 th through 32 nd	$\leq~0.5~\%$
Total harmonic current distortion at rated inverter output (TDD)	≤ 5.0 %

Table 4.3 Current distortion limits in IEC 61727 standard

In the IEC 61727 s tandard, the T HDv constraint is not m entioned. However, according to the IEEE 519-1992 standard, IEEE R ecommended Practices and Requirements for Harmonic Control in Electrical Power Systems, the THDv at a PCC should not exceed 5%.

CHAPTER V ALGORITHM OF OPTIMAL PV-DG SIZING TECHNIQUE AND NUMERICAL RESULTS

5.1 Introduction

This chapter proposes the algorithm of optimal PV-DG sizing technique. Also pr oblem f ormulation a nd c onstraints de tail a re m entioned. Furthermore, t he numerical r esults of various study c ases are investigated. An actual 51-bus radial distribution system of Provincial Electricity Authority (PEA) of Thailand and a heavy load 33-bus radial distribution system are selected as test cases. Results from study cases indi cate that the opt imal P V-DG s ize s olution may be c hanged de pend on system operating conditions. Furthermore, it demonstrates that PV-DGs may improve voltage r egulation and de crease l osses i n di stribution s ystems, how ever, the T HDv may also increase. Impact of static load models and power factor control on optimal sizing of PV-DG are also addressed. Finally, effects of inverter modeling and existing DGs in a distribution system on optimal PV-DG sizing are presented.

5.2 Problem Formulation

The PV-DG installation in a distribution system has several advantages (e.g., vol tage i mprovement, losses r eduction, etc.). In the proposed t echnique, the main objective is to minimize the "average" real power losses of a distribution system by varying the s ize of PV-DG over N_s samples. The problem can be expressed mathematically as follows:

Minimize
$$\frac{1}{N_s} \sum_{r=1}^{N_s} P_{L,r}(PV_{size})$$
(5.1)

subjected to the following constraints:

- $0.95 \text{ pu} \le V_i \le 1.05 \text{ pu}$, at PCC
- THDv and TDD $\leq 5\%$, at PCC
- $I_h \leq \text{IEC limits}$, at PCC

where $P_{L,r}(PV_{size})$ is the real power losses of a radial distribution system shown as a function of the size of PV-DG (PV_{size}). Note that $P_{L,r}(PV_{size})$ is calculated from the sample *r* and the real power losses equation can be written as

$$P_{L,r}(PV_{size}) = \sum_{i=1}^{N_b} \sum_{j=1}^{N_b} \left[\frac{R_{ij} \cos \delta_{ij}}{|V_i| |V_j|} (P_i P_j + Q_i Q_j) + \frac{R_{ij} \sin \delta_{ij}}{|V_i| |V_j|} (Q_i P_j - P_i Q_j) \right]$$
(5.2)

where R_{ii} is resistance of branch i - j

 $|V_i|$ and δ_i are the voltage magnitude and phase angle at bus *i*

 P_i and Q_i are the net real and reactive power at bus i

 $\delta_{ij}\,$ is the voltage phase angle difference between buses i and j

 N_b is the total number of buses in a distribution system

5.3 The Algorithm of Optimal PV-DG Sizing Technique

The algorithm for determining an optimal PV-DG size can be depicted in Figure 5.1. As mentioned in Chapter 2 on PV modeling section, the PV_{size} in Figure 5.1 is the rated size of PV-DG which based on a connection group of Sharp 80Wp PV modules. Several random variables are generated with Monte Carlo simulations i.e., solar radiations (G_a), ambient temperatures (T_a), load demands ($L_{d,i}$) and substation voltages (V_S). The maximum active power outputs of PV-DGs ($P_{mp,i}$) are obtained at each location by PV model and MPPT block.

From t he r eport i n [83], i t s hows t hat the pow er f actor of P V gridconnected inverter is usually controlled to be 100%. However, some inverters have the capability to adjust the power factor for two main purposes. One is leading power factor operation to suppress the voltage rise in a distribution system due to the output power from PV-DGs during light-load hours in the daytime. The other is operated at the lagging power factor during heavy load to compensate for the voltage drop of the distribution l ines. T herefore, v arious pow er factor ope rations and a lso proper l oad models a re important in PV s ystem installation planning. Then, the r eactive pow er output of P V-DGs ($Q_{mp,i}$) in P V m odel bl ock can f low i n bot h di rections t o t he network under lagging or leading power factor operations.
System losses and node voltages are evaluated by the distribution power flow calculation. Based on the data measured from a PV farm (540 units of 11 k W grid-connected i nverters), harmonic di stortions at each bus ar e ev aluated by t he harmonic flow a nalysis. A s s hown in the flow chart in Figure 5.1, the process is calculated repeatedly from a specific range of PV-DG size at each incremental step. The optimal solution of Equation (5.1) is the rated size of PV-DG with minimum the average system loss and under the constraints from 5,000 samples (N_s).



Figure 5.1 Flow chart of the optimal PV-DG sizing technique

5.4 Numerical Results and Discussion

For the purposes of this dissertation, there are three scenarios to determine the optimal PV-DGs size in the difference system operating conditions. However, the hourly solar radiation and ambient temperature based on measured from Chiang Mai province as given in Chapter 2 on section 2.2 are used for all scenarios.

5.4.1 <u>Scenario-1</u>: Optimal P V-DG s izing w ith a nd w ithout consideration of background harmonic in distribution system

An actual 22 kV radial distribution system in Thailand is employed as a test case in this scenario. All system parameter are given in Appendix C, which can be found in [84]. The test system has 51 buses with a total load of 1.92 MW, 1.06 MVar and 1 unit of 900 kVar capacitor bank at bus-13 as shown in Figure 5.2. The results of base case deterministic load flow are given in Appendix D.

This s cenario s hows t he opt imal P V-DGs s izing w ith a nd w ithout consideration of existing background harmonic conditions in distribution system. The PV-DGs pl acements ar e obt ained based on the static vol tage s tability i ndex (VSI) calculations. The system operating conditions in this scenario are given as:

- Substation voltage and load demand are assumed to be random variables with normal distribution, which standard deviations (σ) of substation voltage and load models are set to 1.5% and 10% respectively.
- Power factors of PV-DGs are assumed to be 1.0 constant.
- Load model is assumed to be constant power load.
- The 6 -pulse conv erters ar e m ain harmonic s ources which generate background harmonics (the typical harmonic current spectra are given in Table 4.2 on Chapter 4).
- Three l evels of ba ckground ha rmonics (15%, 25% a nd 35%) a re considered.
- Other DGs are not considered in this test system.
- In this scenario, all constraints (V_i , I_h , THDv and TDD) are considered with 95% confidence interval.
- Range of *PV_{size}* on this study is between 0.1 M Wp to 2 M Wp with a 0.1 MWp increment.



Figure 5.2 Single-line diagram of the 51-bus test system

Firstly, a vol tage s tability inde x is c omputed as a basis to determine proper l ocations of P V-DG. Buses with descending minimum V SI are s elected as candidate locations to install PV-DG. A constant power load model is also assumed in VSI calculation. Table 5.1 shows three candidate locations (i.e., buses 38, 19 and 37) with various voltage levels of substation in the test system. The results in Table 5.1 also show the minimum voltage related to the critical bus with minimum VSI.

Substation voltage (pu)	Candidate buses with VSI min	VSI min	Voltage min (pu)
	38	0.0387	0.4436
0.95	19	0.0392	0.4451
	37	0.0402	0.4478
	38	0.0453	0.4613
1.00	19	0.0457	0.4623
	37	0.0459	0.4630
	38	0.0545	0.4831
1.05	19	0.0554	0.4851
	37	0.0561	0.4868

Table 5.1 Critical bus stability index values of the test system

After selecting proper locations of PV-DG, the proposed technique is then employed to solve the opt imal P V-DG size. I n t his s tudy, e xisting ba ckground harmonic c onditions i n test system are a lso t aken i nto a ccount. The b ackground harmonics (BH) are treated as a p ercentage of nonlinear loads at all load bus except PV-DG bus. Three levels of background harmonics (i.e., 15%, 25% and 35% of load demands) are t ested. Based on t her esults of the vol tage s tability i ndex of t he candidate bus es, three s tudy c ases are investigated to determine the optimal size of PV-DG.

Case-1: Single PV-DG

The PV-DG installation is assumed to be owned by a generation company and located at the bus with minimum VSI (bus-38). This case shows the selection of PV-DG s ize ba sed on t he t echnical c onstraints with a nd w ithout c onsideration of background harmonics.

Figure 5.3 presents the relationship between the average system loss and the average PV-DG active power output. As shown in Figure 5.3, the system losses vary with the size of PV-DG installed at bus-38. The average system loss without installing PV-DG is 30.1 kW. Beside, the system losses decrease when installing PV-DG less than 1.7 MWp. The minimum average system loss in this case is 23.3 kW, which is given by installing a PV-DG at 0.8 MWp. Also note that with the variation of solar radiation and operating temperature, from installing 0.8 MWp PV-DG (peak power output), the average active power output is 0.35 MW.



Figure 5.3 Average system losses as a function of average PV-DG power output in Case-1

The c umulative pr obability of vol tage a t bus -38 w ith a nd w ithout installation of 0.8 MWp PV-DG is shown in Figure 5.4. Similarly, an installation of PV-DG mostly improves the voltage regulation at the PCC. Note from the figure, it shows that the voltage level at bus-38 stays within an acceptable range (i.e., 0.95 t o 1.05 pu.) with 95% confidence interval.



Figure 5.4 Cumulative probability of voltage at PCC with and without PV-DG in Case-1



Figure 5.5 Cumulative probability of THDv at PCC with and without background harmonics in Case-1

Figure 5.5 shows the impact of background harmonics on T HDv at bus-38. Results show that THDv values are less than 1% without considering background harmonics. This indicates that an individual PV-DG produces small voltage distortion waveform. O n t he c ontrary, t he T HDv r ises when t he pe rcentage of background harmonics on t he test system increases. The T HDv r eaches 3.5% when the level of background harmonics is 35%. In this case, the background harmonics produce more impact on T HDv at PCC than PV-DG. However, all THDv values do not reach the 5% limits in Case-1.

Based on SMC-11000TL g rid-connected i nverter, P WM t echnology is employed to control the output waveform. Therefore, the harmonic current (I_h) from the inverter is less than the limits. The cumulative probability of TDD and harmonic current from inverter simulated at PCC of Case-1 are shown in Figures 5.6 to 5.11. The results show that all constraints are complied with IEC standard. T herefore, in Case-1, the opt imal PV-DG s ize at bus -38 is 0.8 M Wp for both w ith and w ithout consideration of background harmonics.



Figure 5.6 Cumulative probability of TDD at PCC of inverter



Figure 5.7 Cumulative probability of I_h (even orders 2 to 8) at PCC of inverter



Figure 5.8 Cumulative probability of I_h (odd orders 3 to 9) at PCC of inverter



Figure 5.9 Cumulative probability of I_h (odd orders 11 to 15) at PCC of inverter



Figure 5.10 Cumulative probability of I_h (odd orders 17 to 21) at PCC of inverter



Figure 5.11 Cumulative probability of I_h (odd orders 23 to 33) at PCC of inverter

<u>Case-2A</u>: Multiple PV-DGs without consideration of background harmonics

In this case, by considering the same constraint as in Case-1, two PV-DGs are installed at buses 38 and 19. This case shows that the proposed technique can be applied to determine the optimal size for multiple locations. Note that, the background harmonics are not considered in this case.

The system losses after installing PV-DGs at buses 38 and 19 are shown as 3 -D plot in Figure 5. 12. Note from the figure that the minimum average system loss occurs when installing a 0.7 MWp PV-DG at bus-38 and a 0.9 MWp at bus-19. With the variation of solar radiation and operating temperature, the total average PV-DGs output is around 0.7 MW which results in 16.86 kW of average system loss. The results in Figure 5.12 also show that, with multiple PV-DGs installations, the average system losses of Case-2A are lower than Case-1 (23.33 kW). Hence, the installations of PV-DGs reduce 56.2% of system losses comparing the case without PV-DG (30.1 kW).



Figure 5.12 Average system losses as a function of PV-DGs size at buses 38 and 19

From installing a 0.7 M Wp PV-DG at bus-38 and a 0.9 M Wp at bus-19, Figure 5.13 shows the cumulative probability of voltages at bus es 38 and 19 (both with and without PV-DGs). The results show that voltages at PCC are increased when the P V-DGs a re p resented. H owever, t he voltages at bot h l ocations stay in a n acceptable level with 95% confidence interval.



Figure 5.13 Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A

Figure 5.14 shows the impact of background harmonics on THDv values. Note from the figure that the THDv at PCC increases and may exceed the limits when higher percentage of background harmonics occurs. The THDv at both locations does not reach the limits for 15% and 25% of background harmonics. However, when the level of background h armonics is 35%, the p robability a t w hich T HDv at bus -19 violates the constraint (exceeds 5%) is 0.1.



Figure 5.14 Cumulative probability of THDv at PCC with and without background harmonics in Case-2A

Although, the THDv constraint is violated in some levels of background harmonics. Fortunately, the process of optimal PV-DG sizing does not considered the background harmonics in this case.

<u>Case-2B</u>: Multiple PV-DGs with consideration of background harmonics

When the level of background harmonics is 35%, as the results in Case-2A, the T HDv at bus -19 vi olates the c onstraint m ore than 0.05 of probability of occurrences. Therefore, to comply with harmonic limits, Case-2A is considered again taking into a ccount the background h armonics. By a pplying the same algorithm as shown in Figure 5.1, the mini mum a verage s ystem loss in Case-2B oc curs w hen installing a 0.7 M Wp PV-DG at bus-38 and a 0.5 M Wp at bus-19 (see Fig.5.12). In this case, the average system loss is 18.39 kW and the total average PV-DGs output is around 0.52 MW.

Figure 5.15 shows the comparison of THDv at buses 38 and 19 be tween Cases-2A and 2B (with 35% of background harmonics). Note that the solution from

Case-2B guarantees the THDv constraint with 95% confidence interval. This case shows the effectiveness of the proposed technique when the background harmonics are presented in an actual distribution system.



Figure 5.15 Comparison of THDv at PCC between Case-2A and Case-2B with 35% of background harmonics

As the results in Case-2B, the optimal size of PV-DG at bus-19 is reduced to 0.5 M Wp from C ase-2A (0.9 M Wp). T his guarantees t he vol tage c onstraint a t buses 38 and 19 with 95% confidence interval.

Also from Figures 5.6 to 5.11, t he c umulative pr obability of % TDD and inverter harmonic current from the same inverter in each order at PCC of Cases-2A and 2B are s imilar t o Case-1. Therefore, the harmonic current constraints ar e maintained at acceptable levels in both cases.

Table 5.2 summarizes the PV-DGs installation for all cases. With various background h armonic levels, a verage values of %THDv at PCC are presented with the c orresponding opt imal s izes of P V-DGs. F or a ll c ases without background harmonics, a verage values of % THDv a relower t han 1%. On the c ontrary, t he average values of % THDv vary de pending on t he background harmonic levels. Furthermore, with higher total installed capacity of PV-DGs, the THDv at PCC may increase. This can be observed from the average of %THDv at bus-38 of all cases.

Location Bus	Optimal Total PV-DG PV-DG size Capacity		Total average PV-DG power output	Minimum average system	Average of %THDv at PCC related to optimal PV-DG size with and without background harmonics (BH)			
	(MWp)	(MWp)	(MW)	losses (kW)	without BH	15% BH	25% BH	35% BH
38 (Case-1)	0.8	0.8	0.346	23.327	0.389	1.322	2.004	2.694
38 19 (Case-2A)	0.7 0.9	1.6	0.696	16.863	0.415 0.518	1.383 2.203	2.058 3.362	2.747 4.537
38 19 (Case-2B)	0.7 0.5	1.2	0.519	18.387	0.392 0.344	1.337 2.052	2.020 3.229	2.710 4.414

Table 5.2 Summarize the optimal size of PV-DGs installation

Although, the THDv at bus-19 violates the harmonic constraint in Case-2A with 35% of background harmonics. While the average of %THDv is less than 5% (4.537%) as shown by bold number in Table 5.2.

Thus, by using the average of %THDv as a criterion, the optimal sizes of PV-DGs s olution i n C ase-2A m ay b e a cceptable w ith c onsidering up to 35% of background ha rmonic l evels. H owever, t he s olution i n C ase-2B indi cates that t he optimal size of PV-DG at bus-19 should be reduced to maintain the THDv constraint. This indicates that when the average of %THDv is used as a criterion, the optimal sizes of PV-DGs may be overestimated.

A summary of the total number of PV modules and inverters for optimal sizes of PV-DGs solution is given in Table 5.3. Note that the total number of PV modules and inverters are based on a connection group of Sharp 80Wp PV module and SMC 11 kW grid-connected inverter.

Location Bus	Optimal PV-DG size (MWp)	Total number of PV modules (module)	Total number of inverters (unit)	
38 (Case-1)	0.8	10,000	72	
38 19 (Case-24)	0.7 0.9	8,750 11,250	63 81	
38 19 (<i>Case-2B</i>)	0.7 0.5	8,750 6,250	63 45	

Table 5.3 Summarize the total number of PV modules and inverter units foroptimal PV-DGs sizes solutions

The results in Scenario-1 show that the proposed technique performs well to obt ain t he opt imal s izes of P V-DGs f or multiple l ocations based on t echnical constraints. In practice, some background harmonic distortion are normally present in the ne twork. B y applying t his t echnique, t he opt imal sizes of P V-DGs can be determined taking into account the background harmonics.

It has been demonstrated that the installation of PV-DGs may affect the power qua lity when s ome ba ckground ha rmonics a re pr esented i n a distribution system. With high ba ckground ha rmonics, the THDv at P CC m ay not s atisfy the standard. As shown in Case-2A, the optimal sizes of PV-DGs are not acceptable with a 35% of background harmonic level. This is due to THDv constraint violation at bus 19. Therefore, as shown in Case-2B, the optimal sizes of PV-DGs with consideration of background harmonics are required. However, in Case-1, the optimal size of PV-DG is s uccessfully obtained in both with and without consideration of background harmonics.

The r esults f rom s everal cases also indicate that P V-DGs ar e likely t o improve the voltage r egulation and decrease s ystem losses in a distribution s ystem. However, i nstalling with high capacity of P V-DGs m ay i ncrease T HDv at P CC especially when the background harmonics are presented.

5.4.2 Scenario-2: Impact of 1 oad m odel a nd pow er f actor c ontrol on optimal PV-DG sizing

The purpose of this scenario is to study an impact on optimal PV-DG sizing in a distribution system using different static load models (i.e., constant power, constant current and constant impedance) and various power factor operations.

The 51-bus radial distribution system in Scenario-1 is employed as a test case again, but the capacitor bank at bus-13 is neglected in this scenario. The system operating conditions in this scenario are given as:

- Substation voltage is set to $1.0 \angle 0^\circ$ constant.
- Load demand is assumed to be random variables with normal distribution, which standard deviations (σ) is set to 10%.
- Various power factor operations of PV-DGs are considered.
- Three static load models are considered i.e., constant power (CP), constant current (CI) and constant impedance (CZ).
- Background harmonics are not considered in this test system.
- Other DGs are not considered in this test system.
- In this scenario, only voltage and THDv constraints are considered.
- Range of *PV_{size}* on this study is between 50 kWp to 2.5 MWp with a 50 kWp increment.

For the purpose of this scenario, it is assumed that the PV-DG installation is located at bus es 10 and 19. T wo cases are studied for determining the impact of load model and various power factor operations on optimal sizing of PV-DG.

<u>Case-1</u>: Single PV-DG

In this case, the PV-DG installation is assumed to locate at only bus-19. The i mpact of PV-DG connection on s ystem losses with different load models is presented in Figure 5.16, which power factor (PF) is set to 1.0 constant. It shows that PV-DG nor mally d ecreases s ystem losses, except when its s ize largely i ncreases. Furthermore, it demonstrates that using different static load models do not impact on optimal PV-DG size, which is 1.1 MWp. Besides, the voltage and THDv constraints are s atisfied for P V-DG s ize with minimum the a verage s ystem los s a s s hown in Figures 5.17 and 5.18, respectively.



