# การหาขนาดของเครื่องกำเนิดไฟฟ้าแบบกระจาชชนิดพลังงานแสงจาทิตย์ ในระบบจำหน่ายไไฟ้้า โดงพิารรณาสภาวะแสงอาทิตย์และความผิดเพี้ยนททงฮาร์มอนิก 



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| Thesis Title | SIZING OF PHOTOVOLTAIC DISTRIBUTED |
| :--- | :--- |
|  | GENERATORS IN A DISTRIBUTION SYSTEM WITH |
|  | CONSIDERATION OF SOLAR RADIATION AND |
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วิชชากร เฮงศรีธวัช : การหาขนาดของเครื่องกำเนิดไฟฟ้าแบบกระจายชนิดพลังงาน แสงอาทิตย์ในระบบจำหน่ายไฟฟ้า โดยพิจารณาสภาวะแสงอาทิตย์และความผิดเพี้ยน ทางฮาร์มอนิก (SIZING OF PHOTOVOLTAIC DISTRIBUTED GENERATORS IN A DISTRIBUTION SYSTEM WITH CONSIDERATION OF SOLAR R ADIATION AND HAR MONIC DISTORTION) อ.ที่ปรึกษา วิทยานิพนธ์หลัก: ผศ.ดร.ธวัชชัย เตชัสอนันต์, 162 หน้า.

วิทยานิพนธ์เล่มนี้นำเสนอวิธีทางความน่าจะเป็น เพื่อหาขนาดที่เหมาะสมของเครื่อง กำเนิดไฟฟ้าแบบกระจายชนิดพลังงานแสงอาทิตย์ในระบบจำหน่ายไฟฟ้า โดยพิจารณาถึง สภาวะการกระจายของแสงอาทิตย์และความผิดเพี้ยนทางฮาร์มอนิก ด้วยวิธีการดังกล่าว การ จำลองแบบมอนติคาร์โลจะถูกนำมาใช้ในการสุ่มค่าการกระจายแสงอาทิตย์, อุณหภูมิแวดล้อม รวมถึงแรงดันที่สถานีไฟฟ้าย่อย และความต้องการของโหลดในระบบจำหน่ายไฟฟ้า โดยมี วัตถุประสงค์ เพื่อทำให้กำลังไฟฟ้าสูญเสีย จริงเฉลี่ยของระบบมีค่าต่ำสุด ในขณะ ที่เงื่อนไข บังคับทางด้านคุณภาพไฟฟ้า ซึ่งได้แก่ แรงดันไฟฟ้าที่โหนด, กระแสฮาร์มอนิก, ค่าความ ผิดเพี้ยนแรงดันฮาร์มอนิกรวม และค่าความผิดเพี้ยนความต้องการฮาร์มอนิกรวม ยังคงอยู่ใน ขอบเขตที่กำหนดตามมาตรฐาน IEC และ IEEE ทั้งนี้ยังได้รวมผลของฮาร์มอนิกที่มีอยู่เดิม ในระบบเพื่อ ประเมิน หาขนาดที่เหมาะสมของเครื่องกำเนิดไฟฟ้าแบบกระจายชนิดพลังง าน แสงอาทิตย์ด้วย วิทยานิพนธ์เล่มนี้ยังได้นำเสนอวิธีการวิเคราะห์ด้วยดัชนีเสถียรภาพแรงดัน เพื่อเลือก ตำแหน่งที่เหมาะสมในการติดตั่งเครื่องกำเนิดไฟฟ้าแบบกระจายชนิดพลังงาน แสงอาทิตย์ นอกจากนี้ ยังได้มีการศึกษาผลกระทบที่มีต่อการหาขนาดที่เหมาะสมของเครื่อง กำเนิดไฟฟ้าแบบกระจายชนิดพลังงานแสงอาทิตย์ จากการใช้แบบจำลองของโหลดและการ ปรับค่าตัวปร ะกอบกำลัง ในการทำงาน ที่แตกต่างกัน รวมถึง ศึกษาผลกระทบของแบบจำลอง ของอินเวอร์เตอร์ และ การพิจารณาถึง เครื่องกำเนิดไฟฟ้าแบบกระจายอื่นที่มีอยู่เดิมในระบบ จำหน่ายไฟฟ้า วิธีการที่พัฒนาขึ้นสามารถประยุกต์ใช้ได้กับระบบจริง โดยได้ทำการทดสอบ กับระบบขนาด 33 บัส และระบบจำหน่ายไฟฟ้าแห่งหนึ่งของประเทศไทยขนาด 51 บัส

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VICHAKORN HENGSRITAWAT: SIZING OF PHOTOVOLTAIC DISTRIBUTED GENERATORS I N A DI STRIBUTION S YSTEM W ITH CONSIDERATION OF SOLAR RADIATION AND HARMONIC DISTORTION. ADVISOR: ASST. PROF. THAVATCHAI TAYJASANANT, Ph. D., 162 pp.

This dissertation presents a probabilistic a pproach to calculate an optimal size of photovoltaic distributed generators (PV-DGs) in a distribution system with consideration of solar radiation and harmonic distortion. Monte Carlo simulation is applied to predict solar radiations, ambient te mperatures, substation vol tages and load de mands. The formulated objective $f$ unction is $t$ o $m$ inimize ave rage $r$ eal power loss, while power qua lity constraints i.e., node vol tage, ha rmonic current, total ha rmonic distortion voltage and total demand di stortion are kept within the limits complied with IEC and IEEE standards. Existing background harmonics are included in an evaluation of the optimal size of PV-DG. In addition, static voltage stability ind ex a nalysis is proposed t o select a proper 1 ocation of P V-DG installation in a distribution system. Furthermore, impacts of $s$ tatic load models and power factor control on optimal PV-DG sizing as well as effects of PV inverter modeling a nd existing D Gs in a di stribution system are taken into a ccount. The developed method can be applied to actual systems and was tested with a 33-Bus test system and an actual 51-Bus radial distribution system in Thailand.

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## Nomenclatures

| BH | Background Harmonic |
| :--- | :--- |
| CdTe | Cadmium Tellluride |
| CIGS | Copper, Indium, Gallium and Selenide |
| CPV | Concentrated Photovoltaic System |
| CSP | Concentrating Solar Power |
| CV | Constant Voltage |
| CP | Constant Power Load |
| CI | Constant Current Load |
| CZ | Constant Impedance Load |
| DEDE | Department of Alternative Energy Development and Efficiency |
| DG | Distributed Generation |
| DLF | Deterministic Load Flow |
| DNO | Distribution Network Operator |
| FF | Fill Factor |
| GA | Genetic Algorithm |
| GFCI | Ground Fault Circuit Interrupter |
| IC | Incremental Conductance Method |
| IEA | International Energy Agency |
| LDC | Line Drop Compensator |
| LTC | Load-Tap-Changing |
| MPPT | Maximum Power Point Tracking |
| NOCT | Normal Operating Cell Temperature |
| PCU | Power Conditioning Unit |
| PCC | Point of Common Coupling |
| PDP | Power Development Plan |
| PEA | Provincial Electricity Authority |
| PF | Power Factor |
| PLF | Probabilistic Load Flow |
| PWM | Pulse Width Modulation |
| PV | Photovoltaic |



## CHAPTER I

## INTRODUCTION

### 1.1 Overview of World's PV Generation

At thi s time, fossil fuel is the $m$ ain e nergy s upplier of $t$ he $w$ orldwide economy. However, using in long time of it as being a major cause of environmental problems a nd it is ne cessary to look for al ternative resources in power generation. Besides, the i ncreasing demand for en ergy in a di stribution system can create problems such as voltage drop, poor reliability, low power quality, losses increasing and grid instability, etc. Distributed generations (DGs) are a one way to solve this problem and it has continuously be en introduced a nd pr omoted around $t$ he $w$ orld. Presently, the necessity of producing more energy combined with the interest in clean technologies using renewable energy such as solar, wind, biomass and biogas, etc.

According to the IEEE standard 1547-2003 [1], DG is by definition that which is of limited size roughly 10 M VA or less. Generally, DG produces electricity close to customer loads and can run on fossil fuels, renewable energy resources or waste he at. DG can be cat egorized into three $t$ ypes ac cording $t$ o their $g$ eneration technologies as shown in Table1.1. These technologies are entering a period of rapid expansion a nd commercialization. In $f$ act, $s$ tudies ha ve pr edicted $t$ hat $D G m$ ay account for up to $20 \%$ of all new generations going online by the year 2010 [2].

Among the renewable energy sources, hydropower and wind energy have the largest utilization. In countries with hydropower potential, s mall hydro turbines are used at the distribution level to sustain the utility network in dispersed or remote locations. The wind power potential in many countries around the world has led to a large interest and fast development of wind turbine technology [3].

Table 1.1 DG's category according to generation technologies

| Type | Application | Operating Mode |
| :---: | :---: | :---: |
| Synchronous | Geothermal, Ocean, Internal combustion engine, <br> Combined cycle, Combustion turbine | Capacitive PF |
| Induction | Wind turbine | Inductive PF |
| Inverter-based | Photovoltaic, Micro turbine, Fuel cells | Unity PF |

Another renewable en ergy technology that gains accept ance as a w ay of maintaining and improving living standard without harming the environment is the photovoltaic (PV) technology. The number of PV installations is mainly depending on the government policy and utility companies that support programs on grid-connected PV system [4-5].

From the studied information in [6], the International E nergy Agency (IEA) says that there a re a mbitious pl ans for t he g lobal de velopment of f he s olar energy industry and the encouraging progress seen in 2009, over $90 \%$ of the world's 192 c ountries have yet to unde rtake large-scale deployment projects. However, just eight c ountries a ccounted f or $89 \%$ of t he w orld's t otal i nstalled PV g enerating capacity of 15 GW in 2008. The IEA has set 2020 t argets of 200 GW of g lobal installed capacity for PV and 148 GW for concentrated solar power (CSP), with both figures targeted to s oar by 2030. The IEA suggests one key to progress towards a strong pol icy r egime. However, it should be considering such r egimes consist of Feed-in T ariffs ( FiT) alone or/s omething w ider-reaching. Furthermore, be yond government policy, the other key areas for action must be addressed.

From the annual review in 2008 [7], which presents basic statistical data about the majority of large-scale photovoltaic power plants ( $>=200 \mathrm{kWp}$ ) worldwide currently in operation. It s hows $t$ hat $t$ he pa st $y$ ear $w$ as ch aracterized by s everal projects of M W-range P V power plants, a nd it was a lso the year with the hi ghest market gr owth $r$ elated tolarge-scale $P$ V s ystems e ver. N ot onl y in S pain, where progress is a bundantly clear, but in s ome ot her c ountries the c umulative installed power increased significantly. In the European Union progress was, a mong ot hers, observed in Italy, the Czech R epublic a nd France; the G erman market de creased slightly, but due to the market explosion in Spain the installed power from 2008 still reached the level of the previous year.

This report's da tabase i ncludes more than 1,90 01 arge-scale $\mathrm{P} V$ pow er plants (put into service in 2008 or earlier), each with peak power of 200 kWp or more as shown in F igure 1.1. The a mount of 1 arge-scale $\mathrm{P} V$ pl ants s orted by country is shown in Figure 1.2. M ore than 5001 arge-scale PV pl ants a re located in Germany, more than 370 are in USA and more than 750 are in Spain. The cumulative power of
all these PV power plants is more than 3.6 GWp and average plant power out put is slightly more than 1.8 MWp as shown in Figure1.3.


Figure 1.1 Annual installed and cumulative amount of large-scale grid-connected PV power plants in the period from 1995 to 2008


Figure 1.2 Amount of large-scale grid-connected PV power plants put into service annually in the period from 1995 to 2008 (sort by country)


Figure 1.3 Large-scale PV power plants - annual and cumulative installed power output capacity worldwide in the period from 1995 to 2008

In 2008, more than 1,000 large-scale PV plants were constructed and put into service worldwide. In Spain more than 590 large-scale PV plants were put into service, more than 120 for each Germany and the USA. Among other countries it is worth $m$ entioning $B$ elgium a nd $C$ zech $R$ epublic $w$ here $s$ everal 1 arge-scale $r$ oofmounted ( Belgium) a nd gr ound-mounted (Czech R epublic) P V p lants w ere constructed. R egarding large-scale PV power plants K orea took on a leading role in Asia. Several M W-range pow er pl ants w ere p ut into s ervice in Korea 1 ast year. Europe is by far the most advanced region with more than 800 large-scale PV plants put into service in 2008. In Europe more than 1500 large-scale PV power plants are currently operating, followed by the USA with about 400 PV plants.

### 1.2 Solar PV Technologies Overview

There are two major solar PV technologies convert from sunlight directly and indirectly into electricity energy.

### 1.2.1 Solar Converting Directly Technology [8]

This solar PV technology converts solar energy into useful energy forms by directly absorbing solar photons, particles of light that act as individual units of energy, and either converting part of the en ergy to electricity (as in a PV cell) or storing part of the energy in a chemical reaction.

In the world of this PV solar power technology, there are several types of semiconductor technologies currently in use for PV solar panels. However, two types based on $t$ he thickness of the semiconductor have be come the most widely adopted namely crystalline silicon and thin film [9]. Conventional crystalline silicon solar cell is relatively speaking very thick of 200-500 $\mu \mathrm{m}$ where "thin" means something like 1 $10 \mu \mathrm{~m}$.

### 1.2.1.1 Crystalline Silicon

Crystalline silicon panels are constructed by first putting a single slice of silicon through a series of processing steps, creating one solar cell. These cel ls are then assembled together in multiples to make a solar panel. Crystalline silicon, also called wafer silicon, is the oldest and the most widely used material in commercial solar panels. There are two main types of crystalline silicon panels as follows:

- Monocrystalline Silicon

Monocrystalline (also called single crystal) panels use solar cells that are cut from a piece of silicon grown from a single, uniform crystal as shown in Figure 1.4. Monocrystalline panels are among the most efficient yet most ex pensive on the market. They require the highest purity silicon and the most involved manufacturing processes.


Figure 1.4 Monocrystalline silicon PV panel

- Multicrystalline Silicon

Multicrystalline (also called polycrystalline) panels use solar cells that are cut f rom mul tifaceted silicon crystals as s hown in Figure 1.5. They are 1 ess uniform in appearance than monocrystalline ce lls, resembling pi eces of s hattered glass. These are the most common solar panels on the market, be ing less expensive
than monocrystalline silicon. They are also less efficient, though the performance gap has begun to close in recent years.


Figure 1.5 Multicrystalline silicon PV panel

### 1.2.1.2 Thin Film

Thin film solar panels are made by placing thin layers of semiconductor material ont ov arious s urfaces, us ually on glass. The term thin film refers to the amount of semiconductor $m$ aterial used. It is applied in a $t$ hin film to a surface structure, such as a sheet of glass. Contrary to popular belief, most thin film panels are not flexible. Overall, thin film solar panels of fer the lowest manufacturing costs and are becoming more prevalent in the industry. There are three main types of thin film used.

- Cadmium Telluride (CdTe)

CdTe is a semiconductor compound formed from cadmium and tellurium. CdTe solar pa nels are manufactured on glass as shown in Figure 1.6. They are the most common type of thin film solar panel on the market and the most cost-effective to manufacture. CdTe panels perform significantly better in high temperatures and in low-light conditions.


Figure 1.6 Cadmium Telluride PV panel

- Amorphous Silicon

Amorphous silicon is the non-crystalline form of silicon and was the first thin film material to yield a commercial product, first used in consumer items such as calculators. It c an be de posited in thin layers on to a va riety of s urfaces and of fers lower costs than traditional crystalline silicon, though it is less efficient at converting sunlight into electricity. Amorphous silicon PV panel is shown in Figure 1.7.


Figure 1.7 Amorphous Silicon PV panel

- Copper, Indium, Gallium and Selenide (CIGS)

CIGS is a compound s emiconductor t hat can be de posited ont o m any different $m$ aterials. CIGS ha s onl y recently be come ava ilable for $s$ mall com mercial applications and is considered a developing PV technology. CIGS PV panel is shown in Figure 1.8.


Figure 1.8 CIGS PV panel
At present, CdTe solar panels technology are chose come first for solar application because of its $s$ uperior ene rgy out put cha racteristic a cross $r$ eal-world conditions, its low cost volume production be nefits a nd its superior e nvironmental
performance. CdTe has lower temperature-related loss than crystalline silicon due to a lower temperature coefficient. It also provides superior energy output in low, indirect and diffuse light conditions, producing more electricity on cloudy days.

### 1.2.1.3 Concentrated Photovoltaic System (CPV) [10]

Concentrated PV system is a technology to increase the efficiency of the cells by concentrate sunlight on solar cells. The PV cells in a CPV system are built into concentrating collectors that use a lens or mirrors to focus the sunlight onto the cells as shown in Figure 1.9. CPV systems must track the s un to ke ep the 1 ight focused on the PV cells. The primary advantages of CPV system are high efficiency, low system cost and low capital investment to facilitate rapid scale-up, it means that the systems can use less expensive semiconducting PV material to achieve a specified electrical out put. However, reliability is a n important te chnical c hallenge for thi s emerging technological approach. Because of the systems are generally require highly sophisticated tracking devices.


Figure 1.9 Concentrated photovoltaic system

### 1.2.2 Solar Converting Indirectly Technology [11]

This technology uses mirrors toconcentrate the sunlight e nergy and convert it into thermal energy to create steam to drive a turbine of the generator that generates el ectrical pow er. This technology is well know n a s C oncentrating S olar Power (CSP) technology.

Generally, CSP pl ants g enerate el ectric pow er b y us ing m irrors t o concentrate the sun's e nergy and convert it into high temperature heat. That he at is then channeled through a conventional generator. The plants consist of two parts, one
that col lects solar ene rgy and converts it to heat and then another that converts the heat e nergy to electricity. C SP te chnology ut ilizes thr ee a lternative te chnological approaches such as trough s ystems, pow er tower s ystems a nd di sh/engine s ystems. All C SP t echnological a pproaches require 1 arge areas for s olar r adiation collection when used to produce electricity at commercial area.

### 1.2.2.1 Trough Systems

Trough s ystems us el arge U -shaped (parabolic) r eflectors (focusing mirrors) $t$ hat ha ve oil 1 illed pi pes $r$ unning a long $t$ heir center or $f$ ocal point. The mirrored reflectors are tilted toward the sun and focus sunlight on the pipes to heat the oil inside to as much as $750^{\circ} \mathrm{F}$. The hot oil is then used to boil water, which makes steam to run conventional steam turbines and generators. The schematic diagram and parabolic trough system are shown in Figure 1.10.


Figure 1.10 Schematic diagram of parabolic trough system

### 1.2.2.2 Power Tower Systems

Power tower s ystems al so called central receivers, use many large, flat heliostats (mirrors) to track the sun and focus its rays onto a receiver. As shown in Figure 1.11, the receiver sits on $t$ op of a tall tower in which concentrated $s$ unlight heats a fluid as hot as $1,050^{\circ} \mathrm{F}$. The hot fluid can be used immediately to make steam for el ectricity generation or stored for 1 ater us e. That $m$ eans el ectricity can be produced during periods of peak needed on cloudy days or even several hours after sunset.


Figure 1.11 Schematic diagram of power tower system

### 1.2.2.3 Dish Engine Systems

Dish engine systems use mirrored dishes to focus and concentrate sunlight onto a receiver. As shown in Figure 1.12, the receiver is mounted at the focal point of the dish. To capture the maximum amount of solar energy, the dish assembly tracks the $s$ un across $t$ he $s k y$. The receiver is integrated into a high efficiency external combustion engine. The engine has thin tubes containing hydrogen or helium gas that runs along $t$ he out side of $t$ he e ngine's $f$ our piston $c$ ylinders and op en into $t$ he cylinders. As concentrated sunlight falls on the receiver, it heats the gas in the tubes to very high temperatures, which causes ho t g as to e xpand inside t he c ylinders. T he expanding gas $d$ rives $t$ he pistons. The pi stons $t$ urn a crankshaft, $w$ hich dr ives an electric generator. The receiver, engine and generator com prise a s ingle, integrated assembly mounted at the focus of the mirrored dish.


Figure 1.12 Schematic diagram of solar dish engine system

### 1.3 PV Generation System in Thailand

From Thailand's e nergy s ituation in 2010 r eport [ 12], its hows t hat Thailand imports variety forms of energy which worth many millions Baths as shown in Figure 1.13. Actually, Thailand's consumption of energy has been increasing every year in forms of gas, oil, coal and electricity. The energy crisis in the past few years has caused energy price rising up a nd affected economic de velopment countrywide. Therefore, in order to lower an import of some energy, the Ministry of Energy has come up with a policy to develop the renewable energy (RE) for a fifteen years period (2008-2022) by the Thailand Power Development P lan 2010 ( PDP 2010) [13]. The objective of the plan is to increase the portfolio of renewable energy to $20.3 \%$ of the final energy consumption in 2022. At the e nd of the plan, the portion of renewable energy in pow er ge neration s hall be $2.4 \%$ or $5,608 \mathrm{M} \mathrm{W}$ from $1.4 \%$ at present as shown in Figure 1.14.


Figure 1.13 Proportion of domestic and import energy of Thailand in 2010


Figure 1.14 Energy source portion of power generation of Thailand in 2010
Furthermore, from the study of Silapakorn University and Department of Alternative Energy Development and Efficiency (DEDE) found that the average solar radiation potential of Thailand is about $18.2 \mathrm{MJ} / \mathrm{m}^{2}$-day or $5.06 \mathrm{kWh} / \mathrm{m}^{2}$-day, which is a very good potential. However, the solar radiation potential of the areas in Thailand (as shown in Figure 1.15) can be classified into three groups as follows [14]:

- The high potential area: ave rage s olar radiation a bout $19-20 \mathrm{M} \mathrm{J} / \mathrm{m}^{2}$-day or $5.28-5.56 \mathrm{kWh} / \mathrm{m}^{2}$-day which covers $14.3 \%$ of the total area
- The medium potential area: a verage solar radiation a bout $18-19 \mathrm{MJ} / \mathrm{m}^{2}$-day or $5-5.28 \mathrm{kWh} / \mathrm{m}^{2}$-day which covers $50.2 \%$ of the total area
- The low potential area: average s olar r adiation 1 ess $t$ han $18 \mathrm{M} \mathrm{J} / \mathrm{m}^{2}$-day or $5 \mathrm{kWh} / \mathrm{m}^{2}$-day which covers $35.5 \%$ of the total area


Figure 1.15 Yearly average solar radiation potential of the areas in Thailand

From Figure 1.15, the highest average solar radiation zone is on the north eastern area and some a rea of the central of Thailand. The pe rcentage of the area which classified by average solar radiation levels is shown in Figure 1.16, while the yearly average solar radiation of the whole country is $18 \mathrm{MJ} / \mathrm{m}^{2}$-day.


Figure 1.16 Percentage of area classified by average solar radiation levels of Thailand Therefore, $f$ rom thi $s$ in formation, it $s$ hows tha $t$ the $s$ olar pot ential in Thailand is very important. And it should not be overlooked because the solar energy resource in Thailand is enough for the future. Table 1.2 shows the renewable potential and target plan of Thailand. Note from Table 1.2 that the solar e nergy potential to produce electricity energy is $50,000 \mathrm{MW}$, which is the highest compared with other energy resources. However, the existing electricity power produced by solar energy is just only 32 MW. This is because the capital investment cost of PV technology is still expensive com pared with ot her t echnologies, although PV t echnology has be en continually reduced at the present.

However, in order to e ncourage to pr oduce more electricity po wer by solar ene rgy, the M inistry of E nergy of T hailand ha s pr omoted the ad der r ate of $8 \mathrm{Bth} / \mathrm{kWh}$ for small power producers (SPPs) or very small power producers (VSPPs). This rate is also using solar energy technology (called the concentrating solar power, CSP) to pr oduce $t$ he $t$ hermal ene rgy and then to produce $t$ he el ectricity power as shown in Table 1.3.

Table1.2 Some of renewable potential and target plan of Thailand

| Electricity Power <br> Produced by | Potential <br> (MW) | Existing <br> (MW) | $\mathbf{2 0 0 8 - 2 0 1 1}$ <br> $(\mathrm{MW})$ | 2012-2016 <br> $(\mathrm{MW})$ | 2017-2022 <br> (MW) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Solar | 50,000 | 32 | 55 | 95 | 500 |
| Wind Energy | 1,600 | 1 | 115 | 375 | 800 |
| Hydro Power | 700 | 56 | 165 | 281 | 324 |
| Biomass | 4,400 | 1,610 | 2,800 | 3,220 | 3,700 |
| Biogas | 190 | 46 | 60 | 90 | 120 |
| Municipal Solid Waste | 400 | 5 | 78 | 130 | 160 |
| Hydrogen | - | - | 0 | 0 | 3.5 |
| Total | $\mathbf{5 7 , 2 9 0}$ | $\mathbf{1 , 7 5 0}$ | $\mathbf{3 , 2 7 3}$ | $\mathbf{4 , 1 9 1}$ | $\mathbf{5 , 6 0 8}$ |

Table1.3 Adder rate for SPPs and VSPPs using renewable energy of Thailand

| Type of power source of power plant | adder <br> (Bth/kWh) | New adder <br> (Bth/kWh) | Adder <br> special plus <br> (Bth/kWh) | Adder special plus for Yala, Pattani, Naratiwas <br> (Bth/kWh) | Given adder duration (years) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.Biomass |  |  |  |  |  |
| $\begin{aligned} & \text {-Installed capacity <= } 1 \mathrm{MW} \\ & \text {-Installed capacity > } 1 \mathrm{MW} \end{aligned}$ | $\begin{gathered} 0.30 \\ 0.30 \end{gathered}$ | $\begin{aligned} & 0.50 \\ & 0.30 \end{aligned}$ | $\begin{aligned} & 1.00 \\ & 1.00 \end{aligned}$ | $\begin{aligned} & 1.00 \\ & 1.00 \end{aligned}$ | 7 7 |
| 2.Biogas |  |  |  |  |  |
| -Installed capacity <= 1 MW | 0.30 | 0.50 | 1.00 | 1.00 | 7 |
| -Installed capacity > 1 MW | 0.30 | 0.30 | 1.00 | 1.00 | 7 |
| 3.Waste |  |  |  |  |  |
| -AD and Land fill | 2.50 | 2.50 | 1.00 | 1.00 | 7 |
| -Thermal process | 2.50 | 3.50 | 1.00 | 1.00 | 7 |
| 4. Wind energy |  |  |  |  |  |
| -Installed capacity $<=50 \mathrm{~kW}$ | 3.50 | 4.50 | 1.50 | 1.50 | 10 |
| -Installed capacity > 50 kW | 3.50 | 3.50 | 1.50 | 1.50 | 10 |
| 5.Micro water turbine |  |  |  |  |  |
| -Installed capacity $50 \mathrm{~kW}-<200 \mathrm{~kW}$ | 0.40 | 0.80 | 1.00 | 1.00 | 7 |
| -Installed capacity $<50 \mathrm{~kW}$ | 0.80 | 1.50 | 1.00 | 1.00 | 7 |
| 6.Solar energy (PV,CSP, etc.) | 8.00 | 8.00 | 1.50 | 1.50 | 10 |

From the PV capacity installation report of Thailand [15], the DEDE has PV pr ojects a round t he c ountry with c apacity $3,510.5 \mathrm{~kW}$ s ince 1983 t o 2010.

However, the PV generation system that was installed in Thailand can be separated into a stand-alone system (off-grid) and grid-connected system. The total capacity of the PV generation system of Thailand in 2010 is 49.21 MW as shown in Figure 1.17, which are 29.65 MW of stand-alone and 19.56 MW of grid-connected system. This installed capacity c an classify b y the solar a pplication system as s hown in F igure 1.18. It s hows t hat t he s olar e nergy is t he m ost a pplied s ource t o p roduce t he electricity as 26.8 MW or $54.4 \%$ of total capacity.


Figure 1.17 PV installation capacity since 1983-2010 of Thailand


Solar application system
Figure 1.18 Installation capacity of solar application system since 1983-2010 of

> Thailand

### 1.4 Motivation

Generally, distribution systems are the radial type systems, which can be found inrural or suburban a reas, are normally de signed to ope rate w ithout a ny generation sources connected to the grid. The i nterconnection of any generation sources on the distribution system can be variously impact on the power flow, voltage regulations at customer load and utility equipments. These impacts may be caused the system ope ration in either pos itively or ne gatively de pending on $t$ he di stribution system ope rating ch aracteristics and the DG/characteristics [2]. There ar e s ome positive impacts which are the system benefits as follows:

- Voltage support and improved power quality.
- Loss reduction in some cases [16].
- Peak shaving.
- Transmission and distribution capacity release.
- Deferment of new or upgraded T\&D infrastructure.
- Improved utility system reliability.

Achieving the above benefits is in practice much more difficult than often realized. DG s ources $m$ ust be reliable, dispatchable of $t$ he pr oper size, and at $t$ he proper 1 ocations. Therefore, w ithout pr oper pl anning a nd a nalysis, D Gs c an ha ve negative impacts to the distribution system as follows:

- Large pe netration level of D Gm ay de teriorate s ystem ope ration, system security and system dynamic performance.
- Conventional distribution systems need adequate protection in order to accommodate exchange of power.
- Signaling for dispatch of resources becomes extremely complicated.
- Connection and revenue contracts are difficult to establish.
- Safety concerns with energy generated from multiple sources.

Since D Gs have a dvantages a nd di sadvantages as mentioned above also many DGs will not be utility owned or will be variable energy sources such as solar and wind. There is no guarantee that these conditions will be satisfied and that the full
system support benefits will be realized. Thus, DG interconnection policy should take into account how to maximize the desired benefits.

The PV generation is one type of inverter-based DGs that will be come more widespread at this time and the future due to anticipated cost reductions in PV technology and installation. PV systems are ex pected to play a p romising role as a clean power el ectricity source in meeting future el ectricity d emands. However, the integration of PV systems into power networks can cause both benefits and drawbacks depending on locations, operating modes and allowable sizes [17-19]. Since, the PV system is int erfaced to the di stribution s ystem $t$ hrough a pul se width modulated (PWM) inverter, which is the main source of harmonic current. They may create the associated i njection of ha rmonic c urrents $i$ nto $t$ he di stribution $s$ ystem 1 ead t o malfunction of harmonic-sensitive equipment if the injection of harmonic currents is allowed to reach excessive levels [20]. Therefore, with the g rowing pe netration of inverter-based DGs especially phot ovoltaic distributed generation (PV-DG). T here should be more concerns about technical constrains and existing regulation by $t$ he Distribution Network Operators (DNO) in order to assess the impact of PV system on the electric power quality and limit their integration.

In system planning and design aspect, there are some of the issue concerns of utilities when PV-DGs are interconnected to the grid as follows:

- Harmonic distortion
- Power fluctuation
- Voltage regulation


### 1.4.1 Harmonic distortion [21]

From a ha rmonic m odeling standpoint, inverter-based D G units can be viewed as a nonlinear load injecting harmonic current into the distribution feeder [22]. This could result in an unacceptable level of total harmonic distortion (THD).

THD can be applying to both current and voltage which are defined as the ratio of the rms value of harmonics and the rms value of the fundamental. THD of currents (THDi) varies from a few pe rcent to m ore than $100 \%$. THD of vol tage (THDv) is usually less than $5 \%$. However, THDv below $5 \%$ is widely considered to
be acceptable, but values above $10 \%$ are un acceptable a nd will c ause problems for sensitive equipment and loads.

It is w idely $r$ ecognized $t$ hat $t$ he pr esence of $n$ onlinear $c$ omponents of power systems $m$ anifests in the appe arance of ha rmonics [23]. T he presence of harmonics in a power system is undesirable for a number of reasons, some of which are:

- Harmonics increase power losses in both utility and customer equipment.
- Sometimes ha rmonics $m$ ay p rovoke $m$ alfunctioning of sensitive load or control equipment.
- Harmonics ha ving s ignificant m agnitudes can caus e ar eduction of lifetime of m otors, t ransformers, capacitor banks a nd s ome ot her equipment.
- A harmonic resonance problem with shunt capacitor c an be o ccurred in some condition. And it produces large spikes of current and voltage on the system which cause the operation of protective devices or the failure of equipment.

Power electronic devices, as used for PV inverter, may cause a harmonic's problems. $T$ he $m$ agnitude $a$ nd $t$ he or der $o f h$ armonic $c$ urrents $i n j e c t e d ~ b y d c h a c$ inverters de pend on $t$ he technology of the inverter a nd mode of its op eration. For example, a forced-commutated inverter with pulse-width-modulation operated in the linear range, will introduce only harmonics in the range of high frequencies, i.e., at and/or around multiples of the carrier frequency [24].

Many $p$ apers s tudied power qua lity pr oblems in ha rmonic a spect associated with a large num ber of distributed grid-connected PV s ystem on a distribution network [25-29]. The $m$ ain obj ective of $t$ hese pa pers is to analyze $t$ he observed phenomena of harmonic interference of large populations of these inverters. From the results of these papers, it indicates that the increasing of grid-connected PV systems can cause the harmonic di stortion problem due to hi gh pe netration of PV system.

### 1.4.2 Power fluctuations

At a large s cale, the uncertainty characteristic of po wer output of PV systems can affect the power quality and reliability. Since, the power generated from PV s ystems will be fluctuating all the time depending on climate conditions a nd geographic location. In the future, if a large number of PV systems are connected to the grids, the fluctuation of PV power output may cause the problems such as voltage fluctuation and large frequency deviation in electric power system operation [30-35]. Therefore, for the high penetration of PV systems interconnection to the grids without reduction of the $r$ eliability and pow er qu ality of ut ility pow er systems, suitable measures should be applied to the PV systems side.

Battery storage is the one device which c an be us ed to reduce the P V power out put fluctuation. There are s everal studies which investigations a imed at improving the performance of PV systems equipped with batteries [36-41]. However, using the energy storage device increases the capital cost, as it needs maintenance.

Therefore, in order to assess the power quality of a distribution system under nor mal op erating conditions with high penetration of PV-DGs and without batteries, electrical characteristics of the current injection into the distribution network are ne cessary to be un derstood thoroughly. Generally, the power s ystem analysis under normal ope ration is based on a deterministic load flow c alculation. However, the solar energy sources of PV-DG units are often uncontrollable and thus introduce uncertain factors into t he di stribution s ystem. As a result, t he PV ou tput power injection into the distribution system is fluctuating throughout the year [34].

As mentioned above, the combination of many uncertain factors may be make the difficulty and complicated to assess a distribution system performance under normal ope rating $c$ onditions through a de terministic approach. Therefore, a probabilistic approach is necessary in order to assess the system power quality, which these uncertain factors are taking into account, e.g. power losses, voltage regulation, power fluctuation and harmonic distortion.

### 1.4.3 Voltage regulation

Generally, load-tap-changing ( LTC) tr ansformers a ts ubstations, supplementary line regulators on feeders, and switched capacitors on feeders are used to regulate the voltage of a radial distribution system. Through the application of these devices, the voltages at a customer load point are kept within the acceptable limit. In practice, the voltage regulation is normally based on $r$ adial pow er flows from the substation to the load points. Interconnection of DG introduces meshed power flows, which may be interfering with the system voltage regulation. The following regulation problems may occur [2]:

- Low voltage caused by DG just downstream of a regulator with line-drop compensation

If a DG i s connected to downstream of a vol tage $r$ egulator or LTC transformer, which is using considerable line drop compensation as shown in Figure 1.19. Then the regulation controls will be unable to properly measure feeder demand. Fig.1.19 demonstrates that the improper voltage profiles may occur under with and without DG. In case of with DG, the voltage is reduced because the DG decreases the observed load at the line drop compensator (LDC) control. In this case, the regulator confuses into setting a voltage low er than is required to maintain adequate service levels at the end of the feeder.


Fig. 1.19 Case of DG unit interfering with voltage regulation on a distribution feeder

- High voltage due to $D G$

DG may also result in high voltage at some electric customers. It can be seen that high penetration of DGs may cause reverse power flow to the substation. For this case, the vol tage can increase al ong the f eeder. In s ome locations where the primary voltage is already high and the load is low, the rise in voltage can be enough to push the voltage over the acceptable limit [21].

Furthermore, the problem of high voltage may occur from the uncertainty of power fluctuation due to both PV-DG as mentioned above and load demand. If PVDG does not operate inc oordinate with the local 1 oad , t hey m ight increase t he variations be tween the maximum a nd minimum vol tage le vel. As the mini mum voltage level could remain in a high load with a low PV-DG power situation, but the maximum voltage level could increase in low load with full PV-DG production.

- Interaction with regulating equipment

Some D Gs us e f eedback to oc ontrol vol tage, $b$ ut th is $w$ ay int eracts negatively to the utility regulation equipment. There may be unde sirable cycling of regulation de vices a nd not iceable pow er qua lity i mpacts unde r such c onditions. In case of intermittent power output of PV-DG, this may change the system voltage or current flows e nough to c ause a regulator tap change or an ope ration of a s witched capacitor [21].

As mentioned all above, it can be seen that there is some interesting issues concern with P V-DG included harmonic distortion, power fluctuation and difficulty of voltage regulation. The installation of PV-DG into a distribution system can cause both benefits and drawbacks depending on locations, operating modes and allowable sizes.

Therefore, this dissertation proposes the sizing of photovoltaic distributed generators in a distribution system with consideration of solar radiation and harmonic distortion. The objective is to maximize the power produced by PV-DG installation and minimize s ystem lo sses, while the vol tage profile as well as harmonic cur rent, total ha rmonic vol tage distortion (THDv) a nd total de mand di stortion (TDD) at the point of common coupling (PCC) are kept at an acceptable limit.

The pr obabilistic a pproach is a pplied t o solve t he pr oblem because distribution utilities de liver electric energy to their customers within an appropriate range to maximize customer satisfaction and to reduce system losses. In the presence of PV-DG, it is difficult to regulate voltage since the PV system is a type of random generation. That is de pendent of $t$ he environmental conditions na mely the vol tage variation of PV-DG at the PCC as a function of solar radiation level [42-43]. So, it is impossible to a chieve a realistic evaluation of $w$ here a nd when an overvoltage can happen in a distribution system during an investigate a period of time by simply using a de terministic 1 oad $f$ low (DLF) analysis, which is ba sed on $t$ he $m$ ean va lues or expected values of customer loads and generations as inputs to solve a problem. For this reason, a probabilistic load flow (PLF) a nalysis is e mployed to ensure that the solution will be effective for the acceptable voltage deviation.

### 1.5 Literature Reviews

### 1.5.1 Literature Review on Optimal DG Sizing and Location

Generally, DG is an electric pow er source connected directly to a distribution ne twork or customer site. Since D G can be installed close to anyplace, which is required the advantages of DG in terms of efficiency and losses, investment, reliability and pow er q uality. However, interconnection of D G can create some technical problems such as difficulty of voltage regulation, over a thermal limit a nd exceeded harmonic di stortion, etc. The severity of t his problem depends on s ize, location, number and operating mode of DG. Therefore, several papers studied how to determine optimal size and location of DG, which is based on the synchronous type, in a di stribution ne twork with consideration of $t$ echnical constraints as $m$ entioned above.

Authors in [44] and [45] proposed technique to minimize power losses in a distribution feeder by optimizing DG model in terms of size, location and operating point of D G. S ensitivity analysis for po wer 1 osses in terms of DG s ize a nd D G operating point was also performed in these papers. The proposed technique has been developed with c onsidering the load cha racteristic w ith constant i mpedance and constant c urrent models. Test results indi cated that real pow er loss can be reduced with a DG of optimal size, located at an optimal place in the feeder.

DGs in [46] ar e treated as mobile reactive com pensators, which can be connected as a kind of reactive compensation equipment to improve voltage stability. A qua ntitative index is proposed to e valuate the vol tage stability of load nodes to decide $t$ he opt imal D G location. The opt imal p enetration level of D G at opt imal location is the n calculated by P rimal-Dual Interior P oint M ethod. T he opt imal calculation realizes the hi ghest vol tage e ligible ratio and minimum pow er los say adjusting the reactive power output of DG in a precondition of system security. The simulation results show $t$ he $b$ est $l$ ocation and $p$ enetration $l$ evel of $D G$ for vol tage stability in the test system.

A multi-objective a pproach for optimal location and sizing to maximize the pe netration of DG in a distribution ne twork is proposed in [47]. The proposed optimization pr ocedure is a n e volutionary m ulti-objective a lgorithm ba sed on $t$ he genetic algorithm (GA) with the $\varepsilon$-constrained $t$ echnique. The goal of this methodology is to maximize the benefits of the presence of DGs and limit the network performance deterioration because DG is not connected at optimal locations.

Reference [48] pr oposed A nt C olony O ptimization (ACO) ba sed algorithm for DG sources allocation and sizing in distribution systems. The objective is de fined a s m inimization of DG i nvestment c ost a nd t otal ope ration c ost of t he system subject to a set of constraints such as capacity of feeder, voltage limit and total DG capacity limitation.

The optimal D G num ber a nd s izing $f$ ormulated a $s$ a NonLinear Programming (NLP) pr oblem ha s been proposed in [49]. The ma jor objective is improving the vol tage p rofiles of di stribution ne tworks us ing multiple DG s ources. The cons traints of this paper are the nodal com plex vol tage and DG po wer factors. Further, t he s tatic l oad m odels a sconstant po wer, c onstant current a nd c onstant impedance are investigated.

In [50], the optimization of DG units and shunt capacitors for economic operation of di stribution s ystems was proposed. T he m inimization of ove rall investment cost with the integration of DG units and shunt capacitors is assessed with the c onsideration of s upply qua lity, r eliability a nd e nergy 1 oss. A n ew pl anning methodology by using Particle $S$ warm Optimization (PSO) is proposed to minimize the overall cost for optimal sizing and location of DG units and shunt capacitors.

The effect of the variation of loads with voltage and frequency for optimal allocation of DG in terms of location and size is addressed in [51]. The objective is to minimize the real power loss a nd to maintain the vol tage within specified limits at buses us ing genetic algorithms in a distribution network. However, an evaluation of frequency on analysis under certain assumptions regarding frequency has been made within the permissible range 0.98 pu to 1.02 pu .

The paper in [52] presents an approach by using the genetic algorithm for optimal a llocation of s ingle a nd multiple D Gs in terms of loc ation and size to minimize an average of locational charges for unit act ive pow er at buses. It means that the bus with maximum locational charge may be chosen as optimal location. The voltage at buses within specified limits is considered as the constraint. The static load models as constant power, constant current and constant impedance were considered.

The paper in [53] proposed the selection of optimal location and size of multiple DGs by using Kalman filter algorithm. The selection of optimal locations of multiple D Gs was considered from tot al pow er los sin as teady-state ope ration. Thereafter, the optimal sizes are determined by using the Kalman filter algorithm. The objective is to minimize the total power loss of system. The merit of this algorithm is that it took the only few samples from a large-scale power system with many data samples and therefore, it reduced the computational requirement dramatically during the optimization process.

The opt imal D G s izing pr oblem in [54] is $t$ ackled $b$ y $t$ he $S$ equential Quadratic Programming deterministic technique. The DG modeling is separated into two types, which a re treated as a P V bus a nd PQ bus. T he obj ective function is minimizing real po wer losses with consideration of the thermal network restrictions and the bus c omplex vo ltage c onstraints. F urthermore, the i mpact of bot $h t$ he $D G$ modeling a nd $t$ he static load response to vol tage upon $t$ he opt imal $D G$ s ize were studied.

A multi-objective placement and penetration level of DGs were examined in [55]. By concerning both technical and economical parameters of a power system using genetic a lgorithm combined with Multi-Attribute D ecision Making (MADM) method. The t echnical parameter including total losses, bus es vol tage profile, 1 ine capacity limits and total reactive power flow were considered. The approach consists
of GA for de termining the be st generation configurations of system by considering technical parameters that are included in the fitness function, and MADM techniques for ranking the selected plans regard to technical and economical attributes.

A combination of genetic algorithm and simulated annealing is presented in [56] f or opt imal D G a llocation in di stribution ne tworks. The obj ective isto minimize di stribution po wer losses for a fixed number of DGs and a s pecific total capacity of D Gs. The constraints a re bus es $v$ oltage $m$ agnitude and 1 ine c urrent capacity limits. Through this algorithm, a significant improvement in the optimization goal is achieved.

From [44-56], methods, objective function, parameter constraints and load models for opt imal sizing a nd location of DG ba sed on the synchronous type in a distribution system can be summarized as shown in Table 1.4. Among the methods for optimal DG sizing and location, the genetic algorithm is the most popular method.

Table 1.4 Summary of the methodologies for optimal DG sizing and location

| Methodologies | Objective functions | Constraints | Load models |
| :--- | :--- | :--- | :--- |
| - Genetic algorithm (GA) |  |  |  |
| - Nonlinear programming |  |  |  |
| - Sequential quadratic programming |  |  |  |
| - Particle swarm optimization | - min (real power loss) | - Bus voltages | - Constant power |
| - Ant colony optimization | $-\min$ (voltage variation) | - Thermal limits | - Constant current |
| - Combination of GA and Simulated | $-\min$ (investment and | - DG capacity | - Constant impedance |
| annealing <br> - Combination of GA and MADM <br> - Kalman filter algorithm | operating cost) |  |  |

### 1.5.2 Literature Review on Optimal PV-DG Sizing

The methodologies as shown in Table 1.4, how ever, are used for optimal synchronous-based DG sizing a nd location, which all are based on a deterministic approach. There a re m any t echniques presented in bot hs tand-alone a nd g ridconnected systems through de terministic a nd p robabilistic a pproaches. In o rder to determine a PV-DG size and assess a distribution system performance under normal operating conditions.

In order to determine PV-DG size based on a probabilistic approach, an analysis of a stand-alone PV system on output of PV systems and load demands were studied in [57]. Reliability indices in terms of 1 oss of 1 oad hou rs (LOLH), e nergy losses and total cost of investment are the main factors for e valuating the opt imal operation of stand-alone P V scheme. Solar radiation a nd load demand in [57] were modeled as s tochastic va riables us ing hi storical da ta a nd experimentation, respectively.

In [58], a uthors presented several techniques to design a stand-alone PV system. Three probabilistic methods (i.e., fixed days of battery backup and recharge, loss of 1 oad probability (LOLP) and Markov Chain modeling) were proposed. The LOLP $t$ echnique ha $s b$ een suggested as the most $r$ eliable be cause it pr ovided a detailed view of the system performance to design the PV system among all proposed techniques.

In [59], a uthors proposed the sizing procedure for stand-alone a nd gridconnected PV systems. It was based on an analytical method and sized not only PV arrays but a lso ba tteries a nd i nverters. T he analytical s izing $m$ ethod could be categorized into three types, which are based on loads and irradiation, available areas and LOLP. The obj ective was not to minimize system cost m athematically, but to give an optimal design at the practical level on the basis of experimental knowledge.

In [60], a uthors pr oposed a pr obabilistic a pproach tod esign a gridconnected P V s ystem in low vol tage feeder. The pr oposed m ethod de termined the optimum PV rating with a voltage constraint at the specified connecting point.

At present, inverter-based DG can perform functions other than supplying real power. The innovation and improvements in electronic devices allow using DG to improve power quality in the grid [61]. For this reason, specific planning tools for optimal placement and sizing of DG should be adopted to consider the multiple and contrasting goals that the DNO strives to achieve [62].

Furthermore, in case of PV-DG, the uncontrollable of solar energy sources can introduce uncertain factors into a distribution system such as voltage fluctuation as mentioned in section 1.4. Therefore, it is necessary to obtain an effective method
for optimal PV-DG sizing and location. To cope with this, a probabilistic approach is an alternative for solving the problem.

However, most research works related to optimal PV-DG sizing normally do not consider the pow er qua lity constraints i.e., ha rmonic c urrents from PV-DG, total harmonic di stortion due to PV-DG as well as background harmonic condition. Furthermore, the PV model in relevant papers is mostly using an approximate model which ac power output of PV system is assumed to be linearly proportional to solar radiation. And they do not mention about optimal location of PV-DG installation.

### 1.6 Objectives and Scope of Works

Objectives of this dissertation can be described as follows:

- To obtain an optimal size of single and multiple PV-DGs in a distribution system with consideration of solar radiation and harmonic distortion.
- To propose the steady state voltage stability index method for determining the proper locations of PV-DG as utility planning and design aspect.
- To compare PV-DG sizing between consideration with and without system background harmonics.
- To assess power qua lity i mpacts on a distribution system unde r nor mal operating conditions with installation of PV-DG units.
- To study an impact of static load models and power factor control on the optimal sizing of PV-DG.
- To study an effect of PV inverter models and existing DGs in a distribution system on the optimal PV-DG sizing.

Scope of the research can be summarized as follows:

- The proposed technique is based on a probabilistic approach, i.e., Monte Carlo simulation.
- The PV model in this research is based on Sharp 80Wp, NE-80E2E solar module, which is pol ycrystalline s ilicon material t ype. T he ma ximum power ( 80 W ) is defined at $1000 \mathrm{~W} / \mathrm{m}^{2}$ solar r adiation and $25^{\circ} \mathrm{C}$ cell temperature under standard test conditions (STC).
- The PV model is integrated with the simplified perturb and observe (P\&O) maximum power point tracking (MPPT) technique to automatically find the $m$ aximum pow er out put unde $r$ a $g$ iven $s$ olar $r$ adiation a nd a mbient temperature, which are based on real statistical data.
- The substation vol tage a nd 1 oad de mand are assumed to be a random variable with a normal distribution function.
- The protection coordination is not considered in this research.
- The c oordination of vol tage regulation e quipments $w$ ith P V-DGs is not considered.
- PV-DGs are considered without batteries storage.
- A distribution system is assumed to be balanced.
- The ba ckground ha rmonics a re $t$ aking i nto a ccount to determine the optimal size of PV-DG.
- Other $t$ ypes of $D$ Gs, such as s ynchronous a nd induction $g$ eneration, are allowed with various locations, ope rating modes and sizes to incorporate with the optimal PV-DG sizing.
- In order to evaluate the harmonic distortion levels in a distribution system, the PV-DG is modeled as a ha rmonic cur rent source based on statistical harmonic current spectra from measurements of a PV farm.
- The steady state voltage stability index (VSI) method is used to determine the proper locations for placing a PV-DG.
- The objective function of the proposed method is to:
- Minimize average system real power loss

Subjected to the technical constraints as follows:

- Node voltage limited as $1 \pm 0.05 p u$ or $0.95 \mathrm{pu} \leq V_{i} \leq 1.05 \mathrm{pu}$
- Harmonic currents at each order (up to $33^{\text {rd }}$ ) should not exceed the limits, which are based on IEC 61727 standard [63].
- Total ha rmonic vol tage di stortion ( $\mathrm{THD}_{\mathrm{v}}$ ) at P CC should not exceed 5\%, which is based on IEEE 519-1992 standard [64].
- Total de mand di stortion (TDD) at P CC s hould not e xceed $5 \%$, which is based on IEC 61727 standard.
- An actual PEA 51-bus radial distribution system in Thailand and a 33-bus system are used for test cases of the proposed method.


### 1.7 Synopsis of Chapters

The material in this dissertation is organized as follows:
Chapter 1 pr esents world's P V ge neration ove rview, s olar P V technologies and PV generation in Thailand. The literature reviews of related research are also addressed. The motivation, objective, scope of work and research a pproach are also mentioned.

Chapter 2 presents models of grid-connected PV system components. The statistical mode ls of $s$ olar $r$ adiation and ambient $t$ emperature a re pr oposed. The probabilistic load model, PV model, MPPT and PV inverter model are also addressed.

Chapter 3 presents the $s$ teady state vol tage stability inde x me thod to determine the proper PV-DG installation location.

Chapter 4 pr esents the modified Newton method to calculate power flow in a radial distribution system. The ha rmonic $m$ odeling a nd calculation are al so presented.

Chapter 5 proposes the algorithm of PV-DG sizing technique and problem formulation. The numerical results of several study cases are also investigated.

Chapter 6 presents contributions of the dissertation, conclusion and future works.

## CHAPTER II MODELING OF SYSTEM COMPONENTS

### 2.1 Grid-Connected Photovoltaic Systems

PV power s ystems have ma de a successful transition from s mall standalone sites to large grid-connected systems. The utility interconnection brings a new dimension to the renewable power economy by pooling the temporal excess or the shortfall in the renewable powerwith the conn ecting grid that $g$ enerates ba se-load power using conventional fuels. Generally, the grid supplies power to the site loads when needed or absorbs the excess power from the site when available. A kilowatthour meter is used to measure the power delivered to the grid and another is used to measure the power drawn from the grid.

As shown in Figure 2.1 [9], the principal components in a single pha se grid-connected, PV system side consists of the array itself with two leads from each string sent to a combiner box that includes blocking diodes, individual fuses for each string and usually a lightning surge arrestor. Two wires from the combiner box deliver dc power to a fused array disconnected switch, which allows the PVs to be completely isolated from the system. The inverter sends ac power through a breaker to the utility service panel. Additional components not shown include the maximum power point tracker (MPPT), a ground-fault circuit interrupter (GFCI) that shuts the system down if any currents flow to ground and circuitry to disconnect the PV system from the grid if the utility loses power. The inverter, some of the fuses and $s$ witches, the MPPT, GFCI and other power management devices are usually integrated into a single power conditioning unit (PCU). Figure 2.2 shows the simplified schematic diagram of the grid-connected PV systems included PV generator, PCU and step-up transformer.


Figure 2.1 Principal components in a single phase grid-connected PV systems


Figure 2.2 Simplified sehematic diagram of grid-connected PV systems

For large-scale grid-connected PV systems, a PV generator consists of a typical c onnection group of P V strings, of which t he t ype ofc onnection is not considered in this dissertation. The MPPT is integrated into the PCU which sends the maximum power through a step-up transformer to the grid. In power quality aspect, a large a mount of c onverted pow er from D C to A C side c an c ause t he ha rmonic problem. This de pends on $t$ ypical i nverter $t$ opologies a nd op erating po int, which depends on power produced by PV generator under a solar radiation condition.

### 2.2 Solar Radiation and Ambient Temperature Modeling

To analyze PV systems, we need to know how much sunlight is available. A fairly straightforward set of equations can be used to predict where the sun is in the
sky at a ny time of a day for an ylocation on earth a s well as solar intensity (or insolation which incident solar radiation) on a clear day. To determine average daily solar radiation under the combination of clear and cloudy conditions that exist at any site long-term measurements of sunlight hitting a horizontal surface is required.

### 2.2.1 Statistical Model of Solar Radiation

In this dissertation, hourly solar radiation is modeled as a statistical model based on data measured from a study area. Hourly variations of solar radiation were collected in one year. Figure 2.3 s hows the e xample of hour ly v ariations of s olar radiation in Chiang Mai during 6.00 am to 6.00 pm on January to December 2007 (see Appendix A for complete data). The S I unit for solar radiation is w att per s quare meter $\left(\mathrm{W} / \mathrm{m}^{2}\right)$.


Figure 2.3 Hourly variations of solar radiation in Chiang Mai during $6.00 \mathrm{am}-6.00 \mathrm{pm}$ on Jan-Dec 2007

From $t$ he $m$ easurements, int his $c$ ase, $t$ he pr obability de nsity of $s$ olar radiation may not be able to accurately model as a conventional distribution function e.g., W eibull, Gamma, Exponential, e tc. Hence the s olar radiation is modeled as a stochastic variable from historical measurement data, as shown in Figure 2.4.


Figure 2.4 Probability density of solar radiation corresponding to Figure 2.3

### 2.2.2 Statistical Model of Ambient Temperature

Generally, the operating t emperature is not c onsidered in P V s ystem analyzing. Because the temperature has a few effect on the PV system output power. Thus, in PV model, the power output of PV system is approximately proportional to solar radiation. However, the power output of PV system can be changed around $10 \%$ (constant solar radiation) when the ambient temperature is varied from the minimum to $m$ aximum va lues, ba sed on $m$ easurement da ta, by simulation. Therefore, in $t$ his dissertation, the temperature effect is included in the PV model.

Similarly to solar radiation, hourly variations of ambient temperature are modeled as a s tatistical model based on data measured from the same area and time (see Appendix A for complete da ta). Figure 2.5 s hows t he hou rly variations of ambient temperature (degree) in Chiang Mai during 6.00 am to 6.00 pm on January to December 2007.


Figure 2.5 Hourly variations of ambient temperature in Chiang Mai during - $6.00 \mathrm{am}-6.00 \mathrm{pm}$ on Jan-Dec 2007

From Figure 2.5, the a mbient temperature can be modeled as a W eibull distribution function, as shown in Figure 2.6. The probability de nsity function of a Weibull random variable $x$ is [65]

$$
\begin{equation*}
f(x)=\frac{\beta}{\alpha^{\beta}} x^{\beta-1} \exp \left[-\left(\frac{x}{\alpha}\right)^{\beta}\right] \tag{2.1}
\end{equation*}
$$

where $0 \leq x<\infty, \beta>0$ is the shape parameter and $\alpha>0$ is the scale parameter of the distribution. The cumulative probability distribution function is

$$
\begin{equation*}
F(x)=1-\exp \left[-\left(\frac{x}{\alpha}\right)^{\beta}\right] \tag{2.2}
\end{equation*}
$$

By the inverse transform method
give

$$
\begin{equation*}
U=F(x)=1-\exp \left[-\left(\frac{x}{\alpha}\right)^{\beta}\right] \tag{2.3}
\end{equation*}
$$

so

$$
\begin{equation*}
X=\alpha[-\ln (1-U)]^{1 / \beta} \tag{2.4}
\end{equation*}
$$

where $U$ is a uniformly distributed random variate between $[0,1]$. Since $1-U$ is also a uniformly distributed random variate between [0,1], Equation (2.4) becomes

$$
\begin{equation*}
X=\alpha(-\ln U)^{1 / \beta} \tag{2.5}
\end{equation*}
$$

where the values of $\alpha$ is 29.2763 and $\beta$ is 6.5052 from the curve fitting.


Figure 2.6 Cumulative probability of ambient temperature corresponding to Figure 2.5

### 2.3 Photovoltaic Modeling

For this research work, a model of moderate complexity was us ed [66]. The PV model included temperature de pendence of the photo-current $\left(I_{p h}\right)$ and the saturation current of the diode $\left(I_{0}\right)$. A series resistance $\left(R_{s}\right)$ was included, but not a shunt resistance. A single shunt diode was used with the di ode qua lity factor set to achieve the best curve match. This model is a simplified version of the two di ode model presented by Gow and Manning [67]. The simplified equivalent circuit of a PV cell is shown in Figure 2.7.


Figure 2.7 Simplified equivalent circuit of the PV cell model

Furthermore, PV model in this dissertation is integrated with maximum power point tracker as will be described in next section. Accuracy and complexity can be introduced to the model by adding in turn

- Temperature dependence of the diode saturation current $I_{0}$
- Temperature dependence of the photo current $I_{p h}$
- Series r esistance $R_{S}$, which gives a m ore accu rate s hape be tween the maximum power point and the open circuit voltage
- Either al lowing the di ode quality factor to become a va riable parameter, instead of being fixed at either 1 or 2

From t he c orresponding s tatistical m odel, r andom s olar r adiation $\left(G_{a}\right)$ and ambient te mperature $\left(T_{a}\right)$ are generated by Monte $C$ arlo simulation. These da ta are required to evaluate the I-V characteristic of PV model. The voltage output of the PV cellis represented by Equation (2.6), which is a function of $t$ he $p$ hotocurrent mainly determined by load current and depended on the solar irradiation level and cell temperature during the operation.

$$
\begin{equation*}
V_{p v}=\left(A k T_{c} / q\right) \ln \left(I_{p h}+I_{0}-I_{p v} / I_{0}\right)-I_{p v} R_{s} \tag{2.6}
\end{equation*}
$$

Equation (2.6) can be rewritten as

$$
\begin{equation*}
I_{p v}=I_{p h}-I_{0}\left(e^{\frac{q\left(V_{p \nu}+I_{p T} R_{s}\right)}{A k T_{y}}}-1\right) \tag{2.7}
\end{equation*}
$$

The equations which describe the I-V characteristic of PV model are as follows:

$$
\begin{align*}
& I_{p h}=I_{p h\left(T_{1}\right)}\left[1+K_{0}\left(T_{c}-T_{1}\right)\right]  \tag{2.8}\\
& I_{p h\left(T_{1}\right)}=G_{a}\left(I_{s c(s t c)} / G_{a(s t c)}\right)  \tag{2.9}\\
& K_{0}=\left(I_{s c\left(T_{2}\right)}-I_{s c\left(T_{1}\right)}\right) /\left(T_{2}-T_{1}\right)  \tag{2.10}\\
& I_{0}=I_{0\left(T_{1}\right)}\left(\frac{T_{c}}{T_{1}}\right)^{3 / A} \times e^{-\frac{q V_{g}}{A k}\left(\frac{1}{T_{c}}-\frac{1}{T_{1}}\right)}  \tag{2.11}\\
& I_{0\left(T_{1}\right)}=I_{s c\left(T_{1}\right)} /\left(e^{\frac{q V_{o c\left(T_{1}\right)}^{A k T_{1}}}{A l}}-1\right) \tag{2.12}
\end{align*}
$$

where $I_{p h}$ is temperature dependence of the photo-current (A)
$I_{0}$ is temperature dependence of the diode saturation current (A)
$I_{p v}$ is cell output current (A)

```
    Vpv is cell output voltage (V)
    Voc is cell open circuit voltage (V)
    Vg is band gap voltage (V)
    R
    q is electron charge (coulomb)
    k is Boltzmann constant (J/K)
    A is diode quality factor
    T
    Ga}\mathrm{ is operating solar radiation (W/m}\mp@subsup{}{}{2}
    G
    T
    T
Isc(stc)}\mathrm{ is short circuit current per cell at STC (A)
Isc(\mp@subsup{T}{2}{})}\mathrm{ is short circuit current per cell at T2 (A)
```

The photo-current is directly proportional to solar radiation. When short circuit oc curs in the cell, negligible current can flows in the di ode. Hence, the proportionality c onstant in Equation (2.9) is set so the rated short circuit c urrent is delivered under rated solar radiation. The relationship between the photo-current and temperature is linear as shown in Equation (2.8) and is deduced by noting the change of photo-current with the change of temperature as follow by Equation (2.10).

When the c ell is not i lluminated, the r elationship between the c ell's terminal voltage and current is given by the Shockley equation. When the cell is open circuited and illuminated, the photo-current flows entirely in the diode. The I-V curve is offset from the origin by the photo generated current as follow by Equation (2.7). For the va lue of the saturation c urrent at $25^{\circ} \mathrm{C}$ is cal culated us ing the open-circuit voltage and short-circuit current at this temperature as follow by Equation (2.12). The relationship of di ode s aturation c urrent t ot emperature i s m ore c omplex, but fortunately it contains no variables requiring evaluation as follow by Equation (2.11).

The va lue of di ode qua lity factor is de pending on the $m$ aterial type of photovoltaic cell, it takes a value be tween 1 and 2. Generally, the value of diode quality factor $A=2$ for crystalline silicon and $A<2$ for amorphous silicon PV cell.

Therefore, the value of 2 i s used astypical in nor mal ope ration of the $m$ odel validation for the Sharp 80 Wp PV module, which is a crystalline silicon material.