Figure 5.16 Average system losses as a function of average PV-DG power output with different load models



Figure 5.17 Cumulative probability of voltage at bus-19 with different load models (PF = 1.0)



Figure 5.18 Cumulative probability of THDv at bus-19 with different load models (PF = 1.0)

Figure 5.17 shows that the voltage values depend on l oad models. The lowest vol tage i s oc curred w hen us ing t he CP m odel. H owever, t he vol tage constraints of all load models are within the limits. Figure 5.18 shows that different load models do not affect the THDv. In reality, the THDv strongly depends on P V-DG size as shown in Figure 5.22. Further, it can be observed from Figure 5.18 that THDv is small and l ess than 1.25%. This shows that the low harmonic distortion power can be generated based on SMC-11000TL inverter.

The impact of leading operation on system losses in Case-1 with CP load model is presented in Figure 5.19. It shows that the solution of optimal PV-DG size may be changed for wide leading power factor range. Unlike the lagging operation which has a few impact on optimal size of PV-DG as shown in Figure 5.20. Further, Figure 5.19 indicates that the system losses are rapidly increasing when PV-DG size is larger. This can be seen by comparing the curve for a given PF values with the curve obt ained for lagging operation. This is due to the fact of PV-DG consumes reactive power at leading operation. Therefore, low leading PF c auses vol tage t o reduce. As a result, the system losses are nonlinearly increasing.



Figure 5.19 Average system losses as a function of average PV-DG power output with different leading power factor (CP-model)



Figure 5.20 Average system losses as a function of average PV-DG power output with different lagging power factor (CP-model)

Figures 5.21 and 5.22 show cumulative probability of voltage and THDv at bus-19 corresponding to the results in Figure 5.19, with different optimal PV-DG sizes at each power factor. Figure 5.21 indicates that voltage is increasing when the size of PV-DG is larger, similar with THDv values as shown in Figure 5.22.



Figure 5.21 Cumulative probability of voltage at bus-19 with different PV-DG sizes corresponding to Figure 5.19



Figure 5.22 Cumulative probability of THDv at bus-19 with different PV-DG sizes corresponding to Figure 5.19

Case-2: Multiple PV-DG

In this case, two PV-DGs are installed at buses 10 and 19. The impact of PV-DGs connection on s ystem losses with different load models are shown as 3-D plot in Figures 5.23 to 5.25, which PF is set to 1.0 constant. It shows that the average system losses decrease more than Case-1 with multiple PV-DGs. It demonstrates that using different static load models do not impact on optimal PV-DGs sizes, which is

1.5 MWp at bus 10 a nd 0.7 MWp at bus-19. The voltage and THDv constraints at each bus related to PV-DGs sizes of constant power load model are shown in Figures 5.26 and 5.27, respectively. The results indicate that all constraints are kept within the limits.



Figure 5.23 Average system losses as a function of PV-DGs capacity at buses 10 and 19 with constant power load model (PF = 1.0)



Figure 5.24 Average system losses as a function of PV-DGs capacity at buses 10 and 19 with constant current load model (PF = 1.0)



Figure 5.25 Average system losses as a function of PV-DGs capacity at buses 10 and 19 with constant impedance load model (PF = 1.0)



Figure 5.26 Cumulative probability of voltage at buses 10 and 19 corresponding to the result in Figure 5.23



Figure 5.27 Cumulative probability of THDv at buses 10 and 19 corresponding to the result in Figure 5.23

From Figure 5.27, the THDv at bus-19 is higher than the THDv at bus-10 although the PV-DG size at bus-19 (0.7 MWp) is about 50% less compared with bus-10 (1.5 MWp). This is due to the increasing system impedance (longer distance from the substation) and also the influence from large PV-DG size at bus-10. Therefore, higher THDv can be observed at the end of the feeder. This finding is critical for PV-DG ins tallation considering in rural a reas where di stribution systems are widely spread over large distances.

The impact of various power factor operations with constant power load model on multiple optimal PV-DGs sizes is presented in Table 5.4. Similarly in Case-1, the optimal sizes solution may be changed for wide leading power factor range and it has a few impact on optimal sizes in lagging power factor operation.

	Lagging type		System losses	Leading type		System losses	
P.F.	Bus-10 (MWp)	Bus-19 (MWp)	(kW)	Bus-10 (MWp)	Bus-19 (MWp)	(kW)	
0.9	1.7	0.8	18.56	0.95	0.4	29.33	
0.925	1.7	0.65	18.57	0.95	0.45	28.35	
0.95	1.7	0.65	19.21	1.0	0.6	27.29	
0.975	1.7	0.8	19.71	1.3	0.65	25.69	
1.0	1.5	0.7	22.53	1.5	0.7	22.53	

Table 5.4 Multiple optimal PV-DGs sizes for various PF operations with CP-model

From the results in Scenario-2, it can be summarized that different static load m odels do not i mpact on opt imal sizes of PV-DGs. It d emonstrates that the voltage has a significant change with both load m odels and PV-DG size (see Figs. 5.17 and 5.21). W hile the T HDv values depend on P V-DG sizes m ore than load models (see Figs. 5.18 and 5.22). Furthermore, an impact of power factor control on optimal sizes of PV-DGs indicates that leading operation changes the optimal size of PV-DG at each power factor operation. This differs from lagging operation which has low impact on optimal PV-DG size.

In addition, fast growing technologies like PV-DGs is emerging as part of a distribution system. Therefore, it is necessary to evaluate and analyze the power quality issue due to various non-linear current. In practice, utilities cannot assign the PV-DGs installation location to be connected to the feeder because it mainly depends on customers who own the PV systems. Thus, for planning a spect, the proper load models and operating mode of inverter are required to accurately find the PV-DG size solution. H owever, t he s imulation r esult f rom C ase-2 s hows t hat t he ha rmonic distortion voltage can be high depending on the distance away from a substation (see Fig. 5.27). Therefore, it may require the harmonic filter if the PV-DGs are located at the end of feeder, especially the large size of PV-DG.

5.4.3 <u>Scenario-3</u>: Effect of i nverter m odeling and e xisting D Gs i n a distribution system on optimal PV-DG sizing

The purpose of this scenario is to study an effect on optimal PV-DG sizing in a distribution system using different PV inverter models (i.e., 6-pulse, 12-pulse and PWM) and existing DGs with various operating conditions.

A heavy load 23 kV radial distribution system is employed as a test case in this scenario. All system parameter are given in Appendix C, which can be found in [85]. The test system has 33 buses with a total load of 9.29 MW, 5.75 MVar as shown in Figure 5.28. The results of base case deterministic load flow are given in Appendix D. And the system operating conditions in this scenario are given as:

- Substation voltage is set to $1.0 \angle 0^\circ$ constant.
- Load demand is assumed to be random variables with normal distribution, which standard deviations (σ) is set to 10%.

- Power factor of PV-DG is assumed to be 1.0 constant.
- Load model is assumed to be constant power load.
- Background harmonics are not considered in this test system.
- Various ope rating c onditions of e xisting DGs in tests ystem are considered.
- Only voltage and THDv constraints are considered in this scenario.
- Range of *PV_{size}* on this study is between 0.2 MWp to 13 MWp with a 0.2 MWp increment.



Figure 5.28 Single-line diagram of the 33-bus test system

For t he pur pose of t his s tudy, it is a ssumed that the single PV-DG installation is located at bus-10. Two cases are studied for investigating the effect of inverter models and existing DGs on optimal PV-DG sizing.

<u>Case-1</u>: Optimal PV-DG sizing without consideration of existing DGs

This cas e s hows t he s election of optimal PV-DG s ize ba sed on t he technical constraints without consideration of e xisting DGs us ing different inverter models, which the typical harmonic current spectra are given by:

- Using data in Table 4.2 from chapter 4 for 6-pulse and 12 pulse inverter models.
- Using d ata b ased on m easurements of grid-connected inverter (SMC-11000TL) from a PV farm for PWM inverter model.



Figure 5.29 Average system losses as a function of average PV-DG power output without consideration of existing DGs

Figure 5.29 presents the relationship between the average system loss and the average PV-DG active power output. From this figure, the system losses vary with the size of PV-DG installed at bus-10. The average system loss without installing PV-DG is 375.1 kW. Besides, the system losses decrease when installing PV-DG less than 12.2 MWp. The minimum average system loss in this case is 271.3 kW, which is given by installing a PV-DG at 5.8 MWp. While the average active power output of PV-DG is around 2.5 MW.

The c umulative pr obability of vol tage a t bus -10 with a nd w ithout installation of 5.8 MWp PV-DG is shown in Figure 5.30. Similarly to scenarios 1 and 2, an installation of PV-DG mostly improves the voltage regulation at the PCC. Note from t he figure, it s hows t hat t he hi ghest vol tage l evel at bus -10 stays w ithin an acceptable limits (i.e., 1.05 pu). Since, however, the test system in this case has heavy load and there is no any compensator elements to regulate the voltage rise up. Hence, voltage at some node before installing PV-DG is lower the limits (i.e., 0.95 pu), this can be found in base case deterministic load flow solution as given in Appendix D. By

this reason, the minimum voltage at bus-10 may lower than the limits after installing PV-DG. However, the probability at which voltage at bus-10 lower than 0.95 pu i s 0.1, and it can be acceptable for this system.



Figure 5.30 Cumulative probability of voltage at bus-10 without consideration of existing DGs

Figure 5.31 shows t he c omparison of T HDv values a t bus -10 us ing different PV inverter models. Since, it need to be installed high capacity of PV-DG (5.8 MWp) to minimize s ystem loss in this case. Therefore, the THDv values can exceed the limits for 6 -pulse and 12 -pulse i nverter models, especially the 6 -pulse inverter. This differs from PWM inverter that the THDv value is less than 2%. This indicates that a PWM technology can produce small voltage distortion waveform. In present, m ostly P V i nverter t echnologies a re b ased on P WM [83]. H owever, t he purpose of t his c ase n eeds t o s how t he distinction of T HDv values f rom us ing different PV inverter models in our study.

Furthermore, t o c omply w ith IEEE s tandard, PV-DG s ize s hould be reduced to 3.0 MWp for 6-pulse inverter. The average system loss is around 295 kW for this installation size, see Figure 5.29.



Figure 5.31 Cumulative probability of THDv at bus-10 using different inverter models without consideration of existing DGs

<u>Case-2</u>: Optimal PV-DG sizing with consideration of existing DGs

This case shows the effect of optimal PV-DG sizing with consideration of existing D Gs in distribution system. Using different inverter models a realso presented to compare THDv values with Case-1. For the purpose of study case, the locations of existing DGs as well as its operating conditions and capacity are given in Table 5.5.

Location Bus	DGs capacity (MW)	DG type	Operating mode
13	1.5	Synchronous	PF. 1.0
25	1.0	Induction	PF. 0.85 leading
33	1.0	Synchronous	PF. 0.95 lagging

Table 5.5 Existing DGs locations, capacity and its operating conditions

As shown in Figure 5.32, it needs to install 2.6 MWp PV-DG to minimize average system loss, which approximately reduced 50% compared with Case-1 (5.8 MWp). This is due to highly generation power of the existing DGs (3.5 MW). So, the average s ystem loss be fore installing PV-DG is more decreased than Case-1 (178 kW). From the figure, the minimum average s ystem loss is 163.6 kW in this case, while the average active power output of PV-DG is around 1.12 MW.



Figure 5.32 Average system losses as a function of average PV-DG power output with consideration of existing DGs

Figure 5.33 s hows c omparison of the voltage c umulative probability at bus-10 before and after installation of 2.6 MWp PV-DG. The voltage level at bus-10 stays within an acceptable range in this case. Note from the figure, it shows that the minimum voltage at bus-10 is higher than Case-1 and kept within the limits, when the existing DGs are presented.



Figure 5.33 Cumulative probability of voltage at bus-10 with consideration of existing DGs

Since the reducing more of PV-DG capacity in Case-2, consequence the THDv values are within the limits for all PV inverter model as shown in Figure 5.34. Similarly to Case-1, however, it indicates that the PWM technology can produce very small voltage distortion waveform, which less than 1% in this case.



Figure 5.34 Cumulative probability of THDv at bus-10 using different inverter models with consideration of existing DGs

From the results in Scenario-3, it c an be summarized that different PV inverter models have effect to optimal size of PV-DG. It demonstrates that the 6-pulse inverter modeling may produce high THDv values at PCC, while the PWM inverter modeling can produce very small THDv values. The THDv values produced from the 12-pulse inverter are in between these two, as seen in Figures 5.31 and 5.34. From these figures, it indicates that int erconnection of s mall P V-DG may not r esult in violation of the power quality standard. However, the THDv values are comply with standard for P WM inverter in all case. While PV-DG size may reduced for 6-pulse and 12 -pulse i nverters, as s hown in C ase-1. Furthermore, a ddition ot her D Gs i n distribution system can effect is to decrease PV-DG size to minimize system losses.

CHAPTER VI

CONCLUSIONS AND FUTURE WORKS

6.1 Conclusions

This dissertation presents a probabilistic approach to calculate an optimal size of PV-DG in a distribution system. The stochastic variables of both generation and I oad have been considered. The proposed technique is based on actual hourly solar radiation, ambient temperature and typical harmonic currents of grid-connected inverter in Thailand. The results from all scenarios show that the proposed technique is effectively to obtain optimal sizes of PV-DGs for both single and multiple locations based on technical constraints.

From s everal s ystem o perating c onditions, it can be s ummarized the optimal PV-DGs sizing based on this approach as follows:

- It need to be collected the data of hourly variations of solar radiation and ambient temperature for a site of interest.
- In practical, a validation of PV model is necessary to accurate the power output of PV-DG corresponding to solar radiation and temperature.
- In pl anning as pect, a m easurement of h armonic cur rent s pectra of P V inverter is necessary to assess the power quality.
- By applying this technique, optimal sizes of PV-DGs can be determined taking into account background harmonics. A nd With high background harmonics or with high c apacity of P V-DGs, %THDv at P CC m ay increase and not satisfy the standard.
- Different static load models do not impact on optimal PV-DGs sizes. And THDv values depend on PV-DG sizes more than load models.
- Leading power factor operation changes optimal PV-DG size but lagging operation has low impact on optimal PV-DG size.
- High distortion voltage waveform may be produced by 6-pulse and 12pulse inverter modeling causes THDv values exceed the limits. While the PWM i nverter m odeling c an pr oduce ve ry s mall di stortion ha rmonic voltage and satisfied the standard.

- Additional DGs in a distribution system may lead to decrease optimal PV-DG size to minimize system losses.
- The PV-DGs are likely to improve voltage regulation and decrease system losses in a distribution system, but increase THDv values at PCC.

6.2 Future Works

In order to determine the optimal PV-DGs sizes in a distribution system for future studies. Some further issue described below may be of interest.

- It is possible for applying the proposed method to determine optimal size and location of PV-DG at the same time while satisfying the number of constraints described in this works. The Genetic Algorithm (GA) may be used for this issue.
- Other technical constraints such as distribution line current limits can also be added into the proposed algorithm.
- The impact of PV-DG on protection coordination should be studied.
- The coordination of voltage regulation equipments in distribution system may be incorporate with optimal PV-DGs sizing.

REFERENCES

- [1] IEEE S tandard 1 547-2003, <u>IEEE S tandard f or Interconnecting Distributed</u> <u>Resources with Electric Power Systems</u>.
- [2] Philip, P. Barder, and R obert, W. de M ello. Determining the impa ct of Distributed G eneration on P ower S ystems: Part1-Radial D istribution Systems. in <u>Power Engineering Society Summer Meeting</u> 3 (July 2000): 1645-1656.
- [3] Frede B laabjerg, Remus T eodorescu, Marco Liserre, and Adrian, V. T imbus. Overview o f C ontrol a nd G rid S ynchronization f or D istributed P ower Generation Systems. <u>IEEE Tr ans. Industrial E lectronics</u> 53, 5 (October 2006): 1398-1409.
- [4] International E nergy A gency (IEA-PVPS). <u>Cumulative Installed PV P ower</u>[Online]. 2010. Available from: http://www.iea-pvps.org [2011, June]
- [5] M., Shahidehpour, and F., Schwartz. Don't let the sun go down on P V. <u>IEEE</u> <u>Power Energy Magazine</u> 2 (May/June 2004): 40-48.
- [6] SEARCA Knowledge Center on Climate Change. <u>Thailand's Solar Lessons for</u> <u>the W orld</u> [Online]. 2011. Available from: http://www.beta.searca.org [2011, June]
- [7] Denis L enardic. <u>Large-Scale P hotovoltaic P ower P lants Annual R eview 2008</u>
 [Online]. 2009. Available from: http://www.pvresources.com [2011, June]
- [8] First S olar. <u>PV T echnology C omparison</u> [Online]. 2011. Available from: http://www.firstsolar.com [2011, June]
- [9] Gilbert, M. Masters. <u>Renewable and Efficient Electric Power Systems</u>. A John Wiley & Sons Inc., 2004.
- [10] Solar Energy Development Programmatic EIS. <u>Solar Photovoltaic Technologies</u> [Online]. 2011. Available from : http://www.solareis.anl.gov/guide/solar/ pv/index.cfm [2011, June]
- [11] Solar Energy Development P rogrammatic E IS. <u>Concentrating S olar P ower</u> <u>Technology</u> [Online]. 2011. Available from: http://www.solareis.anl.gov [2011, June]

- [12] Department of A lternative Energy D evelopment a nd E fficiency (DEDE).
 Ministry of Energy in Thailand. <u>Thailand Energy Situation 2010</u> [Online].
 2010. Available from: http://www.dede.go.th [2011, July]
- [13] System P lanning Division. Electricity Generating A uthority of T hailand.
 <u>Summary of T hailand P ower D evelopment P lan 2010 2030</u> Report no.
 912000-5305, April 2010.
- [14] Department of A lternative E nergy D evelopment a nd E fficiency (DEDE).
 Ministry of Energy in Thailand. <u>Solar Map of Thailand</u> [Online]. 1999.
 Available from: http://www.dede.go.th [2011, August]
- [15] Department of A Iternative E nergy D evelopment a nd E fficiency (DEDE). Ministry of E nergy in T hailand. <u>PV S ystems Installation Status in</u> <u>Thailand since 1983-2010</u> [Online]. 2011. Available from: http://www. dede.go.th [2011, August]
- [16] Victor, H. Mendez Q uezada, Juan Rivier Abbad, and T omas G omez S an Roman. Assessment o f E nergy Distribution Losses f or Increasing Penetration of Distributed Generation. <u>IEEE Trans. Power System</u> 21, 2 (May 2006): 533-540.
- [17] Daniel, S. S hugar. Photovoltaic in the Utility Distribution System: T he Evaluation of S ystem a nd D istributed B enefits. in <u>Proc. C onference</u> <u>Record of the 21st IEEE Photovoltaic Specialists Conference, Kissimmee</u> 2 (1990): 836-843.
- [18] T., lchikawa. Recent R esearch and D evelopment on P ower S ystems with a Large Number of Distributed Generating Facilities. in <u>Transmission and</u> <u>Distribution Conference and Exhibition 2002: Asia Pacific. IEEE/PES</u> 2 (October 2002): 1367-1369.
- [19] Jung Hun So, Young Seok Jung, Byung Gyu Yu, Hye Mi Hwang, and Gwon Jong Yu. Performance Results and Analysis of Large Scale PV System. in <u>Photovoltaic Energy Conversion Conference Record of the 2006 IEEE</u> <u>4th World Conference</u> 2 (May 2006): 2375-2378.
- [20] Alejandro, R. Oliva, and Juan Carlos B alda. A P V D ispersed Generator: A Power Q uality Analysis W ithin the IEEE 51 9. <u>IEEE Tr ans. Power</u> <u>Delivery</u> 18, 2 (April 2003): 525-530.

- [21] K., Tran, and M., Vaziri. Effects of Dispersed Generation (DG) on Distribution Systems. in <u>Power Engineering Society General Meeting</u> 3 (June 2005): 2173-2178.
- [22] A., Bhowmik, A., Maitra, A. M., Halpin, and J. E., Schatz. Determination of Allowable Penetration Levels of Distributed Generation Resources Based on Harmonic Limit C onsideration. <u>IEEE Tr ans. Power D elivery</u> 18, 2 (April 2003): 619-624.
- [23] R., Dugan, M., McGranaghan, and H. W., Beaty. <u>Electrical Power Systems</u> <u>Quality</u>. McGraw-Hill, 1996.
- [24] N., Mohan, T., Undeland, and W., Robbins. <u>Power E lectronics: C onverters</u> <u>Applications and Design</u>. John Wiley & Sons, 1995.
- [25] Johan, H.R. Enslin, and Peter, J.M. Heskes. Harmonic Interaction Between a Large N umber of D istributed P ower Inverters a nd t he D istribution Network. <u>IEEE Trans. Power Electronics</u> 19, 6 (November 2004): 1586-1593.
- [26] M.C., Benhabib, J.M.A., Myrzik, and J.L., Duarte. Harmonic effects caused by large s cale P V installations in LV network. in <u>Electrical Power Quality</u> and <u>Utilisation 2007, 9th International Conference</u> (October 2007): 1-6.
- [27] Florentin Batrinu, Gianfranco Chicco, Jurgen Schlabbach, and Filippo Spertino. Impacts of grid-connected phot ovoltaic pl ant operation on t he harmonic distortion. in <u>IEEE MELECON</u> (May 2006): 861-864.
- [28] Andrew Kotsopoulos, Peter, J.M. Heskes, and Mark, J. Jansen. Zero-Crossing Distortion in Grid-Connected P V Inverters. <u>IEEE Tr ans. Industrial</u> <u>Electronics</u> 52, 2 (April 2005): 558-565.
- [29] A.R., Oliva, J.C., Balda, D.W., McNabb, and R.D., Richardson. Power-Quality Monitoring of a PVG enerator. <u>IEEE T rans. E nergy C onversion</u> 13, 2 (June 1998): 188-193.
- [30] S., Yanagawa, T., Kato, K., Wu, A., Tabata, and Y., Suzuoki. Evaluation of LFC capacity for out put fluctuation of photovoltaic generation systems based on m ulti-point observation of i nsolation. in <u>Proc. IEEE P ower</u> <u>Engineering Society Summer Meeting</u> (2001): 1652-1657.

- [31] Walid, A. Omran, and M., Kazerani. Investigation of Methods for Reduction of Power Fluctuations Generated From Large Grid-Connected Photovoltaics Systems. IEEE Trans. Energy Conversion 26, 1 (March 2011): 318-327.
- [32] Y.T., Tan, D.S., Kirschen, and N., Jenkins. A model of PV generation suitable for stability analysis. <u>IEEE Trans. Energy Conversion</u> 19, 4 (Dec 2004): 748-755.
- [33] Achim W oyte, V u V an T hong, R onnie B elmans, and J ohan Nijs. Voltage Fluctuations on D istribution Level Introduced b y P hotovoltaic Systems. <u>IEEE Trans. Energy Conversion</u> 21, 1 (March 2006): 202-209.
- [34] P., Chen, Z., Chen, B., Bak-Jensen, R., Villafafila, and S., Sorensen. Study of Power Fluctuation from Dispersed Generations and loads and its impact on a Distribution Network through a probabilistic approach. in <u>Electrical</u> <u>Power Q uality and Utilisation 2007, 9th International C onference</u> (October 2007): 1-5.
- [35] Benoit BLETTERIE, and Tomaz PFAJFAR. Impact of Photovoltaic Generation on V oltage V ariations-How S tochastic is P V. in <u>19th I nternational</u> <u>Conference on Electricity Distribution (CIRED), Vienna</u> 513 (May 2007): 1-4.
- [36] T., Kinjo, T., Senjyu, N., Urasaki, and H., Fujita. Output levelling of renewable energy b y el ectric dou ble l ayer capacitor applied for ene rgy s torage system. <u>IEEE Trans. Energy Conversion</u> 21, 1 (March 2006): 221-227.
- [37] Md., H. Rahman, and S., Yamashiro. Novel di stributed power g enerating system of PV-ECaSS using solar energy estimation. <u>IEEE Trans. Energy</u> <u>Conversion</u> 22, 2 (June 2007): 358-367.
- [38] J. P., Barton, and D. G., Infield. A probabilistic m ethod for calculating the usefulness of a store with finite energy capacity for smoothing electricity generation f rom w ind a nd solar pow er. <u>Journal of P ower S ources</u> 162 (2006): 943-948.
- [39] R., Wanger. Large lead/acid batteries for frequency regulation, load levelling and solar power applications. Journal of Power Sources 67 (1997): 163-172.

- [40] H., Sugihara, S., Nishikawa, and Y., Kimura. Observation of the hybrid system using photovoltaic and sodium-sulphur battery. in <u>Proc. JSES/JWEA Joint</u> <u>Conference</u> (2001): 13-16.
- [41] H., Miyauchi, K., Eguchi, a nd H., Hayashi. SEMS t o power quality improvement. in <u>Proc. IEEJ C onference of P ower and E nergy S ociety</u> (2002): 110-115.
- [42] J., Thongpron, U., Sangpanich, C., Limsakul, D., Chenvidya, K., Kirtikara, and C., Jivacate. Study of a P V-Grid C onnected S ystem on i ts O utput Harmonics and Voltage Variation. <u>Asian J. Energy Environ</u> 5, 1 (2004): 59-73.
- [43] D., Chenvidya, J., Thongpron, U., Sangpanich, N., Wongyao, K., Kirtikara, and C., Jivacate. A T hai National D emonstration Project on P V G rid-Interactive Systems: Power Quality Observation. in <u>3rd World Conference</u> on P hotovoltaic E nergy C onversion, O saka J apan (May 2003): 2152 -2154.
- [44] M.A., Kashem, An, D.T. Le, M., Negnevitsky, and G., Ledwich. Distributed Generation for M inimization of P ower Losses in D istribution S ystems. in <u>Conference on Power E ngineering S ociety G eneral M eeting</u> (June 2006): 1-8.
- [45] L., Ramesh, S.P., Chowdhury, S., Chowdhury, Y.H., Song, and A.A., Natarajan. Voltage Stability Analysis and Real Power Loss Reduction in Distributed Distribution System. in <u>Transmission and Distribution C onference a nd</u> <u>Exposition (IEEE/PES)</u> (April 2008): 1-6.
- [46] Yue Yu an, K ejun Q ian, and C hengke Zhou. The O ptimal Location and Penetration Level of Distributed Generation. in <u>42nd International</u> <u>Universities P ower Engineering C onference (UPEC)</u>, Brighton <u>University</u>, UK (September 2007): 917-923.
- [47] G., Celli, E., Ghiani, S., Mocci, and F., Pilo. A Multi-Objective Approach to Maximize the P enetration of D istributed Generation in Distribution Networks. in <u>9th International C onference on P robabilistic M ethods</u> <u>Applied to Power Systems, Stockholm, Sweden</u> (June 2006): 1-6.
- [48] Hamid Falaghi, and M ahmood-Reza H aghifam. ACO B ased Algorithm f or Distributed G eneration Sources A llocation a nd S izing i n D istribution Systems. in <u>Power T ech'07 C onference</u>, <u>Lausanne</u>, <u>S witzerland</u> (July 2007): 555-560.
- [49] M.F., AlHajri, and M.E., El-Hawary. Improving t he vol tage pr ofiles of Distribution Networks using mul tiple D istribution Generation Sources. in <u>Conference on P ower E ngineering</u>, <u>Large E ngineering S ystems</u> (October 2007): 295-299.
- [50] Kai Z ou, A.P., Agalgaonkar, K.M., Muttaqi, and S., Perera. Optimisation of Distributed G eneration U nits a nd Shunt C apacitors f or E conomic Operation of D istribution Systems. in <u>Australasian Universities P ower</u> <u>Engineering Conference (AUPEC)</u>, Australia (2008): P-137/1-P-137/7.
- [51] Raj K umar S ingh, Nalin, B. D ev C houdhury, and S.K., Goswami. Optimal Allocation of Distributed Generation in Distribution Network with Voltage and F requency D ependent L oads. in <u>IEEE R egion 10</u> Colloquium and the Third ICIIS, Kharagpur, India (December 2008): 1-5.
- [52] R.K., Singh, and S.K., Goswami. Optimal S iting a nd Sizing of D istributed Generations i n R adial and N etworked S ystems C onsidering D ifferent Voltage D ependent S tatic Load Models. in <u>2nd IEEE I nternational</u> <u>Conference on P ower a nd E nergy (PECon), J ohor B ahary, M alaysia</u> (December 2008): 1535-1540.
- [53] Soo-Hyoung Lee, and Jung-Wook Park. Selection of Optimal Location and Size of M ultiple D istributed Generations b y Using K alman Filter Algorithm. <u>IEEE Trans. Power Systems</u> 24, 3 (August 2009): 1393-1400.
- [54] M.F., AlHajri, and M.E., El-Hawary. The E ffect of D istributed G eneration Modeling and S tatic Load R epresentation on the O ptimal Integrated Sizing a nd N etwork Losses. in <u>Canadian Conference on Electrical a nd</u> <u>Computer Engineering (CCECE)</u> (May 2008): 1543-1548.
- [55] S., Kamalinia, S., Afsharnia, M.E., Khodayar, A., Rahimikian, and M.A. Sharbafi. A Combination of MADM and Genetic Algorithm for Optimal DG Allocation in Power Systems. in <u>42nd International Universities Power</u> <u>Engineering C onference (UPEC), B righton U niversity, UK</u> (September 2007): 1031-1035.

- [56] M., Gandomkar, M., Vakilian, and M., Ehsan. A C ombination of G enetic Algorithm a nd Simulated Annealing f or O ptimal D G A llocation in Distribution N etworks. in <u>18th</u> Canadian C onference on Electrical an d <u>Computer Engineering</u>, Saskatoon, S askatchewan C anada (May 2005): 645-648.
- [57] G.B., Shrestha, and L., Goel. A S tudy on Optimal S izing of S tand-Alone Photovoltaic S tations. <u>IEEE Trans. Energy Conversion</u> 13, 4 (December 1998): 373-378.
- [58] H.A.M., Maghraby, M.H., Shwehdi, and G.K., Al-Bassam. Probabilistic Assessment of Photovoltaic (PV) Generation Systems. <u>IEEE Trans. Power</u> <u>System</u> 17, 1 (February 2002): 205-208.
- [59] Eiichi Endo and Kosuke Kurokawa. Sizing Procedure for Photovoltaic Systems. in <u>First WCPEC, Hawaii</u> (December 1994): 1196-1199.
- [60] Ferry, A. Viawan, Ferruccio V uinovich, and Ambra S annino. Probabilistic Approach t o the D esign of P hotovoltaic D istributed G eneration in Low Voltage F eeder. in <u>9th International Conference on Probabilistic Methods</u> Applied to Power Systems. KTH, Stockholm, Sweden (June 2006): 1-7.
- [61] Christoph M ayr, R oland B rundlinger, and Benoit B letterie. Photovoltaicinverters as Active Filters to improve Power Quality in the Grid. What can State-of-the-art E quipment A chieve. in <u>9th International C onference on</u> <u>Electrical Power Quality and Utilisation.-Barcelona</u> (October 2007): 1-5.
- [62] G., Carpinelli, G., Celli, S., Mocci, F., Pilo, D., Proto, and A., Russo. Multiobjective Programming for the Optimal Sizing and Siting of Power-Electronic Interfaced D ispersed Generators. in <u>Power T ech'07</u> <u>Conference, Lausanne, Switzerland</u> (July 2007): 443-448.
- [63] International E lectrotechnical C ommission, <u>IEC 61727 P hotovoltaic (PV)</u> <u>systems – Characteristics of the Utility Interface</u>, June 1995.
- [64] IEEE Standard 519-1992, <u>IEEE Recommended Practices and Requirements for</u> <u>Harmonic Control in Electrical Power Systems</u>, 1992.
- [65] Roy B illiton, and Wenyuan Li. <u>Reliability A ssessment of E lectric P ower</u> <u>Systems Using Monte Carlo Methods</u>. Plenum Press, New York, 1994.

- [66] Geoff W alker, Evaluating M PPT C onverter T opologies U sing A M atlab P V Model. Journal of Electrical & Electronics Engineering, Australia, vol. 21, 2001, pp. 49-55.
- [67] J.A., Gow, and C. D., Manning. Development of a photovoltaic array model for use in power electronics simulation studies. <u>IEEE Proceedings on Electric</u> <u>Power Applications</u> 146, 2 (March 1999): 193-200.
- [68] Eduardo L orenzo. <u>Solar E lectricity Engineering o f P hotovoltaic Systems</u>. Progensa, Spain, 1994.
- [69] Anca, D. Hansen, Poul Sorensen, Lars, H. Hansen, and Henrik Bindner. Models for a S tand-Alone P V s ystem. A s tand-alone P V s ystem mode ling a nd simulation report. <u>Riso N ational Laboratory, R oskilde,</u> <u>Denmark (December 2000): 1-78.</u>
- [70] R., Faranda, S., Leva, and V., Maugeri. MPPT t echniques f or P V S ystem: energetic and cost comparison. i n <u>Power and Energy S ociety G eneral</u> <u>Meeting - Conversion and D elivery of E lectrical E nergy i n t he 21 st</u> <u>Century</u> (July 2008): 1-6.
- [71] Trishan Esram, and Patrick, L. Comparison of Photovoltaic A rray Maximum Power P oint T racking T echniques. <u>IEEE T ransactions on E nergy</u> <u>Conversion</u> 22, 2 (June 2007): 439-449.
- [72] Hanifi Guldemir. Sliding Mode Control of Dc-Dc Boost Converter. Journal of <u>Applied Sciences</u> 5, 3 (2005): 588-592.
- [73] N., Mithulananthan, and C. A., Canizares. Effect of Static Load Models on Hopf Bifurcation P oint a nd Critical M odes of P ower S ystems. <u>Thammasat</u> <u>International Journal Science and Technology</u> 9, 4 (October 2004): 69-76.
- [74] U., Eminoglu, and M. H., Hocaoglu. A Voltage S tability Index f or R adial Distribution N etworks. in <u>International U niversities P ower E ngineering</u> <u>Conference (UPEC)</u> (2007): 408-413.
- [75] M., Charkravorty, and D., Das. Voltage S tability A nalysis of Radial Distribution N etworks. <u>International Journal of E lectrical P ower &</u> <u>Energy Systems, Elsevier</u> 23, 2 (2001): 129-135.
- [76] D., Das, D. P., Kothari, and A., Kalam. Simple and efficient method for load flow s olution of r adial di stribution ne tworks. <u>International J ournal of</u> <u>Electrical Power & Energy Systems, Elsevier</u> 17, 5 (1995): 335-346.

- [77] Ashokkumar, R., and Aravindhababu, P. An Improved Power flow Technique for D istribution Systems. <u>Journal of C omputer S cience</u>, <u>Informatics &</u> <u>Electrical Engineering 3</u>, 1 (2009): 1-8.
- [78] Fan Zhang, and C arol, S. C heng. A M odified N ewton M ethod f or Radial Distribution System Power Flow Analysis. <u>IEEE Trans. Power System</u> 12, 1 (February 1997): 389-397.
- [79] W.F., Tinney, and C.E., Hart. Power Flow Solution by Newton's Method. <u>IEEE</u> <u>Trans. Power App. System</u> PAS-86 (November 1967): 1449-1460.
- [80] Behic, R. G ungor, <u>Power S ystems</u>. Harcourt Brace J ovanovich, P ublishers, Florida, 1988.
- [81] Robert, A., Deflandre, T., and Working Group CC02, ELECTRA No. 16: <u>Guide</u> for Assessing the Network Harmonic Impedance, 1996.
- [82] Nick J enkins, R on A llan, P eter C rossley, David Kirschen, and G oran Strbac. <u>Embedded G eneration</u>. The Institution of E lectrical E ngineers, 2000.
- [83] IEA. Grid-connected PV pow er s ystems: S urvey of i nverter a nd related protection equipments. <u>Task V report IEA-PVPS</u> (December 2002).
- [84] Pradit F uangfoo. <u>The Impact of D istributed G eneration on T he T hailand's</u> <u>Electric P ower S ystem</u>. Doctoral dissertation, Faculty of t he Graduate School of The University of Texas at Arlington, 2006.
- [85] Vichakorn Hengsritawat. Optimal Shunt Capacitor Sizing and Location on the <u>Radial D istribution System</u>. Master's Thesis, Department of Electrical Engineering, Chulalongkorn University, 1998.
- [86] Department of A lternative E nergy D evelopment a nd E fficiency (DEDE), Ministry of Energy in Thailand.
- [87] Thai Meteorological Department, Ministry of Information and Communication Technology of Thailand.

APPENDICES

Appendix A

Hourly Variations of Solar Radiation and Ambient Temperature of

Chiang Mai Province

(During 6.00 to 18.00 on Jan-Dec 2007)

A1. Hourly and daily solar radiation (MJ/m²) [86]

January

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1													
2													
3	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.842	0.265	1.108
4	0.000	0.090	0.540	1.482	2.168	2.561	2.735	2.673	2.265	1.658	0.966	0.251	17.388
5	0.000	0.086	0.527	1.445	2.076	2.475	2.679	2.622	2.232	1.661	0.960	0.231	16.995
6	0.000	0.142	0.632	1.030	2.023	2.389	2.500	2.581	2.203	1.689	1.002	0.264	16.454
7	0.000	0.100	0.527	0.938	2.059	2.602	2.781	2.733	2.153	1.561	0.428	0.155	16.038
8	0.000	0.080	0.551	0.755	1.428	2.390	2.792	2.671	2.394	1.788	1.056	0.326	16.232
9	0.000	0.088	0.584	1.529	2.160	2.586	2.759	2.679	2.317	1.773	1.093	0.315	17.883
10	0.000	0.092	0.573	1.436	1.994	2.502	2.669	2.591	2.265	1.681	0.969	0.264	17.036
11	0.000	0.088	0.573	1.459	2.070	2.479	2.685	2.576	2.181	1.655	0.957	0.242	16.966
12	0.000	0.096	0.532	1.368	1.978	2.391	2.679	2.555	2.198	1.798	1.028	0.256	16.879
13	0.000	0.088	0.528	1.402	2.007	2.443	2.674	2.474	2.171	1.552	0.953	0.277	16.571
14	0.000	0.110	0.517	1.384	1.928	2.437	2.594	2.583	2.211	1.682	1.053	0.335	16.832
15	0.000	0.091	0.533	1.526	2.147	2.581	2.796	2.714	2.343	1.789	1.082	0.366	17.968
16	0.000	0.076	0.526	1.570	2.189	2.587	2.810	2.732	2.391	1.883	1.155	0.374	18.294
17	0.000	0.089	0.497	1.464	2.056	2.469	2.692	2.611	2.297	1.751	1.065	0.331	17.322
18	0.000	0.082	0.476	1.515	2.185	2.639	2.853	2.796	2.449	1.858	1.184	0.398	18.434
19	0.000	0.085	0.482	1.458	2.088	2.529	2.740	2.679	2.348	1.784	1.116	0.387	17.698
20	0.000	0.080	0.506	1.631	2.232	2.685	2.878	2.817	2.465	1.889	1.165	0.385	18.735
21	0.000	0.083	0.511	1.588	2.216	2.656	2.864	2.803	2.528	1.936	1.205	0.411	18.803
22	0.000	0.089	0.510	1.535	2.160	2.595	2.844	2.819	2.480	1.942	1.218	0.432	18.631
23	0.000	0.082	0.486	1.470	2.057	2.458	2.653	2.545	2.244	1.720	1.081	0.346	17.145
24	0.000	0.110	0.430	0.863	1.024	1.784	2.315	2.439	2.090	1.538	0.986	0.303	13.886
25	0.000	0.111	0.498	1.105	1.016	2.183	2.354	2.396	2.191	1.704	0.997	0.315	14.876
26	0.000	0.101	0.482	1.364	2.015	2.460	2.637	2.567	2.275	1.703	1.053	0.380	17.042
27	0.000	0.086	0.473	1.286	1.911	2.306	2.556	2.421	2.247	1.530	0.683	0.299	15.804
28	0.000	0.045	0.346	0.717	1.104	1.224	1.194	1.069	0.414	0.284	0.364	0.080	6.841
29	0.000	0.115	0.529	1.364	2.020	2.486	2.662	2.671	2.349	1.795	1.067	0.344	17.414
30	0.000	0.086	0.472	1.165	1.645	2.140	2.491	2.444	2.045	1.665	0.988	0.342	15.493
31	0.000	0.094	0.461	0.843	1.687	1.984	1.905	1.880	1.317	1.206	0.845	0.375	12.612
Average	0.000	0.088	0.493	1.265	1.850	2.311	2.510	2.453	2.106	1.603	0.985	0.312	15.979