For the series resistance $\left(R_{s}\right)$ of PV cell, it can be obtained using the only manufacturer supplied data for the PV modules at Standard Test C onditions (STC), such as open-circuit voltage, short-circuit current and maximum power. The equations which used to evaluate the value of the series resistance are given by the expression [68-69]:

$$
\begin{gather*}
R_{s}=\left[1-\frac{F F}{F F_{0}}\right] \times\left[\frac{V_{o c(s t c)}}{I_{s c(s t)}}\right]  \tag{2.13}\\
F F_{0}=\left[V_{o c(n o m}-P_{\max }^{C} /\left[V_{o c(s t c)} \times I_{s c(s t c)}\right]\right.  \tag{2.14}\\
\left.\left.V_{o c(n o m)}=V_{o c(n o m)}+0.72\right)\right] /\left[V_{o c(\text { nom })}+1\right]  \tag{2.15}\\
V_{t}=A k T_{c} / q / V_{t}  \tag{2.16}\\
P_{\max }^{C}=P_{\max (s t)}^{M} /\left(N_{s m} \times N_{p m}\right)  \tag{2.17}\\
V_{o c(s t c)}=V_{o c(s t c)}^{M} / N_{s m}  \tag{2.18}\\
I_{s c(s t c)}=I_{s c(s t)}^{M} / N_{p m} \tag{2.19}
\end{gather*}
$$

where $V_{o c(s t c)}$ is cell open circuit voltage at STC (V)

$$
V_{o c(s t c)}^{M} \text { is module open circuit voltage at STC (V) }
$$

$V_{t}$ is cell thermal voltage (V)
$I_{s c(s t c)}^{M}$ is module short circuit current at STC (A)
$P_{\max }^{C} \quad$ is cell maximum power (W)
$P_{\max [(\mathrm{Fstc})}^{M} \quad$ is module maximum power at $\mathrm{STC}(\mathrm{W})$
$F F$ is fill factor
$N_{S m}$ is number of series cells in each cell parallel branches
$N_{p m}$ is number of cell parallel branches in module

Normally, cells are grouped in to "modules", which are encapsulated with various ma terials to protect the $c$ ells a nd the e lectrical c onnectors from the environment. T he m anufacturers s upply P V c ells in m odules, c onsisting of $N_{p m}$ parallel branches, each with $N_{s m}$ solar cells in series, as shown in Figure 2.8 [69].


Figure 2.8 PV module consists of $N_{p m}$ parallel branches, each of $N_{s m}$ cells in series
In order to develop the model of PV module, the cell output voltage $\left(V_{p v}\right)$ is then multiplied by the number of the cells connected in series $N_{s m}$ to calculate the full module voltage $\left(V^{M}\right)$, they all have the same voltage in each parallel branches. In the s ame w ay, t he c ell out put c urrent $\left(I_{p v}\right)$ is then m ultiplied b y the num ber of branches connected in parallel $N_{p m}$ to obt ain the full module current $\left(I^{M}\right)$, they all carry the same current in series each branches.

The modules in a PV system are typically conn ected in "arrays". Figure 2.9 illustrates the case of an array with $M_{p}$ parallel branches each with $M_{s}$ modules in series [69]. The a pplied voltage at the a rray's te rminal is de noted by $V^{A}$, while the total c urrent of t he a rray is de noted b y E quation (2.21). If it is a ssumed that the modules are identical and the ambient solar radiation is the same on all the modules, then the array's current is Equation (2.22).

$$
\begin{align*}
I^{A} & =\sum_{i=1}^{M_{p}} I_{i}  \tag{2.21}\\
I^{A} & =M_{p} \times I^{M} \tag{2.22}
\end{align*}
$$



Figure 2.9 PV array consists of $M_{p}$ parallel branches, each with $M_{s}$ modules in series

In $t$ his di ssertation, the $\mathrm{P} V$ a rrays a re $m$ odeled based on a connection group of Sharp 80 Wp PV modules to obtain the rated size of PV-DG. The rated power of PV-DG is de fined as peak power output, when solar radiation is $1000 \mathrm{~W} / \mathrm{m}^{2}$ and cell t emperature i s $25^{\circ} \mathrm{C}$. H owever, a t ype of c onnection of P V m odules is not considered in this work.

Since the working temperature of the P V cells $\left(T_{c}\right)$ depends exclusively on t he s olar r adiation $\left(G_{a}\right)$ and on $t$ he ambient $t$ emperature $\left(T_{a}\right)$. To he lp t he researcher ac count for changes in cell performance with temperature, manufacturers often provide an indicator called the NOCT, which stands for Normal Operating Cell Temperature. The NOCT is cell temperature in a module when ambient is $20^{\circ} \mathrm{C}$, solar radiation is $800 \mathrm{~W} / \mathrm{m}^{2}$ and wind speed is $1 \mathrm{~m} / \mathrm{s}$. T he value of NOCT for modules currently on the market varies from about 42 to $46{ }^{\circ} \mathrm{C}$. However, in this dissertation, the value of NOCT is $42^{\circ} \mathrm{C}$ from testing. To account for other ambient conditions, the following expression may be used [68]:

$$
\begin{equation*}
T_{c}=T_{a}+G_{a}\left[\frac{N O C T-20^{\circ} \mathrm{C}}{800 \mathrm{~W} / \mathrm{m}^{2}}\right] \tag{2.23}
\end{equation*}
$$

where $\quad T_{c}$ is cell temperature ( ${ }^{\circ} \mathrm{C}$ )
$T_{a}$ is ambient temperature $\left({ }^{\circ} \mathrm{C}\right)$
$G_{a}$ is solar radiation $\left(\mathrm{W} / \mathrm{m}^{2}\right)$

### 2.3.1 PV Model Implementation in Matlab/Simulink

This section shows how the mathematical model of PV module described in section 2.3 works by implemented in Matlab/Simulink. The mathematical model of PV module can be represented in Simulink implementation as shown in Figure 2.10. The input of PV module is an operating solar radiation $G_{a}$ and ambient temperature $T_{a}$. The ma jor pa rt of structure is M atlab function bl ocks, w hich e ach c ontains necessary e quations 1 isted in pr evious $s$ ection, as follows from Equations (2.7) to (2.20), to calculate the cell current $I_{p v}$. Then I-V and P-V curve can be established by changing the terminal output cell voltage $V_{p v}$.


Figure 2.10 PV module model implementation in Simulink

A P Vm odule of S harp 80 W p i s us ed o examine on P Vm odel implementation. The electrical characteristics of Sharp 80 Wp under STC $\left(\mathrm{T}_{\mathrm{c}}=25^{\circ} \mathrm{C}\right.$, $\mathrm{G}_{\mathrm{a}}=1000 \mathrm{~W} / \mathrm{m}^{2}$ ) as given in Table 2.1, which the specification sheet can be found in Appendix B. The c urrent a nd pow er v ersus v oltage of P V m odule p rovided b y manufacturer is shown in Figure 2.11.

Table 2.1 The key specifications of the Sharp 80 Wp PV module at STC ( $1000 \mathrm{~W} / \mathrm{m}^{2}$ solar radiation, $25^{\circ} \mathrm{C}$ cell temperature)


Figure 2.11 Current and power versus voltage characteristics of Sharp 80Wp PV module provided by manufacturer $\left(\mathrm{T}_{\mathrm{c}}=25^{\circ} \mathrm{C}\right)$

In or der to compare simulation results with the e lectrical characteristic provided b y m anufacturer. T he out put c urrent a nd pow er r elated to voltage are simulated for va rious solar radiation levels as 600,800 a nd $1000 \mathrm{~W} / \mathrm{m}^{2}$, while cell temperature is fixed at $25^{\circ} \mathrm{C}$. The s imulation r esults of c urrent a nd pow er ve rsus voltage characteristics are shown in Figures 2.12 and 2.13 respectively.


Figure 2.12 I-V characteristics of Sharp 80 Wp PV module by simulation $\left(\mathrm{T}_{\mathrm{c}}=25^{\circ} \mathrm{C}\right)$


Figure 2.13 P-V characteristics of Sharp 80 Wp PV module by simulation $\left(\mathrm{T}_{\mathrm{c}}=25^{\circ} \mathrm{C}\right)$

Note from Figures 2. 12 and 2.13 that t he r esults s how good correspondence to the model. Table 2.2 summarizes the values of various parameters used in PV model.

Table 2.2 Summary of PV model parameters values

| Parameters | Values |
| :---: | :---: |
| Band gap voltage, $V_{g}$ | 1.12 V (for crystalline silicon) |
| Electron charge, q | $1.6 e^{-19}$ Coulomb |
| Boltzmann constant , $k$ | $1.38 e^{-23} \mathrm{~J} / \mathrm{K}$ |
| Diode quality factor, $A$ | 2 (for crystalline silicon) |
| Cell temperature at STC , $T_{1}$ | $25^{\circ} \mathrm{C}$ |
| Cell temperature at condition-2, $T_{2}$ | $75^{\circ} \mathrm{C}$ |
| Short circuit current at STC , $I_{s c(s t c)}$ | $5.31 \mathrm{~A}\left(\mathrm{~T}_{1}\right)$ |
| Short circuit current at $T_{2}, I_{s c}\left(T_{2}\right)$ | $5.47 \mathrm{~A}\left(3 \%\right.$ increase of $\left.I_{s c(s t c)}\right)$ |
| Series resistance , $R_{S}$ | $\square 0.0132 \Omega / \mathrm{cell}$ |
| Number of series cells, $N_{s m}$ | 36 |
| Number of parallel branches , $N_{p m}$ | 1 |
| NOCT | $42^{\circ} \mathrm{C}$ |

### 2.3.2 PV Model Validation

This s ection s hows the r esults of Sharp 80 Wp PV m odule m odel validation using $r$ eal data from me asurement of $s$ olar $r$ adiation. Pyranometer was directly connected to the portable PV module tester (I-V checker/MP-140), as shown in Figure 2.14. Ambient te mperature was recorded by a thermocouple s ensor. The data measured of solar radiation and ambient temperature is shown in Figures 2.15 and 2.16 respectively. All of this is measured in one of a cloudy day on 21 October 2008.


Figure 2.14 PV module tester (I-V Checker/MP-140), EKO Instruments Co., Ltd.


Figure 2.15 Data measured in time series of the solar radiation


Figure 2.16 Data measured in time series of the ambient temperature

The m odel va lidation is done b yc omparing between results which obtained by I-V checker and simulation results obtained by Matlab/Simulink. In order to validate the model, three different levels of solar radiation are considered. Table 2.3 shows $t$ he $s$ pecified values of hi gh, $m$ edium a nd 1 ow solar $r$ adiation levels and ambient temperatures corresponding to a certain solar radiation.

Table 2.3 Solar radiation levels and corresponded ambient temperatures

| Level | Solar radiation $\left(\right.$ W/m $^{2}$ ) | Ambient temperature ${ }^{\circ}{ }^{\circ} \mathrm{C}$ ) | Time ( hr ) |
| :---: | :---: | :---: | :---: |
| High | 1025.3 | 36.04 | 11.50 |
| Medium | 600.6 | 30.91 | 09.20 |
| Low | 205.1 | 33.80 | 14.00 |

Various out puts such as $I_{s c}, V_{o c}, P_{m}$, etc., are compared between $t$ he simulation results and the measurements on three levels of solar radiation, as shown in Table 2.4. A good agreement of the results can be seen although it has a small error. From Table 2.4, it indicates that the error of the fill factor (FF) is less than $5 \%$ for all solar radiation levels. F urthermore, it shows that the e rror of a ll pa rameters is less than $5 \%$ except at low solar radiation. The I-V curve which obtained by I-V checker and simulation on high, medium and low solar radiation are shown in Figures 2.17 to 2.22 respectively.
Table 2.4 Output comparison between the simulation results and the measurements on different

| Level | High solar radiation |  |  | Medium solar radiation |  |  | Low solar radiation |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Output | Measured | Simulated | \% Error | Measured | Simulated | \% Error | Measured | Simulated | \% Error |
| $\mathrm{I}_{\text {cc }}$ (A) | 5.619 | 5.572 | 0.83 | 3.149 | 3.232 | 2.64 | 1.101 | 1.099 | 0.23 |
| $\mathrm{V}_{\text {oc }}$ (V) | 19.18 | 18.51 | 3.49 | 19.51 | 18.66 | 4.36 | 17.50 | 7. | 1.83 |
| $\mathrm{P}_{\mathrm{m}}$ (W) | 69.66 | 67.38 | $3.27$ | - 42.55 | 40.52 | 4.77 | 13.50 |  | 6.81 |
| $\mathrm{I}_{\mathrm{m}}$ (A) | 4.979 | 4.847 | $2.65$ | $2.842$ | 2.834 | 0.29 | 0.969 | 0.960 | $0.93$ |
| $\mathbf{V}_{\mathrm{m}}$ (A) | 13.99 | 13.90 | 0.64 | $=14.97$ | 14.30 | 4.48 | 13.93 | 13.10 | 5.96 |
| FF | 0.6465 | 0.6533 | 1.05 | D 0.6925 | 0.6718 | 2.99 | 0.7011 | 0.666 | 4.96 |

Note. Fill factor (FF) is the ratio of the $P_{m}$ and the product of $I_{s c}$ and $V_{o c}$ as given in Equation (2.14)

MP-140


Figure 2.17 I-V characteristic curve from I-V checker at high solar radiation


Figure 2.18 I-V characteristic curve from simulation at high solar radiation

MP-140


Figure 2.19 I-V characteristic curve from I-V checker at medium solar radiation


Figure 2.20 I-V characteristic curve from simulation at medium solar radiation

MP-140


Figure 2.21 I-V characteristic curve from I-V checker at low solar radiation


Figure 2.22 I-V characteristic curve from simulation at low solar radiation

### 2.3.3 Maximum Power Point Tracking (MPPT)

The maximum power point tracking of a PV array is usually an essential part of a PV system to draw peak power from the solar array in order to maximize the produced energy to DC-DC converter, as a part of PCU in Figure 2.2. Many MPPT methods have be en de veloped a nd i mplemented. The m ethods vary in complexity, sensors $r$ equired, $c$ onvergence $s$ peed, $c$ ost, $r$ ange of effectiveness, $i$ mplementation hardware, popularity, and in other respects. They range from the almost obvious (but not necessarily ineffective) to the most creative (not necessarily most effective).

In fact, so many methods have been developed like, Perturb and Observe Method ( $\mathrm{P} \& \mathrm{O}$ ), Incremental C onductance M ethod ( IC), S liding M ode C ontrol Method that are widely used for MPPT system in PV, and other method like, Constant Voltage ( CV ), S hort-current P ulse M ethod, O pen V oltage M ethod, Fuzzy Logic Control, Neutral Network, and other unpopular method is also used in different field of MPPT [70-72].

Therefore, it has become difficult to adequately determine which method, newly proposed or existing is most appropriate for a given PV system. However, the simplified P\&O MPPT technique is used in this dissertation.

The $\mathrm{P} \& \mathrm{O}$ algorithms operate by periodically perturbing (i.e. incrementing or decrementing) the array terminal voltage and comparing the PV output power with that of the previous perturbation cycle. If the PV array operating voltage changes and power increases $(d P / d V>0)$, the control system moves the PV array operating point in that direction; otherwise the operating point is moved in the opposite direction. In the next perturbation cycle the algorithm continues in the same way [70].

Generally, cl assic P \& O method is widely us ed, the perturbations of the PV ope rating poi nt ha ve a fixed m agnitude. In an analysis, t he m agnitude of perturbation is $0.37 \%$ of $V_{o c}$ of PV array. The algorithm of the classic $\mathrm{P} \& \mathrm{O}$ is shown in Figure 2.23.


Figure 2.23 Flow chart of classic $\mathrm{P} \& \mathrm{O}$ technique

### 2.4 PV Inverter Modeling

Since, PV systems are interfaced to a distribution system through a PWMbased inverter, which is one of the main harmonic sources. These harmonic sources may c reate pr oblemst o vi cinity equipment de pending on $t$ heir ha rmonic or der, amplitudes a nd system characteristic. Unfortunately, there is no s tandard ha rmonic waveform of inverter-based DG since the harmonic injection from inverter-based DG depends on the design of individual manufacture.

Therefore, the P V-DG is m odeled as a ha rmonic c urrent s ource at the point of c ommon c oupling ( PCC ). T he ha rmonic c urrent spectra of P V-DG were collected from m easurements of a 6 MWp PV farm on M ay 2010 in N akhon Ratchasima pr ovince, north-eastern r egion of T hailand. The s ystem s chematic diagram of the PV farm is shown in Figure 2.24.


Figure 2.24 System schematic diagram of the PV farm

Harmonic current measurements are based on 540 units of 11 kW Sunny Mini C entral S MC-11000TL g rid-connected i nverter. Maximum i nverter out put current and total harmonic current distortion (THDi) at various solar radiation levels are shown in Figure 2.25.


Figure 2.25 Maximum inverter output current and $\% \mathrm{THDi}$ at various solar radiations

From Figure 2.25, it in dicates that the T HDi a nd output current of the inverter varied proportionallyt ot he s olar radiation. F urthermore, from $t$ he relationship of \%THDi and solar radiation, nonlinearity of the inverter becomes large at low solar radiation. Under such conditions, the large amount of harmonics will be injected to a distribution system. Although, the magnitudes of harmonic currents are small at l ow s olar r adiation, but the $\% \mathrm{THDi}$ is la rge. This ma y de teriorate the electrical power quality of systems, if the large number of PV-DGs is interconnected to a di stribution system. In this di ssertation, onl y harmonic current magnitudes a re considered for worse-case study.

Figures 2.26 to 2.28 show some of harmonic spectrum up to $33^{\text {rd }}$ order at PCC of the PV farm corresponding to solar radiation at 200, 600 and $1000 \mathrm{~W} / \mathrm{m}^{2}$, respectively. The typical harmonic current in percent of fundamental $(50 \mathrm{~Hz})$ can be seen in Table 2.5.


Figure 2.26 Harmonic current spectrum at PCC of the PV farm corresponding to $200 \mathrm{~W} / \mathrm{m}^{2}$ solar radiation


Figure 2.27 Harmonic current spectrum at PCC of the PV farm corresponding to


Figure 2.28 Harmonic current spectrum at PCC of the PV farm corresponding to $1000 \mathrm{~W} / \mathrm{m}^{2}$ solar radiation

Table 2.5 Typical harmonic current in percent of fundamental corresponding to solar radiation

| Harmonic <br> order | Typical harmonic current in percent of fundamental (\%) |  |  |
| :---: | :---: | :---: | :---: |
|  | $200 \mathrm{~W} / \mathrm{m}^{2}$ | $600 \mathrm{~W} / \mathrm{m}^{2}$ | $1000 \mathrm{~W} / \mathrm{m}^{2}$ |
| 2 | 0.976 | 0.301 | 0.211 |
| 3 | 6.829 | 1.506 | 1.057 |
| 4 | 1.951 | 0.452 | 0.317 |
| 5 | 12.195 | 4.066 | 2.748 |
| 6 | 0.976 | 0.301 | 0.211 |
| 7 | 2.439 | 0.753 | 0.317 |
| 8 | 0.488 | 0.301 | 0.106 |
| 9 | 0.976 | 0.301 | 0.211 |
| 10 | 0.976 | 0.301 | 0.211 |
| 11 | 2.439 | 0.602 | 0.423 |
| 12 | 0.976 | 0.301 | 0.211 |
| 13 | 0.976 | 0.301 | 0.211 |
| 14 | 0.976 | 0.301 | 0.211 |
| 15 | 0.976 | 0.301 | 0.211 |
| 16 | 0.976 | 0.301 | 0.211 |
| 17 | 0.976 | 0.151 | 0.211 |
| 18 | 0.488 | 0.151 | 0.106 |
| 19 | 0.976 | 0.151 | 0.106 |
| 20 | 0.488 | 0.151 | 0.106 |
| 21 | 0.976 | 0.151 | 0.106 |
| 22 | 0.976 | 0.301 | 0.211 |
| 23 | 0.976 | 0.301 | 0.211 |
| 24 | 0.488 | 0.151 | 0.106 |
| 25 | 0.976 | 0.151 | 0.106 |
| 26 | 0.488 | 0.151 | 0.106 |
| 27 | 0.488 | 0.151 | 0.106 |
| 28 | 0.488 | 0.151 | 0.106 |
| 29 | 0.488 | 0.151 | 0.106 |
| 30 | 0.488 | 0.151 | 0.106 |
| 31 | 0.976 | 0.151 | 0.106 |
| 32 | 0.488 | 0.151 | 0.106 |
| 33 | 0.976 | 0.151 | 0.106 |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

In practical, interconnections of small PV-DGs may not result in violation of the power quality standard. However, with the existent of background harmonics and the increase of pe netration level, PV-DGs may create harmonic cu rrents which bring to e xcessive le vels of tot al ha rmonic voltage di stortion (THDv) at P CC. Therefore, pr ior to i interconnect P V-DGs, ut ilities should c onsider s everal technical constraints to avoid the power quality impacts from PV-DGs. Background harmonics modeling will be mentioned in Chapter 4 on harmonic calculations section.

### 2.5 Substation and Load Modeling

Since, in or der to find the opt imal size of P V-DG without c onsidering uncertainties of 1 oad a nd $s$ ubstation vol tage may be que stionable. Therefore, in probabilistic load flows process, load demand and substation voltage are assumed to be a random variable with a normal distribution.

### 2.5.1 Probabilistic Load Models

In $t$ his $w$ ork, all 1 oads a re $c$ orrelated a nd follow the s ame probability density function of load demands $\left(L_{d}\right)$ as given by:

$$
\begin{equation*}
f\left(L_{d}\right)=\frac{1}{\sigma \sqrt{2 \pi}} \exp -\frac{\left(L_{d}-\bar{L}_{d}\right)^{2}}{2 \sigma^{2}} \tag{2.24}
\end{equation*}
$$

where $\bar{L}_{d}$ is the mean value of load demand
$\sigma$ is the standard deviation, which set to $10 \%$ in this dissertation

Generally, the cl assical constant pow er load model is typically us ed in power flow studies of a distribution system. However, the actual load of a distribution system cannot just be modeled us ing constant pow er model. The us e of constant current, constant impedance or a composite of all these load models are required to accurately represent the load. Therefore, three static load models are investigated to study the impact of load model on optimal PV-DG sizing. Probability density function of all static load models follows normal distribution in Equation (2.24). These types of loads are typically categorized as follows [73]:

- Constant Power Load Model (CP) :

The active and reactive powers do not vary with voltage magnitude changes.

- Constant Current Load Model (CI) :

The a ctive and $r$ eactive pow ers are di rectly pr oportional $t$ ot he $v$ oltage magnitude.

- Constant Impedance Load Model (CZ) :

The act ive and reactive pow ers a re pr oportional $t$ ot he $s$ quare of $v$ oltage magnitude.

The active and reactive power characteristics of three static load models are given by:

$$
\begin{align*}
& P=P_{0}\left[a_{p}+b_{p}\left(\frac{|V|}{\left|V_{0}\right|}\right)+c_{p}\left(\frac{|V|}{\left|V_{0}\right|}\right)^{2}\right]  \tag{2.25}\\
& Q=Q_{0}\left[a_{q}+b_{q}\left(\frac{|V|}{\left|V_{0}\right|}\right)+c_{q}\left(\frac{|V|}{\left|V_{0}\right|}\right)^{2}\right] \tag{2.26}
\end{align*}
$$

where $P_{0}$ and $Q_{0}$ are active and reactive powers consumed at a reference voltage $V_{0}$, respectively. C onstant coefficients de pend on $t$ he $t$ ype of 1 oad $t$ hat is be ing represented, e.g.,

$$
\begin{aligned}
& \text { for } \mathrm{CP} \text { model } a_{p}=a_{q}=1, b_{p}=b_{q}=c_{p}=c_{q}=0 \\
& \text { for } \mathrm{CI} \text { model } b_{p}=b_{q}=1, a_{p}=a_{q}=c_{p}=c_{q}=0 \\
& \text { for } \mathrm{CZ} \text { model } c_{p}=c_{q}=1, a_{p}=a_{q}=b_{p}=b_{q}=0
\end{aligned}
$$

Figure 2.29 illustrates an example of act ive pow er probability d ensity function at a load point with a normal distribution, which $\bar{L}_{d}$ is 145 kW , and $\sigma$ is $10 \%$.


Figure 2.29 Probability density function of a load point with a normal distribution

### 2.5.2 Probabilistic Substation Voltage Model

Similarly to load models, substation voltage $\left(V_{s}\right)$ is a ssumed to be a random va riable $w$ ith nor mal di stribution. $B$ ut the $s$ tandard d eviation of substation voltage is set to $1.5 \%$ to cover in 0.95 pu to 1.05 pu range of mean value $\left(\bar{V}_{s}\right)$, which is a ssumed t o be 1.0 p u . T he pr obability density f unction of s ubstation vol tage illustrates in Figure 2.30 and it can be expressed mathematically as follow:

$$
\begin{equation*}
f\left(V_{s}\right)=\frac{1}{\sigma \sqrt{2 \pi}} \exp -\frac{\left(V_{s}-\bar{V}_{s}\right)^{2}}{2 \sigma^{2}} \tag{2.27}
\end{equation*}
$$

where $\bar{V}_{s}$ is the mean value of substation voltage
$\sigma$ is the standard deviation, which set to $1.5 \%$ in this dissertation


Figure 2.30 Probability density function of substation voltage with a normal distribution

## CHAPTER III

## A VOLTAGE STABILITY INDEX FOR RADIAL DISTRIBUTION NETWORKS

### 3.1 Introduction

In practice, utilities cannot assign the PV -DGs in stallation location to be connected to the feeder because it mainly de pends on customers who own the PV systems. However, for planning aspect, this chapter presents a voltage stability index (VSI) for ide ntifying the mos ts ensitive bus to the vol tage collapse in a radial distribution network for selecting the proper PV-DG located.

With an increased 1 oading a nde xploitation of $t$ he e xisting pow er structure, the probability of occurrence of voltage collapse is significantly greater than before and the identification of the nodes which are prone to the voltage fluctuations has attracted more attention for the transmission and as well a s the distribution systems. The main causes of voltage instability are as follows:

- The load on transmission line is too high
- The voltage sources are too far from the load centers
- The voltage sources are too low
- There is insufficient load reactive compensation

For operating a power system in a safe and secure manner, all insecure operating states must be identified well in advance to facilitate corrective measures to overcome the threat of possible voltage collapse [74].

### 3.2 Voltage Stability Index Methodology [75]

For deriving the voltage stability index of radial distribution networks, we need to consider a simple two-node system as shown in Figure 3.1.


Figure 3.1 Simple two-node system
From Figure 3.1, the following equations can be written:
and

$$
\begin{equation*}
I_{1}=\frac{\left|V_{n 1}\right| \angle \delta_{n 1}-\left|V_{n 2}\right| \angle \delta_{n 2}}{R_{l}+j X_{I}} \tag{3.1}
\end{equation*}
$$

where $l$ is branch number
$n_{1}$ is branch end node
$n_{2}$ is receiving end node
$I_{l}$ is current of branch $l$
$V_{n 1}$ is voltage of node $n_{1}$
$V_{n 2}$ is voltage of node $n_{2}$
$P_{n 2}$ is total active power load fed through node $n_{2}$
$Q_{n 2}$ is total reactive power load fed through node $n_{2}$
From Equations (3.1) and (3.2), we obtain:

$$
\begin{equation*}
\frac{\left|V_{n 1}\right| \angle \delta_{n 1}-\left|V_{n 2}\right| \angle \delta_{n 2}}{R_{l}+j X_{l}}=\frac{P_{n 2}-j Q_{n 2}}{V_{n 2}^{*}} \tag{3.3}
\end{equation*}
$$

therefore

$$
\begin{equation*}
\left|V_{n 1}\right|\left|V_{n 2}\right| \angle\left(\delta_{n 1}-\delta_{n 2}\right)-\left|V_{n 2}\right|^{2}=\left(P_{n 2}-j Q_{n 2}\right)\left(R_{l}+j X_{l}\right) \tag{3.4}
\end{equation*}
$$

and

$$
\begin{align*}
&\left|V_{n 1}\right|\left|V_{n 2}\right| \cos \left(\delta_{n 1}-\delta_{n 2}\right)-\left|V_{n 2}\right|^{2}+j\left|V_{n 1}\right|\left|V_{n 2}\right| \sin \left(\delta_{n 1}-\delta_{n 2}\right) \\
&=\left(P_{n 2} R_{l}+Q_{n 2} X_{l}\right)+j\left(P_{n 2} X_{1}-Q_{n 2} R_{l}\right) \tag{3.5}
\end{align*}
$$

Separating real and imaginary parts of Equation (3.5), we obtain:

$$
\begin{equation*}
\left|V_{n 1}\right|\left|V_{n 2}\right| \cos \left(\delta_{n 1}-\delta_{n 2}\right)-\left|V_{n 2}\right|^{2}=P_{n 2} R_{l}+Q_{n 2} X_{l} \tag{3.6}
\end{equation*}
$$

therefore

$$
\begin{equation*}
\left|V_{n 1}\right|\left|V_{n 2}\right| \cos \left(\delta_{n 1}-\delta_{n 2}\right)=\left|V_{n 2}\right|^{2}+P_{n 2} R_{l}+Q_{n 2} X_{l} \tag{3.7}
\end{equation*}
$$

and

$$
\begin{equation*}
\left|V_{n 1}\right|\left|V_{n 2}\right| \sin \left(\delta_{n 1}-\delta_{n 2}\right)=P_{n 2} X_{1}-Q_{n 2} R_{l} \tag{3.8}
\end{equation*}
$$

Squaring and adding Equations (3.7) and (3.8), we obtain:

$$
\begin{equation*}
\left|V_{n 1}\right|^{2}\left|V_{n 2}\right|^{2}=\left(\left|V_{n 2}\right|^{2}+P_{n 2} R_{l}+Q_{n 2} X_{l}\right)^{2}+\left(P_{n 2} X_{l}-Q_{n 2} R_{l}\right)^{2} \tag{3.9}
\end{equation*}
$$

From algebraic formula:

$$
\begin{equation*}
(a+b+c)^{2}=a^{2}+b^{2}+c^{2}+2(a b+b c+a c) \tag{3.10}
\end{equation*}
$$

We can rearrange Equation (3.9) to

$$
\begin{equation*}
\left|V_{n 2}\right|^{4}+2\left(P_{n 2} R_{l}+Q_{n 2} X_{1}-0.5\left|V_{n 1}\right|^{2}\right)\left|V_{n 2}\right|^{2}+\left(R_{l}^{2}+X_{l}^{2}\right)\left(P_{n 2}^{2}+Q_{n 2}^{2}\right)=0 \tag{3.11}
\end{equation*}
$$

or

$$
\begin{equation*}
\left|V_{n 2}\right|^{4}-\left.\left(\left|V_{n 1}\right|^{2}-2 P_{n 2} R_{1}-2 Q_{n 2} X_{l}\right) V_{n 2}\right|^{2}+\left(P_{n 2}^{2}+Q_{n 2}^{2}\right)\left(R_{l}^{2}+X_{l}^{2}\right)=0 \tag{3.12}
\end{equation*}
$$

Equation (3.12) has a straightforward solution and does not depend on the phase angle, which simplifies the problem formulation. In a distribution system, the voltage angle is not so important be cause the $v$ ariation of vol tage angle from the substation to the tail-end of a distribution feeder is only few degrees [76].

Let

$$
\begin{equation*}
b_{l}=\left(\left|V_{n 1}\right|^{2}-2 P_{n 2} R_{l}-2 Q_{n 2} X_{l}\right) \tag{3.13}
\end{equation*}
$$

and

$$
\begin{equation*}
c_{l}=\left(P_{n 2}^{2}+Q_{n 2}^{2}\right)\left(R_{l}^{2}+X_{l}^{2}\right) \tag{3.14}
\end{equation*}
$$

From Equations (3.12) to (3.14), we get

$$
\begin{equation*}
\left|V_{n 2}\right|^{4}-b_{l}\left|V_{n 2}\right|^{2}+c_{l}=0 \tag{3.15}
\end{equation*}
$$

From Equation (3.15), it is seen that the receiving end voltage $\left|V_{n 2}\right|$ has four solutions follow to a given formulation:

$$
\begin{equation*}
\left|V_{n 2}\right|= \pm \sqrt{\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}} \tag{3.16}
\end{equation*}
$$

and these solutions are:

1. $0.707 \sqrt{b_{l}-\sqrt{b_{l}^{2}-4 c_{l}}}$
2. $-0.707 \sqrt{b_{l}-\sqrt{b_{l}^{2}-4 c_{l}}}$
3. $-0.707 \sqrt{b_{l}+\sqrt{b_{l}^{2}-4 c_{l}}}$
4. $0.707 \sqrt{b_{l}+\sqrt{b_{l}^{2}-4 c_{l}}}$

Now, for realistic data, when $P, Q, R, X$ and $V$ are expressed in per unit, $b_{l}$ is always positive because the term $2\left\{P_{n 2} R_{l}+Q_{n 2} X_{l}\right\}$ is very small as compared to $\left|V_{n 1}\right|^{2}$ and also the term $4 c_{l}$ is very small as compared to $b_{l}^{2}$. Therefore, $\sqrt{b_{l}^{2}-4 c_{l}}$ is nearly equal to $b_{1}$ and hence the first two solutions of $\left|V_{n 2}\right|$ are nearly equal to zero and not feasible. The third solution is negative and so not feasible. The fourth solution of $\left|V_{n 2}\right|$ is positive and feasible. Therefore, the solution of Equation (3.15) is unique.