February

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.000	0.090	0.489	1.229	1.863	2.329	2.561	2.475	2.189	1.660	0.958	0.295	16.156
2	0.000	0.108	0.604	0.989	1.697	1.969	2.006	2.143	1.826	1.440	0.826	0.340	13.964
3	0.000	0.120	0.408	1.097	1.650	2.124	2.306	2.141	2.017	1.593	0.944	0.299	14.710
4	0.000	0.105	0.450	1.003	1.540	1.968	2.178	2.136	1.938	1.424	0.796	0.265	13.810
5	0.000	0.085	0.453	1.017	1.627	2.115	2.394	2.443	2.109	1.581	0.918	0.314	15.063
6	0.000	0.092	0.514	1.137	1.709	2.132	2.389	2.396	2.097	1.533	0.919	0.313	15.243
7	0.000	0.095	0.488	1.048	1.606	2.003	2.211	1.789	1.806	1.544	0.846	0.291	13.738
8	0.000	0.091	0.439	0.910	1.296	1.726	1.888	2.326	2.000	1.542	0.935	0.318	13.480
9	0.000	0.088	0.559	1.224	1.858	2.304	2.559	2.495	2.192	1.745	1.083	0.369	16.487
10	0.000	0.092	0.646	1.387	2.037	2.488	2.725	2.669	2.344	1.767	1.083	0.404	17.662
11	0.000	0.140	0.562	1.143	1.787	2.245	2.478	2.530	2.244	1.704	1.021	0.355	16.227
12	0.000	0.097	0.600	1.325	1.979	2.430	2.658	2.612	2.293	1.738	0.825	0.368	16.944
13	0.000	0.100	0.663	1.468	2.136	2.567	2.754	2.704	2.382	1.739	1.065	0.494	18.100
14	0.000	0.088	0.634	1.488	2.163	2.629	2.889	2.848	2.494	1.772	1.219	0.443	18.685
15	0.000	0.124	0.506	1.617	1.787	2.825	1.563	1.826	1.390	0.818	0.565	0.679	13.745
16	0.000	0.091	0.694	1.620	2.266	2.744	2.915	2.713	2.389	1.555	0.874	0.258	18.152
17	0.000	0.099	0.692	1.555	2.205	2.680	2.917	2.861	2.570	2.017	1.261	0.517	19.408
18	0.000	0.096	0.643	1.537	2.232	2.695	2.884	2.847	2.592	1.992	1.290	0.493	19.339
19	0.000	0.099	0.598	1.401	2.028	2.473	2.858	2.732	2.460	1.917	1.235	0.526	18.357
20	0.000	0.090	0.585	1.408	2.069	2.547	2.720	2.686	2.410	1.866	1.170	0.501	18.082
21	0.000	0.095	0.615	1.490	2.159	2.601	2.748	2.710	2.514	1.891	1.218	0.506	18.591
22	0.000	0.097	0.652	1.516	2.199	2.792	3.028	2.853	2.383	1.852	1.157	0.473	19.034
23	0.000	0.110	0.584	1.414	2.051	2.570	2.742	2.596	2.236	1.740	1.110	0.437	17.624
24	0.000	0.106	0.555	1.313	1.942	2.391	2.596	2.501	2.175	1.599	0.983	0.380	16.582
25	0.000	0.107	0.635	1.493	2.165	2.597	2.848	2.684	2.311	1.655	1.055	0.532	18.133
26	0.001	0.108	0.654	1.625	2.213	2.697	2.898	2.765	1.762	1.867	1.296	0.650	18.606
27	0.001	0.151	0.672	1.613	2.210	2.708	2.867	2.819	2.217	1.244	1.072	0.421	18.040
28	0.000	0.112	0.610	1.476	2.082	2.631	2.793	2.656	2.305	1.759	1.058	0.414	17.927
Average	0.000	0.103	0.579	1.341	1.948	2.428	2.585	2.534	2.202	1.663	1.028	0.416	16.853

March

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.000	0.103	0.551	1.338	1.947	2.385	2.531	2.479	2.219	1.614	0.968	0.358	16.519
2	0.000	0.108	0.514	1.261	1.884	2.518	2.670	2.780	2.312	1.676	1.081	0.469	17.314
3	0.001	0.124	0.605	1.480	2.075	2.499	2.677	2.402	2.114	1.544	0.963	0.375	16.890
4	0.001	0.111	0.529	1.216	1.791	2.266	2.202	2.197	1.958	1.533	0.910	0.277	15.013
5	0.000	0.094	0.501	1.170	1.669	2.054	1.767	1.636	1.154	1.404	0.711	0.191	12.386
6	0.000	0.073	0.599	1.174	1.530	1.846	2.216	2.283	2.298	1.671	1.017	0.409	15.155
7	0.001	0.146	0.988	1.755	2.199	2.695	3.044	2.995	2.622	2.018	1.223	0.492	20.226
8	0.004	0.145	0.837	1.570	2.294	2.740	2.843	2.922	2.530	1.933	1.267	0.460	19.583
9	0.002	0.166	1.015	1.776	2.413	3.063	3.222	3.056	2.556	2.046	1.364	0.562	21.291
10	0.002	0.148	0.667	1.219	1.774	2.227	2.410	2.507	2.214	1.563	0.959	0.354	16.078
11	0.002	0.125	0.641	1.217	1.711	2.185	2.413	2.389	2.164	1.408	0.955	0.343	15.582
12	0.002	0.125	0.553	1.084	1.554	2.017	2.216	2.181	1.961	1.385	0.794	0.305	14.208
13	0.002	0.125	0.517	0.983	1.426	1.796	1.832	1.734	1.437	1.020	0.572	0.217	11.688
14	0.004	0.142	0.596	1.160	1.717	2.217	2.399	2.182	1.833	1.344	0.879	0.301	14.802
15	0.005	0.174	0.753	1.462	2.036	2.563	2.736	2.624	2.267	1.690	1.000	0.428	17.779
16	0.005	0.176	0.723	1.339	1.818	2.394	2.584	2.131	2.065	1.677	0.952	0.310	16.222
17	0.006	0.197	0.539	1.356	1.860	1.487	1.468	1.631	1.523	0.849	0.615	0.432	12.022
18	0.007	0.200	0.727	1.341	1.838	2.191	2.423	2.387	2.052	1.585	0.985	0.421	16.194
19	0.006	0.192	0.579	1.261	1.941	2.435	2.545	2.574	2.308	1.871	1.232	0.535	17.512
20	0.007	0.211	0.690	1.258	1.863	2.328	2.517	2.575	2.318	1.834	1.146	0.455	17.259
21	0.013	0.297	0.996	1.754	2.422	2.822	3.022	2.990	2.665	2.053	1.252	0.387	20.737
22	0.013	0.284	0.958	1.634	2.323	2.833	3.032	2.972	2.626	1.981	0.983	0.497	20.191
23	0.013	0.307	1.114	1.912	2.686	3.253	3.414	3.262	2.892	2.234	1.451	0.630	23.232
24	0.011	0.252	0.840	1.546	2.247	2.718	3.045	2.951	2.484	1.807	1.033	0.417	19.394
25	0.010	0.252	0.837	1.551	2.247	2.804	3.066	2.921	2.485	1.778	1.064	0.469	19.535
26	0.013	0.281	0.919	1.619	2.284	2.836	3.033	3.023	2.518	1.967	1.256	0.548	20.349
27	0.017	0.292	0.919	1.625	2.280	2.787	3.069	3.120	2.772	2.318	1.467	0.624	21.363
28	0.016	0.307	0.980	1.723	2.435	2.963	3.201	3.232	2.910	2.104	1.339	0.512	21.787
29	0.017	0.314	0.953	1.675	2.328	2.788	3.004	2.990	2.642	2.049	1.311	0.518	20.646
30	0.013	0.215	0.778	1.577	2.254	2.793	3.038	2.034	0.382	1.333	0.500	0.325	15.400
31	0.021	0.357	1.126	1.935	2.623	3.082	3.259	2.960	1.436	1.722	1.149	0.587	20.316
Average	0.007	0.195	0.759	1.451	2.047	2.503	2.674	2.585	2.184	1.710	1.045	0.426	17.635

April

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.024	0.389	1.184	2.032	2.770	3.192	3.352	3.214	2.950	2.359	1.243	0.563	23.351
2	0.026	0.475	1.363	2.170	2.888	3.343	3.504	3.461	3.096	2.467	1.617	0.711	25.200
3	0.023	0.324	0.909	1.597	2.267	2.794	3.082	3.068	2.800	2.166	1.221	0.459	20.800
4	0.029	0.411	1.133	1.907	2.613	3.127	3.241	3.248	2.794	2.192	1.330	0.543	22.637
5	0.030	0.364	1.019	1.723	2.371	2.752	2.904	2.959	2.547	2.052	1.330	0.598	20.726
6	0.026	0.330	0.908	1.604	2.036	2.564	2.659	2.400	1.992	1.564	0.936	0.406	17.467
7	0.033	0.354	0.952	1.661	2.144	2.669	2.834	2.861	2.070	1.516	0.718	0.297	18.161
8	0.030	0.337	0.912	1.613	2.241	2.652	2.822	2.561	2.444	1.872	1.106	0.437	19.070
9	0.035	0.415	1.103	1.847	2.465	2.864	3.047	2.994	2.660	2.002	1.244	0.476	21.235
10	0.034	0.397	1.067	1.816	2.446	2.856	2.933	2.853	2.604	1.463	0.798	0.595	19.939
11	0.040	0.388	0.991	1.677	2.370	2.828	3.047	2.935	1.252	1.615	1.342	0.590	19.163
12	0.058	0.424	1.239	2.065	2.817	3.224	3.376	1.244	1.873	2.301	0.999	0.208	19.908
13	0.065	0.413	1.409	2.091	2.844	2.842	2.556	1.839	2.029	1.075	1.050	0.357	18.628
14	0.046	0.275	0.887	1.222	1.376	1.156	2.138	2.198	1.996	0.434	0.480	0.385	12.633
15	0.034	0.248	0.881	1.525	2.496	2.983	3.038	2.461	1.812	0.736	0.270	0.111	16.620
16	0.054	0.430	1.112	1.732	1.975	3.151	3.623	2.562	1.229	0.993	0.476	0.204	17.583
17	0.058	0.458	0.899	2.183	2.592	2.491	2.508	3.189	1.608	1.154	1.374	0.318	18.933
18	0.074	0.637	1.443	2.214	2.705	3.335	3.207	0.570	1.664	2.628	1.302	0.172	19.975
19	0.056	0.377	0.411	0.675	1.793	3.312	3.201	3.434	3.061	2.418	1.620	0.806	21.287
20	0.083	0.700	1.571	2.381	3.041	3.489	3.658	3.532	3.124	2.401	1.718	0.839	26.669
21	0.086	0.731	1.583	2.404	3.089	3.495	3.619	3.469	2.974	2.473	1.467	0.853	26.382
22	0.094	0.755	1.587	2.387	3.024	3.437	3.551	3.462	3.174	2.561	1.757	0.747	26.675
23	0.092	0.725	1.587	2.419	3.088	3.533	3.624	3.534	3.089	2.430	1.150	0.695	26.153
24	0.097	0.719	1.541	2.322	2.967	3.410	3.542	3.421	3.016	2.370	1.559	0.755	25.791
25	0.097	0.691	1.484	2.228	2.859	3.304	3.495	3.313	2.247	2.231	1.366	0.654	24.110
26	0.024	0.178	0.537	1.544	1.442	2.154	3.557	3.279	2.950	2.271	0.849	0.372	19.380
27	0.047	0.714	1.628	2.449	3.100	3.489	3.661	2.926	2.434	1.665	1.833	0.307	24.371
28	0.051	0.167	0.459	1.776	2.780	3.655	3.845	3.533	2.953	1.643	1.798	0.791	23.562
29	0.073	0.396	1.555	2.391	3.055	3.549	2.119	0.774	2.006	1.024	0.848	0.985	18.867
30	0.094	0.784	1.621	2.450	2.970	3.577	3.837	2.413	1.877	0.813	1.570	0.935	23.070
Average	0.054	0.467	1.166	1.937	2.554	3.041	3.186	2.790	2.411	1.830	1.212	0.539	21.278

May

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.133	0.579	1.424	2.311	2.617	3.052	3.406	3.545	3.101	2.594	1.761	0.960	25.720
2	0.090	0.733	0.938	1.807	2.275	3.074	2.912	1.656	2.321	1.486	1.084	0.537	18.969
3	0.046	0.161	0.251	0.534	0.742	1.512	1.944	1.906	1.520	1.749	0.683	0.263	11.379
4	0.029	0.147	0.333	0.741	0.764	0.926	0.420	0.780	0.745	0.679	0.385	0.207	6.200
5	0.028	0.067	0.146	0.336	0.666	1.342	1.892	1.311	1.031	1.064	0.492	0.130	8.534
6	0.052	0.258	0.340	0.378	0.955	0.910	1.296	1.541	2.017	1.961	1.162	0.581	11.562
7	0.091	0.476	0.673	1.538	2.043	1.832	1.486	2.198	2.272	2.637	0.898	0.417	16.620
8	0.024	0.181	0.503	1.211	2.555	2.994	2.748	3.359	3.072	2.500	0.628	0.427	20.271
9	0.130	0.641	1.353	1.733	2.685	2.491	2.216	3.593	2.917	2.630	1.761	0.643	22.852
10	0.113	0.167	0.668	1.036	2.903	3.537	3.297	2.429	2.914	2.612	1.863	0.942	22.504
11	0.043	0.241	0.665	0.965	1.196	1.972	2.861	3.209	2.159	1.600	0.689	0.415	16.139
12	0.054	0.460	1.226	2.142	1.805	1.979	1.394	0.325	0.252	0.047	0.117	0.333	10.285
13	0.050	0.181	0.287	0.963	0.554	1.101	1.785	1.570	0.989	0.791	1.185	0.609	10.178
14	0.065	0.224	0.577	1.490	0.484	2.158	1.111	1.930	2.606	2.205	1.383	0.342	14.595
15	0.074	0.511	1.578	1.861	1.398	1.363	2.893	3.420	2.540	0.252	0.974	0.853	17.772
16	0.119	0.511	1.734	2.546	3.247	3.129	3.727	3.486	3.268	2.604	1.327	0.770	26.584
17	0.085	0.355	1.369	2.076	2.559	3.099	3.624	2.270	2.940	2.119	1.447	1.168	23.209
18	0.118	0.408	1.185	2.514	1.188	3.007	2.518	2.446	1.329	0.823	2.131	0.912	18.739
19	0.178	0.371	0.820	1.880	2.460	2.995	1.837	1.643	0.712	1.059	1.639	0.807	16.591
20	0.023	0.128	0.353	0.685	1.631	2.374	2.488	1.464	1.394	0.968	0.856	0.432	12.860
21	0.153	0.668	0.622	1.330	1.303	1.641	1.948	1.575	1.159	1.317	0.787	0.380	12.975
22	0.107	0.577	1.142	0.581	1.497	1.890	2.343	2.091	2.000	1.572	0.946	0.346	15.179
23	0.150	0.658	0.907	1.759	2.009	2.205	2.686	2.675	2.996	1.924	1.492	0.908	20.551
24	0.119	0.874	1.716	2.519	2.697	3.340	3.520	3.305	3.189	2.219	1.828	0.954	26.512
25	0.099	0.822	1.720	2.368	3.041	3.421	3.527	3.443	2.960	0.181	0.180	0.381	22.278
26	0.103	0.858	1.709	2.506	3.117	3.499	3.655	3.459	0.860	0.314	0.946	0.918	22.114
27	0.129	0.708	1.633	2.449	3.080	3.473	3.627	3.527	3.198	2.591	1.867	0.919	27.490
28	0.189	0.908	1.641	2.410	2.839	3.235	2.978	2.342	2.440	1.606	2.013	0.388	23.110
29	0.155	0.736	1.671	2.383	2.993	3.213	2.978	2.804	3.030	1.735	0.712	0.459	22.950
30	0.119	0.635	0.949	1.425	1.731	2.955	3.408	3.590	2.388	2.149	1.307	0.504	21.228
31	0.112	0.495	0.885	1.919	2.516	3.174	3.714	3.420	3.627	1.215	0.275	0.041	21.414
Average	0.096	0.476	1.001	1.626	1.986	2.480	2.588	2.462	2.192	1.587	1.123	0.579	18.302

June

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.106	0.484	0.570	1.456	2.137	2.653	2.636	3.292	2.523	1.514	0.996	0.338	18.843
2	0.105	0.775	1.585	2.458	3.000	2.799	3.096	3.500	3.191	1.987	0.572	0.563	23.777
3	0.148	0.769	1.790	2.518	3.131	3.525	3.583	3.236	1.979	1.750	0.394	0.335	23.294
4	0.108	0.504	1.273	2.250	2.748	3.343	3.783	0.954	1.795	2.876	1.906	1.146	22.894
5	0.131	0.417	0.977	2.338	2.849	3.299	3.197	1.841	2.457	2.635	1.776	0.258	22.313
6	0.062	0.382	1.234	1.681	2.172	2.705	2.216	3.259	3.135	2.014	0.839	0.116	19.877
7	0.128	0.786	1.692	2.264	3.112	3.599	3.198	2.143	1.817	1.765	1.173	0.952	22.789
8	0.127	0.613	1.779	2.281	2.713	2.869	3.560	2.993	2.814	2.707	1.966	1.188	25.805
9	0.147	0.523	0.656	1.638	2.220	3.071	3.208	3.281	3.249	1.947	1.210	1.056	22.353
10	0.134	0.852	1.737	2.531	3.195	3.342	2.976	2.990	1.211	2.786	2.096	1.171	25.250
11	0.146	0.804	1.294	1.816	2.462	2.772	1.654	0.969	2.988	2.497	1.028	0.178	18.787
12	0.176	0.848	1.538	1.557	2.527	1.798	1.749	3.427	1.819	0.703	1.518	0.340	18.040
13	0.082	0.291	0.786	0.936	1.750	2.298	2.065	2.243	1.984	1.200	0.933	0.333	15.058
14	0.130	0.431	0.936	1.956	2.871	3.466	3.265	1.020	0.413	0.385	0.937	0.901	17.034
15	0.141	0.504	0.845	1.675	2.406	3.672	3.549	1.970	2.642	1.559	1.852	1.308	22.541
16	0.069	0.338	1.229	2.405	2.556	2.002	1.948	2.828	1.897	2.202	1.652	0.890	20.205
17	0.122	0.521	1.300	1.874	1.547	2.092	1.605	2.623	2.478	2.646	1.829	0.527	19.249
18	0.153	0.654	1.092	1.139	1.653	2.758	2.552	3.085	1.790	0.730	0.335	0.409	16.591
19	0.131	0.646	0.840	2.036	1.986	2.681	1.826	2.953	1.888	1.811	0.823	0.167	17.869
20	0.112	0.650	0.841	1.414	1.587	1.930	2.513	2.668	3.214	2.527	2.110	1.299	21.262
21	0.135	0.706	1.010	2.294	3.260	3.419	3.792	3.287	2.759	1.841	0.951	0.589	24.190
22	0.097	0.762	1.647	2.488	3.110	3.453	3.609	3.527	3.225	2.781	1.997	1.182	28.228
23	0.106	0.758	1.698	2.500	3.140	3.484	3.722	3.801	3.208	2.752	2.028	1.168	28.705
24	0.101	0.756	2.031	2.221	3.057	3.505	3.649	3.747	2.733	1.062	1.171	1.275	25.552
25	0.140	0.613	1.376	1.582	1.596	3.046	3.304	2.573	2.400	1.585	0.756	0.459	19.593
26	0.069	0.414	0.792	1.288	2.149	2.623	3.092	3.660	2.910	0.993	0.370	0.063	18.439
27	0.105	0.546	0.747	1.684	1.737	2.109	1.213	0.270	0.176	0.454	0.652	0.360	10.142
28	0.040	0.247	1.368	2.125	1.482	2.287	2.203	1.532	1.004	0.612	0.780	0.534	14.365
29	0.168	0.466	0.672	0.718	2.140	1.981	1.840	1.765	1.615	1.521	0.628	0.198	13.905
30	0.082	0.623	1.205	2.018	1.529	2.186	2.870	1.615	1.507	2.370	1.468	1.162	18.856
Average	0.117	0.590	1.218	1.905	2.394	2.826	2.782	2.568	2.227	1.807	1.225	0.682	20.527

July

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.102	0.408	0.789	2.280	2.759	3.129	2.437	1.891	3.127	1.542	0.505	0.460	19.617
2	0.077	0.424	0.834	1.527	0.915	2.625	1.047	3.662	3.342	1.819	1.850	0.775	19.154
3	0.131	0.490	1.740	1.706	1.900	1.790	1.459	1.428	1.751	2.875	1.292	0.619	17.255
4	0.095	0.560	1.677	1.588	0.824	2.230	1.695	2.292	1.795	2.243	1.358	0.527	17.064
5	0.056	0.386	0.807	1.794	1.361	1.568	1.552	2.399	3.021	1.277	0.921	0.522	15.822
6	0.046	0.298	0.422	0.808	0.540	1.166	1.094	1.016	0.752	0.617	0.692	0.309	7.855
7	0.094	0.517	1.246	1.695	1.906	3.139	3.447	2.731	2.517	2.316	1.280	0.330	21.393
8	0.086	0.665	1.507	2.130	2.703	3.455	3.546	3.617	2.781	1.218	0.880	0.472	23.210
9	0.063	0.682	1.662	2.428	3.074	3.369	3.828	3.355	2.552	2.284	2.073	0.778	26.328
10	0.099	0.448	1.228	2.777	2.914	2.760	2.562	2.486	2.144	2.149	1.908	0.813	22.645
11	0.074	0.459	1.425	2.322	3.097	2.861	2.234	0.712	0.924	1.886	1.104	0.649	17.931
12	0.107	0.717	1.039	1.062	2.097	2.004	2.390	1.716	1.882	1.300	1.330	0.792	16.851
13	0.080	0.490	1.543	1.841	1.397	2.253	2.747	2.301	0.734	0.246	0.600	0.387	14.843
14	0.113	0.668	1.212	1.903	2.884	1.503	1.237	1.403	1.280	1.819	0.744	0.422	15.330
15	0.107	0.389	0.920	1.383	1.788	1.327	1.945	1.983	1.897	2.081	1.491	0.924	16.389
16	0.041	0.386	0.937	1.291	0.854	1.112	1.369	2.101	2.659	2.558	0.542	1.247	15.498
17	0.100	0.682	1.316	1.443	2.247	2.903	2.194	1.771	1.700	1.389	1.235	0.571	17.820
18	0.050	0.316	0.968	1.843	2.003	2.271	3.155	3.230	1.845	1.425	0.859	0.567	18.628
19	0.078	0.453	0.843	1.378	2.040	1.925	1.793	1.135	1.952	1.344	0.359	0.061	13.392
20	0.062	0.354	0.919	1.182	1.273	1.050	0.998	1.160	1.199	0.823	0.498	0.253	9.848
21	0.043	0.192	0.427	0.476	0.747	0.735	0.735	0.584	0.770	0.938	1.056	0.509	7.386
22	0.082	0.386	0.798	1.370	2.444	3.174	2.548	2.182	2.270	1.862	1.083	0.366	18.686
23	0.058	0.405	1.260	2.329	2.579	3.727	3.707	2.154	2.569	0.458	0.416	0.938	20.775
24	0.022	0.168	0.358	0.808	1.174	1.275	1.117	0.772	0.935	0.755	0.489	0.240	8.191
25	0.019	0.360	0.525	1.442	1.874	1.680	2.226	2.446	2.338	1.966	2.158	1.024	18.329
26	0.078	0.769	1.768	2.465	2.668	2.631	2.926	2.744	0.727	1.058	1.318	0.930	20.161
27	0.038	0.304	0.665	1.244	1.563	1.983	2.535	2.452	1.882	1.252	0.999	0.751	15.801
28	0.083	0.610	1.611	2.428	3.089	3.529	3.753	2.608	1.439	2.973	1.366	0.836	24.466
29	0.029	0.183	0.566	1.774	2.410	3.181	2.042	2.054	1.819	2.091	1.745	0.559	18.549
30	0.050	0.411	0.842	0.992	2.670	2.191	3.534	2.292	1.575	1.675	1.237	0.372	17.899
31	0.058	0.352	0.520	0.700	1.325	3.228	2.238	1.582	2.118	2.068	2.041	1.381	17.800
Average	0.072	0.449	1.044	1.626	1.972	2.315	2.261	2.073	1.880	1.623	1.143	0.625	17.255

August

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.044	0.319	0.774	1.219	1.282	1.622	1.467	1.844	1.672	1.636	1.163	0.531	13.699
2	0.024	0.372	0.251	1.171	2.194	1.475	1.468	1.984	1.902	1.589	1.015	0.371	13.878
3	0.022	0.254	0.863	2.028	1.617	2.354	2.855	1.706	1.480	1.341	0.764	0.598	16.160
4	0.055	0.347	0.969	1.709	3.270	3.471	2.698	2.482	3.021	2.143	1.135	0.784	22.134
5	0.091	0.450	1.022	1.835	2.183	2.519	2.465	3.220	3.288	2.305	1.929	1.170	22.617
6	0.083	0.520	1.307	2.269	2.938	3.195	3.746	2.682	3.105	2.752	1.963	0.767	25.447
7	0.055	0.649	1.531	2.169	2.814	3.005	2.618	3.442	2.898	2.483	1.531	0.796	24.235
8	0.022	0.157	0.531	1.011	1.549	2.816	2.322	1.849	1.849	1.856	0.127	0.123	14.245
9	0.027	0.129	0.539	0.972	1.581	1.451	0.615	0.550	0.875	1.286	0.835	0.498	9.515
10	0.041	0.422	1.215	1.625	2.002	3.148	2.757	1.305	1.418	1.571	1.049	0.267	16.951
11	0.057	0.336	0.795	0.781	1.247	1.015	2.310	2.591	1.492	1.880	0.641	0.327	13.498
12	0.022	0.158	0.303	0.994	1.617	2.129	1.703	2.035	1.355	0.612	0.618	0.455	12.100
13	0.058	0.378	0.943	2.447	2.489	3.492	2.288	2.232	2.737	1.862	1.833	0.623	21.666
14	0.005	0.285	0.796	0.677	1.849	3.419	2.782	3.263	3.030	1.454	0.913	0.277	18.931
15	0.026	0.156	0.415	0.931	1.407	1.409	2.477	3.084	2.715	2.248	1.330	0.443	16.777
16	0.007	0.044	0.134	0.269	0.326	1.370	2.909	2.578	3.078	0.751	0.079	0.035	11.592
17	0.037	0.398	1.106	1.880	1.538	2.928	2.948	3.112	3.001	2.597	1.622	0.701	22.071
18	0.056	0.545	1.328	2.517	2.505	3.173	3.856	3.675	2.892	1.714	2.046	0.668	25.235
19	0.044	0.594	1.580	2.412	3.084	3.544	3.392	3.252	3.344	2.968	1.658	0.571	26.562
20	0.075	0.722	1.574	2.238	2.776	3.377	3.727	3.348	0.561	0.588	1.508	0.786	21.470
21	0.044	0.331	1.144	1.916	2.333	3.465	3.736	2.517	2.163	0.759	0.329	0.533	19.420
22	0.022	0.241	0.532	1.593	1.946	2.513	3.563	3.562	2.396	1.535	1.059	0.381	19.374
23	0.038	0.347	1.106	1.487	2.082	2.099	1.436	2.309	2.551	2.713	1.593	0.083	17.864
24	0.041	0.226	0.360	0.628	0.615	1.061	1.568	1.945	2.424	1.379	0.728	0.346	11.394
25	0.009	0.123	0.509	0.918	0.957	1.228	1.509	1.391	1.603	1.742	1.154	0.561	11.803
26	0.044	0.348	1.240	2.245	2.085	3.351	3.265	2.949	1.362	2.003	1.212	0.445	20.631
27	0.044	0.506	1.619	1.652	3.111	2.848	3.527	3.685	3.058	2.524	1.732	1.054	25.552
28	0.039	0.414	0.908	2.317	2.859	2.534	1.485	0.487	0.490	1.000	0.590	0.528	13.721
29	0.044	0.302	0.845	1.658	2.580	3.351	3.083	2.871	2.813	1.750	1.052	0.951	21.464
30	0.041	0.273	0.867	0.981	1.447	2.276	2.658	3.480	3.413	2.073	0.711	0.156	18.439
31	0.019	0.276	0.824	1.812	2.710	2.656	3.408	2.904	3.251	2.146	1.571	0.587	22.221
Average	0.040	0.343	0.901	1.560	2.032	2.526	2.601	2.527	2.298	1.783	1.145	0.529	18.409

September

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.065	0.338	0.881	1.883	2.489	3.489	3.360	3.565	2.862	1.951	1.204	0.495	22.650
2	0.045	0.386	1.125	1.217	1.843	2.407	3.355	3.398	3.192	2.120	1.530	0.690	21.371
3	0.052	0.559	1.471	2.592	2.566	2.051	2.720	3.893	2.337	0.538	0.241	0.277	19.340
4	0.050	0.307	0.628	1.031	1.649	3.122	2.479	2.758	1.436	1.574	0.857	0.375	16.333
5	0.015	0.129	0.476	1.110	1.087	1.846	2.587	3.353	2.429	1.727	0.323	0.181	15.327
6	0.022	0.329	0.831	1.386	1.632	2.126	3.105	2.990	1.773	1.611	0.213	0.179	16.257
7	0.033	0.235	0.921	1.143	1.303	1.738	3.265	2.675	2.433	1.963	1.521	0.470	17.748
8	0.029	0.455	1.235	2.359	2.940	3.288	3.441	3.539	3.084	2.757	1.841	0.756	25.900
9	0.044	0.559	1.514	2.387	2.484	3.179	3.308	3.018	2.191	2.794	1.045	0.635	23.261
10	0.029	0.269	0.582	1.801	2.287	2.426	2.131	2.932	2.503	1.659	1.207	0.689	18.621
11	0.001	0.029	0.142	0.324	0.851	1.300	1.873	2.108	2.152	1.637	1.189	0.475	12.170
12	0.015	0.241	0.895	1.897	2.937	3.133	2.410	2.271	3.372	2.598	1.957	0.699	22.490
13	0.041	0.304	0.555	2.497	2.893	3.239	3.583	2.679	2.780	2.486	0.887	0.189	22.165
14	0.024	0.425	0.572	2.725	2.676	3.481	2.280	2.237	2.713	0.895	0.688	0.430	19.195
15	0.049	0.416	0.662	0.846	1.671	2.496	2.803	1.708	3.016	2.395	1.378	0.420	17.928
16	0.017	0.408	0.933	1.805	2.492	2.981	2.309	2.957	2.998	2.398	1.606	0.817	21.807
17	0.035	0.380	1.473	2.127	2.288	2.144	3.370	3.088	3.054	2.382	1.559	0.840	22.804
18	0.044	0.557	0.985	1.512	1.828	1.916	1.502	1.624	1.217	1.581	0.441	0.344	13.622
19	0.038	0.559	1.002	1.009	2.782	2.680	3.406	1.519	2.368	0.383	1.077	0.224	17.062
20	0.009	0.061	0.511	0.759	1.053	0.824	1.560	1.642	1.131	1.873	1.598	0.504	11.548
21	0.071	0.443	0.835	1.883	1.896	2.682	3.187	3.402	2.895	2.163	0.800	0.376	20.673
22	0.022	0.602	1.482	2.137	2.323	2.766	2.542	2.922	1.986	1.415	0.684	0.308	19.223
23	0.052	0.493	1.313	2.202	2.901	3.249	3.400	3.284	2.953	2.131	1.160	0.201	23.359
24	0.030	0.344	1.266	2.170	2.800	3.320	3.123	3.136	2.859	2.310	1.069	0.189	22.631
25	0.023	0.424	1.202	1.880	1.790	2.553	2.321	2.590	2.444	2.091	1.261	0.448	19.048
26	0.026	0.230	0.626	1.149	1.557	2.185	1.750	2.003	2.220	2.060	0.862	0.305	14.994
27	0.019	0.144	0.269	0.772	1.720	1.324	1.760	1.950	1.352	1.448	1.251	0.318	12.337
28	0.028	0.447	1.284	1.424	1.983	2.867	3.490	0.975	1.033	0.947	0.484	0.286	15.279
29	0.037	0.351	1.011	1.502	1.890	2.101	2.011	2.654	2.597	2.456	1.361	0.303	18.288
30	0.028	0.130	0.702	1.998	2.673	2.917	3.596	2.827	3.011	2.445	1.535	0.606	22.490
Average	0.033	0.352	0.913	1.651	2.109	2.528	2.734	2.657	2.413	1.893	1.094	0.434	18.864

October

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.032	0.326	0.918	2.047	2.517	3.610	2.699	2.746	2.749	1.962	0.972	0.378	20.983
2	0.029	0.394	1.246	2.039	2.777	3.245	3.327	2.095	2.518	1.708	0.647	0.274	20.334
3	0.023	0.338	0.756	1.097	1.873	2.183	1.700	1.621	1.782	1.813	0.834	0.347	14.378
4	0.037	0.348	0.736	1.502	1.380	1.445	1.352	2.328	1.286	1.324	0.811	0.285	12.853
5	0.011	0.196	0.755	1.038	1.495	1.083	1.234	1.235	0.758	0.136	0.044	0.032	8.018
6	0.012	0.263	0.680	0.722	0.972	1.424	1.423	1.978	1.861	1.796	0.234	0.133	11.501
7	0.024	0.296	0.815	0.960	0.808	1.044	0.753	1.045	1.153	0.723	0.477	0.159	8.271
8	0.018	0.288	0.691	1.787	2.506	3.303	3.054	3.349	2.091	2.248	1.172	0.480	20.995
9	0.019	0.329	0.692	0.787	1.785	1.447	3.092	1.291	0.357	0.369	0.198	0.062	10.435
10	0.012	0.208	0.940	1.959	2.463	1.845	1.261	2.695	2.830	2.547	0.487	0.111	17.365
11	0.022	0.225	0.700	1.765	1.845	2.698	3.425	1.653	1.032	1.659	1.112	0.454	16.594
12	0.017	0.247	0.852	1.673	2.170	2.359	1.985	1.178	1.383	2.170	1.317	0.456	15.817
13	0.015	0.138	0.843	1.149	1.653	1.923	1.092	1.069	1.467	0.865	0.559	0.239	11.023
14	0.027	0.376	0.618	1.992	2.518	2.830	2.776	2.595	2.373	0.506	0.486	0.128	17.228
15	0.016	0.142	0.290	0.482	0.789	2.469	2.959	2.559	0.703	0.431	0.712	0.326	11.899
16	0.017	0.217	0.357	1.020	1.430	2.387	2.231	2.275	2.013	1.290	0.271	0.203	13.715
17	0.010	0.275	1.137	1.485	2.070	2.370	2.981	1.548	0.705	0.813	0.415	0.271	14.085
18	0.013	0.176	0.643	2.227	2.837	3.016	3.388	3.039	2.581	2.191	1.137	0.335	21.585
19	0.019	0.295	0.981	1.903	2.730	2.665	3.016	2.994	2.622	1.660	1.058	0.376	20.320
20	0.027	0.262	1.153	1.942	2.656	3.082	3.169	1.609	1.055	0.748	0.296	0.092	16.090
21	0.016	0.202	0.555	1.647	2.540	2.973	3.148	2.965	2.510	1.553	1.006	0.285	19.404
22	0.018	0.290	1.020	1.828	2.557	2.929	3.404	2.738	2.282	1.760	1.002	0.198	20.029
23	0.011	0.252	0.869	1.807	2.176	2.979	3.150	3.051	2.602	1.875	1.120	0.305	20.199
24	0.019	0.242	0.840	1.822	2.629	2.972	2.232	1.896	2.615	1.798	0.818	0.153	18.040
25	0.023	0.268	1.065	1.910	2.660	3.069	2.624	2.417	2.053	1.840	1.114	0.263	19.308
26	0.011	0.243	0.849	1.585	2.343	2.981	3.241	3.049	2.534	1.537	0.832	0.179	19.385
27	0.016	0.355	1.084	1.676	2.325	2.906	2.815	2.811	2.534	1.683	0.781	0.214	19.201
28	0.016	0.260	0.612	1.727	2.517	2.956	3.122	2.954	2.551	1.877	1.053	0.260	19.905
29	0.016	0.253	1.021	1.824	2.520	2.922	3.118	2.880	2.568	1.665	1.054	0.230	20.071
30	0.005	0.080	0.683	1.227	2.208	2.146	1.252	2.182	1.959	1.748	1.148	0.279	14.916
31	0.023	0.173	0.559	1.559	2.093	2.000	1.569	2.311	1.385	0.688	0.374	0.051	12.785
Average	0.019	0.257	0.805	1.554	2.124	2.492	2.471	2.263	1.900	1.451	0.759	0.244	16.346

November

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.007	0.086	0.349	0.489	1.037	1.972	1.589	2.153	1.799	0.808	0.430	0.256	10.975
2	0.005	0.164	0.455	0.661	1.252	2.097	2.040	1.172	0.972	0.685	0.263	0.082	9.848
3	0.001	0.045	0.079	0.196	0.259	0.417	0.568	0.417	0.399	0.284	0.120	0.051	2.838
4	0.002	0.075	0.125	0.275	0.583	1.032	0.858	0.484	0.498	0.644	0.282	0.129	4.991
5	0.002	0.089	0.352	0.842	1.519	2.236	1.940	1.362	1.404	0.941	0.466	0.246	11.399
6	0.005	0.130	0.458	1.234	2.641	3.032	2.899	1.817	1.353	0.960	0.565	0.150	15.243
7	0.010	0.168	0.924	1.927	2.576	2.985	3.141	3.051	2.662	1.089	1.111	0.127	19.771
8	0.012	0.248	0.940	1.934	2.563	2.959	3.075	2.901	2.477	1.844	1.056	0.258	20.267
9	0.007	0.156	0.920	1.924	2.548	2.932	3.056	2.931	2.520	1.880	1.067	0.259	20.202
10	0.006	0.156	0.909	1.877	2.512	2.910	3.018	2.858	2.421	1.737	0.966	0.237	19.606
11	0.007	0.191	0.933	1.699	2.409	2.691	2.768	2.602	2.492	1.852	1.054	0.200	18.898
12	0.005	0.168	0.577	1.734	1.589	2.084	1.818	1.508	1.291	1.773	0.646	0.090	13.284
13	0.005	0.119	0.419	0.800	1.288	2.025	1.599	1.570	1.929	1.899	0.902	0.184	12.738
14	0.002	0.071	0.256	0.750	1.056	1.538	1.424	1.137	1.244	0.806	0.380	0.099	8.761
15	0.004	0.090	0.385	0.755	1.294	1.255	0.898	1.536	1.953	2.028	1.086	0.192	11.474
16	0.005	0.187	0.824	1.381	2.451	1.464	2.394	2.614	2.485	1.817	0.637	0.229	16.488
17	0.006	0.230	0.891	1.888	2.517	2.922	3.045	2.893	2.491	1.841	1.026	0.224	19.974
18	0.004	0.124	0.773	1.863	2.474	2.876	3.009	2.960	2.455	1.817	0.994	0.096	19.445
19	0.001	0.118	0.576	1.163	1.992	2.095	3.022	2.116	1.020	0.680	0.417	0.082	13.283
20	0.002	0.117	0.974	1.396	2.382	1.916	1.177	1.110	0.957	1.456	0.912	0.080	12.477
21	0.001	0.032	0.144	0.532	0.697	1.058	1.301	1.852	1.065	0.246	0.068	0.022	7.017
22	0.001	0.153	0.668	1.469	1.383	2.322	1.938	1.187	1.627	1.038	0.769	0.152	12.707
23	0.001	0.190	0.562	1.692	2.211	2.676	1.995	1.366	1.431	0.891	0.585	0.130	13.731
24	0.004	0.103	0.321	1.065	1.794	1.916	2.196	2.178	1.480	0.745	0.482	0.082	12.365
25	0.001	0.156	0.599	1.484	2.123	2.563	2.721	2.578	2.219	1.602	0.835	0.175	17.054
26	0.001	0.153	0.606	1.574	2.209	2.619	2.757	2.622	2.211	1.588	0.837	0.185	17.362
27	0.001	0.150	0.598	1.498	2.119	2.558	2.704	2.602	2.248	1.632	0.863	0.181	17.154
28	0.001	0.148	0.604	1.423	2.052	2.472	2.636	2.540	2.149	1.501	0.854	0.189	16.569
29	0.001	0.152	0.600	1.441	2.063	2.474	2.630	2.514	2.029	1.348	0.770	0.164	16.188
30	0.001	0.145	0.602	1.611	2.277	2.654	2.520	2.651	2.286	1.613	0.791	0.179	17.331
Average	0.004	0.137	0.581	1.286	1.862	2.225	2.225	2.043	1.786	1.301	0.708	0.158	14.315