That is

$$
\begin{equation*}
\left|V_{n 2}\right|=0.707 \sqrt{b_{l}+\sqrt{b_{l}^{2}-4 c_{l}}} \tag{3.17}
\end{equation*}
$$

From Equation (3.17), it is seen that a feasible load flow solution of radial distribution networks will exist if:

$$
\begin{equation*}
b_{l}^{2}-4 c_{l} \geq 0 \tag{3.18}
\end{equation*}
$$

Thus, from Equations (3.13), (3.14) and (3.18), we get

$$
\begin{equation*}
\left(\left|V_{n 1}\right|^{2}-2 P_{n 2} R_{l}-2 Q_{n 2} X_{l}\right)^{2}-4\left(P_{n 2}^{2}+Q_{n 2}^{2}\right)\left(R_{l}^{2}+X_{l}^{2}\right) \geq 0 \tag{3.19}
\end{equation*}
$$

After simplification we get

$$
\begin{equation*}
\left|V_{n 1}\right|^{4}-4\left(P_{n 2} X_{l}-Q_{n 2} R_{l}\right)^{2}-\left.4\left(P_{n 2} R_{l}+Q_{n 2} X_{l}\right) V_{n 1}\right|^{2} \geq 0 \tag{3.20}
\end{equation*}
$$

Let

$$
\begin{equation*}
\operatorname{VSI}\left(n_{2}\right)=\left|V_{n 1}\right|^{4}-4\left(P_{n 2} X_{l}-Q_{n 2} R_{l}\right)^{2}-4\left(P_{n 2} R_{l}+Q_{n 2} X_{l}\right)\left|V_{n 1}\right|^{2} \tag{3.21}
\end{equation*}
$$

where $\operatorname{VSI}\left(n_{2}\right)$ is voltage stability index of node $n_{2}$, for stable operation of the radial distribution networks, $\operatorname{VSI}\left(n_{2}\right) \geq 0$ for $n_{2}=2,3, \ldots, N_{b}$

By using this voltage stability index, one can measure the level of stability of $r$ adial di stribution ne tworks a nd $t$ hereby a ppropriate a ction may be $t$ aken if $t$ he index indicates a poor level of stability.

Actually, $P_{n 2}$ and $Q_{n 2}$ are sum of the active and reactive power loads of all the nodes be yond no de $n_{2}$ plus the active and reactive power load of node $n_{2}$ itself plus the sum of the active and reactive power losses of all the branches beyond node $n_{2}$.

After load flow calculation, when the load was i ncreased gradually, the voltages of all nodes are known, the branch currents are known. Therefore, $P_{n 2}$ and $Q_{n 2}$ for $n_{2}=2,3, \ldots ., N_{b}$ can easily be calculated using Equation (3.2) and hence one can easily calculate the vol tage stability index of each node. The node at which the value of the stability index is minimum, is more sensitive to the voltage collapse and more candidate to install PV-DG.

In $t$ his di ssertation, load flow a nalysis $w$ as a chieved $b y$ us ing the 1 oad flow algorithm given in Chapter 4 in which each nodes power is multiplied by a load factor as [74]:

$$
\begin{equation*}
S=\lambda S_{b} \tag{3.22}
\end{equation*}
$$

where $\lambda$ is load factor and $S_{b}$ is base load

The c ritical bus id entified by e valuating bus v oltage m agnitudes jus t before the load flow diverges. Divergence is assumed when the iteration number of the 1 oad f low a lgorithm r eaches to 200 . T he a lgorithm of vol tage s tability index calculation can be summarized as seen the flow chart in Figure 3.2.


Figure 3.2 Flow chart of voltage stability index calculation

### 3.3 Test Results of Voltage Stability Index Calculation

To demonstrate the methodology of the voltage stability index (VSI), this section presents a 15 -bus radial distribution system from [77] for VSI calculation. The single-line diagram of the 15 -bus test system is shown in Figure 3.3. Line and load data of this system are given in Table 3.1.


Figure 3.3 Single-line diagram of the 15 -bus radial distribution system

Table 3.1 Line data and load data of the 15 -bus radial distribution system

| Branch | Line impedance (ohm) |  | Load demand (kW/kVar) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{R}$ | $\boldsymbol{X}$ | $\boldsymbol{P}_{\boldsymbol{L}}$ | $\boldsymbol{Q}_{\boldsymbol{L}}$ |
| $1-2$ | 1.35309 | 1.32349 | 44.10 | 44.99 |
| $2-3$ | 1.17024 | 1.14464 | 70.00 | 71.41 |
| $3-4$ | 0.84111 | 0.82271 | 140.00 | 142.82 |
| $4-5$ | 1.52348 | 1.02760 | 44.10 | 44.99 |
| $4-6$ | 1.19702 | 0.80740 | 140.00 | 142.82 |
| $4-7$ | 2.23081 | 1.50470 | 70.00 | 71.41 |
| $3-8$ | 1.79553 | 1.21110 | 140.00 | 142.82 |
| $8-9$ | 2.44845 | 1.65150 | 70.00 | 71.41 |
| $9-10$ | 2.01317 | 1.35790 | 44.10 | 44.99 |
| $2-11$ | 2.01317 | 1.35790 | 70.00 | 71.41 |
| $11-12$ | 1.68671 | 1.13770 | 44.10 | 44.99 |
| $2-13$ | 2.55727 | 1.72490 | 140.00 | 142.82 |
| $13-14$ | 1.08820 | 0.73400 | 140.00 | 142.82 |
| $13-15$ | 1.25143 | 0.84410 | 70.00 | 71.41 |

Total base load $=1.226$ MW, 1.251 MVar

For thi s s imulation, a di fferent $m$ agnitude substation vol tages $\left(\left|V_{s}\right|\right)$ and different static load models of constant power (CP), constant current (CI) and constant impedance ( CZ ) a re c onsidered. T able 3.2 s hows bus stability indi ces and i ts minimum bus voltage for different load models and substation voltage 1.0 pu of the 15 -bus test system.

Table 3.2 Bus stability indices for different load models of the 15-bus test system

$$
\left(\left|V_{s}\right|=1.0 p u\right)
$$

| Bus No. | CP model |  | CI model |  | CZ model |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | VSI | $\left\|\mathbf{V}_{\text {min }}\right\| \mathbf{p u}$ | $\mathbf{V S I}$ | $\left\|\mathbf{V}_{\text {min }}\right\| \mathbf{p u}$ | VSI | $\left\|\mathbf{V}_{\text {min }}\right\| \mathbf{p u}$ |
| 2 | 0.2042 | 0.7259 | 0.3259 | 0.7854 | 0.4841 | 0.8479 |
| 3 | 0.0936 | 0.5737 | 0.1991 | 0.6768 | 0.3505 | 0.7731 |
| 4 | 0.0679 | 0.5140 | 0.1600 | 0.6339 | 0.3048 | 0.7436 |
| 5 | 0.0644 | 0.5038 | 0.1541 | 0.6266 | 0.2975 | 0.7385 |
| 6 | 0.0563 | 0.4879 | 0.1434 | 0.6156 | 0.2855 | 0.7311 |
| 7 | 0.0572 | 0.4897 | 0.1446 | 0.6169 | 0.2868 | 0.7319 |
| 8 | 0.0600 | 0.5004 | 0.1523 | 0.6268 | 0.2971 | 0.7391 |
| 9 | 0.0411 | 0.4528 | 0.1257 | 0.5963 | 0.2663 | 0.7187 |
| 10 | 0.0365 | 0.4374 | 0.1183 | 0.5866 | 0.2572 | 0.7122 |
| 11 | 0.2407 | 0.7009 | 0.3334 | 0.7603 | 0.4707 | 0.8285 |
| 12 | 0.2302 | 0.6927 | 0.3200 | 0.7522 | 0.4572 | 0.8223 |
| 13 | 0.1310 | 0.6126 | 0.2139 | 0.6873 | 0.3590 | 0.7774 |
| 14 | 0.1234 | 0.5930 | 0.2021 | 0.6707 | 0.3431 | 0.7655 |
| 15 | 0.1308 | 0.6015 | 0.2109 | 0.6778 | 0.3523 | 0.7705 |

From Table 3.2, when the load is increased gradually, it founds that the minimum value of voltage stability index is occurring at bus-10 for all types of load models. It is also observed that bus 10 has the minimum voltage.

Table 3.3 shows critical bus index value and its bus voltage of the 15 -bus test s ystem for di fferent s ubstation vol tage a nd different static loa d mode ls . The system loads are increased from zero to the critical loading point by multiplying each node act ive and reactive pow er b y al oad factor $1 \mathrm{ambda}(\lambda)$ as 0.01 t imes of its previous value in each step for all loads. Note from Table 3.3 that, for all loading conditions, minimum stability index value is observed of the bus 10 .

Table 3.3 Critical bus stability index value for different types of load and substation voltage

| Load model | Substation <br> voltage (pu) | Critical loading condition |  |
| :---: | :---: | :---: | :---: |
|  |  | $\mathrm{VSI}_{\min }=\mathrm{VSI}_{10}$ | $\left\|\mathrm{~V}_{\min }\right\| \mathrm{pu}$ |
| CP | 0.95 | 0.0296 | 0.4152 |
|  | 1.00 | 0.0365 | 0.4374 |
|  | 1.05 | 0.0433 | 0.4566 |
| CI | 0.95 | 0.1151 | 0.5825 |
|  | 1.00 | 0.1183 | 0.5866 |
|  | 1.05 | 0.1730 | 0.6450 |
|  | 0.95 | 0.2104 | 0.6773 |
|  | 1.00 | 0.2582 | 0.7129 |
|  | 1.05 | 0.3139 | 0.7485 |

Figures 3.4 and 3.5 show the variations of the critical bus index value at bus-10 and its bus voltages with the increase of the system loads for different load models, substation voltage 1.0 pu. Points $\mathrm{A}, \mathrm{B}$ and C indicate the critical loading point beyond which a small increment of load causes the voltage collapse.

From Figures 3.4 and 3.5 , it is $s$ een that the critical bus inde x va lue decrease with the increase of the system load, a nd it closes to zero when system's total power closes to the critical loading point. From the each loading conditions, it is observed that the critical bus indices are always at the minimum. Moreover, it is also observed that the different load models cause only different stability index value and bus voltage magnitudes, it does not affect the critical bus number of the test system.


Figure 3.4 Variation of critical bus stability index value with system load for different static load models


Figure 3.5 Variation of critical minimum bus voltage with system load for different static load models

Similarly, Figures 3.6 and 3.7 show the variations of the critical bus index value at bus-10 and its bus voltages with the increase of the system loads for different substation voltage, constant power load model. Points A, B and C indicate the critical loading point beyond which a small increment of load causes the voltage collapse.


Figure 3.6 Variation of critical bus stability index value with system load for different substation voltages


Figure 3.7 Variation of critical minimum bus voltage with system load for different substation voltages

From simulation results, in this case, it can summarize that the stability index a nd c onsequently, the vol tage a re m inimum f or c onstant pow er l oad a nd maximum for constant impedance load and hat for onstant c urrent l oad is in between these two, as seen in Table 3.3.

Finally, if we have a planning to install PV-DG in this system, the most candidate bus is bus-10 based on the voltage stability index.

## CHAPTER IV

## RADIAL DISTRIBUTION SYSTEM POWER FLOW AND HARMONIC CALCULATION

### 4.1 Introduction

In pr actical, configurations of a di stribution system ha ve been high $\mathrm{r} / \mathrm{x}$ ratio (ill-condition) which deteriorates the diagonal dominance of the Jacobian matrix. Therefore, the conventional Newton's power flow method may be divergence in some case. Therefore, this chapter presents a modified Newton method from [78] to solve the pr oblem. Furthermore, ha rmonic $m$ odeling a nd ha rmonic c alculation i na distribution system are mentioned.

A modified Newton method is utilized to solve the power flow for a radial distribution system without reducing the problem size, yet still capable of a chieving robust convergence and high efficiency. This method is derived a Newton formulation where the Jacobian matrix is in $U D U^{T}$ form, where $U$ is a constant upper triangular matrix de pending s olely on s ystem topology and $D$ is a bl ock di agonal m atrix resulting from the radial structure and special properties of the distribution system.

With this formulation, the conventional Newton algorithm of forming the Jacobian matrix, LU factorization and forward back substitution can be replaced by back/forward sweeps on radial feeders with equivalent impedances.

### 4.2 The Modified Newton Method

In conventional N ewton m ethod [79], the e quation to solve pow er flow problem for $\Delta \theta$ and $\Delta V$ is expressed in Equation (4.1).

$$
\left[\begin{array}{cc}
H & N  \tag{4.1}\\
J & L
\end{array}\right]\left[\begin{array}{c}
\Delta \theta \\
\Delta V / V
\end{array}\right]=\left[\begin{array}{c}
\Delta P \\
\Delta Q
\end{array}\right]
$$

where

$$
\begin{align*}
& H_{i j}=-V_{i} V_{j}\left(G_{i j} \sin \theta_{i j}-B_{i j} \cos \theta_{i j}\right) \quad j \neq i  \tag{4.2}\\
& H_{i i}=V_{i} \sum_{j \in i, j \neq i} V_{j}\left(G_{i j} \sin \theta_{i j}-B_{i j} \cos \theta_{i j}\right) \tag{4.3}
\end{align*}
$$

$$
\begin{align*}
& N_{i j}=-V_{i} V_{j}\left(G_{i j} \cos \theta_{i j}+B_{i j} \sin \theta_{i j}\right) \quad j \neq i  \tag{4.4}\\
& N_{i i}=-V_{i} \sum_{j \in, j \neq i} V_{j}\left(G_{i j} \cos \theta_{i j}+B_{i j} \sin \theta_{i j}\right)-2 V_{i}^{2} G_{i i}  \tag{4.5}\\
& J_{i j}=V_{i} V_{j}\left(G_{i j} \cos \theta_{i j}+B_{i j} \sin \theta_{i j}\right) \quad j \neq i  \tag{4.6}\\
& J_{i i}=-V_{i} \sum_{j \in, j \neq i} V_{j}\left(G_{i j} \cos \theta_{i j}+B_{i j} \sin \theta_{i j}\right)  \tag{4.7}\\
& L_{i j}=-V_{i} V_{j}\left(G_{i j} \sin \theta_{i j}-B_{i j} \cos \theta_{i j}\right) \quad j \neq i  \tag{4.8}\\
& L_{i i}=-V_{i} \sum_{j \in, j \neq i} V_{j}\left(G_{i j} \sin \theta_{i j}-B_{i j} \cos \theta_{i j}\right)+2 V_{i}^{2} B_{i i} \tag{4.9}
\end{align*}
$$

Term $G_{i j}+j B_{i j}$ is the entry of nodal admittance matrix. Under assumption the voltage difference between two adjacent nodes is $\operatorname{small}\left(\sin \theta_{i j} \approx 0\right)$ as well as term $G_{i i}+j B_{i i}=-\sum_{j e, j \neq i}\left(G_{i j}+j B_{i j}\right)$. Thus the Jacobian matrix can be approximated as:

$$
\begin{align*}
& H_{i j} \approx V_{i} V_{j} B_{i j} \cos \theta_{i j} \quad j \neq i  \tag{4.10}\\
& H_{i i} \approx-V_{i} \sum_{j \in i, j \neq i} V_{j} B_{i j} \cos \theta_{i j}  \tag{4.11}\\
& N_{i j} \approx-V_{i} V_{j} G_{i j} \cos \theta_{i j} \quad j \neq i  \tag{4.12}\\
& N_{i i} \approx V_{i} \sum_{j \in i, j \neq i} V_{j} G_{i j} \cos \theta_{i j} \vartheta \varepsilon า \text { al } \varepsilon  \tag{4.13}\\
& J_{i j} \approx V_{i} V_{j} G_{i j} \cos \theta_{i j} \quad j \neq i  \tag{4.14}\\
& J_{i i} \approx-V_{i} \sum_{j \in i, j \neq i} V_{j} G_{i j} \cos \theta_{i j}  \tag{4.15}\\
& L_{i j} \approx V_{i} V_{j} B_{i j} \cos \theta_{i j} \quad j \neq i  \tag{4.16}\\
& L_{i i} \approx-V_{i} \sum_{j \in, j \neq i} V_{j} B_{i j} \cos \theta_{i j} \tag{4.17}
\end{align*}
$$

Equations (4.10) to (4.17) show that matrices $H, N, J$ and $L$ all have the same properties (symmetry, sparsity pattern) as the Nodal Admittance Matrix, hence they can be formed as:

$$
\begin{align*}
& H=L=A_{n-1} D_{B} A_{n-1}^{T}  \tag{4.18}\\
& J=-N=A_{n-1} D_{G} A_{n-1}^{T} \tag{4.19}
\end{align*}
$$

where $D_{B}$ and $D_{G}$ are diagonal matrices with diagonal entries to be:

$$
\begin{align*}
& D_{B}=V_{i} V_{j} B_{i j} \cos \theta_{i j}  \tag{4.20}\\
& D_{G}=V_{i} V_{j} G_{i j} \cos \theta_{i j} \tag{4.21}
\end{align*}
$$

and $A_{n-1}$ is node to branch incidence matrix, defined as:

$$
A_{i j}=\left\{\begin{array}{l}
1, \text { if brance } j \text { is directed away from node } i \\
-1, \text { if brance } j \text { is directed towards node } i \\
0, \text { if brance } j \text { is not incident to node } i
\end{array}\right.
$$

For a radial distribution system with n nodes and without shunt branches, the num ber of $b r$ anches is $n-1$. Also by know ing the noda 1 vol tage at one node, assuming it is the first node for convenience. Hence, there are remaining $\mathrm{n}-1$ unknown nodal voltages and we obtain matrix $A_{n-1}$ is a square matrix, which its dimension is $(\mathrm{n}-1) \times(\mathrm{n}-1)$.

Furthermore, if nodes and branches are ordered appropriately, $A_{n-1}$ is an upper triangular matrix with all diagonal entries to be 1 and all non-zero off-diagonal entries to be -1 . One way to achieve such an $A_{n-1}$ is ordering branches by layers away from the r oot node ( source node orr eference node) as s een in Figure 4.1. T he direction of each branch is towards the root node. The node or dering is proceeded simultaneously with the branch or dering. Note from Figure 4.1 that the branch from side node number is the same as the branch number. And the node to branch incident matrix of it is given in Equation (4.22).


Figure 4.1 A simple radial distribution system with 10 -nodes and 9 -branches

From Equations (4.18) and (4.19), thus Equation (4.1) can be rewritten as:

$$
\left[\begin{array}{cc}
A_{n-1} &  \tag{4.23}\\
& A_{n-1}
\end{array}\right]\left[\begin{array}{cc}
D_{B} & -D_{G} \\
D_{G} & D_{B}
\end{array}\right]\left[\begin{array}{ll}
A_{n-1}^{T} & \\
& A_{n-1}^{T}
\end{array}\right]\left[\begin{array}{c}
\Delta \theta \\
\Delta V / V
\end{array}\right]=\left[\begin{array}{c}
\Delta P \\
\Delta Q
\end{array}\right]
$$

$\Delta P$ and $\Delta Q$ are ve ctor of real and reactive node po wer m ismatches respectively, which can be expressed as:

$$
\begin{align*}
\Delta P_{i} & =P_{i(\text { scheduled })}-P_{i(\text { cal })} \quad i \neq \text { reference node }  \tag{4.24}\\
& =\left[P_{i(\text { gen })}-P_{i(\text { load })}\right]-P_{i(\text { cal })} \\
\Delta Q_{i} & =Q_{i(\text { scheduled })}-Q_{i(\text { cal })} \quad i \neq \text { reference node }  \tag{4.25}\\
& =\left[Q_{i(\text { gen })}-Q_{i(\text { load })}\right]-Q_{i(\text { cal })}
\end{align*}
$$

where
$\Delta P_{i}$ and $\Delta Q_{i}$ are vector of real and reactive node power mismatches at node $i$ $P_{i(\text { gen })}$ and $Q_{i(g e n)}$ are real and reactive node power generation at node $i$ $P_{i(\text { load })}$ and $Q_{i(\text { load })}$ are real and reactive node power load at node $i$ $P_{i(\text { cal })}$ and $Q_{i(\text { cal })}$ are net real and reactive node power load at node $i$

The expression for the net real and reactive node power, $P_{i(\text { cal })}$ and $Q_{i(\text { cal })}$ are

$$
\begin{align*}
& P_{i(\text { cal })}=V_{i} \sum_{j=1}^{n} V_{j}\left[G_{i j} \cos \theta_{i j}+B_{i j} \sin \theta_{i j}\right]  \tag{4.26}\\
& Q_{i(\text { cal })}=V_{i} \sum_{j=1}^{n} V_{j}\left[G_{i j} \sin \theta_{i j}-B_{i j} \cos \theta_{i j}\right] \tag{4.27}
\end{align*}
$$

where

$$
\begin{aligned}
& V_{i}, V_{j} \text { are voltage magnitude at node } i \text { and } j \\
& \theta_{i}, \theta_{j} \text { are voltage phase angle at node } i \text { and } j \\
& G_{i j}, B_{i j} \text { are elements of bus admittance matrix }\left[Y_{b u s}\right] \\
& \theta_{i j}=\theta_{i}-\theta_{j} \\
& Y_{i j}=G_{i j}+j B_{i j}
\end{aligned}
$$

It has been shown that the Jacobian matrix can be formed as the product of three square matrices in Equations (4.23). Next will showing the Equation (4.23) can be solved by back/forward sweeps. Let's define:

$$
\begin{align*}
& E=\Delta \theta+j \Delta V / V  \tag{4.28}\\
& S=\Delta P+j \Delta Q  \tag{4.29}\\
& W=D_{B}+j D_{G} \tag{4.30}
\end{align*}
$$

then equation (4.23) can be written as
or

$$
\begin{align*}
& A_{n-1} W A_{n-1}^{T} E=S  \tag{4.31}\\
& A_{n-1} S_{L}=S  \tag{4.32}\\
& W A_{n-1}^{T} E=S_{L} \tag{4.33}
\end{align*}
$$

where Equation (4.32) is the back sweep and Equation (4.33) is the forward sweep.

To solve $E$ in Equation (4.33) in forward sweep ( $A_{n-1}^{T} E=W^{-1} S_{L}$ ), the diagonal matrix $W$ can be inverted for each line. The diagonal in $W^{-1}$ is denoted as the equivalent line impedance:

$$
\begin{equation*}
Z_{e q, i j}=R_{e q, i j}+j X_{e q, i j} \tag{4.34}
\end{equation*}
$$

where

$$
\begin{align*}
& R_{e q, i j}=\frac{X_{i j}}{V_{i} V_{j} \cos \theta_{i j}}  \tag{4.35}\\
& X_{e q, i j}=\frac{R_{i j}}{V_{i} V_{j} \cos \theta_{i j}} \tag{4.36}
\end{align*}
$$

$R_{i j}$ and $X_{i j}$ are resistance and reactance of line $i-j$ respectively. The Diagonal matrix $W^{-1}$ is a square matrix, which its dimension is $(\mathrm{n}-1) \times(\mathrm{n}-1)$.

In order to find the po wer flow s olution, the power flow p rocess h as finished w hen power mismatch of bot hr eal a nd r eactive pow er should be corresponding to:

$$
\begin{equation*}
\max \left|\Delta P^{k}\right| \text { and } \max \left|\Delta Q^{k}\right| \leq \varepsilon \tag{4.37}
\end{equation*}
$$

where
$\max \left|\Delta P^{k}\right|$ is maximum real power mismatch for any iteration $k$ $\max \left|\Delta Q^{k}\right|$ is maximum reactive power mismatch for any iteration $k$
$\varepsilon$ is power mismatch tolerance which set to $10^{-5}$

### 4.2.1 Loss Equations From System Data

Generally, the system real and reactive power loss can be derived into two sets of loss equations i.e., loss equations in terms of $Y_{b u s}$ and $I_{b u s}$, and loss equations in terms of $Z_{\text {bus }}$ and $V_{b u s}$. The following two sets of loss e quations a re de rived in exactly the same manner, which results in the identical forms for partial derivative equations.

In $t$ his di ssertation, 1 oss e quations in term of $Z_{\text {bus }}$ and $V_{b u s}$ is us ed to obtain system real power loss in probabilistic power flow calculation. However, the derivation of two sets of loss equations can be found in [80]. The loss equations in term of $Z_{\text {bus }}$ and $V_{\text {bus }}$ can be expressed by:

$$
\begin{equation*}
P_{L}=\sum_{i=1}^{N_{b}} \sum_{k=1}^{N_{b}}\left[\left(P_{i} P_{k}+Q_{i} Q_{k}\right) \alpha_{i k}+\left(P_{i} Q_{k}-Q_{i} P_{k}\right) \beta_{i k}\right] \tag{4.38}
\end{equation*}
$$

and

$$
\begin{equation*}
Q_{L}=\sum_{i=1}^{N_{b}} \sum_{k=1}^{N_{b}}\left[\left(P_{i} P_{k}+Q_{i} Q_{k}\right) \tau_{i k}+\left(P_{i} Q_{k}-Q_{i} P_{k}\right) \theta_{i k}\right] \tag{4.39}
\end{equation*}
$$

where
$P_{L}, Q_{L}$ are system real and reactive power losses
$P_{i}, Q_{i} \quad$ are real and reactive power load at bus $i$
$R_{i k}, X_{i k}$ are resistance and reactance of branch $i-k$
$V_{i}$ is voltage magnitude at bus $i$
$\delta_{i k}$ is different in voltage phase angle of bus $i, k$ and $\delta_{i k}=\delta_{i}-\delta_{k}$
$N_{b}$ is total number of buses

### 4.2.2 The Modified Newton Method Calculation Steps

The flow c hart of radial di stribution s ystem p ower f low algorithm is shown in Figure 4.2. A nd the calculation step of modified Newton method based on backward and forward sweeps can be summarized as follows:
(1) Read the radial system data and form bus admittance matrix $\left[Y_{\text {bus }}\right]$.
(2) Order branches by layers aw ay from the reference node to construct the node to branch incidence matrix $\left[A_{n-1}\right]$.
(3) Initialize all node voltage and set iteration $k=0$
(4) Calculate net real and reactive nod e pow er load $P_{i(\text { cal })}$ and $Q_{i(\text { cal })}$ from Equations (4.26) and (4.27).
(5) Calculate power mismatch $\Delta P_{i}$ and $\Delta Q_{i}$ from Equations (4.24) and (4.25).
(6) Test for convergence from Equation (4.37). If po wer flow c onverge, the solution is obtained but if not go to step (7).
(7) Calculate $S_{L}$ in backward sweep from Equation (4.32).
(8) Calculate equivalent line impedance $Z_{\text {eq }, i j}$ from Equation (4.34).
(9) Calculate $E$ in forward sweep from Equation (4.33) to find out $\Delta \theta$ and $\Delta V$
(10) Update the adopted node voltage to

$$
\begin{aligned}
& \theta_{i}^{(k+1)}=\theta_{i}^{(k)}+\operatorname{real}\left(E_{i}\right) \\
& V_{i}^{(k+1)}=V_{i}^{(k)}+\left[\operatorname{imag}\left(E_{i}\right) \times V_{i}^{(k)}\right]
\end{aligned}
$$

(11) Set ne w ite ration $k=k+1$ and $r$ epeat to s tep (4) by u sing ne w node voltage.



Figure 4.2 Flow chart of radial distribution system power flow calculation

### 4.3 Test Results of Radial Distribution System Power Flow Calculation

To demonstrate the methodology of the radial distribution system power flow calculation. The 15 -bus radial distribution system from Chapter 3 is used again. Figure 4.3 shows the ordering of nodes and branches of the 15-bus radial distribution system, which node 1 is the reference node.


Figure 4.3 Single-line diagram of the 15 -bus radial distribution system with nodes to branches ordering

From Figure 4.3, the node to branch incident matrix $A_{n-1}$ has a dimension of $(14 \times 14)$ and it is given as:

$$
A_{n-1}=\left[\begin{array}{ccccccccccccccc}
1 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & -1 & 0 \\
& 1 & -1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
& & 1 & -1 & -1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
& & & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
& & & & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
& & & & & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
& & & & & 1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\
& & & & & & 1 & -1 & 0 & 0 & 0 & 0 & 0 \\
& & & & & & & 1 & 0 & 0 & 0 & 0 & 0 \\
& & & & & & & & 1 & -1 & 0 & 0 & 0 \\
& & & & & & & & & 1 & 0 & 0 & 0 \\
& & & & & & & & & & 1 & -1 & -1 \\
& & & & & & & & & & & 1 & 0 \\
& & & & & & & & & & & 1
\end{array}\right]
$$

For t his t est, t he pow er f low r esults a re c ompared with t he s olution obtained b y a c onventional N ewton m ethod a s s hown in T able 4.1. T his t able indicates that the modified Newton method offers the same solution as that obtained by the conventional Newton method, which validates its solution accuracy.

Table 4.1 Power flow solution obtained for the 15-bus radial distribution system

| Node no. | Modified Newton method | Conventional Newton method |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\|\mathrm{V}\|(\mathrm{pu})$ | $\delta(\mathrm{deg})$ | $\|\mathrm{V}\|(\mathrm{pu})$ | $\delta(\mathrm{deg})$ |
| 1 | 1.00000 | 0.00000 | 1.00000 | 0.00000 |
| 2 | 0.97130 | 0.03194 | 0.97129 | 0.03193 |
| 3 | 0.95669 | 0.04929 | 0.95668 | 0.04928 |
| 4 | 0.95093 | 0.05645 | 0.95091 | 0.05644 |
| 5 | 0.94994 | 0.06862 | 0.94993 | 0.06861 |
| 6 | 0.94846 | 0.08685 | 0.94845 | 0.08685 |
| 7 | 0.94863 | 0.08477 | 0.94862 | 0.08477 |
| 8 | 0.94997 | 0.13142 | 0.94996 | 0.13144 |
| 9 | 0.94585 | 0.18229 | 0.94584 | 0.18233 |
| 10 | 0.94454 | 0.19855 | 0.94453 | 0.19859 |
| 11 | 0.96798 | 0.07191 | 0.96797 | 0.07191 |
| 12 | 0.96691 | 0.08492 | 0.96690 | 0.08492 |
| 13 | 0.95825 | 0.18928 | 0.95824 | 0.18931 |
| 14 | 0.95603 | 0.21649 | 0.95601 | 0.21653 |
| 15 | 0.95697 | 0.20491 | 0.95696 | 0.20495 |
| $\boldsymbol{P}_{\text {loss }}, \boldsymbol{Q}_{\text {loss }}$ | $61.74 \mathrm{~kW}, 57.25 \mathrm{kVar}$ |  | $61.78 \mathrm{~kW}, 57.28 \mathrm{kVar}$ |  |

### 4.4 Harmonic Modeling

For harmonic calculation, in this dissertation, the electrical equipments in a di stribution system are modeled based on C IGRE model [81], which is a balance system. Therefore, the impedance va lues of each model arer epresented in all per phase.

### 4.4.1 Harmonic Load Modeling

Generally, a ha rmonic load model is represented as a s imple m odel for harmonic study. This model includes a connection in series or parallel of resistance $(R)$ a nd i nductance ( $L$ ), which s ome ph ysical of 1 oad is ne glected. C onsequence, harmonic voltage and harmonic current calculations may be incorrect.

Therefore, an effective harmonic load model is used in this dissertation. This ha rmonic load model can be di vided into t wo types (CIGRE a nd $\mathrm{R} / / \mathrm{L}$ ) for a different harmonic order consideration, as seen in Figure 4.4.