December

Date/Time	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	Total
1	0.000	0.134	0.542	1.467	2.131	2.538	2.695	2.586	2.233	1.516	0.761	0.153	16.755
2	0.000	0.127	0.518	1.467	2.170	2.598	2.768	2.648	2.284	1.642	0.769	0.164	17.155
3	0.001	0.147	0.466	1.398	2.196	2.619	2.785	2.729	2.349	1.712	0.916	0.167	17.485
4	0.000	0.123	0.508	0.937	1.549	2.462	2.789	2.721	2.305	1.673	0.712	0.068	15.848
5	0.000	0.127	0.493	1.154	1.939	2.556	2.659	2.882	2.424	1.418	0.604	0.230	16.485
6	0.000	0.131	0.503	1.487	2.160	2.623	2.755	2.461	2.332	1.763	0.993	0.185	17.394
7	0.000	0.131	0.465	1.302	2.154	2.372	2.685	2.641	2.305	1.687	0.944	0.151	16.838
8	0.000	0.120	0.459	1.244	2.079	2.510	2.732	2.659	1.918	1.559	0.891	0.153	16.324
9	0.000	0.140	0.445	1.246	2.079	2.501	2.658	2.611	2.248	1.638	0.912	0.151	16.628
10	0.000	0.101	0.414	0.978	1.609	2.231	2.680	2.660	2.249	1.669	0.663	0.100	15.354
11	0.000	0.100	0.400	1.218	2.076	2.548	2.738	2.657	2.304	1.682	0.671	0.136	16.531
12	0.000	0.212	0.549	0.918	1.754	2.092	2.822	2.757	2.474	1.766	0.556	0.146	16.045
13	0.000	0.101	0.376	1.262	2.226	2.642	2.843	2.804	2.430	1.796	0.662	0.100	17.243
14	0.000	0.102	0.391	1.230	2.222	2.673	2.826	2.732	2.475	1.873	0.706	0.101	17.332
15	0.000	0.086	0.347	1.174	2.127	2.542	2.721	2.606	2.093	1.689	0.662	0.130	16.179
16	0.000	0.067	0.381	0.877	1.785	2.433	2.542	2.583	2.225	1.669	0.635	0.148	15.346
17	0.000	0.080	0.392	1.251	1.974	2.433	2.647	2.640	2.272	1.665	0.667	0.114	16.135
18	0.000	0.096	0.371	1.083	2.053	2.310	2.637	2.614	2.261	1.726	0.699	0.110	15.960
19	0.000	0.089	0.366	1.055	2.003	2.398	2.589	2.567	2.241	1.683	0.699	0.117	15.806
20	0.000	0.101	0.374	1.047	2.002	2.426	2.603	2.528	2.197	1.653	0.669	0.139	15.738
21	0.000	0.095	0.352	1.066	2.124	2.516	2.709	2.662	2.301	1.755	0.712	0.106	16.397
22	0.000	0.110	0.372	1.092	2.152	2.595	2.758	2.692	2.356	1.839	0.738	0.090	16.793
23	0.000	0.086	0.348	1.075	2.191	2.628	2.766	2.703	2.343	1.802	0.757	0.116	16.814
24	0.000	0.083	0.354	1.049	2.136	2.592	2.759	2.708	2.390	1.837	0.769	0.123	16.800
25	0.000	0.080	0.358	1.027	2.081	2.505	2.696	2.657	2.357	1.818	0.790	0.120	16.490
26	0.000	0.086	0.432	1.016	1.983	2.440	2.651	2.555	2.276	1.725	0.766	0.144	16.073
27	0.000	0.072	0.361	1.005	1.981	2.402	2.619	2.573	2.287	1.715	0.768	0.140	15.926
28	0.000	0.073	0.370	0.873	1.854	2.488	2.578	2.494	2.095	1.605	0.730	0.173	15.332
29	0.000	0.069	0.382	0.986	1.952	2.446	2.677	2.603	2.277	1.727	0.794	0.215	16.134
30	0.000	0.077	0.380	0.895	1.914	2.391	2.624	2.591	2.264	1.744	0.795	0.159	15.836
31	0.000	0.072	0.377	0.947	1.908	2.359	2.581	2.508	2.267	1.753	1.003	0.203	15.981
Average	0.000	0.104	0.414	1.123	2.018	2.480	2.697	2.640	2.285	1.703	0.755	0.140	16.360

A2. Hourly and daily ambient temperature (celsius) [87]

January

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	13.3	13.2	15	17.4	19.8	23.7	24.1	26.2	27.6	27.8	27.4	27.4	23.7
2	13.9	13.5	14.5	17.1	20.2	22.4	24.1	26.1	27.3	26.7	27.8	26.6	23.6
3	13.6	12.9	14.8	16.7	19.5	22.1	23.6	25.6	26.4	27.9	27.6	27.4	23.1
4	13.9	12.3	14.5	17	19.7	21.8	24.4	26.2	27.3	28.3	28.6	28.3	24.8
5	14.5	13.8	15.7	18.2	21.7	25	26.9	27.5	29.1	29.5	29.3	28.8	24.7
6	15.8	15.4	16.3	19	22.8	25.5	28.9	28.6	30.4	29	31.3	29.5	25.6
7	15.5	14.9	16.7	18.1	21.2	25.4	26.5	27.8	27.7	27.9	28.2	27.4	25.2
8	17.6	17.1	17.8	19.7	21.7	24.8	25.9	26.8	26.8	28.7	28.7	27.4	24.8
9	14	13.5	15.7	19.2	22.3	24.7	25.8	26.8	26.9	27.8	27.5	27.2	24
10	14.7	14.3	15.4	18.3	21.5	25.3	26.3	27.3	27.3	28.5	28.3	27.6	24.5
11	15	14.6	15.3	18.4	22.4	23.6	26.3	27.1	29	29	28.9	28.4	25.1
12	14.7	15	16.2	19.5	22.2	24.4	26.4	27.5	28.5	29.5	29.2	28.9	24.9
13	14.4	14.6	15.8	19.6	21.3	24.7	26.6	28.4	28.7	29.2	29.6	29.5	25.8
14	15.6	15.3	16.7	19.3	21.1	24.3	26.9	28.8	29.2	30.5	30.3	30.8	26.4
15	15	14.6	16.8	19.2	21.7	24.5	27	28.4	29.5	29.9	31.3	31	26.6
16	14.1	13.8	16.7	21	22.4	24.5	26	28.5	29.4	30.4	31.1	30.7	26.1
17	13.7	13.7	15	18.4	21.1	23.7	25.8	28.7	29.7	30.7	31.7	30.7	26.6
18	13.9	13.4	16.4	19.6	21.8	24.1	26.7	29.3	30	31.4	32	30.9	25.5
19	12.1	12.2	14	17.7	20.4	25.1	25.8	27.8	29.1	30.5	31.5	30.9	26.6
20	13.1	12.8	14.1	18.6	21.9	25.2	27	28.8	30.5	30.1	30.8	30.9	25.6
21	13	11.8	13.8	17.5	21.1	23.7	26.3	28.6	29.6	29.8	31	30	28.5
22	12	12	14.2	16.6	19.1	23.4	26.3	27.7	29.3	29.9	30.2	31.3	25.2
23	12.1	12.3	13.8	17.2	20.6	24.1	26.9	27.5	29.3	29.9	30.3	29.8	26.6
24	17.6	17.7	18.1	20.2	22.3	26.9	27.4	29	30.6	30	31	30.1	29.1
25	20.3	20.6	21.3	23.8	24.1	26.1	27.6	28.9	30	30.2	30.2	30.6	27.8
26	18.7	17.9	19	20.9	23.8	27	28	29.1	30.6	30.5	31.4	31.2	28.5
27	19.3	19.6	20.4	22.4	25.2	26.9	28.1	28.9	29.7	30.5	29.7	29.3	28.3
28	20.5	18.5	19.7	21.6	22.5	23.9	24.5	23.7	24.6	24.1	23.8	22.7	21.6
29	17.6	17.2	17.9	19.5	22	23.8	24.4	24	25.6	25.3	26.2	25.4	24
30	13.8	13	14.3	16.6	19.6	23.4	25.6	25.6	28	28.4	28.3	27.5	24.5
31	13.1	13.7	14.1	16.6	19.2	22.8	24.1	25.4	27.5	27	27.3	25.8	23.6

February

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	12.7	12.7	13.5	16	18.8	22.5	24.9	25.5	26.4	26.9	27.1	26.6	23.9
2	14.9	15.3	16.1	19	20.6	23.9	24.1	24.6	27.3	25.4	25.6	24.8	22.5
3	13.4	13.3	13.6	15.7	19	22.7	23.7	23.2	24.5	25.4	25.4	24.7	22.4
4	12	12.9	13.1	15.1	17.7	21.4	22.8	23.8	25.7	26.5	27.2	26.8	23.2
5	13.4	12.6	13.8	16.7	19.1	22.4	23.9	25.8	27.7	28.4	29.1	27.6	24.5
6	13.5	12.4	13.5	16.9	19.6	22.8	25.1	26.2	27.9	29.1	28.8	28.7	25.4
7	14	13.7	14.7	17.2	19.5	22.2	25.9	27.1	28	29.4	29.4	28.7	25.7
8	14.4	14.3	14.8	18.7	19.6	23	25.6	27.7	29.2	29.8	29.5	29.4	25.6
9	17.1	16.1	16.6	19.4	22.4	24.7	27.3	29.6	31.3	32.7	32.8	30.4	28.2
10	15.1	15.5	16.7	19.5	23.1	26.8	30.8	31.6	32.4	32.3	33.2	31.3	28.9
11	16.2	16	17.2	21.8	24.8	26.7	28.6	29.4	31.3	32	32.1	31.7	29
12	16.2	16	17.8	21	23.9	26.6	28.4	30.8	32	33.1	32.8	32.7	29.4
13	16.8	16.9	20	22.6	25.4	28.6	29.8	30.7	32.1	32.7	33.3	32.8	30.9
14	16.6	15.1	17.5	21.7	24.4	26.7	29.2	30.4	31.9	33.3	33.6	34	30.4
15	18.2	17.9	20.4	25	26.4	28.7	30.1	32.5	32.6	32.3	32.1	31.2	30.8
16	17.9	17.2	20	25.2	26.3	27.8	29	30.2	31.5	30.6	30.9	32.6	30.8
17	18.3	18.1	20.5	24.5	27.2	28.2	31.6	32.4	32.1	31.9	32.4	31.9	27.5
18	17.2	16.1	18.6	21.8	25.6	29.1	30.4	29.9	32.5	32.1	32.2	31.8	30.5
19	16.2	16.1	18	22.9	25.6	28.9	31	31.5	33	32.8	33.3	32.4	30.2
20	14.3	14.6	17.3	19.8	23.3	26.3	29.6	31.3	32	32.8	32.9	32.8	29.7
21	16	14.2	17.1	20.7	24.8	28.5	30.7	31.4	33.4	34.2	34.5	33.8	31.1
22	16.4	14.8	17.6	23.4	26.9	29.6	32.2	32.4	33	33.5	33.9	33.3	29.9
23	15.9	15	18.4	22.1	25.1	28.1	32	32.8	34.3	34.1	34.3	34.6	30.6
24	18.6	17.4	20.4	23.5	26.7	30.8	32.5	33.8	34.3	34.8	36.1	35.1	33.3
25	19.2	18.8	20.6	24.4	27.1	30.4	32.2	33.7	35.1	35.2	36.5	35.7	33.4
26	21.2	19.7	23.3	27.1	29.4	31.3	33	34.4	35.2	34.7	36	36.3	34.1
27	20.8	20.1	24.8	27.9	29.3	31.1	32.3	34	35.2	34.2	35.6	36	33.6
28	20.3	18.5	21.1	24.6	28.7	31.4	33.1	33.4	33.7	33.7	33.4	33.3	30.6

March

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	17.3	16.8	18.3	21.2	26.3	29.8	31.6	33.3	34.5	34.2	34.1	34	29.9
2	16.6	15.8	18.1	21.1	26	27.9	30.5	32.5	33.9	34.7	35.6	35.1	31.5
3	16.2	16.1	18.3	21.3	26	28.2	31.2	32.7	33.3	34.1	34.6	34	30.8
4	16.5	17.4	17.8	20.3	24.3	28.1	30.4	33.7	33.4	33.8	33.9	33.9	30
5	17.1	16.8	18.1	21.4	23.9	27.2	29.3	30.8	32.6	34.2	34.8	34.1	30.5
6	17.9	16.8	17.4	21.1	23.5	26	28.1	31	32.8	33.9	34.1	33.7	30.7
7	17	15	19	23.8	25.5	28.6	30.8	32.5	34.3	35.1	35	35.2	32.1
8	15.8	15.5	19.1	23.3	26.5	30	30.6	31.7	33.3	34.7	34.9	34.3	32.5
9	16.1	15.2	18.9	23.4	26.3	29.4	31.5	32.4	33.2	34.2	34.5	34.2	32.3
10	16.2	15.7	17.7	20.5	22.8	26.5	28.6	31.8	32.9	33.5	33.6	33.3	30.5
11	15.2	14.7	16.2	20.1	23.5	26.6	28.8	31.4	32.8	33.6	34.5	34.4	30.6
12	15.7	15.8	17.4	20.6	23.2	26.7	29.6	31.9	34	35	35.3	35.1	30.1
13	17.9	17	18.3	21.3	24.3	28.3	30.7	32.4	33.5	33.8	33.4	32	30.5
14	17.7	17.3	19.3	22	25.1	29	31.8	33.5	35.2	35.8	36	35.7	31.2
15	19.3	19.4	20.6	25.7	28.3	31	33.3	34.8	36.7	36.9	37	36.3	33.3
16	19.1	18.7	21.1	25.7	27.4	30.8	32.3	34	34.8	35.8	36	35.8	32.9
17	21.8	20.8	23.6	26.2	28.4	29.8	31.5	33.3	33.8	33.8	33.4	33.2	31.8
18	19.4	18.7	21.5	23.6	27	29.1	32	34.8	35.5	36.1	35.6	34.8	31.5
19	19	19.5	21.1	23.4	27.1	30.5	31.8	33	33.7	35.1	35.8	34.8	33.4
20	22.7	23.1	24.9	28.9	29.5	31.2	33.1	34.1	34.6	36.1	35	34.6	33.5
21	20.5	20.1	22.4	25.1	26.2	28.3	29.8	30.7	32	32.4	33.5	32.5	31.6
22	21.5	20.7	23.8	26.3	28.8	29.5	32.1	32.4	34.1	35	33.2	33.2	32.4
23	20.7	20.4	23.6	27.4	28.9	30.7	32.9	33.9	35.1	35.4	35.3	34.9	34
24	20.4	19.8	22.3	24.5	26.9	29.7	31.7	33	34.4	35.4	35.4	35.1	33.3
25	20	20.6	23.1	26.5	27.9	29.9	32.3	33.9	36.1	37.6	36.5	36.6	34.5
26	21.7	22.1	25.1	27.2	29.2	31.7	33.8	34.7	36.7	36.5	37.3	36.9	35.9
27	22.1	21.4	24.7	28.6	30.5	32.3	35.9	36.3	37.5	38.5	38.3	37.7	36.4
28	21.5	22.8	24.9	27.5	29.8	32.3	34.6	36.2	37.6	37.5	38	37.2	35.7
29	22.9	21.5	24.4	27	30.2	33.2	35.5	37.2	37.2	38.2	38.5	37.5	36.7
30	26.3	25.7	28	30.4	31.5	33.9	36.2	35.3	37.7	32.6	31.4	34.3	33.1
31	22.9	23	25.9	28.2	30.4	32.2	34.4	36.3	37.7	37.8	37.6	37	36.2

April

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	24	24.7	29.1	31.3	33.2	34.7	35.8	36.8	38.1	39.1	39.8	38.4	37
2	23.5	23.6	27.7	30.6	31.7	34	35.9	37	38.1	38.9	39	37.8	35.4
3	21.6	21.1	23.9	28.2	30.3	32.3	34	35.5	37.7	37	37.5	37.1	34.7
4	20.1	21.2	23.4	28.5	31.5	33.5	34.2	36	36.1	36.9	36.6	36.2	34.9
5	23.9	23.2	26.3	30	31	32.6	33.5	34.6	35.7	36.5	36.9	36.6	35
6	23.6	23.6	26.5	28.8	31	32	32.9	34	34.5	35.5	35.9	35.5	34.2
7	24.4	24.1	26.5	28.2	30.9	31.6	33	34.6	35.4	36.3	36.6	36	33.3
8	23.9	23.8	26.6	28.5	30.6	31.6	33.2	34.2	34.9	35.8	36.4	36.5	35.1
9	24.3	23.6	28	29	30.4	31.9	33.6	34.5	35.6	36.3	36.6	36.3	34.9
10	23.4	24.9	27.6	29.7	30.3	31.7	33.4	34.7	35.4	36.1	36.3	36.5	35.2
11	22.2	23	26.9	29.1	30.9	31.1	32.1	32.1	33.4	29.4	32.3	32.7	29.9
12	24.2	24.2	26.8	28.1	30	30.7	32.7	32.9	31.8	34.1	35.8	30.7	27.5
13	23.5	23.5	26.1	28	28.8	30.8	32.1	33.7	35	35	31.7	33.1	31.9
14	24.5	24.2	25.5	28.2	30.1	30.2	30.7	32.5	32.2	31.3	31.7	30.8	28.6
15	24.4	24.5	25.8	28.1	29.1	32.7	33.3	34.4	34.6	34.1	33.4	29.6	27.8
16	23.8	24.2	26.1	27.4	29.3	31.2	31.4	33.9	33.3	33.8	33.1	33	31.5
17	24.7	24.9	27.1	29.8	31.8	33.1	34.4	35.2	34.3	34.5	36.3	34	34.1
18	23.5	24.8	28.4	29.9	31.4	33.8	35.3	36.1	38.6	37.1	37.1	24.3	25.6
19	24.9	25.6	26.4	27.4	28	30.9	31.6	32.8	33.6	34.3	34.6	35	34.3
20	23.3	24	27.1	30.2	31.2	32.4	34.8	35.5	35.6	36.4	35.8	37.5	36.6
21	24.3	25	28.8	31.3	33.3	34.6	35.6	37	37.4	38.3	38.4	39.5	38.6
22	25.7	26.6	30.8	32.4	33.1	34.4	36	37.7	38.3	39.1	38.4	38.9	38.5
23	25.8	26.2	30.1	32.3	34.6	34.6	36.2	36.7	37.5	38.2	38.5	38.6	37.3
24	24.4	26.6	29.4	31.4	33.8	36.4	36.6	37.2	38.2	38.5	38.9	38.2	37.8
25	24.4	26.4	28.8	31.3	33.7	35.2	37.2	38	40.3	39.3	38.9	38.7	37.9
26	23.7	22.2	22.5	23.4	26.1	26.8	30.3	32.1	33.5	34.3	32.6	31.9	31.2
27	21.1	21.6	24.5	26.5	29.1	30.5	30.9	33.6	33.9	35.3	35.4	33.6	33
28	21.6	21.5	21.6	22.9	24.8	28.2	28.7	30.6	29.7	30.3	30.1	30.7	29.9
29	24.8	25.5	27.3	29.4	30.7	32.5	32.4	32.9	35.9	32.7	30.6	32.4	31.5
30	23.2	23.9	27	29.1	31	32.3	33.3	34.4	36.2	32.2	31.3	32.3	32.3

May

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	23.5	24.2	25.8	27.8	30.8	33.1	33	34.3	34.7	36.3	35.9	36.3	35.3
2	25.6	26.4	27	28.1	29.5	29.8	31.1	29.9	30.8	30.9	30.4	28.8	27.9
3	24.2	24.3	23.9	24	24.4	25.6	26.5	31.5	29.4	31	26.5	24.7	24.8
4	23.5	23.3	23.5	24.3	24.3	25.3	24.4	24.6	24.8	24.4	24.5	24.1	24.2
5	22.3	22.3	22.4	22.4	22.7	23.2	24.5	24.7	26.7	26.2	23.7	24	23.7
6	22.6	22.3	22.5	22.3	22.8	23	22.9	23.2	23	23.3	24.4	25.2	24.9
7	23.2	23.5	24.1	24.5	24.7	26.2	26.7	25.9	26.9	28.9	29.2	28.4	27.8
8	22.5	22.6	22.9	23.4	25.2	25.7	27.8	29.5	28.5	30.1	29.8	30	27.4
9	23.7	23.8	25	25.8	27.2	28.6	29.2	29.6	30.3	31.5	32	31.7	31.2
10	24.8	24.5	25	26.1	27.9	28.3	30.5	28.8	31.7	32.1	32.2	32.2	31.5
11	21.4	23.5	23.1	24.3	25.5	26.5	28.4	29.5	30.7	29.3	26.7	27.7	27.2
12	23.5	23.6	24.8	26.3	27.9	27.9	28.7	30	27.2	25.1	23.5	24.5	24.7
13	23.8	23.8	24.2	24.2	24	24.4	26.3	27.1	26.6	26.1	26.2	27.6	27.5
14	23	23.1	23.6	25.6	25.4	26.8	27.7	27.8	29.9	29.2	29.2	29	24.2
15	23.6	23.7	25.6	26.3	26.8	27.7	28.7	29.9	31.2	23.7	24.9	27.4	26.1
16	22.6	23	25.7	27.1	27.4	28.3	29.4	30.4	31.5	31.7	32.2	31.7	31.2
17	23.5	23.9	24.9	26.6	28	29.2	30.6	30.4	30.2	31.3	30.6	30.9	30.8
18	24	24.4	24.9	26.9	26.9	28.7	30	31.1	31.1	29.4	30.2	29.2	29.2
19	24.4	24.4	25.3	27	27.6	28.9	29.1	29.5	29.8	31.2	31.6	31.7	30.4
20	24.1	23.1	23	23.4	24.3	25.4	26.4	27.3	28.1	27.8	28.3	27.8	27.2
21	24	24.1	26	26	26.7	27.1	27.9	29.3	28.7	29.3	28.3	28.6	27.5
22	24.2	24.3	25.9	26.7	28.1	28.8	29.2	29.8	30.3	30.2	31.1	30.6	29.4
23	22.9	24	25.9	26.5	28	29.9	31	32.6	31.5	32.5	32.2	31.4	31.1
24	22.9	24.4	26.3	27.8	29.5	30.6	31.6	32.8	33.3	33.8	34.6	34.3	33.8
25	24.2	25.2	27.7	29.7	30.3	32.8	32.4	33.2	34.2	34.2	31.2	30.8	30.5
26	23.9	25.3	27.9	29.3	29.5	30.9	32.1	33.3	34	33.8	28.4	28.4	28.5
27	24	24.8	27.4	28.3	30	32.4	33.4	33.5	36	34.9	35.5	34.2	31.9
28	24.5	26.2	29	29.7	30.9	33.6	34.2	33.7	33.3	30.9	30.8	32.8	29.6
29	24.2	25	27.4	29	30.5	30.6	32.1	33.4	33.8	34.6	30.8	29.6	27.5
30	23.5	23.8	24.9	26.1	26.5	28.1	30.4	30.5	32.2	32.4	33.5	29.6	28.9
31	24.3	24.5	25.4	25.7	27.5	29.6	30.2	31.5	32.9	33.8	32.9	27.6	22.9

June

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	23.7	23.7	24.3	25.3	26.2	27.2	28.2	29.2	30.2	30.9	31.4	30.7	29.5
2	24.4	25.3	27.5	27.5	29	29.9	31.3	29.4	31.2	32.2	32.8	31.1	30.4
3	23.4	24.6	26.9	27.6	29.1	31.1	31.8	32.6	32	31.2	30.7	29.5	28.6
4	24	24	25.6	27.4	28.5	29.8	31.3	32.5	31	31	31.4	30.1	29.5
5	23.6	23.5	24.4	26.9	27.1	28.3	29.8	30.8	29.4	32.4	32.6	29.1	27.3
6	23.9	24.3	25.6	26.8	27	28.2	29.5	30.6	31.5	31.8	32.3	28.8	27.3
7	24.3	25.1	26.5	27.3	28.1	30.1	31.2	31.7	31.2	31.6	32.4	32.4	30.7
8	24.5	25.9	26.4	28.3	29.5	30.9	31.8	32.1	31.8	33.1	33.5	32.4	31
9	24.7	25.3	26.4	27.5	29.7	31.6	32.3	31.7	32.3	32.9	33.1	33.9	32.1
10	25.1	26.1	28.4	29.3	30.5	32.1	32.4	32	32.7	33.4	34.3	33.4	33
11	25	26.3	28	29.2	30.4	32.1	31.5	29.8	32.2	33.1	32.4	31.3	29.2
12	25.2	25.4	27.5	28	29.1	31	29.6	29.8	31.7	31	32.6	31.2	24.7
13	24.3	24.5	25.7	26.9	27.6	28.1	29.9	29.5	30.2	31.1	31.5	30.6	29.6
14	24.7	25.1	26.2	27.7	29.8	30.3	31.6	32.2	33.3	32.2	28.3	27.9	27.4
15	24.6	25.3	26.7	27.7	28.8	30.1	30.9	31.9	32.6	33	32.6	33.1	32
16	26.4	25.7	26.5	27.9	29.5	30.5	31.4	32.6	29.2	26.1	28.3	30	30.3
17	24.7	25.2	26.9	27.8	28.2	29	30.2	31.1	31.4	31.7	32.2	32.4	32.1
18	25.3	26.7	27.9	28.9	29.3	31.6	30.8	32.1	32.3	31.9	31.9	31	30.9
19	24.8	24.9	25.9	27.3	28.3	28.8	30.5	31.3	31.7	32.3	30.8	29.3	29
20	24.6	24.4	25.5	27.8	27.7	29.1	30.3	31	31.6	32.9	32.5	32.5	32.2
21	23.9	24.6	26	27	30.6	30.4	32.3	33.2	33.5	33.5	33.9	30.5	30.2
22	25.3	25.9	28.8	30	31.2	33.9	34.7	34.1	35.1	35.3	35.3	35.1	34.1
23	25.2	25.6	27.3	28.9	31.1	33.4	33.8	35	35.9	36	36.7	36.7	35.6
24	26.2	27.1	28.1	29.6	31	32.3	33.8	35.6	35.3	31.2	31.1	31.4	30.8
25	26.4	25.9	26.7	28.7	29.6	29.9	31.5	32.3	33.7	33.9	27.5	28.9	27.2
26	25.5	25.5	25.9	27	27.5	28.7	30.9	31.9	33	31.8	31.3	25.3	26
27	24.6	24.9	25.4	26.2	27.4	28.5	29.5	27.4	25	25.2	26.7	25.8	25.8
28	24	22.5	23.2	24.5	25.8	26.5	27.7	27.8	28.8	26.6	27.5	27.5	27.6
29	24.2	24.9	25.6	26.6	26.7	27.8	28.3	28.6	29.1	29.8	29.3	26.8	26.9
30	23.9	24	26.2	26.8	28	29.7	31.2	32.2	32.6	32.5	31	31.4	31.3

July

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	24.8	25.4	26.6	27.7	29.3	29.8	31.2	31.1	28.6	27.4	29.6	28.3	28.9
2	24.7	25.5	26.7	28.2	28.7	29.3	29.1	29.6	31.4	32	32.8	32.7	31.8
3	24.9	26.1	27.4	28	28.5	29.4	29.7	29.7	28.8	30.8	30	30.3	26
4	24.3	25	26.2	26.8	27.9	28.7	29.9	30.3	30.6	31.5	30.9	30.9	29.7
5	25.4	25.3	25.7	27	27.4	28.3	29.3	29.9	31.4	31.4	31.1	29.8	29.3
6	25.1	25.5	25.9	26.6	23.8	24.3	24.4	24.7	25	25.1	24.9	24.9	25.3
7	24.1	24.3	26.2	26.6	26.9	28.6	29.5	30.6	31.3	32	29.1	26.9	27.4
8	22.9	23.4	24.7	26.2	28.8	29.9	30.7	31.7	31.9	32.2	25.7	25.5	26.2
9	23.2	23.9	25.6	27	28.1	30.6	31.1	32.7	32.6	32.8	33	32.6	32.1
10	24.9	25.4	26.5	27.5	28.8	29.8	30.3	30.8	32	32.6	32.9	32.6	33.7
11	25.1	25.3	26.4	27.8	29	30.5	31	31.2	31.7	32.4	31.9	30.7	30.7
12	25.3	25.5	26.7	27.3	27.8	29	29.6	30.4	32.3	31.5	31.3	30.9	29.9
13	24.9	25.7	26.5	27.7	29.2	29.2	30.9	31.7	31.6	29.3	29	29.7	29.2
14	24.6	25.7	26.4	27.4	28.6	29.8	30.2	30.4	29.6	31.3	30.8	30.5	29.6
15	26.3	26.3	26.9	27.4	28.2	28.7	29.1	29.6	29.4	30.1	30.3	30.9	30
16	25.7	25.8	27.4	27.8	28.1	28.4	28.2	30.6	31	32.4	32	30.2	26.9
17	25.1	25.4	26.6	27.7	28.9	31.2	31.6	32.7	31.9	32.7	33.4	33.1	31
18	25.3	25.9	26.8	28.1	30.1	30.5	31	31	32.1	33.1	32.3	32.6	30.9
19	24.3	24.6	26.3	27.3	28.4	29.7	29.9	30	32.3	27.1	30	25.9	25
20	23.9	24.2	25.3	26.1	26.6	26.9	26.9	26.8	27	26.7	26.6	25.9	25.6
21	23.3	23.5	23.7	24	24.3	24.5	24.6	24.1	24.2	23.6	24	24.6	24.7
22	22.7	22.8	23.7	24.7	25.8	27.8	27.7	29	29.3	29.9	29.1	29.4	28.8
23	23.2	23.7	24.9	27.1	28.2	29.9	31	32.1	32.3	32.1	30.3	28.8	28.1
24	23.2	23.2	23.5	23.6	23.9	24.9	26	26.4	26.1	26	25.7	24.9	24.5
25	21.3	21.4	21.9	22.7	24	24.9	26.3	27.5	28.7	29.3	29.8	30.2	29.7
26	23.3	24.3	26.2	26.7	28.5	29.4	30.3	31.4	30.8	24.6	28	30.5	29.3
27	24.1	24	25.5	26.7	27.5	28	28.4	29.2	30.2	30.4	30.6	30.3	29.5
28	23.2	24.6	26.4	27.9	28.8	29.9	30.9	32.9	32.3	33	33.2	33.5	31.4
29	24	24.3	24.6	25.6	26.8	29.7	30.6	32.6	32.4	32.3	29.7	29.4	27.8
30	24.3	24.5	25.5	25.9	27.4	30.2	30.1	33.1	31.3	32.6	33.3	32.6	31
31	24.3	25.4	25.7	26.9	28.1	31.7	31.6	30.1	27.5	25.5	27.2	29.9	29.8

August

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	24.4	24.6	25.7	28	28.5	29.5	30.5	31	29.5	29.8	29.7	29.5	29.3
2	24.5	24.5	25	24	24.4	25.4	26.7	27.6	28.9	28.8	29.7	30	28.8
3	23.8	23.9	24.4	25.8	26.5	28.2	28.6	28.6	29.6	29	29	29	28.3
4	24.2	24.7	26.2	27.4	27.7	29.4	29.7	30.6	31.1	31.9	32.9	29.5	27.3
5	23.7	23.9	25.1	26.1	27.7	28.6	29.4	30.6	31.3	31.7	31.3	32.3	31.6
6	24.3	24.9	25.8	27.3	27.7	29.8	30.8	30.7	32.1	32.6	32.7	31.4	30.1
7	24	24.3	26.5	27.6	29.6	31.3	32.8	32.4	31.1	32.2	31.5	31.4	31.6
8	24.9	25	25.5	26.7	27.6	29	30.3	31.4	31.5	31.6	32	26.1	24.6
9	24.5	24.6	24.7	26	27.2	29.3	29.5	25.6	26	27.9	28.5	27.2	26.4
10	24.1	24.6	25.6	26.5	27.4	28.7	28.7	29.4	28	27.8	27.4	27.9	27.3
11	24.9	25.1	25.1	26.4	26.8	26.8	27.8	28.3	29.8	29.7	30	29.1	28.4
12	24.2	24.7	25.1	25.6	26.5	28	29	28.8	30	30.3	29.3	29.2	28.6
13	24.6	24.8	26.2	26.9	28.4	29.5	31.1	30.9	31.8	32.5	33.1	32.8	31.8
14	25.2	25.3	26.3	27.8	28	29.8	30.4	31.9	32.1	32.8	31.7	32.6	31.1
15	25.1	24.9	26	26.7	28.1	28.4	29.3	30.3	31	31.9	31.6	31.6	31.2
16	25.6	25.4	25.7	25.3	25.6	26.3	29.7	29.1	27.1	28.7	27.8	24.8	24.4
17	23.6	23.7	24.6	25.2	26	26.9	28	29.5	30.5	31.3	31.3	31.1	29.9
18	23.1	23.2	25.4	26.7	27.1	28.6	29.5	29.8	30.9	31.9	32.1	32.1	32
19	23.4	24.1	25.7	27.5	28.5	29.8	30.1	30.8	29.8	29.4	31	31.9	30.4
20	23.3	23.8	25.9	27.1	28.7	29.9	31.3	32.5	32.3	32.3	30.7	30.9	30.1
21	25.2	24.8	25.6	28	28.8	29.7	31.2	32.4	33.1	31.3	25.2	28.2	27.4
22	24.6	24.8	25.7	26.8	27.8	30.1	30.4	31.4	30.7	31	30.7	30.8	26.5
23	24.1	24.3	25.1	25.9	27.2	28.5	30.2	28.6	30	31.6	30.8	27.3	24.3
24	24	24.1	24.7	25.4	25.9	26.4	26.4	27.2	28.1	28.9	28.7	28.1	26.7
25	23.5	23.8	24.2	25.3	25.9	26.2	26.8	27.6	28.3	29.3	28.9	26.6	25.3
26	23.7	23.5	24.1	26.1	26.9	29.6	29.8	30.4	31.4	32	31.9	30.2	29.7
27	24.1	24.5	25.6	26.7	28.1	30.5	31.8	31.3	32.5	33	33.2	32.9	32.6
28	25.1	24.7	26	27.8	29.4	30.4	31.5	31.1	30.2	28.1	27.5	27.2	27.8
29	24	23.9	24.9	27	29.2	30.8	31.8	31	32.4	31.9	28.2	28.9	30
30	23.7	24.2	24.5	25.6	26.1	26.9	28	30	30.5	31.8	27.4	24.9	25.9
31	23.2	23.6	24.2	25.9	26.5	28.2	29.3	30.2	30.7	30.9	30	29.3	28.1

September

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	24.2	24.2	24.8	26.6	27.1	28.8	29.8	30.7	31.7	32.1	31.8	31.4	28.6
2	25.2	25	25.8	28.4	27.9	28.6	29.8	31.2	32	32.2	32	32.3	31
3	24.1	24.4	26.1	26.9	28	29	29.7	30.1	31.7	31.2	31	27.1	27.3
4	24.9	24.8	26	26.5	27.4	29	29.8	31	31.5	31.6	30.6	30.8	28.9
5	23.7	23.6	24.4	25.5	26.8	27.5	29.2	31.6	32	31.1	28.7	27.8	27.4
6	24.1	24.1	24.7	25.9	26.4	27.1	28.2	29.9	30.7	29.8	28.8	27.9	27.3
7	24.2	24.5	25	26.4	26.6	27.1	28.2	30.1	29.5	30.9	30.4	30.4	29
8	24.4	24.6	25.6	26.8	28	30.5	32.6	32.3	32.9	34	28.1	28.7	27.2
9	24.5	24.4	27	28.6	29.3	30.4	31.1	32.2	31.7	25.1	25.8	28.4	28
10	24.5	24.3	25.4	27	28.5	30.3	30.4	30.7	31.2	31.9	31.8	31.7	31
11	25.2	25.2	24.6	24.9	25.8	26	27.8	28.1	28	28.5	29	28.2	28
12	24.3	24.5	24.8	26.8	27.8	29.4	30.4	30.6	32.3	33	32.8	32.7	26.4
13	24.6	24.7	25.9	27.4	28.5	30	30.9	31.8	32.6	32.3	32.1	27	27.4
14	24.3	24.6	25.8	27.4	29.1	29.5	31	31.9	31.5	32.3	29.3	27.2	27.5
15	24.3	24.4	24.7	25.6	26.9	28.8	29.9	30.8	30.5	30.3	32.2	30.1	28.9
16	24.8	25.4	25.2	28	30	31.2	25.2	28.6	30	30.8	31.4	31.5	30.9
17	24.9	24.6	26.6	27.6	28	29.7	31.8	31.4	32.7	33.5	33.5	31.9	30.8
18	25.2	25.5	27.4	28.2	30.4	29.5	32	31.3	25.8	27.2	27.8	27.6	27.4
19	23.9	24.2	25	26.9	28.8	30.1	30.4	31	30.2	28.7	27	30.4	26.5
20	23.3	23.9	24.6	26.8	24.3	24.4	25.5	26.3	27.3	27.8	28.5	28.1	27
21	22.3	22.7	23.3	24.5	25.4	26.8	28.1	28.2	29.4	29.3	29.8	29	27
22	22.3	22.2	24.5	26.3	28.5	28.7	29.6	29.9	30.3	30.4	30.2	29.2	28.3
23	22.5	23.1	24.7	26.1	27.6	29.6	31.1	31.4	31.5	31.3	31.4	30.5	29.9
24	22.7	23.4	24.6	27.1	29.2	29.1	30.9	33.4	32.6	32.8	33.8	29.5	29
25	22.7	23	25.2	27.3	28.3	29.3	30.7	31.3	32	32.4	32	31.6	30.4
26	22.8	23.2	22.9	24	25.6	26.9	27.5	28.1	28.7	29.7	29.9	30.4	29.1
27	23.8	24.3	23.9	25.1	26.4	27.3	27.9	28.7	29.8	29.9	30.9	30.3	28.8
28	24.3	24.3	24.4	26.2	27.8	28.9	29.6	29.4	29.9	29.8	29.8	28.7	27.9
29	23	23.6	24.7	27.1	26.6	28.6	28.8	29.6	30.9	29.9	29.9	29.3	28.8
30	23.6	23.6	24.6	25.9	28.1	29.2	30.4	31	30.7	31.6	30.4	31	29.3