Figure 4.4 Harmonic load model of CIGRE and R//L

From Figure 4.4, the CIGRE load model is us ed to study for ha rmonic frequency order $5^{\text {th }}$ to $20^{\text {th }}$. This model consists of a s eries reactance ( $X_{s}$ ), a parallel reactance $\left(X_{p}\right)$ and a resistance $(R)$. The other is $\mathrm{R} / / \mathrm{L}$ load model, which consists of a resistance $(R)$ and a reactance $(X)$ in parallel connection. The $\mathrm{R} / / \mathrm{L}$ lode model is used to $s$ tudy for ha rmonic frequency in order $m$ ore $t$ han $20^{\text {th }}$. The parameters in each model can be expressed as follows:

$$
\begin{equation*}
R=\frac{U_{n, \text { net }}^{2}}{P_{1}} \tag{4.44}
\end{equation*}
$$

$$
\begin{equation*}
X_{s}=(0.0073) \times h \times R \tag{4.45}
\end{equation*}
$$

$$
\begin{gather*}
X_{p}=\frac{h \times R}{(6.7) \tan \theta_{1}-0.74}  \tag{4.46}\\
X=h \times \frac{U_{n, \text { net }}^{2}}{Q_{1}} \tag{4.47}
\end{gather*}
$$

where $\quad U_{n, \text { net }}$ is normal system voltage
$P_{1} \quad$ is real power load at fundamental frequency under $U_{n, \text { net }}$
$Q_{1} \quad$ is reactive power load at fundamental frequency under $U_{n, \text { net }}$
$h \quad$ is harmonic order

$$
\tan \theta_{1}=Q_{1} / P_{1}
$$

### 4.4.2 Harmonic Capacitor Modeling

For harmonic calculation, the capacitor modeling c an be represented by capacitance which depends on harmonic frequency as:

$$
\begin{equation*}
X_{c}^{h}=-j \frac{1}{h 2 \pi f_{1} C} \tag{4.48}
\end{equation*}
$$

and

$$
\begin{equation*}
y_{c}^{h}=-\frac{1}{X_{c}^{h}} \tag{4.49}
\end{equation*}
$$

where $\quad X_{c}^{h}$ is capacitive reactance at harmonic frequency order $h$
$y_{c}^{h} \quad$ is capacitive admittance at harmonic frequency order $h$
$C$ is capacitance of capacitor
$f_{1}$ is fundamental frequency

### 4.4.3 Harmonic Feeder Modeling

The equivalent circuit of feeder can be represented by a series connection of feeder resistance and reactance, which depends on harmonic frequency as shown in Figure 4.5. And its expression is given in Equation (4.50).


Figure 4.5 Equivalent circuit of harmonic feeder modeling

$$
\begin{equation*}
y_{\text {line }}^{\mathrm{h}}=\frac{1}{R_{\text {line }}+j h X_{\text {line }}} \tag{4.50}
\end{equation*}
$$

where $\quad R_{\text {line }}$ is line resistance
$X_{\text {line }}$ is line reactance at fundamental frequency
$y_{\text {line }}^{h}$ is line admittance at harmonic frequency order $h$

### 4.4.4 Background Harmonic Modeling

In t his di ssertation, e xisting ba ckground ha rmonic c onditions in a distribution $s$ ystem ar e taken into a ccount $f$ or opt imal PV-DG s izing. Actually, background harmonics may occur from several nonlinear equipments such as 6-pulse
and 12 -pulse rectifier, arc furnaces, adjustable s peed drives, etc. However, 6-pulse converters are the main harmonic sources which ge nerate background harmonics in this study. A nd the ba ckground ha rmonics a re treated as a pe rcentage of nonl inear loads at all load buses except PV-DG buses.

### 4.5 Harmonic Calculation in a Distribution System

This s ection pr esents ha rmonic vol tage a nd c urrent c alculations in a distribution system. Also total ha rmonic di stortion of voltage a nd current a re mentioned.


Figure 4.6 A simplified distribution system for fundamental frequency analysis

Figure 4. 6 shows as implified di stribution s ystem for fundamental frequency a nalysis. In this figure, 6 -pulse con verters are $t$ reated as background harmonic sources of the system and it can be represented by harmonic current source with the typical harmonic current spectra $\left(I_{B H}\right)$ as shown in Table 4.2 [82]. For the PV-DGs are interconnected at an y bus, they are treated as harmonic cur rent sources with the typical harmonic current spectra based on measurements at a PV farm ( $I_{P V}$ ) as $m$ entioned in Chapter 2. The ot her pa rameter in Figure 4.6 can be defined as follows:
$y_{i j}^{1}$ is line admittance at fundamental frequency of branch $i-j$
$y_{c i}^{1}$ is capacitive admittance at fundamental frequency at bus $i$
$P_{l i}$ is real power load at bus $i$
$Q_{1 i}$ is reactive power load at bus $i$

Table 4.2 Characteristic AC line harmonic currents in multi-pulse systems

| Harmonic | Rectifier system pulse number |  |  |  | Harmonic frequency | Harmonic current in percent of fundamental |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 6 | 12 | 18 | 24 |  | Theoretical | Typical |
| 5 | X |  |  |  | 300 | 20.00 | 19.20 |
| 7 | X |  |  |  | 420 | 14.20 | 13.20 |
| 11 | X | X |  |  | 660 | 9.09 | 7.30 |
| 13 | X | X |  |  | 780 | 7.69 | 5.70 |
| 17 | X |  | X |  | 1020 | 5.88 | 3.50 |
| 19 | X |  | X |  | 1140 | 5.26 | 2.70 |
| 23 | X | X |  | X | 1380 | 4.36 | 2.00 |
| 25 | X | X |  | X | - 1500 | 4.00 | 1.60 |
| 29 | X |  |  |  | 1740 | 3.45 | 1.40 |
| 31 | X |  |  |  | 1860 | 3.23 | 1.20 |
| 35 | X |  | X |  | 2100 | 2.86 | 1.10 |
| 37 | X |  | X |  | 2220 | 2.70 | 1.00 |
| NOTE-The theoretical values are given for a 6-pulse converter with ideal characteristics (i.e., square current waves with $120^{\circ}$ conduction). The last column gives typical values based on a commutating impedance of 0.12 pu and a firing angle of $30^{\circ}$ and infinite dc reactor (IEEE Std 519-1992, Table 13.1). These values are on the basis of one 6 -pulse converter or all converters, assuming that the harmonics are additive. Since some harmonics will be canceled, but not entirely, a small percentage value may be assumed, as explained earlier in this subclause. Note that if the dc reactor is not large, some of the harmonics can be greater than typical (or theoretical) and some smaller. |  |  |  |  |  |  |  |

The e quivalent circuit for harmonic frequency analysis corresponding to the simplified system in Figure 4.6 is shown in Figure 4.7. Note from this figure that the 6-pulse converters and the PV-DGs are modeled as harmonic cur rent sources to inject ha rmonic currents into the c onnected bus. The load de mand, s hunt c apacitor and feeder line are modeled as admittance of each components.


Figure 4.7 A simplified distribution system for harmonic frequency analysis
where the parameters in Figure 4.7 can be defined as follows:
$y_{i j}^{h} \quad$ is line admittance at harmonic frequency order $h$ of branch $i-j$
$y_{c i}^{h}$ is capacitive admittance at harmonic frequency order $h$ at bus $i$
$y_{l i}^{h}$ is load admittance at harmonic frequency order $h$ at bus $i$
$y_{s}^{h}$ is source admittance at harmonic frequency order $h$
$V_{i}^{h}$ is voltage at harmonic frequency order $h$ at bus $i$
$I_{i}^{h}$ is current source at harmonic frequency order $h$ at bus $i$

The s ource i mpedance ( $Z_{s}$ ) c an be obt ained from the given s ource da ta such as transformer voltage ratio, R/X ratio and MVA short circuit. The example for source impedance calculation can be expressed by the given source data as:

- Transformer ratio $\left(\mathrm{V}_{\text {high }} / \mathrm{V}_{\text {low }}\right)=22 \mathrm{kV} / 416 \mathrm{~V}$
- $\mathrm{R} / \mathrm{X}$ ratio $=10$
- MVA short circuit = 100

From source data, we can calculate the short circuit current $\left(I_{s c}\right)$ as:

$$
I_{\text {sc }}=\frac{M V A_{s c} \times 10^{6}}{\sqrt{3} \times V_{\text {low }}}=\frac{\left(100 \times 10^{6}\right)}{\sqrt{3} \times 416}=138.79 \mathrm{kA}
$$

And we can calculate the source impedance magnitude $\left(\left|Z_{s}\right|\right)$ as:

$$
\left|Z_{s}\right|=\frac{\left(V_{\text {low }} / \sqrt{3}\right)}{I_{\text {sc }}}=\frac{(416 / \sqrt{3})}{138.79 \mathrm{kA}}=0.00173 \Omega
$$

Thus, we get a source resistance $\left(R_{s}\right)$ and reactance $\left(X_{s}\right)$ as:

$$
\begin{aligned}
& R_{s}=\frac{\left|Z_{s}\right|}{\sqrt{(R / X \text { ratio })^{2}+1}}=\frac{(0.00173)}{\sqrt{10^{2}+1}}=0.000172 \Omega \\
& X_{s}=(R / X \text { ratio }) \times R_{s}=10 \times 0.000172=0.00172 \Omega
\end{aligned}
$$

Therefore, we can find the source impedance and source admittance as:

$$
\begin{aligned}
& Z_{s}=R_{s}+j X_{s}=0.000172+j 0.00172 \Omega \\
& y_{s}=\frac{1}{Z_{s}}=\frac{1}{0.000172+j 0.00172}=57.563-j 575.639 \mathrm{mho}
\end{aligned}
$$

From Figure 4. 7, we can form bus adm ittance matrix at ha rmonic frequency or der $h$ directly from the admittance of each component in a distribution system as mentioned ab ove. The ha rmonic bus admittance matrix $\left[Y_{b u s}^{h}\right]$ of system with $m$ nodes is a square matrix which its dimension is ( $\mathrm{m} \times \mathrm{m}$ ) as given by:

$$
\begin{align*}
& \text { where } \tag{4.52}
\end{align*}
$$

By know ing the ha rmonic c urrent s ource at a ny bus $\left[I_{i}^{h}\right]$ and a lso the harmonic bus admittance $\left[Y_{b u s}^{h}\right]$, we can obtain the harmonic voltage at any bus $\left[V_{i}^{h}\right]$ from Equation (4.53).

$$
\begin{equation*}
\left[I_{i}^{h}\right]=\left[Y_{b u s}^{h}\right]\left[V_{i}^{h}\right] \tag{4.53}
\end{equation*}
$$

and we get

$$
\left[\begin{array}{c}
V_{1}^{h}  \tag{4.54}\\
V_{2}^{h} \\
\cdot \\
\cdot \\
V_{m-1}^{h} \\
V_{m}^{h}
\end{array}\right]=\left[\begin{array}{cccccc}
Y_{11}^{h} & Y_{12}^{h} & 0 & & 0 \\
Y_{21}^{h} & Y_{22}^{h} & 0 & R N & & 0 \\
0 & \cdot & \cdot & & & \\
& & & \cdot & \cdot & 0 \\
& & & \cdot & Y_{m-1, m-1}^{h} & Y_{m-1, m}^{h} \\
0 & & & 0 & Y_{m, m-1}^{h} & Y_{m m}^{h}
\end{array}\right]^{-1}\left[\begin{array}{c}
I_{1}^{h} \\
I_{2}^{h} \\
\cdot \\
\cdot \\
I_{m-1}^{h} \\
I_{m}^{h}
\end{array}\right]
$$

In optimal P V-DGs s izing pr ocess, t he ha rmonic c onstraints i .e., total harmonic voltage distortion (THDv), and total demand distortion (TDD) at a point of common coupling (PCC) are taken into accounted. The THDv and TDD are defined with harmonic frequency from order $2^{\text {nd }}$ to $33^{\text {rd }}$ as given by:

$$
\begin{align*}
& T H D_{v, i}=\frac{\sqrt{\sum_{h=2}^{33}\left|V_{i}^{h}\right|^{2}}}{\left|V_{i}^{1}\right|} \times 100 \%  \tag{4.55}\\
& T D D_{i}=\frac{\sqrt{\sum_{h=2}^{33}\left|I_{i}^{h}\right|^{2}}}{\left|I_{m, i}^{1}\right|} \times 100 \% \tag{4.56}
\end{align*}
$$

where $\quad V_{i}{ }^{1}$ is fundamental voltage at bus $i$
$V_{i}^{h} \quad$ is harmonic voltage order $h$ at bus $i$
$T H D_{V, i}$ is total harmonic distortion voltage at bus $i$
$I_{i}^{1}$ is fundamental current flow through bus $i$
$I_{i}^{h}$ is harmonic current order $h$ flow through bus $i$
$I_{m, i}^{1}$ is fundamental maximum load current flow through bus $i$
$T D D_{i}$ is total demand distortion at bus $i$

From IE C 61727 standard in P hotovoltaic s ystems-Characteristic of the utility interface, low levels of current and voltage harmonics at a connection point of PV-DG are desirable. Acceptable levels of harmonic voltage and current depend upon distribution system characteristic, type of s ervice, connected loads/apparatus and established utility pr actice. The P V-DG out put s hould ha ve 1 ow c urrent di stortion levels to ensure that no adverse effects are caused to other equipment connected to the utility system.

To comply with IEC 61727 standard, the total harmonic current distortion shall be less than $5 \%$ at rated inverter output. Hence, in order to calculate the TDD at the c onnection point of P V-DG, t he m aximum 1 oad c urrent in Equation (4.56) is replaced by rated current of PV inverter. And each individual harmonic current from PV inverter shall be limited to the percentages listed in Table 4.3.

Table 4.3 Current distortion limits in IEC 61727 standard

| Odd harmonics | Distortion limit |
| :---: | :---: |
| $3^{\text {rd }}$ through $9^{\text {th }}$ | $\leq 4.0 \%$ |
| $11^{\text {th }}$ through $15^{\text {th }}$ | $\leq 2.0 \%$ |
| $17^{\text {th }}$ through $21^{\text {st }}$ | $\leq 1.5 \%$ |
| $23^{\text {rd }}$ through $33^{\text {rd }}$ | $\leq 0.6 \%$ |
| Even harmonics $^{2^{\text {nd }} \text { through } 8^{\text {th }}}$ | Distortion limit |
| $10^{\text {th }}$ through $32^{\text {nd }}$ | $\leq 1.0 \%$ |
| Total harmonic current distortion at <br> rated inverter output (TDD) | $\leq 0.5 \%$ |

In $t$ he IEC 61727 s tandard, the T HDv constraint is not m entioned. However, according to the IEEE 519-1992 standard, IEEE Recommended Practices and Requirements for Harmonic Control in Electrical Power Systems, the THDv at a PCC should not exceed 5\%.

## CHAPTER V

## ALGORITHM OF OPTIMAL PV-DG SIZING TECHNIQUE AND NUMERICAL RESULTS

### 5.1 Introduction

This chapter proposes the algorithm of optimal PV-DG sizing technique. Also pr oblem formulation a nd constraints de tail a re $m$ entioned. Furthermore, $t$ he numerical $r$ esults of various study cases are investigated. An actual 51-bus radial distribution system of Provincial Electricity Authority (PEA) of Thailand and a heavy load 33-bus radial distribution system a re selected as test cases. Results from study cases indi cate tha $t$ the opt imal P V-DG s ize s olution may be c hanged de pend on system operating conditions. Furthermore, it demonstrates that PV-DGs may improve voltage r egulation and de crease $/$ osses in di stribution systems, how ever, the THDv may al so increase. Impact of static load models and power factor control on optimal sizing of PV-DG are also addressed. Finally, effects of inverter modeling and existing DGs in a distribution system on optimal PV-DG sizing are presented.

### 5.2 Problem Formulation

The P V-DG installation in a distribution system has several a dvantages (e.g., vol tage improvement, losses reduction, etc.). In the proposed technique, the main objective is to minimize the "average" real power losses of a distribution system by va rying $t$ he s ize of PV-DG ove $r N_{s}$ samples. The pr oblem can be ex pressed mathematically as follows:

$$
\begin{equation*}
\text { Minimize } \quad \frac{1}{N_{s}} \sum_{r=1}^{N_{s}} P_{L, r}\left(P V_{\text {size }}\right) \tag{5.1}
\end{equation*}
$$

subjected to the following constraints:

- $0.95 \mathrm{pu} \leq V_{i} \leq 1.05 \mathrm{pu}$, at PCC
- THDv and TDD $\leq 5 \%$, at PCC
- $\quad I_{h} \leq$ IEC limits, at PCC
where $P_{L, r}\left(P V_{\text {size }}\right)$ is the real power losses of a radial distribution system shown as a function of the size of PV-DG $\left(P V_{\text {size }}\right)$. Note that $P_{L, r}\left(P V_{\text {size }}\right)$ is calculated from the sample $r$ and the real power losses equation can be written as

$$
\begin{equation*}
P_{L, r}\left(P V_{\text {size }}\right)=\sum_{i=1}^{N_{b}} \sum_{j=1}^{N_{b}}\left[\frac{R_{i j} \cos \delta_{i j}}{\left|V_{i}\right|\left|V_{j}\right|}\left(P_{i} P_{j}+Q_{i} Q_{j}\right)+\frac{R_{i j} \sin \delta_{i j}}{\left|V_{i}\right| V_{j} \mid}\left(Q_{i} P_{j}-P_{i} Q_{j}\right)\right] \tag{5.2}
\end{equation*}
$$

where $\quad R_{i j}$ is resistance of branch $i-j$
$\left|V_{i}\right|$ and $\delta_{i}$ are the voltage magnitude and phase angle at bus $i$
$P_{i}$ and $Q_{i}$ are the net real and reactive power at bus $i$
$\delta_{i j}$ is the voltage phase angle difference between buses $i$ and $j$
$N_{b}$ is the total number of buses in a distribution system

### 5.3 The Algorithm of Optimal PV-DG Sizing Technique

The algorithm for determining an optimal PV-DG size can be depicted in Figure 5.1. As mentioned in Chapter 2 on PV modeling section, the $P V_{\text {size }}$ in Figure 5.1 is the rated size of PV-DG which based on a connection group of Sharp 80Wp PV modules. Several random variables are generated with Monte Carlo simulations i.e., solar radiations $\left(G_{a}\right)$, ambient temperatures ( $T_{a}$ ), load de mands ( $L_{d, i}$ ) and substation voltages $\left(V_{S}\right)$. The maximum active power outputs of PV-DGs $\left(P_{m p, i}\right)$ are obtained at each location by PV model and MPPT block.

From $t$ he $r$ eport in [83], it s hows $t$ hat the pow er $f$ actor of $P V$ gridconnected inverter is us ually controlled to be $100 \%$. However, some inverters have the capability to adjust the power factor for two main purposes. One is leading power factor operation to suppress the voltage rise in a distribution system due to the output power from PV-DGs during light-load hours in the daytime. The other is operated at the lagging power factor during heavy load to compensate for the voltage drop of the distribution 1 ines. Therefore, various pow er factor ope rations a nd a lso proper 1 oad models a re important in PV s ystem ins tallation planning. Then, the reactive power output of P V-DGs $\left(Q_{m p, i}\right)$ in P V m odel bl ock can flow in bot h di rections tot he network under lagging or leading power factor operations.

System losses and node voltages are evaluated by the distribution power flow calculation. B ased on the data measured from a PV farm ( 540 units of 11 kW grid-connected i nverters), harmonic di stortions at each bus ar eev aluated by the harmonic flow a nalysis. A s s hown in the flow chart in Figure 5.1, the process is calculated repeatedly from a s pecific range of PV-DG size at each incremental step. The optimal solution of Equation (5.1) is the rated size of PV-DG with minimum the average system loss and under the constraints from 5,000 samples $\left(N_{s}\right)$.


Figure 5.1 Flow chart of the optimal PV-DG sizing technique

### 5.4 Numerical Results and Discussion

For the purposes of this dissertation, there are three scenarios to determine the optimal PV-DGs size in the difference system operating conditions. However, the hourly solar radiation and ambient temperature based on measured from Chiang Mai province as given in Chapter 2 on section 2.2 are used for all scenarios.
5.4.1 Scenario-1: Optimal P V-DG s izing w itha nd w ithout consideration of background harmonic in distribution system

An actual 22 kV radial distribution system in Thailand is employed as a test case in this scenario. All system parameter are given in Appendix C, which can be found in [84]. The test system has 51 buses with a total load of 1.92 MW, 1.06 MVar and 1 unit of 900 kVar capacitor bank at bus-13 as shown in Figure 5.2. The results of base case deterministic load flow are given in Appendix D.

This s cenario s hows t he opt imal P V-DGs s izing w ith a nd w ithout consideration of existing background harmonic conditions in distribution system. The PV-DGs pl acements are obt ained based on the static vol tage stability i ndex (VSI) calculations. The system operating conditions in this scenario are given as:

- Substation voltage and load demand are assumed to be random variables with normal distribution, which standard deviations ( $\sigma$ ) of substation voltage and load models are set to $1.5 \%$ and $10 \%$ respectively.
- Power factors of PV-DGs are assumed to be 1.0 constant.
- Load model is assumed to be constant power load.
- The 6 -pulse conv erters ar e m ain harmonic s ources which generate background harmonics (the typical harmonic current spectra are given in Table 4.2 on Chapter 4).
- Three 1 evels of ba ckground ha rmonics ( $15 \%, 25 \%$ a nd $35 \%$ ) a re considered.
- Other DGs are not considered in this test system.
- In this scenario, all c onstraints ( $V_{i}, I_{h}, T H D v$ and TDD) are cons idered with $95 \%$ confidence interval.
- Range of $P V_{\text {size }}$ on this study is between 0.1 MWp to 2 MWp with a 0.1 MWp increment.


Figure 5.2 Single-line diagram of the 51-bus test system

Firstly, a vol tage stability inde x is c omputed as a ba sis to determine proper locations of P V-DG. Buses with descending mini mum V SI a re s elected as candidate locations to install PV-DG. A constant power load model is also assumed in VSI calculation. Table 5.1 shows three candidate locations (i.e., buses 38, 19 and 37) with various voltage levels of substation in the test system. The results in Table 5.1 also show the minimum voltage related to the critical bus with minimum VSI.

Table 5.1 Critical bus stability index values of the test system

| Substation voltage <br> $(\boldsymbol{p u})$ | Candidate buses with <br> VSI min | VSI min | Voltage min <br> $(\boldsymbol{p u})$ |
| :---: | :---: | :---: | :---: |
| 0.95 | 38 | 0.0387 | 0.4436 |
|  | 19 | 0.0392 | 0.4451 |
|  | 37 | 0.0402 | 0.4478 |
| 1.00 | 38 | 0.0453 | 0.4613 |
|  | 19 | 0.0457 | 0.4623 |
|  | 37 | 0.0459 | 0.4630 |
| 1.05 | 38 | 0.0545 | 0.4831 |
|  | 19 | 0.0554 | 0.4851 |
|  | 37 | 0.0561 | 0.4868 |

After selecting proper locations of PV-DG, the proposed technique is then employed to solve the opt imal P V-DG size. Int his study, e xisting ba ckground harmonic c onditions in test system are a lso t aken i nto a ccount. The b ackground harmonics $(\mathrm{BH})$ are treated as a p ercentage of nonlinear loads at all load bus except PV-DG bus. Three levels of background harmonics (i.e., $15 \%, 25 \%$ and $35 \%$ of load
demands) ar e $t$ ested. Based on $t$ he $r$ esults of the vol tage $s$ tability i ndex of $t$ he candidate buses, three study cases are investigated to determine the optimal size of PV-DG.

## Case-1: Single PV-DG

The PV-DG installation is assumed to be owned by a generation company and located at the bus with minimum VSI (bus-38). This case shows the selection of PV-DG s ize ba sed on $t$ he $t$ echnical constraints $w$ ith a nd $w$ ithout $c$ onsideration of background harmonics.

Figure 5.3 presents the relationship between the average system loss and the average PV-DG active power output. As shown in Figure 5.3, the system losses vary with the size of PV-DG ins talled at bus -38 . The average system loss without installing PV-DG is 30.1 kW . Beside, the system losses decrease when installing PVDG less than 1.7 MWp . The minimum average system loss in this case is 23.3 kW , which is given by installing a PV-DG at 0.8 MWp . Also note that with the variation of solar radiation and operating temperature, from installing 0.8 MWp PV-DG (peak power output), the average active power output is 0.35 MW .


Figure 5.3 Average system losses as a function of average PV-DG power output in Case-1

The c umulative pr obability of vol tage a t bus -38 w ith a nd w ithout installation of 0.8 MWp PV-DG is shown in Figure 5.4. Similarly, an installation of PV-DG mostly improves the voltage regulation at the PCC. Note from the figure, it shows that the vol tage level at bus -38 stays within an acceptable range (i.e., 0.95 to 1.05 pu.) with $95 \%$ confidence interval.


Figure 5.4 Cumulative probability of voltage at PCC with and without PV-DG in Case-1


Figure 5.5 Cumulative probability of THDv at PCC with and without background harmonics in Case-1

Figure 5.5 shows the impact of background harmonics on T HDv at bus38. Results show that THDv values are less than $1 \%$ without considering background harmonics. This indicates that an individual PV-DG produces small voltage distortion waveform. Ont he c ontrary, t he T HDv r ises when t he pe rcentage of background harmonics on $t$ he test system increases. The THDv reaches $3.5 \%$ when the level of background harmonics is $35 \%$. In this case, the background harmonics produce more impact on T HDv at PCC than PV-DG. However, all THDv values do not reach the $5 \%$ limits in Case- 1

Based on SMC-11000TL g rid-connected i nverter, P WM t echnology is employed to control the output waveform. Therefore, the harmonic current ( $I_{h}$ ) from the inverter is less than the limits. The cumulative probability of TDD and harmonic current from inverter simulated at PCC of C ase-1 are shown in Figures 5.6 to 5.11. The results show that all constraints are complied with IEC standard. T herefore, in Case-1, the opt imal P V-DG size at bus -38 is 0.8 M Wp for both with and without consideration of background harmonics.


Figure 5.6 Cumulative probability of TDD at PCC of inverter


Figure 5.7 Cumulative probability of $I_{h}$ (even orders 2 to 8 ) at PCC of inverter


Figure 5.8 Cumulative probability of $I_{h}$ (odd orders 3 to 9 ) at PCC of inverter


Figure 5.9 Cumulative probability of $I_{h}$ (odd orders 11 to 15 ) at PCC of inverter


Figure 5.10 Cumulative probability of $I_{h}$ (odd orders 17 to 21) at PCC of inverter


Figure 5.11 Cumulative probability of $I_{h}$ (odd orders 23 to 33 ) at PCC of inverter

## Case-2A: Multiple PV-DGs without consideration of background harmonics

In this case, by considering the same constraint as in Case-1, two PV-DGs are installed at buses 38 and 19. This case shows that the proposed technique can be applied to determine the optimal size for multiple locations. Note that, the background harmonics are not considered in this case.

The system losses after installing PV-DGs at buses 38 a nd 19 a re shown as $3-\mathrm{D}$ plot in Figure 5.12. Note from the figure that the mini mum a verage system loss occurs when installing a 0.7 MWp PV-DG at bus-38 and a 0.9 MWp at bus-19. With the variation of solar radiation and operating temperature, the total average PVDGs output is around 0.7 MW which results in 16.86 kW of average system loss. The results in Figure 5.12 also show that, with multiple PV-DGs installations, the average system losses of Case-2A are lower than Case-1 $(23.33 \mathrm{~kW})$. Hence, the installations of PV-DGs reduce $56.2 \%$ of system losses comparing the case without PV-DG (30.1 $\mathrm{kW})$.


Figure 5.12 Average system losses as a function of PV-DGs size at buses 38 and 19

From installing a 0.7 M Wp PV-DG at bus- 38 and a 0.9 MWp at bus-19, Figure 5.13 shows the c umulative probability of voltages at buses 38 a nd 19 (both with and without PV-DGs). The results show that voltages at PCC are increased when the P V-DGs a re p resented. H owever, t he vol tages a t bot h 1 ocations stay i n a n acceptable level with $95 \%$ confidence interval.


Figure 5.13 Cumulative probability of voltage at buses 38 and 19 with and without PV-DGs in Case-2A

Figure 5.14 shows the impact of background harmonics on THDv values. Note from the figure that the THDv at PCC increases and may exceed the limits when
higher percentage of background harmonics occurs. The THDv at both locations does not reach the limits for $15 \%$ and $25 \%$ of background harmonics. However, when the level of ba ckground $h$ armonics is $35 \%$, $t$ he p robability at which T HDv at bus -19 violates the constraint (exceeds $5 \%$ ) is 0.1 .


Figure 5.14 Cumulative probability of THDv at PCC with and without background harmonics in Case-2A

Although, the THDv constraint is violated in some levels of background harmonics. Fortunately, the process of optimal PV-DG sizing does not considered the background harmonics in this case.

## Case-2B: Multiple PV-DGs with consideration of background harmonics

When the level of background harmonics is $35 \%$, as the results in Case2 A , t he T HDv a t bus -19 vi olates $t$ he c onstraint $m$ ore $t$ han 0.05 of pr obability of occurrences. Therefore, to comply with harmonic limits, Case-2A is considered again taking into a ccount the background h armonics. By a pplying the s ame algorithm as shown in Figure 5.1, the mini mum a verage $s$ ystem los $s$ in Case-2B oc curs when installing a 0.7 MWp PV-DG at bus-38 and a 0.5 MWp at bus-19 (see Fig.5.12). In this case, the average system loss is 18.39 kW and the total average PV-DGs output is around 0.52 MW .

Figure 5.15 shows the comparison of THDv at buses 38 a nd 19 be tween Cases-2A and 2B (with 35\% of background harmonics). Note that the solution from

Case-2B guarantees the THDv constraint with $95 \%$ confidence interval. T his case shows the effectiveness of the proposed technique when the ba ckground harmonics are presented in an actual distribution system.


Figure 5.15 Comparison of THDv at PCC between Case-2A and Case-2B with $35 \%$ of background harmonics

As the results in Case-2B, the optimal size of PV-DG at bus-19 is reduced to 0.5 M Wp from C ase- $2 \mathrm{~A}(0.9 \mathrm{M} \mathrm{Wp})$. This guarantees t he vol tage c onstraint at buses 38 and 19 with $95 \%$ confidence interval.

Also from Figures 5.6 to 5.11 , the c umulative pr obability of \% TDD and inverter harmonic current from the same inverter in each order at PCC of Cases-2A and 2B are s imilar to Case-1. Therefore, the ha rmonic current co nstraints ar e maintained at acceptable levels in both cases.

Table 5.2 summarizes the PV-DGs installation for all cases. With various background $h$ armonic levels, a verage values of \%THDv at PCC are presented with the c orresponding opt imal s izes of P V-DGs. F or a 1 c c ases w ithout background harmonics, a verage va lues of $\% \mathrm{THDv}$ a re 1 ower t han $1 \%$. On t he c ontrary, t he average va lues of $\%$ THDv va ry de pending ont he ba ckground ha rmonic 1 evels. Furthermore, with higher total installed capacity of PV-DGs, the THDv at PCC may increase. This can be observed from the average of $\% \mathrm{THDv}$ at bus- 38 of all cases.

Table 5.2 Summarize the optimal size of PV-DGs installation

| $\begin{aligned} & \text { Location } \\ & \text { Bus } \end{aligned}$ | Optimal <br> PV-DG <br> size <br> (MWp) | Total PV-DG <br> Capacity <br> (MWp) | Total average PV-DG power output <br> (MW) | Minimum average system losses (kW) | Average of \%THDv at PCC related to optimal PV-DG size with and without background harmonics (BH) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | without BH | 15\% BH | 25\% BH | 35\% BH |
| $\begin{gathered} 38 \\ \text { (Case-1) } \end{gathered}$ | 0.8 | 0.8 | 0.346 | 23.327 | 0.389 | 1.322 | 2.004 | 2.694 |
| $\begin{gathered} 38 \\ 19 \\ \text { (Case-2A) } \end{gathered}$ | $\begin{aligned} & 0.7 \\ & 0.9 \end{aligned}$ | 1.6 | 0.696 | 16.863 | $\begin{aligned} & 0.415 \\ & 0.518 \end{aligned}$ | $\begin{aligned} & 1.383 \\ & 2.203 \end{aligned}$ | $\begin{aligned} & 2.058 \\ & 3.362 \end{aligned}$ | $\begin{aligned} & 2.747 \\ & 4.537 \end{aligned}$ |
| $\begin{gathered} 38 \\ 19 \\ \text { (Case-2B) } \end{gathered}$ | $\begin{aligned} & 0.7 \\ & 0.5 \end{aligned}$ | 1.2 | 0.5 | 8.3 | $\begin{aligned} & 0.392 \\ & 0.344 \end{aligned}$ | $\begin{aligned} & 1.337 \\ & 2.052 \end{aligned}$ | $\begin{aligned} & 2.020 \\ & 3.229 \end{aligned}$ | $\begin{aligned} & 2.710 \\ & 4.414 \end{aligned}$ |

Although, the THDy at bus -19 violates the harmonic constraint in Case2 A with $35 \%$ of background harmonics. While the average of $\% \mathrm{THDv}$ is less than $5 \%$ (4.537\%) as shown by bold number in Table 5.2.

Thus, by using the average of $\% \mathrm{THDv}$ as a criterion, the optimal sizes of PV-DGs s olution in C ase-2A may be a cceptable with considering up to $35 \%$ of background ha rmonic 1 evels. H owever, $t$ he s olution in $C$ ase-2B indi cates tha $t ~ t h e ~$ optimal size of PV-DG at bus- 19 should be reduced to maintain the THDv constraint. This indicates that when the av erage of $\%$ THDv is used as a criterion, the optimal sizes of PV-DGs may be overestimated.

A summary of the total number of PV modules and inverters for optimal sizes of P V-DGs s olution is g iven in T able 5.3. Note that the tot al nu mber of P V modules and inverters are based on a connection group of Sharp 80Wp PV module and SMC 11 kW grid-connected inverter.

Table 5.3 Summarize the total number of PV modules and inverter units for optimal PV-DGs sizes solutions

| Location <br> Bus | Optimal <br> PV-DG size <br> $(M W P)$ | Total number <br> of $\boldsymbol{P V}$ modules <br> (module) | Total number <br> of inverters <br> (unit) |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 38 | 0.8 | 10,000 | 72 |
| (Case-1) |  |  |  |
| 38 | 0.7 | 8,750 | 63 |
| 19 | 0.9 | 11,250 | 81 |
| (Case-2A) |  |  |  |
| 38 | 0.7 | 8,750 | 63 |
| 19 | 0.5 | 6,250 | 45 |
| (Case-2B) |  |  |  |

The results in Scenario-1 show that the proposed technique performs well to obt ain $t$ he opt imal $s$ izes of $P$ V-DGs for $m$ ultiple 1 ocations ba sed on $t$ echnical constraints. In practice, some background harmonic distortion are normally present in the ne twork. B y applying $t$ his $t$ echnique, $t$ he opt imal sizes of P V-DGs can be determined taking into account the background harmonics.

It has been demonstrated that the installation of PV-DGs may affect the power qua lity when $s$ ome ba ckground ha rmonics a re pr esented in a distribution system. With high ba ckground ha rmonics, the THDv a t P CC m ay not $s$ atisfy the standard. As shown in Case-2A, the optimal sizes of PV-DGs are not acceptable with a $35 \%$ of background harmonic level. This is due to THDv constraint violation at bus 19. Therefore, as shown in Case-2B, the optimal sizes of PV-DGs with consideration of background harmonics are required. However, in Case-1, the optimal size of PVDG is successfully obt ained in both w ith a nd w ithout consideration of ba ckground harmonics.

The r esults from s everal cases also indicate that P V-DGs ar e likely to improve the vol tage regulation and de crease system losses in a di stribution system. However, i nstalling with hi gh capacity of P V-DGs m ay i ncrease T HDv at P CC especially when the background harmonics are presented.
5.4.2 Scenario-2: Impact of 1 oad $m$ odel a nd pow er factor $c$ ontrol on optimal PV-DG sizing

The pur pose ofthis scenario is to study an impact on optimal PV-DG sizing in a distribution system using different static load models (i.e., constant power, constant current and constant impedance) and various power factor operations.

The 51-bus radial distribution system in Scenario-1 is employed as a test case again, but the capacitor bank at bus-13 is neglected in this scenario. The system operating conditions in this scenario are given as:

- Substation voltage is set to $1.0 \angle 0^{\circ}$ constant.
- Load demand is assumed to be random variables with normal distribution, which standard deviations $(\sigma)$ is set to $10 \%$.
- Various power factor operations of PV-DGs are considered.
- Three static load models are considered i.e., constant power (CP), constant current $(\mathrm{CI})$ and constant impedance $(\mathrm{CZ})$.
- Background harmonics are not considered in this test system.
- Other DGs are not considered in this test system.
- In this scenario, only voltage and THDv constraints are considered.
- Range of $P V_{\text {size }}$ on this study is between 50 kWp to 2.5 MWp with a 50 kWp increment.

For the purpose of this scenario, it is assumed that the PV-DG installation is located at bus es 10 and 19 . T wo cases are studied for determining the impact of load model and various power factor operations on optimal sizing of PV-DG.

## Case-1: Single PV-DG

In this case, the PV-DG installation is assumed to locate at only bus-19. The i mpact of P V-DG connection on s ystem 1 osses with di fferent 1 oad m odels is presented in Figure 5.16, which power factor (PF) is set to 1.0 constant. It shows that PV-DG nor mally d ecreases s ystem 1 osses, except when its size 1 argely i ncreases. Furthermore, it demonstrates that using different static load models do not impact on optimal PV-DG size, which is 1.1 MWp . Besides, the voltage and THDv constraints are satisfied for P V-DG size with minimum the a verage s ystem los as shown in Figures 5.17 and 5.18, respectively.


Figure 5.16 Average system losses as a function of average PV-DG power output with different load models


Figure 5.17 Cumulative probability of voltage at bus-19 with different load models

$$
(\mathrm{PF}=1.0)
$$



Figure 5.18 Cumulative probability of THDv at bus-19 with different load models

$$
(\mathrm{PF}=1.0)
$$

Figure 5.17 shows that the vol tage values de pend on 1 oad models. T he lowest vol tage i s oc curred w hen us ing the CP m odel. H owever, t he vol tage constraints of all load models are within the limits. Figure 5.18 shows that different load models do not a ffect the THDv. In reality, the THDv strongly depends on P VDG size as shown in Figure 5.22. Further, it can be observed from Figure 5.18 that THDv is s mall a nd less than $1.25 \%$. This shows that the low ha rmonic di stortion power can be generated based on SMC-11000TL inverter.

The impact of leading operation on system losses in Case-1 with CP load model is presented in Figure 5.19. It shows that the solution of optimal PV-DG size may be changed for $w$ ide leading pow er factor $r$ ange. Unlike the lagging ope ration which has a few impact on optimal size of PV-DG as shown in Figure 5.20. Further, Figure 5.19 indicates that the system losses are rapidly increasing when PV-DG size is larger. This can be seen by com paring the curve for a given PF values w ith the curve obt ained for lagging ope ration. This is due to the fact of P V-DG consumes reactive po wer at 1 eading ope ration. Therefore, 1 ow 1 eading PF c auses vol tage to reduce. As a result, the system losses are nonlinearly increasing.


Figure 5.19 Average system losses as a function of average PV-DG power output with different leading power factor (CP-model)


Figure 5.20 Average system losses as a function of average PV-DG power output with different lagging power factor (CP-model)

Figures 5.21 and 5.22 show cumulative probability of voltage and THDv at bus-19 corresponding to the results in Figure 5.19, with different optimal PV-DG sizes at each power factor. Figure 5.21 indicates that voltage is increasing when the size of PV-DG is larger, similar with THDv values as shown in Figure 5.22.


Figure 5.21 Cumulative probability of voltage at bus-19 with different PV-DG sizes corresponding to Figure 5.19


Figure 5.22 Cumulative probability of THDv at bus-19 with different PV-DG sizes corresponding to Figure 5.19

## Case-2: Multiple PV-DG

In this case, two PV-DGs are installed at buses 10 and 19. The impact of PV-DGs c onnection on s ystem losses with different load models are shown as 3-D plot in Figures 5.23 to 5.25 , which PF is set to 1.0 constant. It shows that the average system losses decrease more than Case-1 with multiple PV-DGs. It demonstrates that using different static load models do not impact on optimal PV-DGs sizes, which is
1.5 MWp at bus 10 a nd 0.7 M Wp at bus-19. The vol tage and THDv constraints at each bus related to PV-DGs sizes of constant power load model are shown in Figures 5.26 and 5.27 , respectively. The results indicate that all constraints are kept within the limits.


Figure 5.23 Average system losses as a function of PV-DGs capacity at buses 10 and 19 with constant power load model $(\mathrm{PF}=1.0)$


Figure 5.24 Average system losses as a function of PV-DGs capacity at buses 10 and 19 with constant current load model $(\mathrm{PF}=1.0)$


Figure 5.25 Average system losses as a function of PV-DGs capacity at buses 10 and 19 with constant impedance load model $(\mathrm{PF}=1.0)$


Figure 5.26 Cumulative probability of voltage at buses 10 and 19 corresponding to the result in Figure 5.23


Figure 5.27 Cumulative probability of THDv at buses 10 and 19 corresponding to the result in Figure 5.23

From Figure 5.27, the THDv at bus-19 is higher than the THDv at bus-10 although the PV-DG size at bus-19 ( 0.7 MWp ) is about $50 \%$ less compared with bus$10(1.5 \mathrm{MWp})$. This is due to the increasing system impedance (longer distance from the substation) and a so the influence from 1 arge P V-DG size at bus -10 . Therefore, higher THDv can be observed at the end of the feeder. This finding is critical for PVDG ins tallation considering in rural a reas where di stribution systems are w idely spread over large distances.

The impact of various power factor operations with constant power load model on multiple optimal PV-DGs sizes is presented in Table 5.4. Similarly in Case1, the optimal sizes solution may be changed for wide leading power factor range and it has a few impact on optimal sizes in lagging power factor operation.

Table 5.4 Multiple optimal PV-DGs sizes for various PF operations with CP-model

|  | Lagging type |  | System losses | Leading type |  | System losses |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P.F. | Bus-10 <br> (MWp) | Bus-19 <br> $(\mathrm{MWp})$ |  | Bus-10 <br> $(\mathrm{MWp})$ | Bus-19 <br> $(\mathrm{MWp})$ |  |
| $\mathbf{0 . 9}$ | 1.7 | 0.8 | 18.56 | 0.95 | 0.4 | 29.33 |
| $\mathbf{0 . 9 2 5}$ | 1.7 | 0.65 | 18.57 | 0.95 | 0.45 | 28.35 |
| $\mathbf{0 . 9 5}$ | 1.7 | 0.65 | 19.21 | 1.0 | 0.6 | 27.29 |
| $\mathbf{0 . 9 7 5}$ | 1.7 | 0.8 | 19.71 | 1.3 | 0.65 | 25.69 |
| $\mathbf{1 . 0}$ | 1.5 | 0.7 | 22.53 | 1.5 | 0.7 | 22.53 |

From the results in Scenario-2, it can be summarized that different static load m odels do not i mpact on opt imal sizes of P V-DGs. It d emonstrates that the voltage has a significant change with both 1 oad $m$ odels a nd P V-DG size ( see Figs. 5.17 and 5.21). W hile $t$ he T HDv va lues de pend on P V-DG s izes m ore t han 1 oad models (see Figs. 5.18 and 5.22). Furthermore, an impact of power factor control on optimal sizes of PV-DGs indicates that leading operation changes the optimal size of PV-DG at each power factor operation. This differs from lagging operation which has low impact on optimal PV-DG size.

In addition, fast growing technologies like PV-DGs is emerging as part of a di stribution system. Therefore, it is ne cessary to evaluate and analyze the pow er quality issue due to various non-linear current. In practice, utilities cannot assign the PV-DGs installation location to be connected to the feeder because it mainly depends on customers who own the P Y systems. Thus, for planning a spect, the proper load models and operating mode of inverter are required to accurately find the PV-DG size solution. H owever, $t$ he s imulation $r$ esult $f$ rom $C$ ase- $2 s$ hows $t$ hat $t$ he ha rmonic distortion voltage can be high depending on the distance away from a substation (see Fig. 5.27). Therefore, it may require the harmonic filter if the PV-DGs are located at the end of feeder, especially the large size of PV-DG.
5.4.3 Scenario-3: Effect of inverter m odeling and e xisting D Gs in a distribution system on optimal PV-DG sizing

The pur pose of $t$ his scenario is $t o s$ tudy a $n$ effect on optimal PV-DG sizing in a distribution system using different PV inverter models (i.e., 6-pulse, 12pulse and PWM) and existing DGs with various operating conditions.

A heavy load 23 kV radial distribution system is employed as a test case in this scenario. All system parameter are given in Appendix C, which can be found in [85]. The test system has 33 buses with a total load of $9.29 \mathrm{MW}, 5.75 \mathrm{MVar}$ as shown in Figure 5.28. The results of base case deterministic load flow are given in Appendix D. And the system operating conditions in this scenario are given as:

- Substation voltage is set to $1.0 \angle 0^{\circ}$ constant.
- Load demand is assumed to be random variables with normal distribution, which standard deviations $(\sigma)$ is set to $10 \%$.
- Power factor of PV-DG is assumed to be 1.0 constant.
- Load model is assumed to be constant power load.
- Background harmonics are not considered in this test system.
- Various ope rating c onditions of e xisting DGs in test s ystem are considered.
- Only voltage and THDv constraints are considered in this scenario.
- Range of $P V_{\text {size }}$ on this study is between 0.2 MWp to 13 MWp with a 0.2 MWp increment.


Figure 5.28 Single-line diagram of the 33 -bus test system

For t he pur pose o ft his s tudy, it is a ssumed that the single PV-DG installation is located at bus-10. Two cases are studied for investigating the effect of inverter models and existing DGs on optimal PV-DG sizing.

## Case-1: Optimal PV-DG sizing without consideration of existing DGs

This cas e s hows $t$ he s election of optimal PV-DG s ize ba sed on $t$ he technical cons traints without consideration of e xisting DGs us ing di fferent inverter models, which the typical harmonic current spectra are given by:

- Using data in Table 4.2 from chapter 4 for 6-pulse and 12 pul se inverter models.
- Using d ata b ased on m easurements of grid-connected inverter (SMC11000TL) from a PV farm for PWM inverter model.


Figure 5.29 Average system losses as a function of average PV-DG power output without consideration of existing DGs

Figure 5.29 presents the relationship between the average system loss and the a verage P V-DG active pow er out put. From this figure, the s ystem losses vary with the size of PV-DG installed at bus-10. The average system loss without installing PV-DG is 375.1 kW . Besides, the system losses decrease when installing PV-DG less than 12.2 MWp. The minimum average system loss in this case is 271.3 kW , which is given by installing a PV-DG at 5.8 MWp . While the a verage active power output of PV-DG is around 2.5 MW.

The c umulative pr obability of vol tage a t bus -10 with a nd $w$ ithout installation of 5.8 MWp PV-DG is shown in Figure 5.30. Similarly to scenarios 1 and 2, an installation of PV-DG mostly improves the voltage regulation at the PCC. Note from the figure, it s hows that the hi ghest vol tage level at bus -10 stays $w$ ithin an acceptable limits (i.e., 1.05 pu ). Since, however, the test system in this case has heavy load and there is no any compensator elements to regulate the voltage rise up. Hence, voltage at some node before installing PV-DG is lower the limits (i.e., 0.95 pu ), this can be found in base case deterministic load flow solution as given in Appendix D. By
this reason, the minimum voltage at bus-10 may lower than the limits after installing PV-DG. However, the probability at which voltage at bus -10 lower than 0.95 pu is 0.1 , and it can be acceptable for this system.


Figure 5.30 Cumulative probability of voltage at bus-10 without consideration of existing DGs

Figure 5.31 shows t he c omparison of T HDv va lues a t bus -10 us ing different PV inverter models. Since, it need to be installed high c apacity of PV-DG $(5.8 \mathrm{MWp})$ to minimize $s$ ystem loss in this case. Therefore, t he THDv va lues can exceed the limits for 6 -pulse a nd 12 -pulse inverter m odels, especially the 6 -pulse inverter. This differs from PWM inverter that the THDv value is less than $2 \%$. This indicates that a PWM technology can produce small voltage distortion waveform. In present, m ostly P V i nverter t echnologies a re b ased on P WM [83]. H owever, t he purpose of $t$ his c ase n eeds t o s how t he distinction of $\mathrm{T} H D v$ va lues f rom us ing different PV inverter models in our study.

Furthermore, t o c omply w ith IEEE s tandard, PV-DG s ize s hould be reduced to 3.0 MWp for 6 -pulse inverter. The average system loss is around 295 kW for this installation size, see Figure 5.29.


Figure 5.31 Cumulative probability of THDv at bus-10 using different inverter models without consideration of existing DGs

## Case-2: Optimal PV-DG sizing with consideration of existing DGs

This case shows the effect of optimal PV-DG sizing with consideration of existing D Gs in distribution system. Using different inve rter models a re also presented to compare THDv values with Case-1. For the purpose of study case, the locations of existing DGs as well as its operating conditions and capacity are given in Table 5.5.

Table 5.5 Existing DGs locations, capacity and its operating conditions

| Location Bus | DGs capacity (MW) | DG type | Operating mode |
| :---: | :---: | :---: | :---: |
| 13 | 1.5 | Synchronous | PF. 1.0 |
| 25 | 1.0 | Induction | PF. 0.85 leading |
| 33 | 1.0 | Synchronous | PF. 0.95 lagging |

As shown in Figure 5.32, it needs to install 2.6 MWp PV-DG to minimize average system loss, which approximately reduced $50 \%$ compared with Case-1 (5.8 MWp). This is due to highly generation power of the existing DGs (3.5 MW). So, the average s ystem 1 oss be fore ins talling P V-DG is m ore de creased than Case-1 ( 178 $\mathrm{kW})$. From the figure, the mini mum a verage system loss is 163.6 kW in this case, while the average active power output of PV-DG is around 1.12 MW.


Figure 5.32 Average system losses as a function of average PV-DG power output with consideration of existing DGs

Figure 5.33 s hows c omparison of the voltage c umulative probability at bus-10 before and after installation of 2.6 MWp PV-DG. The voltage level at bus-10 stays within an acceptable range in this case. Note from the figure, it shows that the minimum voltage at bus- 10 is higher than Case- 1 and kept within the limits, when the existing DGs are presented.


Figure 5.33 Cumulative probability of voltage at bus-10 with consideration of existing DGs

Since the reducing more of PV-DG capacity in Case-2, consequence the THDv values are within the limits for all PV inverter model as shown in Figure 5.34. Similarly to Case-1, however, it indicates that the PWM technology can produce very small voltage distortion waveform, which less than $1 \%$ in this case.


Figure 5.34 Cumulative probability of THDv at bus-10 using different inverter models with consideration of existing DGs

From the results in Scenario-3, it c an be summarized that different PV inverter models have effect to optimal size of PV-DG. It demonstrates that the 6-pulse inverter modeling may produce high THDv values at PCC, while the PWM inverter modeling can produce very small THDv values. The THDv values produced from the 12-pulse inverter are in between these two, as seen in Figures 5.31 and 5.34. From these f igures, it indi cates tha t int erconnection of s mall P V-DG ma y notr esult in violation of the power quality standard. However, the THDv values are comply with standard for P WM inverter in all case. While PV-DG size may reduced for 6-pulse and 12 -pulse i nverters, as s hown in C ase-1. Furthermore, a ddition ot her D Gs in distribution system can effect is to decrease PV-DG size to minimize system losses.

## CHAPTER VI

## CONCLUSIONS AND FUTURE WORKS

### 6.1 Conclusions

This dissertation presents a probabilistic approach to calculate an optimal size of PV-DG in a distribution system. The stochastic variables of both ge neration and $l$ oad ha ve been considered. The p roposed technique is ba sed on actual hour ly solar radiation, ambient temperature and typical harmonic currents of grid-connected inverter in Thailand. The results from all scenarios show that the proposed technique is effectively to obtain optimal sizes of PV-DGs for both single and multiple locations based on technical constraints.

From s everal s ystem o perating c onditions, it can be s ummarized the optimal PV-DGs sizing based on this approach as follows:

- It need to be collected the data of hourly variations of solar radiation and ambient temperature for a site of interest.
- In practical, a validation of PV model is necessary to accurate the power output of PV-DG corresponding to solar radiation and temperature.
- In pl anning as pect, a m easurement of $h$ armonic cur rent s pectra of $\mathrm{P} V$ inverter is necessary to assess the power quality.
- By applying this technique, optimal sizes of PV-DGs can be determined taking into account background harmonics. A nd W ith high background harmonics or $w$ ith hi gh c apacity of P V-DGs, \%THDv at P CC m ay increase and not satisfy the standard.
- Different static load models do not impact on optimal PV-DGs sizes. And THDv values depend on PV-DG sizes more than load models.
- Leading power factor operation changes optimal PV-DG size but lagging operation has low impact on optimal PV-DG size.
- High distortion voltage waveform may be produced by 6-pulse and 12 pulse inverter modeling causes THDv values exceed the limits. While the PWM i nverter modeling c an pr oduce ve ry s mall di stortion ha rmonic voltage and satisfied the standard.
- Additional DGs in a distribution system may lead to decrease optimal PVDG size to minimize system losses.
- The PV-DGs are likely to improve voltage regulation and decrease system losses in a distribution system, but increase THDv values at PCC.


### 6.2 Future Works

In order to determine the optimal PV-DGs sizes in a distribution system for future studies. Some further issue described below may be of interest.

- It is possible for applying the proposed method to determine optimal size and location of PV-DG at the same time while satisfying the number of constraints described in this works. The Genetic Algorithm (GA) may be used for this issue.
- Other technical constraints such as distribution line current limits can also be added into the proposed algorithm.
- The impact of PV-DG on protection coordination should be studied.
- The coordination of voltage regulation equipments in distribution system may be incorporate with optimal PV-DGs sizing.



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## Appendix A

Hourly Variations of Solar Radiation and Ambient Temperature of

## Chiang Mai Province

(During 6.00 to 18.00 on Jan-Dec 2007)

## A1. Hourly and daily solar radiation ( $\mathrm{MJ} / \mathrm{m}^{2}$ ) [86]

## January

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  | - |  | ? |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  | \% |  |  |  |  |
| 3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | $\bigcirc 0.000$ | 0.000 | 0.842 | 0.265 | 1.108 |
| 4 | 0.000 | 0.090 | 0.540 | 1.482 | 2,168 | 2.561 | 2.735 | 2.673 | 2.265 | 1.658 | 0.966 | 0.251 | 17.388 |
| 5 | 0.000 | 0.086 | 0.527 | 1.445 | 2.076 | 2.475 | 2.679 | 2.622 | 2.232 | 1.661 | 0.960 | 0.231 | 16.995 |
| 6 | 0.000 | 0.142 | 0.632 | 1.030 | 2.023 | 2.389 | 2.500 | 2.581 | 2.203 | 1.689 | 1.002 | 0.264 | 16.454 |
| 7 | 0.000 | 0.100 | 0.527 | 0.938 | 2.059 | 2.602 | 2.781 | 2.733 | 2.153 | 1.561 | 0.428 | 0.155 | 16.038 |
| 8 | 0.000 | 0.080 | 0.551 | 0.755 | 1.428 | 2.390 | 2.792 | 2.671 | 2.394 | 1.788 | 1.056 | 0.326 | 16.232 |
| 9 | 0.000 | 0.088 | 0.584 | 1.529 | 2.160 | 2.586 | 2.759 | 2.679 | 2.317 | 1.773 | 1.093 | 0.315 | 17.883 |
| 10 | 0.000 | 0.092 | 0.573 | 1.436 | 1.994 | 2.502 | 2.669 | 2.591 | 2.265 | 1.681 | 0.969 | 0.264 | 17.036 |
| 11 | 0.000 | 0.088 | 0.573 | 1.459 | 2.070 | 2.479 | 2.685 | 2.576 | 2.181 | 1.655 | 0.957 | 0.242 | 16.966 |
| 12 | 0.000 | 0.096 | 0.532 | 1.368 | 1.978 | 2.391 | 2.679 | 2.555 | 2.198 | 1.798 | 1.028 | 0.256 | 16.879 |
| 13 | 0.000 | 0.088 | 0.528 | 1.402 | 2.007 | 2.443 | 2.674 | 2.474 | 2.171 | 1.552 | 0.953 | 0.277 | 16.571 |
| 14 | 0.000 | 0.110 | 0.517 | 1.384 | 1.928 | 2.437 | 2.594 | 2.583 | 2.211 | 1.682 | 1.053 | 0.335 | 16.832 |
| 15 | 0.000 | 0.091 | 0.533 | 1.526 | 2.147 | 2.581 | 2.796 | 2.714 | 2.343 | 1.789 | 1.082 | 0.366 | 17.968 |
| 16 | 0.000 | 0.076 | 0.526 | 1.570 | 2.189 | 2.587 | 2.810 | 2.732 | 2.391 | 1.883 | 1.155 | 0.374 | 18.294 |
| 17 | 0.000 | 0.089 | 0.497 | 1.464 | 2.056 | 2.469 | 2.692 | 2.611 | 2.297 | 1.751 | 1.065 | 0.331 | 17.322 |
| 18 | 0.000 | 0.082 | 0.476 | 1.515 | 2.185 | 2.639 | 2.853 | 2.796 | 2.449 | 1.858 | 1.184 | 0.398 | 18.434 |
| 19 | 0.000 | 0.085 | 0.482 | 1.458 | 2.088 | 2.529 | 2.740 | 2.679 | 2.348 | 1.784 | 1.116 | 0.387 | 17.698 |
| 20 | 0.000 | 0.080 | 0.506 | 1.631 | 2.232 | 2.685 | 2.878 | 2.817 | 2.465 | 1.889 | 1.165 | 0.385 | 18.735 |
| 21 | 0.000 | 0.083 | 0.511 | 1.588 | 2.216 | 2.656 | 2.864 | 2.803 | 2.528 | 1.936 | 1.205 | 0.411 | 18.803 |
| 22 | 0.000 | 0.089 | 0.510 | 1.535 | 2.160 | 2.595 | 2.844 | 2.819 | 2.480 | 1.942 | 1.218 | 0.432 | 18.631 |
| 23 | 0.000 | 0.082 | 0.486 | 1.470 | 2.057 | 2.458 | 2.653 | 2.545 | 2.244 | 1.720 | 1.081 | 0.346 | 17.145 |
| 24 | 0.000 | 0.110 | 0.430 | 0.863 | 1.024 | 1.784 | 2.315 | 2.439 | 2.090 | 1.538 | 0.986 | 0.303 | 13.886 |
| 25 | 0.000 | 0.111 | 0.498 | 1.105 | 1.016 | 2.183 | 2.354 | 2.396 | 2.191 | 1.704 | 0.997 | 0.315 | 14.876 |
| 26 | 0.000 | 0.101 | 0.482 | 1.364 | 2.015 | 2.460 | 2.637 | 2.567 | 2.275 | 1.703 | 1.053 | 0.380 | 17.042 |
| 27 | 0.000 | 0.086 | 0.473 | 1.286 | 1.911 | 2.306 | 2.556 | 2.421 | 2.247 | 1.530 | 0.683 | 0.299 | 15.804 |
| 28 | 0.000 | 0.045 | 0.346 | 0.717 | 1.104 | 1.224 | 1.194 | 1.069 | 0.414 | 0.284 | 0.364 | 0.080 | 6.841 |
| 29 | 0.000 | 0.115 | 0.529 | 1.364 | 2.020 | 2.486 | 2.662 | 2.671 | 2.349 | 1.795 | 1.067 | 0.344 | 17.414 |
| 30 | 0.000 | 0.086 | 0.472 | 1.165 | 1.645 | 2.140 | 2.491 | 2.444 | 2.045 | 1.665 | 0.988 | 0.342 | 15.493 |
| 31 | 0.000 | 0.094 | 0.461 | 0.843 | 1.687 | 1.984 | 1.905 | 1.880 | 1.317 | 1.206 | 0.845 | 0.375 | 12.612 |
| Average | 0.000 | 0.088 | 0.493 | 1.265 | 1.850 | 2.311 | 2.510 | 2.453 | 2.106 | 1.603 | 0.985 | 0.312 | 15.979 |

February

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.090 | 0.489 | 1.229 | 1.863 | 2.329 | 2.561 | 2.475 | 2.189 | 1.660 | 0.958 | 0.295 | 16.156 |
| 2 | 0.000 | 0.108 | 0.604 | 0.989 | 1.697 | 1.969 | 2.006 | 2.143 | 1.826 | 1.440 | 0.826 | 0.340 | 13.964 |
| 3 | 0.000 | 0.120 | 0.408 | 1.097 | 1.650 | 2.124 | 2.306 | 2.141 | 2.017 | 1.593 | 0.944 | 0.299 | 14.710 |
| 4 | 0.000 | 0.105 | 0.450 | 1.003 | 1.540 | 1.968 | 2.178 | 2.136 | 1.938 | 1.424 | 0.796 | 0.265 | 13.810 |
| 5 | 0.000 | 0.085 | 0.453 | 1.017 | 1.627 | 2.115 | 2.394 | 2.443 | 2.109 | 1.581 | 0.918 | 0.314 | 15.063 |
| 6 | 0.000 | 0.092 | 0.514 | 1.137 | 1.709 | 2.132 | 2.389 | 2.396 | 2.097 | 1.533 | 0.919 | 0.313 | 15.243 |
| 7 | 0.000 | 0.095 | 0.488 | 1.048 | 1.606 | 2.003 | 2.211 | 1.789 | 1.806 | 1.544 | 0.846 | 0.291 | 13.738 |
| 8 | 0.000 | 0.091 | 0.439 | 0.910 | 1.296 | 1.726 | 1.888 | 2.326 | 2.000 | 1.542 | 0.935 | 0.318 | 13.480 |
| 9 | 0.000 | 0.088 | 0.559 | 1.224 | 1.858 | 2.304 | 2.559 | 2.495 | 2.192 | 1.745 | 1.083 | 0.369 | 16.487 |
| 10 | 0.000 | 0.092 | 0.646 | 1.387 | 2.037 | 2.488 | 2.725 | 2.669 | 2.344 | 1.767 | 1.083 | 0.404 | 17.662 |
| 11 | 0.000 | 0.140 | 0.562 | 1.143 | 1.787 | 2.245 | 2.478 | 2.530 | 2.244 | 1.704 | 1.021 | 0.355 | 16.227 |
| 12 | 0.000 | 0.097 | 0.600 | 1.325 | 1.979 | 2.430 | 2.658 | 2.612 | 2.293 | 1.738 | 0.825 | 0.368 | 16.944 |
| 13 | 0.000 | 0.100 | 0.663 | 1.468 | 2.136 | 2.567 | 2.754 | 2.704 | 2.382 | 1.739 | 1.065 | 0.494 | 18.100 |
| 14 | 0.000 | 0.088 | 0.634 | 1.488 | 2,163 | 2.629 | 2.889 | 2.848 | 2.494 | 1.772 | 1.219 | 0.443 | 18.685 |
| 15 | 0.000 | 0.124 | 0.506 | 1.617 | 1.787 | 2.825 | 1.563 | 1.826 | 1.390 | 0.818 | 0.565 | 0.679 | 13.745 |
| 16 | 0.000 | 0.091 | 0.694 | 1.620 | 2.266 | 2.744 | 2.915 | 2.713 | 2.389 | 1.555 | 0.874 | 0.258 | 18.152 |
| 17 | 0.000 | 0.099 | 0.692 | 1.555 | 2.205 | 2.680 | 2.917 | 2.861 | 2.570 | 2.017 | 1.261 | 0.517 | 19.408 |
| 18 | 0.000 | 0.096 | 0.643 | 1.537 | 2.232 | 2.695 | 2.884 | 2.847 | 2.592 | 1.992 | 1.290 | 0.493 | 19.339 |
| 19 | 0.000 | 0.099 | 0.598 | 1.401 | 2.028 | 2.473 | 2.858 | 2.732 | 2.460 | 1.917 | 1.235 | 0.526 | 18.357 |
| 20 | 0.000 | 0.090 | 0.585 | 1.408 | 2.069 | 2.547 | 2.720 | 2.686 | 2.410 | 1.866 | 1.170 | 0.501 | 18.082 |
| 21 | 0.000 | 0.095 | 0.615 | 1.490 | 2.159 | 2.601 | 2.748 | 2.710 | 2.514 | 1.891 | 1.218 | 0.506 | 18.591 |
| 22 | 0.000 | 0.097 | 0.652 | 1.516 | 2.199 | 2.792 | 3.028 | 2.853 | 2.383 | 1.852 | 1.157 | 0.473 | 19.034 |
| 23 | 0.000 | 0.110 | 0.584 | 1.414 | 2.051 | 2.570 | 2.742 | 2.596 | 2.236 | 1.740 | 1.110 | 0.437 | 17.624 |
| 24 | 0.000 | 0.106 | 0.555 | 1.313 | 1.942 | 2.391 | 2.596 | 2.501 | 2.175 | 1.599 | 0.983 | 0.380 | 16.582 |
| 25 | 0.000 | 0.107 | 0.635 | 1.493 | 2.165 | 2.597 | 2.848 | 2.684 | 2.311 | 1.655 | 1.055 | 0.532 | 18.133 |
| 26 | 0.001 | 0.108 | 0.654 | 1.625 | 2.213 | 2.697 | 2.898 | 2.765 | 1.762 | 1.867 | 1.296 | 0.650 | 18.606 |
| 27 | 0.001 | 0.151 | 0.672 | 1.613 | 2.210 | 2.708 | 2.867 | 2.819 | 2.217 | 1.244 | 1.072 | 0.421 | 18.040 |
| 28 | 0.000 | 0.112 | 0.610 | 1.476 | 2.082 | 2.631 | 2.793 | 2.656 | 2.305 | 1.759 | 1.058 | 0.414 | 17.927 |
| Average | 0.000 | 0.103 | 0.579 | 1.341 | 1.948 | 2.428 | 2.585 | 2.534 | 2.202 | 1.663 | 1.028 | 0.416 | 16.853 |