October

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	22.9	23.1	24.5	26.4	27.7	29.6	30.7	30.9	30.8	31.7	32.1	30	29.2
2	23	23.3	24.1	26.1	28.9	30.8	32.9	33.8	33.2	29.5	31.1	31.4	29.7
3	24.4	24.7	25.8	26.2	27.3	30.2	31	31.8	33.5	34	34.1	32	29.9
4	24.1	24.4	25.6	26.3	29.3	29.8	30.9	29.9	32.9	32.6	32.8	32	31.2
5	24.8	24.6	24.9	25.9	27.8	30.1	30	30.9	28.8	24.8	24.3	24.3	24.2
6	23.9	24	24.6	25.1	24.5	25.7	26.9	27.2	28	28.4	25.8	26.2	24.6
7	23.7	23.8	24.6	24.1	24.2	25.2	25.3	24.7	25.4	24.9	25	25	24.8
8	22.6	22.7	23.5	24.7	26.2	27.9	28.6	29.8	30.1	30.4	31.1	30.4	28.3
9	24.4	24.4	25	25.8	27.4	29.5	30	30.9	27.2	25.6	25.9	26.2	24.7
10	22.7	22.8	23.4	25.7	27.4	28.8	30.3	28.6	30.2	30	30.4	28.6	27.7
11	23.6	23.4	23.9	26.8	27.8	29.1	29.2	30.3	29.3	28	29	28.2	27.4
12	22.7	22.8	23.7	26.9	28.2	29.1	28.3	28.9	29.6	28.1	30	29.5	27
13	23.4	23.5	23.8	25.9	26.6	27.3	26.7	24.9	24.6	25.2	25.3	25.6	25.1
14	22.2	22.4	22.9	24.1	28.1	28.6	29.1	29.6	28	29.3	25.9	27.6	26.1
15	23	23.2	23.7	24.2	26	26.6	27.3	27	29.8	28.6	26	25	24.2
16	22.4	22.2	23.1	25.5	26.4	27.9	28.5	28.3	28.3	28.6	28.2	27.3	26.8
17	23.3	23.4	24.4	25.5	27.7	28.9	28.7	28.5	28.5	28.7	28.9	27.6	26.2
18	22.4	22.5	24.4	26.2	27.2	28.7	29.7	30.7	30.3	30.2	31.6	30.2	28.6
19	22.3	22.5	24.8	26.4	28.9	29.9	30.3	31.8	32.3	31.6	31.8	30.6	28.1
20	21.8	21.5	23.2	25.4	26.8	28.2	29.4	29.9	29	29.2	28.3	28	27
21	20.9	21.1	22.8	24.9	27.5	28.7	29.1	28.6	29.5	29.5	29.9	29	26.6
22	20.9	21	22.2	24.4	25.8	27.7	30.3	29.3	30.3	30.8	30.3	29.7	28
23	20.9	21	21.5	24.8	26.9	28.4	29.8	30.7	30.7	31.6	31.4	31	27.9
24	21.3	21.5	22.3	24.4	27.9	30.3	30.4	31.6	31.4	32	32.3	31.2	28.3
25	21.2	21.6	22.9	26	28.1	29.2	30	29.5	30.8	30.8	31	30	27.4
26	20.5	20.2	21.4	23.8	26.2	27.7	29.9	30.6	31.1	31	30.6	28.6	26.4
27	20.4	20.8	21.8	24.7	26.7	28.6	29.9	30.7	31.1	30.9	30.9	29.3	26.2
28	19.9	20.1	22.3	24.5	26.5	28.4	30.2	31	31.6	31.5	31.2	30.6	27.9
29	21.3	21.5	24.2	25.4	28.1	29.7	30.8	31.3	31.7	31.7	32.4	31.5	30
30	22.4	22.4	22.7	24.3	28	30.3	30.6	30.7	31.5	32	32	30.8	27.9
31	20.3	19.7	20.3	22.1	23.6	25.8	28.4	30.4	30.2	29.9	29.4	24.6	22.9

November

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	21.1	21.8	22	22.7	23	23.9	25.1	26	26.5	27.1	26.9	25.9	25.2
2	22.3	22.2	23	23.8	24.7	27.1	27.5	28.8	29.8	29.2	28.6	28.2	27.1
3	22.5	22.3	22.2	21.6	21.8	21.8	21.7	21.4	21.1	21.2	20.8	20.4	20.9
4	19.8	19.5	19.7	20.4	20.5	21.3	22.7	22.8	22.7	23.4	23.2	23.1	22.3
5	21.6	21.8	21.8	21.9	22.5	24.6	26.2	26.5	25.9	25.2	25	24.2	23.4
6	20.8	20.8	21.5	23.9	25.5	26.9	28	28.7	28.1	27.7	27.5	27.1	25.1
7	19.1	19.3	19.5	22.3	26	27.8	28.5	28.3	30.2	30.7	30	28.4	26.7
8	19.1	19.8	21	22.9	26.3	28.1	28.8	29.7	30	30.1	30.2	28.8	25.3
9	16.2	16.2	18.7	20	22.8	27.4	28.6	29.6	29.2	29.6	29.3	26.7	24.5
10	17.4	16.7	18.5	21.8	22.5	26.8	28.5	29.5	30.2	30	29.9	28.3	24.3
11	18.3	20.6	20	22.9	23.3	26.8	26.9	28.9	30	29.9	30.6	29.1	26.3
12	20.4	20.5	22.8	24.3	26	28.3	29.5	30.5	30	29.7	30.3	28.7	27.7
13	21.2	21.4	22.8	23.7	25.1	27.2	28.5	28.9	30.4	30.4	30.2	28.3	26.2
14	22.4	22.6	23.1	24.1	25.7	27.9	27.5	28.3	28.3	28.5	25.5	25.7	25
15	22.6	22.9	23.6	24.9	26.9	26.4	26.4	26.8	27.5	28.4	28.5	27.4	25.8
16	20.8	22.7	21.9	23.7	25.2	27.9	30.6	29.2	29.9	31	30.4	30.1	27
17	20.5	20.3	21.4	24.5	26.2	27.9	29.1	31	31.8	31.8	31.9	30.4	27
18	19.1	19.1	19.6	22.4	24.8	28.1	29.7	31.1	31.7	32	31.6	30.6	28.2
19	23.5	23.2	23.8	24.6	28.2	29.1	30.6	29.2	29.8	29.3	28.8	27.3	26.2
20	23.1	23.1	23.8	26.3	27.2	28	29.8	29.9	29.9	27.1	25.7	26	24.3
21	21.4	21.5	22	22.4	22.9	24.1	24.6	25.9	27	26.2	24.7	21.8	20.9
22	20.3	20	21	22.4	23.4	24.2	27	26.9	28.4	28.2	28.8	27.1	24.8
23	19.7	19.3	19.5	21.4	25.1	26.1	26.7	26.6	26.8	26.7	27.9	25.4	24.8
24	18.6	18.9	19.4	20.2	24.5	25.7	26.4	27.4	26.9	25.9	25.6	24.9	24.1
25	17.1	16.5	18.1	19.5	23.1	25.4	26.7	27.5	27.9	28.1	27.9	26.2	23.2
26	15.7	15.5	16.3	18.4	20.3	23	26.2	27.9	28.4	28.4	28.3	26.5	24.1
27	15.6	15.5	16.4	18.2	20.6	24.3	26.6	27.5	27.5	27.9	27.7	26	22
28	15.2	14.7	15.6	17.5	20.2	22.6	24	24.5	26.5	25.9	26.1	25.2	21.3
29	14.5	14.4	15.8	18.3	19.3	21.9	23.2	24.8	25.7	26.6	25.9	25.1	21.9
30	14.7	14.2	15.5	17.4	20.6	23.5	23.5	23.3	23.8	24.4	24.7	23.6	20.2

December

Date/Time	6.00	7.00	8.00	09.00	10.00	11.00	12.00	13.00	14.00	15.00	16.00	17.00	18.00
1	13.1	12.9	13.8	16	18	21.7	22.6	24	24.5	24.7	25	24.3	20.2
2	12.6	12.6	14	15.6	18.3	21.4	22.5	24.2	26.2	27.1	26	25.4	21.7
3	14.3	14.5	15.4	17.3	20.4	22.4	24.3	26.6	26.8	27.6	27.1	26.4	24.5
4	15.7	15.6	16.4	18	21.2	23.5	25.6	26.1	26.6	27.1	26	25.4	23.1
5	17	17.3	17.7	19.3	21.3	24.8	27	27.7	27.4	28.6	28.2	26	23.3
6	16	15.6	16.8	18.7	21.5	25.1	26.9	28.1	28.6	29.3	28.8	27.4	23.9
7	16.1	16.5	17.8	19.7	22	24.7	26.7	27.7	28.8	28.7	28.6	28.4	24.4
8	17.3	17.1	18.5	20.4	22	24.4	26.5	27.9	28.5	29.4	28.9	28.1	24.3
9	17.1	17.7	19	21.4	22.2	24.5	26.5	27.8	28.8	29	29.2	28.3	24.5
10	17.8	17.4	18.2	20.1	22.7	25.1	27	28.1	28.3	28.8	29.2	28.7	24
11	16.9	16.4	18.4	21.1	23.8	26.2	29.8	29.4	30.1	30.3	30	29.3	24.8
12	16.3	16.4	19.1	20.2	20.8	22.5	26.2	28.6	28.5	28.9	28.3	26.2	22.3
13	14.9	15.2	16.5	19.7	22.7	24.8	26	26.8	28.7	29.2	29.6	29.1	23.8
14	14.4	14	16.4	19.8	21.3	24.6	26.8	27.8	29.1	30.3	30.6	28.6	23.3
15	14.7	14.4	16.5	18.7	22.2	24.6	26.7	27.7	28.9	29.5	29.6	28.8	24.5
16	17.2	17.3	18.9	19.9	21.9	25.6	27.4	27.6	28.8	29.4	29.6	29.1	26.1
17	19.6	19.3	20.7	24	25.7	27.4	28.6	30.1	30.3	30.6	31.1	30.6	26.9
18	19.9	19.4	21.2	24.2	24.7	26.8	29	30.2	30.8	31.1	31.6	31.2	27.5
19	20.1	20.1	20.7	22.2	24.6	27.3	29.2	30	31	31.5	31.8	31.1	27.7
20	20.5	20.1	21.4	24.1	25.4	27.7	29.2	30.1	31.3	31.7	31.9	31.4	28.6
21	20.1	19.7	21.6	23.8	25.4	27.1	29.7	30.4	31.5	31.8	32.5	32.5	28.3
22	18.2	17.6	20.3	22.9	24.6	26.1	28.5	29	30.8	31.7	32.2	31.6	26.4
23	16.4	15.5	17.2	19.8	24	25.4	27.4	28.3	28.9	28.6	29.4	28.3	23.9
24	14.2	13.9	16	17.8	20	22.5	24.6	26.2	27.7	28.7	28.8	28.7	23.3
25	14.3	13.8	15.7	17.3	19.8	22.8	24.5	25.8	27.5	28.6	28.9	28.6	24.5
26	15.4	15.3	15.8	18.5	21	24.6	27.2	27.9	28.9	28.8	29.1	28.5	24.9
27	17	16.8	17.3	19.9	22.1	26.3	27.9	28.2	28.5	29.2	29.3	28.8	25.5
28	16	15.8	16	18.1	20.3	23.4	26.6	26.8	28	28.4	28.5	27.4	24.3
29	16	15.9	16.8	18.9	21.8	24.3	26.4	28.4	28.6	29	29.2	28.9	25.7
30	16.3	16.2	16.7	19.4	22.8	25.2	26.6	28.2	28.7	28.8	29.3	28.7	25.7
31	17.2	17	18.1	20.1	22.3	25.3	26.2	27.4	28	28.9	29.6	28.8	25.6

Appendix B

Specification Sheets of Sharp 80 Wp NE-80E2E Photovoltaic Module





Appendix C

Radial Distribution Test System Parameters

Branch	Line impedance (ohm)		Load demand at bus-j	
i - j	R	X	P_L (kW)	Q_L (kVar)
1-2	0.4214	0.7334	0	0
2-3	0.4214	0.7334	14.58	8.07
3-4	0.2107	0.3667	0	0
4-5	0.4214	0.7334	0	0
5-6	0.2107	0.3667	0	0
6-7	0.2107	0.3667	14.58	8.07
7-8	0.4214	0.7334	0	0
8-9	0.4214	0.7334	0	0
9-10	0.3996	0.67215	58.33	32.27
10-11	0.5328	0.8962	0	0
11-12	0.2664	0.4481	0	0
12-13	0.7992	1.3443	20	15
13-14	0.5328	0.8962	0	0
14-15	1.66675	1.102	0	0
15-16	2.0001	1.3224	0	0
16-17	0.6667	0.4408	29.17	16.14
17-18	1.3334	0.8816	72.92	40.34
18-19	0.6667	0.4408	20	15
3-20	5.3336	3.5264	145.67	80.69
4-21	1.3334	0.8816	62.88	33.33
5-22	3.3335	2.204	14.58	8.07
22-23	2.6668	1.7632	94.79	52.45
23-24	0.6667	0.4408	14.58	8.07
24-25	6.667	4.408	0	0
25-26	1.3334	0.8816	14.58	8.07
26-27	2.0001	1.3224	35	19.36
23-28	5.3336	3.5264	29.17	16.14
24-29	1.3334	0.8816	29.17	16.14
7-30	5.00025	3.306	91.88	50.83
30-31	0.6667	0.4408	85.9	36.83
31-32	1.3334	0.8816	29.17	16.14
32-33	1.3334	0.8816	14.58	8.07
33-34	1.00005	0.6612	43.75	24.21
34-35	1.3334	0.8816	43.75	24.21
35-36	2.33345	1.5428	0	0
36-37	1.3334	0.8816	145.83	80.69
37-38	1.00005	0.6612	91.88	50.83
30-39	2.0001	1.3224	29.17	16.14
35-40	1.3334	0.8816	58.33	32.27
8-41	1.00005	0.6612	14.58	8.07
9-42	1.3334	0.8816	29.17	16.14
10-43	4.0002	2.6448	29.17	16.14
11-44	1.3334	0.8816	29.17	16.14
12-45	4.6669	3.0856	148.75	82.3
14-46	0.6667	0.4408	29.17	16.14
46-47	2.0001	1.3224	0	0
47-48	2.0001	1.3224	29.17	16.14
46-49	0.13334	0.08816	58.33	32.27
15-50	4.6669	3.0856	43.75	24.21
17-51	2.6668	1.7632	116.67	64.55

C1. Data for 51-Bus Base Case Radial Distribution Test System

Note. 900 kVar shunt capacitor bank installed at bus-13

Branch	Line impedance (ohm)		Load demand at bus-j	
i - j	R	X	P_L (MW)	Q_L (MVar)
1 -2	0.0922	0.047	0.25	0.15
2 - 3	0.493	0.2511	0.225	0.1
3 - 4	0.366	0.1864	0.3	0.2
4 - 5	0.3811	0.1941	0.15	0.075
5 - 6	0.819	0.707	0.15	0.05
6 - 7	0.1872	0.6188	0.5	0.25
7 - 8	0.7114	0.2351	0.5	0.25
8 - 9	1.03	0.74	0.15	0.05
9 - 10	1.044	0.74	0.15	0.05
10 - 11	0.1966	0.065	0.1125	0.075
11 - 12	0.3744	0.1238	0.15	0.0875
12 - 13	1.468	1.155	0.15	0.0875
13 - 14	0.5416	0.7129	0.3	0.2
14 - 15	0.591	0.526	0.15	0.025
15 - 16	0.7463	0.545	0.15	0.05
16 - 17	1.289	1.721	0.15	0.05
17 - 18	0.732	0.574	0.225	0.1
2 - 19	0.164	0.1565	0.225	0.1
19 - 20	1.5042	1.3554	0.225	0.1
20 - 21	0.4095	0.4784	0.225	0.1
21 - 22	0.7089	0.9373	0.225	0.1
3 - 23	0.4512	0.3083	0.225	0.125
23 - 24	0.898	0.7091	1.05	0.5
24 - 25	0.896	0.7011	1.05	0.5
6 - 26	0.203	0.1034	0.15	0.0625
26 - 27	0.2842	0.1447	0.15	0.0625
27 - 28	1.059	0.9337	0.15	0.05
28 - 29	0.8042	0.7006	0.3	0.175
29 - 30	0.5075	0.2585	0.5	1.5
30 - 31	0.9744	0.963	0.375	0.175
31 - 32	0.3105	0.3619	0.525	0.25
32 - 33	0.341	0.5302	0.15	0.1

C2. Data for 33-Bus Base Case Radial Distribution Test System

Appendix D

Deterministic Load Flow Solutions of Test Systems

Bus no.	V (pu)	δ (deg)
1	1.00000	0.00000
2	0.99800	-0.15996
3	0.99603	-0.31970
4	0.99510	-0.39788
5	0.99328	-0.55380
6	0.99263	-0.62263
7	0.99201	-0.69112
8	0.99171	-0.79377
9	0.99146	-0.89472
10	0.99135	-0.98312
11	0.99128	-1.09890
12	0.99140	-1.15139
13	0.99194	-1.30381
14	0.99062	-1.34773
15	0.98834	-1.35728
16	0.98627	-1.36573
17	0.98563	-1.36830
18	0.98499	-1.37055
19	0.98471	-1.37182
20	0.99509	-0.32495
21	0.99505	-0.39813
22	0.99033	-0.56718
23	0.98870	-0.57464
24	0.98838	-0.57613
25	0.98687	-0.58300
26	0.98663	-0.58413
27	0.98646	-0.58489
28	0.98826	-0.57668
29	0.98803	-0.57773
30	0.98405	-0.73403
31	0.98326	-0.73766
32	0.98178	-0.74443
33	0.98036	-0.75095
34	0.97942	-0.75528
35	0.97834	-0.76028
36	0.97654	-0.76861
37	0.97607	-0.77077

0.97599

0.98372

0.97828

0.99162

0.99135

0.99102

0.99071

0.99101

0.99037

0.98987

0.98954

0.99035

0.98678

0.98493

38

39

40

41

42 43

44

45

46 47

48

49

50

51

-0.77116

-0.73557

-0.76054

-0.79415

-0.89522

-0.98464

-1.10148

-1.15316

-1.34887

-1.35115

-1.35267

-1.34895

-1.36441

-1.37153

D1. Load Flow Results for 51-Bus Base Case System

<u>Note</u>. $P_{loss} = 29.83$ kW and $Q_{loss} = 39.93$ kVar

Bus no.	V (pu)	δ (deg)
1	1.00000	0.00000
2	0.99778	0.01074
3	0.98728	0.07103
4	0.98172	0.11937
5	0.97623	0.16824
6	0.96258	0.09844
7	0.95999	-0.07043
8	0.95640	-0.04425
9	0.95176	-0.09780
10	0.94745	-0.14346
11	0.94681	-0.13822
12	0.94570	-0.12994
13	0.94118	-0.19632
14	0.93950	-0.25330
15	0.93846	-0.28057
16	0.93745	-0.29739
17	0.93595	-0.35319
18	0.93550	-0.36011
19	0.99738	0.00255
20	0.99468	-0.04805
21	0.99415	-0.06266
22	0.99367	-0.07801
23	0.98458	0.04779
24	0.97957	-0.01860
25	0.97707	-0.05120
26	0.96115	0.12738
27	0.95925	0.16852
28	0.95078	0.22943
29	0.94469	0.28628
30	0.94205	0.36268
31	0.93898	0.30154
32	0.93830	0.28487
33	0.93809	0.27928

D2. Load Flow Results for 33-Bus Base Case System

<u>*Note.*</u> $P_{loss} = 369.76 \text{ kW}$ and $Q_{loss} = 246.41 \text{ kVar}$

BIOGRAPHY

Vichakorn Hengsritawat received the B.E. degree in electrical engineering from University of the Thai Chamber of Commerce, Bangkok, Thailand, in 1995. And he received the M.E. degree in electrical engineering from Chulalongkorn University, Bangkok, Thailand, in 1998. He has joined with the Sripatum University in 1998 as the instructor in the department of electrical engineering to pr esent. His r esearch interests i nclude di stributed ge neration, pow er qua lity, renewable energy, e nergy saving and power system simulation.