March

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.103 | 0.551 | 1.338 | 1.947 | 2.385 | 2.531 | 2.479 | 2.219 | 1.614 | 0.968 | 0.358 | 16.519 |
| 2 | 0.000 | 0.108 | 0.514 | 1.261 | 1.884 | 2.518 | 2.670 | 2.780 | 2.312 | 1.676 | 1.081 | 0.469 | 17.314 |
| 3 | 0.001 | 0.124 | 0.605 | 1.480 | 2.075 | 2.499 | 2.677 | 2.402 | 2.114 | 1.544 | 0.963 | 0.375 | 16.890 |
| 4 | 0.001 | 0.111 | 0.529 | 1.216 | 1.791 | 2.266 | 2.202 | 2.197 | 1.958 | 1.533 | 0.910 | 0.277 | 15.013 |
| 5 | 0.000 | 0.094 | 0.501 | 1.170 | 1.669 | 2.054 | 1.767 | 1.636 | 1.154 | 1.404 | 0.711 | 0.191 | 12.386 |
| 6 | 0.000 | 0.073 | 0.599 | 1.174 | 1.530 | 1.846 | 2.216 | 2.283 | 2.298 | 1.671 | 1.017 | 0.409 | 15.155 |
| 7 | 0.001 | 0.146 | 0.988 | 1.755 | 2.199 | 2.695 | 3.044 | 2.995 | 2.622 | 2.018 | 1.223 | 0.492 | 20.226 |
| 8 | 0.004 | 0.145 | 0.837 | 1.570 | 2.294 | 2.740 | 2.843 | 2.922 | 2.530 | 1.933 | 1.267 | 0.460 | 19.583 |
| 9 | 0.002 | 0.166 | 1.015 | 1.776 | 2.413 | 3.063 | 3.222 | 3.056 | 2.556 | 2.046 | 1.364 | 0.562 | 21.291 |
| 10 | 0.002 | 0.148 | 0.667 | 1.219 | 1.774 | 2.227 | 2.410 | 2.507 | 2.214 | 1.563 | 0.959 | 0.354 | 16.078 |
| 11 | 0.002 | 0.125 | 0.641 | 1.217 | 1.711 | 2.185 | 2.413 | 2.389 | 2.164 | 1.408 | 0.955 | 0.343 | 15.582 |
| 12 | 0.002 | 0.125 | 0.553 | 1.084 | 1.554 | 2.017 | 2.216 | 2.181 | 1.961 | 1.385 | 0.794 | 0.305 | 14.208 |
| 13 | 0.002 | 0.125 | 0.517 | 0.983 | 1.426 | 1.796 | 1.832 | 1.734 | 1.437 | 1.020 | 0.572 | 0.217 | 11.688 |
| 14 | 0.004 | 0.142 | 0.596 | 1.160 | 1.717 | 2.217 | 2.399 | 2.182 | 1.833 | 1.344 | 0.879 | 0.301 | 14.802 |
| 15 | 0.005 | 0.174 | 0.753 | 1.462 | 2.036 | 2.563 | 2.736 | 2.624 | 2.267 | 1.690 | 1.000 | 0.428 | 17.779 |
| 16 | 0.005 | 0.176 | 0.723 | 1.339 | 1.818 | 2.394 | 2.584 | 2.131 | 2.065 | 1.677 | 0.952 | 0.310 | 16.222 |
| 17 | 0.006 | 0.197 | 0.539 | 1.356 | 1.860 | 1.487 | 1.468 | 1.631 | 1.523 | 0.849 | 0.615 | 0.432 | 12.022 |
| 18 | 0.007 | 0.200 | 0.727 | 1.341 | 1.838 | 2.191 | 2.423 | 2.387 | 2.052 | 1.585 | 0.985 | 0.421 | 16.194 |
| 19 | 0.006 | 0.192 | 0.579 | 1.261 | 1.941 | 2.435 | 2.545 | 2.574 | 2.308 | 1.871 | 1.232 | 0.535 | 17.512 |
| 20 | 0.007 | 0.211 | 0.690 | 1.258 | 1.863 | 2.328 | 2.517 | 2.575 | 2.318 | 1.834 | 1.146 | 0.455 | 17.259 |
| 21 | 0.013 | 0.297 | 0.996 | 1.754 | 2.422 | 2.822 | 3.022 | 2.990 | 2.665 | 2.053 | 1.252 | 0.387 | 20.737 |
| 22 | 0.013 | 0.284 | 0.958 | 1.634 | 2.323 | 2.833 | 3.032 | 2.972 | 2.626 | 1.981 | 0.983 | 0.497 | 20.191 |
| 23 | 0.013 | 0.307 | 1.114 | 1.912 | 2.686 | 3.253 | 3.414 | 3.262 | 2.892 | 2.234 | 1.451 | 0.630 | 23.232 |
| 24 | 0.011 | 0.252 | 0.840 | 1.546 | 2.247 | 2.718 | 3.045 | 2.951 | 2.484 | 1.807 | 1.033 | 0.417 | 19.394 |
| 25 | 0.010 | 0.252 | 0.837 | 1.551 | 2.247 | 2.804 | 3.066 | 2.921 | 2.485 | 1.778 | 1.064 | 0.469 | 19.535 |
| 26 | 0.013 | 0.281 | 0.919 | 1.619 | 2.284 | 2.836 | 3.033 | 3.023 | 2.518 | 1.967 | 1.256 | 0.548 | 20.349 |
| 27 | 0.017 | 0.292 | 0.919 | 1.625 | 2.280 | 2.787 | 3.069 | 3.120 | 2.772 | 2.318 | 1.467 | 0.624 | 21.363 |
| 28 | 0.016 | 0.307 | 0.980 | 1.723 | 2.435 | 2.963 | 3.201 | 3.232 | 2.910 | 2.104 | 1.339 | 0.512 | 21.787 |
| 29 | 0.017 | 0.314 | 0.953 | 1.675 | 2.328 | 2.788 | 3.004 | 2.990 | 2.642 | 2.049 | 1.311 | 0.518 | 20.646 |
| 30 | 0.013 | 0.215 | 0.778 | 1.577 | 2.254 | 2.793 | 3.038 | 2.034 | 0.382 | 1.333 | 0.500 | 0.325 | 15.400 |
| 31 | 0.021 | 0.357 | 1.126 | 1.935 | 2.623 | 3.082 | 3.259 | 2.960 | 1.436 | 1.722 | 1.149 | 0.587 | 20.316 |
| Average | 0.007 | 0.195 | 0.759 | 1.451 | 2.047 | 2.503 | 2.674 | 2.585 | 2.184 | 1.710 | 1.045 | 0.426 | 17.635 |

## April

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.024 | 0.389 | 1.184 | 2.032 | 2.770 | 3.192 | 3.352 | 3.214 | 2.950 | 2.359 | 1.243 | 0.563 | 23.351 |
| 2 | 0.026 | 0.475 | 1.363 | 2.170 | 2.888 | 3.343 | 3.504 | 3.461 | 3.096 | 2.467 | 1.617 | 0.711 | 25.200 |
| 3 | 0.023 | 0.324 | 0.909 | 1.597 | 2.267 | 2.794 | 3.082 | 3.068 | 2.800 | 2.166 | 1.221 | 0.459 | 20.800 |
| 4 | 0.029 | 0.411 | 1.133 | 1.907 | 2.613 | 3.127 | 3.241 | 3.248 | 2.794 | 2.192 | 1.330 | 0.543 | 22.637 |
| 5 | 0.030 | 0.364 | 1.019 | 1.723 | 2.371 | 2.752 | 2.904 | 2.959 | 2.547 | 2.052 | 1.330 | 0.598 | 20.726 |
| 6 | 0.026 | 0.330 | 0.908 | 1.604 | 2.036 | 2.564 | 2.659 | 2.400 | 1.992 | 1.564 | 0.936 | 0.406 | 17.467 |
| 7 | 0.033 | 0.354 | 0.952 | 1.661 | 2.144 | 2.669 | 2.834 | 2.861 | 2.070 | 1.516 | 0.718 | 0.297 | 18.161 |
| 8 | 0.030 | 0.337 | 0.912 | 1.613 | 2.241 | 2.652 | 2.822 | 2.561 | 2.444 | 1.872 | 1.106 | 0.437 | 19.070 |
| 9 | 0.035 | 0.415 | 1.103 | 1.847 | 2.465 | 2.864 | 3.047 | 2.994 | 2.660 | 2.002 | 1.244 | 0.476 | 21.235 |
| 10 | 0.034 | 0.397 | 1.067 | 1.816 | 2.446 | 2.856 | 2.933 | 2.853 | 2.604 | 1.463 | 0.798 | 0.595 | 19.939 |
| 11 | 0.040 | 0.388 | 0.991 | 1.677 | 2.370 | 2.828 | 3.047 | 2.935 | 1.252 | 1.615 | 1.342 | 0.590 | 19.163 |
| 12 | 0.058 | 0.424 | 1.239 | 2.065 | 2.817 | 3.224 | 3.376 | 1.244 | 1.873 | 2.301 | 0.999 | 0.208 | 19.908 |
| 13 | 0.065 | 0.413 | 1.409 | 2.091 | 2.844 | 2.842 | 2.556 | 1.839 | 2.029 | 1.075 | 1.050 | 0.357 | 18.628 |
| 14 | 0.046 | 0.275 | 0.887 | 1.222 | 1.376 | 1.156 | 2.138 | 2.198 | 1.996 | 0.434 | 0.480 | 0.385 | 12.633 |
| 15 | 0.034 | 0.248 | 0.881 | 1.525 | 2.496 | 2.983 | 3.038 | 2.461 | 1.812 | 0.736 | 0.270 | 0.111 | 16.620 |
| 16 | 0.054 | 0.430 | 1.112 | 1.732 | 1.975 | 3.151 | 3.623 | 2.562 | 1.229 | 0.993 | 0.476 | 0.204 | 17.583 |
| 17 | 0.058 | 0.458 | 0.899 | 2.183 | 2.592 | 2.491 | 2.508 | 3.189 | 1.608 | 1.154 | 1.374 | 0.318 | 18.933 |
| 18 | 0.074 | 0.637 | 1.443 | 2.214 | 2.705 | 3.335 | 3.207 | 0.570 | 1.664 | 2.628 | 1.302 | 0.172 | 19.975 |
| 19 | 0.056 | 0.377 | 0.411 | 0.675 | 1.793 | 3.312 | 3.201 | 3.434 | 3.061 | 2.418 | 1.620 | 0.806 | 21.287 |
| 20 | 0.083 | 0.700 | 1.571 | 2.381 | 3.041 | 3.489 | 3.658 | 3.532 | 3.124 | 2.401 | 1.718 | 0.839 | 26.669 |
| 21 | 0.086 | 0.731 | 1.583 | 2.404 | 3.089 | 3.495 | 3.619 | 3.469 | 2.974 | 2.473 | 1.467 | 0.853 | 26.382 |
| 22 | 0.094 | 0.755 | 1.587 | 2.387 | 3.024 | 3.437 | 3.551 | 3.462 | 3.174 | 2.561 | 1.757 | 0.747 | 26.675 |
| 23 | 0.092 | 0.725 | 1.587 | 2.419 | 3.088 | 3.533 | 3.624 | 3.534 | 3.089 | 2.430 | 1.150 | 0.695 | 26.153 |
| 24 | 0.097 | 0.719 | 1.541 | 2.322 | 2.967 | 3.410 | 3.542 | 3.421 | 3.016 | 2.370 | 1.559 | 0.755 | 25.791 |
| 25 | 0.097 | 0.691 | 1.484 | 2.228 | 2.859 | 3.304 | 3.495 | 3.313 | 2.247 | 2.231 | 1.366 | 0.654 | 24.110 |
| 26 | 0.024 | 0.178 | 0.537 | 1.544 | 1.442 | 2.154 | 3.557 | 3.279 | 2.950 | 2.271 | 0.849 | 0.372 | 19.380 |
| 27 | 0.047 | 0.714 | 1.628 | 2.449 | 3.100 | 3.489 | 3.661 | 2.926 | 2.434 | 1.665 | 1.833 | 0.307 | 24.371 |
| 28 | 0.051 | 0.167 | 0.459 | 1.776 | 2.780 | 3.655 | 3.845 | 3.533 | 2.953 | 1.643 | 1.798 | 0.791 | 23.562 |
| 29 | 0.073 | 0.396 | 1.555 | 2.391 | 3.055 | 3.549 | 2.119 | 0.774 | 2.006 | 1.024 | 0.848 | 0.985 | 18.867 |
| 30 | 0.094 | 0.784 | 1.621 | 2.450 | 2.970 | 3.577 | 3.837 | 2.413 | 1.877 | 0.813 | 1.570 | 0.935 | 23.070 |
| Average | 0.054 | 0.467 | 1.166 | 1.937 | 2.554 | 3.041 | 3.186 | 2.790 | 2.411 | 1.830 | 1.212 | 0.539 | 21.278 |

May

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.133 | 0.579 | 1.424 | 2.311 | 2.617 | 3.052 | 3.406 | 3.545 | 3.101 | 2.594 | 1.761 | 0.960 | 25.720 |
| 2 | 0.090 | 0.733 | 0.938 | 1.807 | 2.275 | 3.074 | 2.912 | 1.656 | 2.321 | 1.486 | 1.084 | 0.537 | 18.969 |
| 3 | 0.046 | 0.161 | 0.251 | 0.534 | 0.742 | 1.512 | 1.944 | 1.906 | 1.520 | 1.749 | 0.683 | 0.263 | 11.379 |
| 4 | 0.029 | 0.147 | 0.333 | 0.741 | 0.764 | 0.926 | 0.420 | 0.780 | 0.745 | 0.679 | 0.385 | 0.207 | 6.200 |
| 5 | 0.028 | 0.067 | 0.146 | 0.336 | 0.666 | 1.342 | 1.892 | 1.311 | 1.031 | 1.064 | 0.492 | 0.130 | 8.534 |
| 6 | 0.052 | 0.258 | 0.340 | 0.378 | 0.955 | 0.910 | 1.296 | 1.541 | 2.017 | 1.961 | 1.162 | 0.581 | 11.562 |
| 7 | 0.091 | 0.476 | 0.673 | 1.538 | 2.043 | 1.832 | 1.486 | 2.198 | 2.272 | 2.637 | 0.898 | 0.417 | 16.620 |
| 8 | 0.024 | 0.181 | 0.503 | 1.211 | 2.555 | 2.994 | 2.748 | 3.359 | 3.072 | 2.500 | 0.628 | 0.427 | 20.271 |
| 9 | 0.130 | 0.641 | 1.353 | 1.733 | 2.685 | 2.491 | 2.216 | 3.593 | 2.917 | 2.630 | 1.761 | 0.643 | 22.852 |
| 10 | 0.113 | 0.167 | 0.668 | 1.036 | 2.903 | 3.537 | 3.297 | 2.429 | 2.914 | 2.612 | 1.863 | 0.942 | 22.504 |
| 11 | 0.043 | 0.241 | 0.665 | 0.965 | 1.196 | 1.972 | 2.861 | 3.209 | 2.159 | 1.600 | 0.689 | 0.415 | 16.139 |
| 12 | 0.054 | 0.460 | 1.226 | 2.142 | 1.805 | 1.979 | 1.394 | 0.325 | 0.252 | 0.047 | 0.117 | 0.333 | 10.285 |
| 13 | 0.050 | 0.181 | 0.287 | 0.963 | 0.554 | 1.101 | 1.785 | 1.570 | 0.989 | 0.791 | 1.185 | 0.609 | 10.178 |
| 14 | 0.065 | 0.224 | 0.577 | 1.490 | 0.484 | 2.158 | 1.111 | 1.930 | 2.606 | 2.205 | 1.383 | 0.342 | 14.595 |
| 15 | 0.074 | 0.511 | 1.578 | 1.861 | 1.398 | 1.363 | 2.893 | 3.420 | 2.540 | 0.252 | 0.974 | 0.853 | 17.772 |
| 16 | 0.119 | 0.511 | 1.734 | 2.546 | 3.247 | 3.129 | 3.727 | 3.486 | 3.268 | 2.604 | 1.327 | 0.770 | 26.584 |
| 17 | 0.085 | 0.355 | 1.369 | 2.076 | 2.559 | 3.099 | 3.624 | 2.270 | 2.940 | 2.119 | 1.447 | 1.168 | 23.209 |
| 18 | 0.118 | 0.408 | 1.185 | 2.514 | 1.188 | 3.007 | 2.518 | 2.446 | 1.329 | 0.823 | 2.131 | 0.912 | 18.739 |
| 19 | 0.178 | 0.371 | 0.820 | 1.880 | 2.460 | 2.995 | 1.837 | 1.643 | 0.712 | 1.059 | 1.639 | 0.807 | 16.591 |
| 20 | 0.023 | 0.128 | 0.353 | 0.685 | 1.631 | 2.374 | 2.488 | 1.464 | 1.394 | 0.968 | 0.856 | 0.432 | 12.860 |
| 21 | 0.153 | 0.668 | 0.622 | 1.330 | 1.303 | 1.641 | 1.948 | 1.575 | 1.159 | 1.317 | 0.787 | 0.380 | 12.975 |
| 22 | 0.107 | 0.577 | 1.142 | 0.581 | 1.497 | 1.890 | 2.343 | 2.091 | 2.000 | 1.572 | 0.946 | 0.346 | 15.179 |
| 23 | 0.150 | 0.658 | 0.907 | 1.759 | 2.009 | 2.205 | 2.686 | 2.675 | 2.996 | 1.924 | 1.492 | 0.908 | 20.551 |
| 24 | 0.119 | 0.874 | 1.716 | 2.519 | 2.697 | 3.340 | 3.520 | 3.305 | 3.189 | 2.219 | 1.828 | 0.954 | 26.512 |
| 25 | 0.099 | 0.822 | 1.720 | 2.368 | 3.041 | 3.421 | 3.527 | 3.443 | 2.960 | 0.181 | 0.180 | 0.381 | 22.278 |
| 26 | 0.103 | 0.858 | 1.709 | 2.506 | 3.117 | 3.499 | 3.655 | 3.459 | 0.860 | 0.314 | 0.946 | 0.918 | 22.114 |
| 27 | 0.129 | 0.708 | 1.633 | 2.449 | 3.080 | 3.473 | 3.627 | 3.527 | 3.198 | 2.591 | 1.867 | 0.919 | 27.490 |
| 28 | 0.189 | 0.908 | 1.641 | 2.410 | 2.839 | 3.235 | 2.978 | 2.342 | 2.440 | 1.606 | 2.013 | 0.388 | 23.110 |
| 29 | 0.155 | 0.736 | 1.671 | 2.383 | 2.993 | 3.213 | 2.978 | 2.804 | 3.030 | 1.735 | 0.712 | 0.459 | 22.950 |
| 30 | 0.119 | 0.635 | 0.949 | 1.425 | 1.731 | 2.955 | 3.408 | 3.590 | 2.388 | 2.149 | 1.307 | 0.504 | 21.228 |
| 31 | 0.112 | 0.495 | 0.885 | 1.919 | 2.516 | 3.174 | 3.714 | 3.420 | 3.627 | 1.215 | 0.275 | 0.041 | 21.414 |
| Average | 0.096 | 0.476 | 1.001 | 1.626 | 1.986 | 2.480 | 2.588 | 2.462 | 2.192 | 1.587 | 1.123 | 0.579 | 18.302 |

June

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.106 | 0.484 | 0.570 | 1.456 | 2.137 | 2.653 | 2.636 | 3.292 | 2.523 | 1.514 | 0.996 | 0.338 | 18.843 |
| 2 | 0.105 | 0.775 | 1.585 | 2.458 | 3.000 | 2.799 | 3.096 | 3.500 | 3.191 | 1.987 | 0.572 | 0.563 | 23.777 |
| 3 | 0.148 | 0.769 | 1.790 | 2.518 | 3.131 | 3.525 | 3.583 | 3.236 | 1.979 | 1.750 | 0.394 | 0.335 | 23.294 |
| 4 | 0.108 | 0.504 | 1.273 | 2.250 | 2.748 | 3.343 | 3.783 | 0.954 | 1.795 | 2.876 | 1.906 | 1.146 | 22.894 |
| 5 | 0.131 | 0.417 | 0.977 | 2.338 | 2.849 | 3.299 | 3.197 | 1.841 | 2.457 | 2.635 | 1.776 | 0.258 | 22.313 |
| 6 | 0.062 | 0.382 | 1.234 | 1.681 | 2.172 | 2.705 | 2.216 | 3.259 | 3.135 | 2.014 | 0.839 | 0.116 | 19.877 |
| 7 | 0.128 | 0.786 | 1.692 | 2.264 | 3.112 | 3.599 | 3.198 | 2.143 | 1.817 | 1.765 | 1.173 | 0.952 | 22.789 |
| 8 | 0.127 | 0.613 | 1.779 | 2.281 | 2.713 | 2.869 | 3.560 | 2.993 | 2.814 | 2.707 | 1.966 | 1.188 | 25.805 |
| 9 | 0.147 | 0.523 | 0.656 | 1.638 | 2.220 | 3.071 | 3.208 | 3.281 | 3.249 | 1.947 | 1.210 | 1.056 | 22.353 |
| 10 | 0.134 | 0.852 | 1.737 | 2.531 | 3.195 | 3.342 | 2.976 | 2.990 | 1.211 | 2.786 | 2.096 | 1.171 | 25.250 |
| 11 | 0.146 | 0.804 | 1.294 | 1.816 | 2.462 | 2.772 | 1.654 | 0.969 | 2.988 | 2.497 | 1.028 | 0.178 | 18.787 |
| 12 | 0.176 | 0.848 | 1.538 | 1.557 | 2.527 | 1.798 | 1.749 | 3.427 | 1.819 | 0.703 | 1.518 | 0.340 | 18.040 |
| 13 | 0.082 | 0.291 | 0.786 | 0.936 | 1.750 | 2.298 | 2.065 | 2.243 | 1.984 | 1.200 | 0.933 | 0.333 | 15.058 |
| 14 | 0.130 | 0.431 | 0.936 | 1.956 | 2.871 | 3.466 | 3.265 | 1.020 | 0.413 | 0.385 | 0.937 | 0.901 | 17.034 |
| 15 | 0.141 | 0.504 | 0.845 | 1.675 | 2.406 | 3.672 | 3.549 | 1.970 | 2.642 | 1.559 | 1.852 | 1.308 | 22.541 |
| 16 | 0.069 | 0.338 | 1.229 | 2.405 | 2.556 | 2.002 | 1.948 | 2.828 | 1.897 | 2.202 | 1.652 | 0.890 | 20.205 |
| 17 | 0.122 | 0.521 | 1.300 | 1.874 | 1.547 | 2.092 | 1.605 | 2.623 | 2.478 | 2.646 | 1.829 | 0.527 | 19.249 |
| 18 | 0.153 | 0.654 | 1.092 | 1.139 | 1.653 | 2.758 | 2.552 | 3.085 | 1.790 | 0.730 | 0.335 | 0.409 | 16.591 |
| 19 | 0.131 | 0.646 | 0.840 | 2.036 | 1.986 | 2.681 | 1.826 | 2.953 | 1.888 | 1.811 | 0.823 | 0.167 | 17.869 |
| 20 | 0.112 | 0.650 | 0.841 | 1.414 | 1.587 | 1.930 | 2.513 | 2.668 | 3.214 | 2.527 | 2.110 | 1.299 | 21.262 |
| 21 | 0.135 | 0.706 | 1.010 | 2.294 | 3.260 | 3.419 | 3.792 | 3.287 | 2.759 | 1.841 | 0.951 | 0.589 | 24.190 |
| 22 | 0.097 | 0.762 | 1.647 | 2.488 | 3.110 | 3.453 | 3.609 | 3.527 | 3.225 | 2.781 | 1.997 | 1.182 | 28.228 |
| 23 | 0.106 | 0.758 | 1.698 | 2.500 | 3.140 | 3.484 | 3.722 | 3.801 | 3.208 | 2.752 | 2.028 | 1.168 | 28.705 |
| 24 | 0.101 | 0.756 | 2.031 | 2.221 | 3.057 | 3.505 | 3.649 | 3.747 | 2.733 | 1.062 | 1.171 | 1.275 | 25.552 |
| 25 | 0.140 | 0.613 | 1.376 | 1.582 | 1.596 | 3.046 | 3.304 | 2.573 | 2.400 | 1.585 | 0.756 | 0.459 | 19.593 |
| 26 | 0.069 | 0.414 | 0.792 | 1.288 | 2.149 | 2.623 | 3.092 | 3.660 | 2.910 | 0.993 | 0.370 | 0.063 | 18.439 |
| 27 | 0.105 | 0.546 | 0.747 | 1.684 | 1.737 | 2.109 | 1.213 | 0.270 | 0.176 | 0.454 | 0.652 | 0.360 | 10.142 |
| 28 | 0.040 | 0.247 | 1.368 | 2.125 | 1.482 | 2.287 | 2.203 | 1.532 | 1.004 | 0.612 | 0.780 | 0.534 | 14.365 |
| 29 | 0.168 | 0.466 | 0.672 | 0.718 | 2.140 | 1.981 | 1.840 | 1.765 | 1.615 | 1.521 | 0.628 | 0.198 | 13.905 |
| 30 | 0.082 | 0.623 | 1.205 | 2.018 | 1.529 | 2.186 | 2.870 | 1.615 | 1.507 | 2.370 | 1.468 | 1.162 | 18.856 |
| Average | 0.117 | 0.590 | 1.218 | 1.905 | 2.394 | 2.826 | 2.782 | 2.568 | 2.227 | 1.807 | 1.225 | 0.682 | 20.527 |

## July

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.102 | 0.408 | 0.789 | 2.280 | 2.759 | 3.129 | 2.437 | 1.891 | 3.127 | 1.542 | 0.505 | 0.460 | 19.617 |
| 2 | 0.077 | 0.424 | 0.834 | 1.527 | 0.915 | 2.625 | 1.047 | 3.662 | 3.342 | 1.819 | 1.850 | 0.775 | 19.154 |
| 3 | 0.131 | 0.490 | 1.740 | 1.706 | 1.900 | 1.790 | 1.459 | 1.428 | 1.751 | 2.875 | 1.292 | 0.619 | 17.255 |
| 4 | 0.095 | 0.560 | 1.677 | 1.588 | 0.824 | 2.230 | 1.695 | 2.292 | 1.795 | 2.243 | 1.358 | 0.527 | 17.064 |
| 5 | 0.056 | 0.386 | 0.807 | 1.794 | 1.361 | 1.568 | 1.552 | 2.399 | 3.021 | 1.277 | 0.921 | 0.522 | 15.822 |
| 6 | 0.046 | 0.298 | 0.422 | 0.808 | 0.540 | 1.166 | 1.094 | 1.016 | 0.752 | 0.617 | 0.692 | 0.309 | 7.855 |
| 7 | 0.094 | 0.517 | 1.246 | 1.695 | 1.906 | 3.139 | 3.447 | 2.731 | 2.517 | 2.316 | 1.280 | 0.330 | 21.393 |
| 8 | 0.086 | 0.665 | 1.507 | 2.130 | 2.703 | 3.455 | 3.546 | 3.617 | 2.781 | 1.218 | 0.880 | 0.472 | 23.210 |
| 9 | 0.063 | 0.682 | 1.662 | 2.428 | 3.074 | 3.369 | 3.828 | 3.355 | 2.552 | 2.284 | 2.073 | 0.778 | 26.328 |
| 10 | 0.099 | 0.448 | 1.228 | 2.777 | 2.914 | 2.760 | 2.562 | 2.486 | 2.144 | 2.149 | 1.908 | 0.813 | 22.645 |
| 11 | 0.074 | 0.459 | 1.425 | 2.322 | 3.097 | 2.861 | 2.234 | 0.712 | 0.924 | 1.886 | 1.104 | 0.649 | 17.931 |
| 12 | 0.107 | 0.717 | 1.039 | 1.062 | 2.097 | 2.004 | 2.390 | 1.716 | 1.882 | 1.300 | 1.330 | 0.792 | 16.851 |
| 13 | 0.080 | 0.490 | 1.543 | 1.841 | 1.397 | 2.253 | 2.747 | 2.301 | 0.734 | 0.246 | 0.600 | 0.387 | 14.843 |
| 14 | 0.113 | 0.668 | 1.212 | 1.903 | 2.884 | 1.503 | 1.237 | 1.403 | 1.280 | 1.819 | 0.744 | 0.422 | 15.330 |
| 15 | 0.107 | 0.389 | 0.920 | 1.383 | 1.788 | 1.327 | 1.945 | 1.983 | 1.897 | 2.081 | 1.491 | 0.924 | 16.389 |
| 16 | 0.041 | 0.386 | 0.937 | 1.291 | 0.854 | 1.112 | 1.369 | 2.101 | 2.659 | 2.558 | 0.542 | 1.247 | 15.498 |
| 17 | 0.100 | 0.682 | 1.316 | 1.443 | 2.247 | 2.903 | 2.194 | 1.771 | 1.700 | 1.389 | 1.235 | 0.571 | 17.820 |
| 18 | 0.050 | 0.316 | 0.968 | 1.843 | 2.003 | 2.271 | 3.155 | 3.230 | 1.845 | 1.425 | 0.859 | 0.567 | 18.628 |
| 19 | 0.078 | 0.453 | 0.843 | 1.378 | 2.040 | 1.925 | 1.793 | 1.135 | 1.952 | 1.344 | 0.359 | 0.061 | 13.392 |
| 20 | 0.062 | 0.354 | 0.919 | 1.182 | 1.273 | 1.050 | 0.998 | 1.160 | 1.199 | 0.823 | 0.498 | 0.253 | 9.848 |
| 21 | 0.043 | 0.192 | 0.427 | 0.476 | 0.747 | 0.735 | 0.735 | 0.584 | 0.770 | 0.938 | 1.056 | 0.509 | 7.386 |
| 22 | 0.082 | 0.386 | 0.798 | 1.370 | 2.444 | 3.174 | 2.548 | 2.182 | 2.270 | 1.862 | 1.083 | 0.366 | 18.686 |
| 23 | 0.058 | 0.405 | 1.260 | 2.329 | 2.579 | 3.727 | 3.707 | 2.154 | 2.569 | 0.458 | 0.416 | 0.938 | 20.775 |
| 24 | 0.022 | 0.168 | 0.358 | 0.808 | 1.174 | 1.275 | 1.117 | 0.772 | 0.935 | 0.755 | 0.489 | 0.240 | 8.191 |
| 25 | 0.019 | 0.360 | 0.525 | 1.442 | 1.874 | 1.680 | 2.226 | 2.446 | 2.338 | 1.966 | 2.158 | 1.024 | 18.329 |
| 26 | 0.078 | 0.769 | 1.768 | 2.465 | 2.668 | 2.631 | 2.926 | 2.744 | 0.727 | 1.058 | 1.318 | 0.930 | 20.161 |
| 27 | 0.038 | 0.304 | 0.665 | 1.244 | 1.563 | 1.983 | 2.535 | 2.452 | 1.882 | 1.252 | 0.999 | 0.751 | 15.801 |
| 28 | 0.083 | 0.610 | 1.611 | 2.428 | 3.089 | 3.529 | 3.753 | 2.608 | 1.439 | 2.973 | 1.366 | 0.836 | 24.466 |
| 29 | 0.029 | 0.183 | 0.566 | 1.774 | 2.410 | 3.181 | 2.042 | 2.054 | 1.819 | 2.091 | 1.745 | 0.559 | 18.549 |
| 30 | 0.050 | 0.411 | 0.842 | 0.992 | 2.670 | 2.191 | 3.534 | 2.292 | 1.575 | 1.675 | 1.237 | 0.372 | 17.899 |
| 31 | 0.058 | 0.352 | 0.520 | 0.700 | 1.325 | 3.228 | 2.238 | 1.582 | 2.118 | 2.068 | 2.041 | 1.381 | 17.800 |
| Average | 0.072 | 0.449 | 1.044 | 1.626 | 1.972 | 2.315 | 2.261 | 2.073 | 1.880 | 1.623 | 1.143 | 0.625 | 17.255 |

## August

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.044 | 0.319 | 0.774 | 1.219 | 1.282 | 1.622 | 1.467 | 1.844 | 1.672 | 1.636 | 1.163 | 0.531 | 13.699 |
| 2 | 0.024 | 0.372 | 0.251 | 1.171 | 2.194 | 1.475 | 1.468 | 1.984 | 1.902 | 1.589 | 1.015 | 0.371 | 13.878 |
| 3 | 0.022 | 0.254 | 0.863 | 2.028 | 1.617 | 2.354 | 2.855 | 1.706 | 1.480 | 1.341 | 0.764 | 0.598 | 16.160 |
| 4 | 0.055 | 0.347 | 0.969 | 1.709 | 3.270 | 3.471 | 2.698 | 2.482 | 3.021 | 2.143 | 1.135 | 0.784 | 22.134 |
| 5 | 0.091 | 0.450 | 1.022 | 1.835 | 2.183 | 2.519 | 2.465 | 3.220 | 3.288 | 2.305 | 1.929 | 1.170 | 22.617 |
| 6 | 0.083 | 0.520 | 1.307 | 2.269 | 2.938 | 3.195 | 3.746 | 2.682 | 3.105 | 2.752 | 1.963 | 0.767 | 25.447 |
| 7 | 0.055 | 0.649 | 1.531 | 2.169 | 2.814 | 3.005 | 2.618 | 3.442 | 2.898 | 2.483 | 1.531 | 0.796 | 24.235 |
| 8 | 0.022 | 0.157 | 0.531 | 1.011 | 1.549 | 2.816 | 2.322 | 1.849 | 1.849 | 1.856 | 0.127 | 0.123 | 14.245 |
| 9 | 0.027 | 0.129 | 0.539 | 0.972 | 1.581 | 1.451 | 0.615 | 0.550 | 0.875 | 1.286 | 0.835 | 0.498 | 9.515 |
| 10 | 0.041 | 0.422 | 1.215 | 1.625 | 2.002 | 3.148 | 2.757 | 1.305 | 1.418 | 1.571 | 1.049 | 0.267 | 16.951 |
| 11 | 0.057 | 0.336 | 0.795 | 0.781 | 1.247 | 1.015 | 2.310 | 2.591 | 1.492 | 1.880 | 0.641 | 0.327 | 13.498 |
| 12 | 0.022 | 0.158 | 0.303 | 0.994 | 1.617 | 2.129 | 1.703 | 2.035 | 1.355 | 0.612 | 0.618 | 0.455 | 12.100 |
| 13 | 0.058 | 0.378 | 0.943 | 2.447 | 2.489 | 3.492 | 2.288 | 2.232 | 2.737 | 1.862 | 1.833 | 0.623 | 21.666 |
| 14 | 0.005 | 0.285 | 0.796 | 0.677 | 1.849 | 3.419 | 2.782 | 3.263 | 3.030 | 1.454 | 0.913 | 0.277 | 18.931 |
| 15 | 0.026 | 0.156 | 0.415 | 0.931 | 1.407 | 1.409 | 2.477 | 3.084 | 2.715 | 2.248 | 1.330 | 0.443 | 16.777 |
| 16 | 0.007 | 0.044 | 0.134 | 0.269 | 0.326 | 1.370 | 2.909 | 2.578 | 3.078 | 0.751 | 0.079 | 0.035 | 11.592 |
| 17 | 0.037 | 0.398 | 1.106 | 1.880 | 1.538 | 2.928 | 2.948 | 3.112 | 3.001 | 2.597 | 1.622 | 0.701 | 22.071 |
| 18 | 0.056 | 0.545 | 1.328 | 2.517 | 2.505 | 3.173 | 3.856 | 3.675 | 2.892 | 1.714 | 2.046 | 0.668 | 25.235 |
| 19 | 0.044 | 0.594 | 1.580 | 2.412 | 3.084 | 3.544 | 3.392 | 3.252 | 3.344 | 2.968 | 1.658 | 0.571 | 26.562 |
| 20 | 0.075 | 0.722 | 1.574 | 2.238 | 2.776 | 3.377 | 3.727 | 3.348 | 0.561 | 0.588 | 1.508 | 0.786 | 21.470 |
| 21 | 0.044 | 0.331 | 1.144 | 1.916 | 2.333 | 3.465 | 3.736 | 2.517 | 2.163 | 0.759 | 0.329 | 0.533 | 19.420 |
| 22 | 0.022 | 0.241 | 0.532 | 1.593 | 1.946 | 2.513 | 3.563 | 3.562 | 2.396 | 1.535 | 1.059 | 0.381 | 19.374 |
| 23 | 0.038 | 0.347 | 1.106 | 1.487 | 2.082 | 2.099 | 1.436 | 2.309 | 2.551 | 2.713 | 1.593 | 0.083 | 17.864 |
| 24 | 0.041 | 0.226 | 0.360 | 0.628 | 0.615 | 1.061 | 1.568 | 1.945 | 2.424 | 1.379 | 0.728 | 0.346 | 11.394 |
| 25 | 0.009 | 0.123 | 0.509 | 0.918 | 0.957 | 1.228 | 1.509 | 1.391 | 1.603 | 1.742 | 1.154 | 0.561 | 11.803 |
| 26 | 0.044 | 0.348 | 1.240 | 2.245 | 2.085 | 3.351 | 3.265 | 2.949 | 1.362 | 2.003 | 1.212 | 0.445 | 20.631 |
| 27 | 0.044 | 0.506 | 1.619 | 1.652 | 3.111 | 2.848 | 3.527 | 3.685 | 3.058 | 2.524 | 1.732 | 1.054 | 25.552 |
| 28 | 0.039 | 0.414 | 0.908 | 2.317 | 2.859 | 2.534 | 1.485 | 0.487 | 0.490 | 1.000 | 0.590 | 0.528 | 13.721 |
| 29 | 0.044 | 0.302 | 0.845 | 1.658 | 2.580 | 3.351 | 3.083 | 2.871 | 2.813 | 1.750 | 1.052 | 0.951 | 21.464 |
| 30 | 0.041 | 0.273 | 0.867 | 0.981 | 1.447 | 2.276 | 2.658 | 3.480 | 3.413 | 2.073 | 0.711 | 0.156 | 18.439 |
| 31 | 0.019 | 0.276 | 0.824 | 1.812 | 2.710 | 2.656 | 3.408 | 2.904 | 3.251 | 2.146 | 1.571 | 0.587 | 22.221 |
| Average | 0.040 | 0.343 | 0.901 | 1.560 | 2.032 | 2.526 | 2.601 | 2.527 | 2.298 | 1.783 | 1.145 | 0.529 | 18.409 |

## September

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.065 | 0.338 | 0.881 | 1.883 | 2.489 | 3.489 | 3.360 | 3.565 | 2.862 | 1.951 | 1.204 | 0.495 | 22.650 |
| 2 | 0.045 | 0.386 | 1.125 | 1.217 | 1.843 | 2.407 | 3.355 | 3.398 | 3.192 | 2.120 | 1.530 | 0.690 | 21.371 |
| 3 | 0.052 | 0.559 | 1.471 | 2.592 | 2.566 | 2.051 | 2.720 | 3.893 | 2.337 | 0.538 | 0.241 | 0.277 | 19.340 |
| 4 | 0.050 | 0.307 | 0.628 | 1.031 | 1.649 | 3.122 | 2.479 | 2.758 | 1.436 | 1.574 | 0.857 | 0.375 | 16.333 |
| 5 | 0.015 | 0.129 | 0.476 | 1.110 | 1.087 | 1.846 | 2.587 | 3.353 | 2.429 | 1.727 | 0.323 | 0.181 | 15.327 |
| 6 | 0.022 | 0.329 | 0.831 | 1.386 | 1.632 | 2.126 | 3.105 | 2.990 | 1.773 | 1.611 | 0.213 | 0.179 | 16.257 |
| 7 | 0.033 | 0.235 | 0.921 | 1.143 | 1.303 | 1.738 | 3.265 | 2.675 | 2.433 | 1.963 | 1.521 | 0.470 | 17.748 |
| 8 | 0.029 | 0.455 | 1.235 | 2.359 | 2.940 | 3.288 | 3.441 | 3.539 | 3.084 | 2.757 | 1.841 | 0.756 | 25.900 |
| 9 | 0.044 | 0.559 | 1.514 | 2.387 | 2.484 | 3.179 | 3.308 | 3.018 | 2.191 | 2.794 | 1.045 | 0.635 | 23.261 |
| 10 | 0.029 | 0.269 | 0.582 | 1.801 | 2.287 | 2.426 | 2.131 | 2.932 | 2.503 | 1.659 | 1.207 | 0.689 | 18.621 |
| 11 | 0.001 | 0.029 | 0.142 | 0.324 | 0.851 | 1.300 | 1.873 | 2.108 | 2.152 | 1.637 | 1.189 | 0.475 | 12.170 |
| 12 | 0.015 | 0.241 | 0.895 | 1.897 | 2.937 | 3.133 | 2.410 | 2.271 | 3.372 | 2.598 | 1.957 | 0.699 | 22.490 |
| 13 | 0.041 | 0.304 | 0.555 | 2.497 | 2.893 | 3.239 | 3.583 | 2.679 | 2.780 | 2.486 | 0.887 | 0.189 | 22.165 |
| 14 | 0.024 | 0.425 | 0.572 | 2.725 | 2.676 | 3.481 | 2.280 | 2.237 | 2.713 | 0.895 | 0.688 | 0.430 | 19.195 |
| 15 | 0.049 | 0.416 | 0.662 | 0.846 | 1.671 | 2.496 | 2.803 | 1.708 | 3.016 | 2.395 | 1.378 | 0.420 | 17.928 |
| 16 | 0.017 | 0.408 | 0.933 | 1.805 | 2.492 | 2.981 | 2.309 | 2.957 | 2.998 | 2.398 | 1.606 | 0.817 | 21.807 |
| 17 | 0.035 | 0.380 | 1.473 | 2.127 | 2.288 | 2.144 | 3.370 | 3.088 | 3.054 | 2.382 | 1.559 | 0.840 | 22.804 |
| 18 | 0.044 | 0.557 | 0.985 | 1.512 | 1.828 | 1.916 | 1.502 | 1.624 | 1.217 | 1.581 | 0.441 | 0.344 | 13.622 |
| 19 | 0.038 | 0.559 | 1.002 | 1.009 | 2.782 | 2.680 | 3.406 | 1.519 | 2.368 | 0.383 | 1.077 | 0.224 | 17.062 |
| 20 | 0.009 | 0.061 | 0.511 | 0.759 | 1.053 | 0.824 | 1.560 | 1.642 | 1.131 | 1.873 | 1.598 | 0.504 | 11.548 |
| 21 | 0.071 | 0.443 | 0.835 | 1.883 | 1.896 | 2.682 | 3.187 | 3.402 | 2.895 | 2.163 | 0.800 | 0.376 | 20.673 |
| 22 | 0.022 | 0.602 | 1.482 | 2.137 | 2.323 | 2.766 | 2.542 | 2.922 | 1.986 | 1.415 | 0.684 | 0.308 | 19.223 |
| 23 | 0.052 | 0.493 | 1.313 | 2.202 | 2.901 | 3.249 | 3.400 | 3.284 | 2.953 | 2.131 | 1.160 | 0.201 | 23.359 |
| 24 | 0.030 | 0.344 | 1.266 | 2.170 | 2.800 | 3.320 | 3.123 | 3.136 | 2.859 | 2.310 | 1.069 | 0.189 | 22.631 |
| 25 | 0.023 | 0.424 | 1.202 | 1.880 | 1.790 | 2.553 | 2.321 | 2.590 | 2.444 | 2.091 | 1.261 | 0.448 | 19.048 |
| 26 | 0.026 | 0.230 | 0.626 | 1.149 | 1.557 | 2.185 | 1.750 | 2.003 | 2.220 | 2.060 | 0.862 | 0.305 | 14.994 |
| 27 | 0.019 | 0.144 | 0.269 | 0.772 | 1.720 | 1.324 | 1.760 | 1.950 | 1.352 | 1.448 | 1.251 | 0.318 | 12.337 |
| 28 | 0.028 | 0.447 | 1.284 | 1.424 | 1.983 | 2.867 | 3.490 | 0.975 | 1.033 | 0.947 | 0.484 | 0.286 | 15.279 |
| 29 | 0.037 | 0.351 | 1.011 | 1.502 | 1.890 | 2.101 | 2.011 | 2.654 | 2.597 | 2.456 | 1.361 | 0.303 | 18.288 |
| 30 | 0.028 | 0.130 | 0.702 | 1.998 | 2.673 | 2.917 | 3.596 | 2.827 | 3.011 | 2.445 | 1.535 | 0.606 | 22.490 |
| Average | 0.033 | 0.352 | 0.913 | 1.651 | 2.109 | 2.528 | 2.734 | 2.657 | 2.413 | 1.893 | 1.094 | 0.434 | 18.864 |

October

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.032 | 0.326 | 0.918 | 2.047 | 2.517 | 3.610 | 2.699 | 2.746 | 2.749 | 1.962 | 0.972 | 0.378 | 20.983 |
| 2 | 0.029 | 0.394 | 1.246 | 2.039 | 2.777 | 3.245 | 3.327 | 2.095 | 2.518 | 1.708 | 0.647 | 0.274 | 20.334 |
| 3 | 0.023 | 0.338 | 0.756 | 1.097 | 1.873 | 2.183 | 1.700 | 1.621 | 1.782 | 1.813 | 0.834 | 0.347 | 14.378 |
| 4 | 0.037 | 0.348 | 0.736 | 1.502 | 1.380 | 1.445 | 1.352 | 2.328 | 1.286 | 1.324 | 0.811 | 0.285 | 12.853 |
| 5 | 0.011 | 0.196 | 0.755 | 1.038 | 1.495 | 1.083 | 1.234 | 1.235 | 0.758 | 0.136 | 0.044 | 0.032 | 8.018 |
| 6 | 0.012 | 0.263 | 0.680 | 0.722 | 0.972 | 1.424 | 1.423 | 1.978 | 1.861 | 1.796 | 0.234 | 0.133 | 11.501 |
| 7 | 0.024 | 0.296 | 0.815 | 0.960 | 0.808 | 1.044 | 0.753 | 1.045 | 1.153 | 0.723 | 0.477 | 0.159 | 8.271 |
| 8 | 0.018 | 0.288 | 0.691 | 1.787 | 2.506 | 3.303 | 3.054 | 3.349 | 2.091 | 2.248 | 1.172 | 0.480 | 20.995 |
| 9 | 0.019 | 0.329 | 0.692 | 0.787 | 1.785 | 1.447 | 3.092 | 1.291 | 0.357 | 0.369 | 0.198 | 0.062 | 10.435 |
| 10 | 0.012 | 0.208 | 0.940 | 1.959 | 2.463 | 1.845 | 1.261 | 2.695 | 2.830 | 2.547 | 0.487 | 0.111 | 17.365 |
| 11 | 0.022 | 0.225 | 0.700 | 1.765 | 1.845 | 2.698 | 3.425 | 1.653 | 1.032 | 1.659 | 1.112 | 0.454 | 16.594 |
| 12 | 0.017 | 0.247 | 0.852 | 1.673 | 2.170 | 2.359 | 1.985 | 1.178 | 1.383 | 2.170 | 1.317 | 0.456 | 15.817 |
| 13 | 0.015 | 0.138 | 0.843 | 1.149 | 1.653 | 1.923 | 1.092 | 1.069 | 1.467 | 0.865 | 0.559 | 0.239 | 11.023 |
| 14 | 0.027 | 0.376 | 0.618 | 1.992 | 2.518 | 2.830 | 2.776 | 2.595 | 2.373 | 0.506 | 0.486 | 0.128 | 17.228 |
| 15 | 0.016 | 0.142 | 0.290 | 0.482 | 0.789 | 2.469 | 2.959 | 2.559 | 0.703 | 0.431 | 0.712 | 0.326 | 11.899 |
| 16 | 0.017 | 0.217 | 0.357 | 1.020 | 1.430 | 2.387 | 2.231 | 2.275 | 2.013 | 1.290 | 0.271 | 0.203 | 13.715 |
| 17 | 0.010 | 0.275 | 1.137 | 1.485 | 2.070 | 2.370 | 2.981 | 1.548 | 0.705 | 0.813 | 0.415 | 0.271 | 14.085 |
| 18 | 0.013 | 0.176 | 0.643 | 2.227 | 2.837 | 3.016 | 3.388 | 3.039 | 2.581 | 2.191 | 1.137 | 0.335 | 21.585 |
| 19 | 0.019 | 0.295 | 0.981 | 1.903 | 2.730 | 2.665 | 3.016 | 2.994 | 2.622 | 1.660 | 1.058 | 0.376 | 20.320 |
| 20 | 0.027 | 0.262 | 1.153 | 1.942 | 2.656 | 3.082 | 3.169 | 1.609 | 1.055 | 0.748 | 0.296 | 0.092 | 16.090 |
| 21 | 0.016 | 0.202 | 0.555 | 1.647 | 2.540 | 2.973 | 3.148 | 2.965 | 2.510 | 1.553 | 1.006 | 0.285 | 19.404 |
| 22 | 0.018 | 0.290 | 1.020 | 1.828 | 2.557 | 2.929 | 3.404 | 2.738 | 2.282 | 1.760 | 1.002 | 0.198 | 20.029 |
| 23 | 0.011 | 0.252 | 0.869 | 1.807 | 2.176 | 2.979 | 3.150 | 3.051 | 2.602 | 1.875 | 1.120 | 0.305 | 20.199 |
| 24 | 0.019 | 0.242 | 0.840 | 1.822 | 2.629 | 2.972 | 2.232 | 1.896 | 2.615 | 1.798 | 0.818 | 0.153 | 18.040 |
| 25 | 0.023 | 0.268 | 1.065 | 1.910 | 2.660 | 3.069 | 2.624 | 2.417 | 2.053 | 1.840 | 1.114 | 0.263 | 19.308 |
| 26 | 0.011 | 0.243 | 0.849 | 1.585 | 2.343 | 2.981 | 3.241 | 3.049 | 2.534 | 1.537 | 0.832 | 0.179 | 19.385 |
| 27 | 0.016 | 0.355 | 1.084 | 1.676 | 2.325 | 2.906 | 2.815 | 2.811 | 2.534 | 1.683 | 0.781 | 0.214 | 19.201 |
| 28 | 0.016 | 0.260 | 0.612 | 1.727 | 2.517 | 2.956 | 3.122 | 2.954 | 2.551 | 1.877 | 1.053 | 0.260 | 19.905 |
| 29 | 0.016 | 0.253 | 1.021 | 1.824 | 2.520 | 2.922 | 3.118 | 2.880 | 2.568 | 1.665 | 1.054 | 0.230 | 20.071 |
| 30 | 0.005 | 0.080 | 0.683 | 1.227 | 2.208 | 2.146 | 1.252 | 2.182 | 1.959 | 1.748 | 1.148 | 0.279 | 14.916 |
| 31 | 0.023 | 0.173 | 0.559 | 1.559 | 2.093 | 2.000 | 1.569 | 2.311 | 1.385 | 0.688 | 0.374 | 0.051 | 12.785 |
| Average | 0.019 | 0.257 | 0.805 | 1.554 | 2.124 | 2.492 | 2.471 | 2.263 | 1.900 | 1.451 | 0.759 | 0.244 | 16.346 |

## November

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.007 | 0.086 | 0.349 | 0.489 | 1.037 | 1.972 | 1.589 | 2.153 | 1.799 | 0.808 | 0.430 | 0.256 | 10.975 |
| 2 | 0.005 | 0.164 | 0.455 | 0.661 | 1.252 | 2.097 | 2.040 | 1.172 | 0.972 | 0.685 | 0.263 | 0.082 | 9.848 |
| 3 | 0.001 | 0.045 | 0.079 | 0.196 | 0.259 | 0.417 | 0.568 | 0.417 | 0.399 | 0.284 | 0.120 | 0.051 | 2.838 |
| 4 | 0.002 | 0.075 | 0.125 | 0.275 | 0.583 | 1.032 | 0.858 | 0.484 | 0.498 | 0.644 | 0.282 | 0.129 | 4.991 |
| 5 | 0.002 | 0.089 | 0.352 | 0.842 | 1.519 | 2.236 | 1.940 | 1.362 | 1.404 | 0.941 | 0.466 | 0.246 | 11.399 |
| 6 | 0.005 | 0.130 | 0.458 | 1.234 | 2.641 | 3.032 | 2.899 | 1.817 | 1.353 | 0.960 | 0.565 | 0.150 | 15.243 |
| 7 | 0.010 | 0.168 | 0.924 | 1.927 | 2.576 | 2.985 | 3.141 | 3.051 | 2.662 | 1.089 | 1.111 | 0.127 | 19.771 |
| 8 | 0.012 | 0.248 | 0.940 | 1.934 | 2.563 | 2.959 | 3.075 | 2.901 | 2.477 | 1.844 | 1.056 | 0.258 | 20.267 |
| 9 | 0.007 | 0.156 | 0.920 | 1.924 | 2.548 | 2.932 | 3.056 | 2.931 | 2.520 | 1.880 | 1.067 | 0.259 | 20.202 |
| 10 | 0.006 | 0.156 | 0.909 | 1.877 | 2.512 | 2.910 | 3.018 | 2.858 | 2.421 | 1.737 | 0.966 | 0.237 | 19.606 |
| 11 | 0.007 | 0.191 | 0.933 | 1.699 | 2.409 | 2.691 | 2.768 | 2.602 | 2.492 | 1.852 | 1.054 | 0.200 | 18.898 |
| 12 | 0.005 | 0.168 | 0.577 | 1.734 | 1.589 | 2.084 | 1.818 | 1.508 | 1.291 | 1.773 | 0.646 | 0.090 | 13.284 |
| 13 | 0.005 | 0.119 | 0.419 | 0.800 | 1.288 | 2.025 | 1.599 | 1.570 | 1.929 | 1.899 | 0.902 | 0.184 | 12.738 |
| 14 | 0.002 | 0.071 | 0.256 | 0.750 | 1.056 | 1.538 | 1.424 | 1.137 | 1.244 | 0.806 | 0.380 | 0.099 | 8.761 |
| 15 | 0.004 | 0.090 | 0.385 | 0.755 | 1.294 | 1.255 | 0.898 | 1.536 | 1.953 | 2.028 | 1.086 | 0.192 | 11.474 |
| 16 | 0.005 | 0.187 | 0.824 | 1.381 | 2.451 | 1.464 | 2.394 | 2.614 | 2.485 | 1.817 | 0.637 | 0.229 | 16.488 |
| 17 | 0.006 | 0.230 | 0.891 | 1.888 | 2.517 | 2.922 | 3.045 | 2.893 | 2.491 | 1.841 | 1.026 | 0.224 | 19.974 |
| 18 | 0.004 | 0.124 | 0.773 | 1.863 | 2.474 | 2.876 | 3.009 | 2.960 | 2.455 | 1.817 | 0.994 | 0.096 | 19.445 |
| 19 | 0.001 | 0.118 | 0.576 | 1.163 | 1.992 | 2.095 | 3.022 | 2.116 | 1.020 | 0.680 | 0.417 | 0.082 | 13.283 |
| 20 | 0.002 | 0.117 | 0.974 | 1.396 | 2.382 | 1.916 | 1.177 | 1.110 | 0.957 | 1.456 | 0.912 | 0.080 | 12.477 |
| 21 | 0.001 | 0.032 | 0.144 | 0.532 | 0.697 | 1.058 | 1.301 | 1.852 | 1.065 | 0.246 | 0.068 | 0.022 | 7.017 |
| 22 | 0.001 | 0.153 | 0.668 | 1.469 | 1.383 | 2.322 | 1.938 | 1.187 | 1.627 | 1.038 | 0.769 | 0.152 | 12.707 |
| 23 | 0.001 | 0.190 | 0.562 | 1.692 | 2.211 | 2.676 | 1.995 | 1.366 | 1.431 | 0.891 | 0.585 | 0.130 | 13.731 |
| 24 | 0.004 | 0.103 | 0.321 | 1.065 | 1.794 | 1.916 | 2.196 | 2.178 | 1.480 | 0.745 | 0.482 | 0.082 | 12.365 |
| 25 | 0.001 | 0.156 | 0.599 | 1.484 | 2.123 | 2.563 | 2.721 | 2.578 | 2.219 | 1.602 | 0.835 | 0.175 | 17.054 |
| 26 | 0.001 | 0.153 | 0.606 | 1.574 | 2.209 | 2.619 | 2.757 | 2.622 | 2.211 | 1.588 | 0.837 | 0.185 | 17.362 |
| 27 | 0.001 | 0.150 | 0.598 | 1.498 | 2.119 | 2.558 | 2.704 | 2.602 | 2.248 | 1.632 | 0.863 | 0.181 | 17.154 |
| 28 | 0.001 | 0.148 | 0.604 | 1.423 | 2.052 | 2.472 | 2.636 | 2.540 | 2.149 | 1.501 | 0.854 | 0.189 | 16.569 |
| 29 | 0.001 | 0.152 | 0.600 | 1.441 | 2.063 | 2.474 | 2.630 | 2.514 | 2.029 | 1.348 | 0.770 | 0.164 | 16.188 |
| 30 | 0.001 | 0.145 | 0.602 | 1.611 | 2.277 | 2.654 | 2.520 | 2.651 | 2.286 | 1.613 | 0.791 | 0.179 | 17.331 |
| Average | 0.004 | 0.137 | 0.581 | 1.286 | 1.862 | 2.225 | 2.225 | 2.043 | 1.786 | 1.301 | 0.708 | 0.158 | 14.315 |

## December

| Date/Time | 6-7 | 7-8 | 8-9 | 9-10 | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.134 | 0.542 | 1.467 | 2.131 | 2.538 | 2.695 | 2.586 | 2.233 | 1.516 | 0.761 | 0.153 | 16.755 |
| 2 | 0.000 | 0.127 | 0.518 | 1.467 | 2.170 | 2.598 | 2.768 | 2.648 | 2.284 | 1.642 | 0.769 | 0.164 | 17.155 |
| 3 | 0.001 | 0.147 | 0.466 | 1.398 | 2.196 | 2.619 | 2.785 | 2.729 | 2.349 | 1.712 | 0.916 | 0.167 | 17.485 |
| 4 | 0.000 | 0.123 | 0.508 | 0.937 | 1.549 | 2.462 | 2.789 | 2.721 | 2.305 | 1.673 | 0.712 | 0.068 | 15.848 |
| 5 | 0.000 | 0.127 | 0.493 | 1.154 | 1.939 | 2.556 | 2.659 | 2.882 | 2.424 | 1.418 | 0.604 | 0.230 | 16.485 |
| 6 | 0.000 | 0.131 | 0.503 | 1.487 | 2.160 | 2.623 | 2.755 | 2.461 | 2.332 | 1.763 | 0.993 | 0.185 | 17.394 |
| 7 | 0.000 | 0.131 | 0.465 | 1.302 | 2.154 | 2.372 | 2.685 | 2.641 | 2.305 | 1.687 | 0.944 | 0.151 | 16.838 |
| 8 | 0.000 | 0.120 | 0.459 | 1.244 | 2.079 | 2.510 | 2.732 | 2.659 | 1.918 | 1.559 | 0.891 | 0.153 | 16.324 |
| 9 | 0.000 | 0.140 | 0.445 | 1.246 | 2.079 | 2.501 | 2.658 | 2.611 | 2.248 | 1.638 | 0.912 | 0.151 | 16.628 |
| 10 | 0.000 | 0.101 | 0.414 | 0.978 | 1.609 | 2.231 | 2.680 | 2.660 | 2.249 | 1.669 | 0.663 | 0.100 | 15.354 |
| 11 | 0.000 | 0.100 | 0.400 | 1.218 | 2.076 | 2.548 | 2.738 | 2.657 | 2.304 | 1.682 | 0.671 | 0.136 | 16.531 |
| 12 | 0.000 | 0.212 | 0.549 | 0.918 | 1.754 | 2.092 | 2.822 | 2.757 | 2.474 | 1.766 | 0.556 | 0.146 | 16.045 |
| 13 | 0.000 | 0.101 | 0.376 | 1.262 | 2.226 | 2.642 | 2.843 | 2.804 | 2.430 | 1.796 | 0.662 | 0.100 | 17.243 |
| 14 | 0.000 | 0.102 | 0.391 | 1.230 | 2.222 | 2.673 | 2.826 | 2.732 | 2.475 | 1.873 | 0.706 | 0.101 | 17.332 |
| 15 | 0.000 | 0.086 | 0.347 | 1.174 | 2.127 | 2.542 | 2.721 | 2.606 | 2.093 | 1.689 | 0.662 | 0.130 | 16.179 |
| 16 | 0.000 | 0.067 | 0.381 | 0.877 | 1.785 | 2.433 | 2.542 | 2.583 | 2.225 | 1.669 | 0.635 | 0.148 | 15.346 |
| 17 | 0.000 | 0.080 | 0.392 | 1.251 | 1.974 | 2.433 | 2.647 | 2.640 | 2.272 | 1.665 | 0.667 | 0.114 | 16.135 |
| 18 | 0.000 | 0.096 | 0.371 | 1.083 | 2.053 | 2.310 | 2.637 | 2.614 | 2.261 | 1.726 | 0.699 | 0.110 | 15.960 |
| 19 | 0.000 | 0.089 | 0.366 | 1.055 | 2.003 | 2.398 | 2.589 | 2.567 | 2.241 | 1.683 | 0.699 | 0.117 | 15.806 |
| 20 | 0.000 | 0.101 | 0.374 | 1.047 | 2.002 | 2.426 | 2.603 | 2.528 | 2.197 | 1.653 | 0.669 | 0.139 | 15.738 |
| 21 | 0.000 | 0.095 | 0.352 | 1.066 | 2.124 | 2.516 | 2.709 | 2.662 | 2.301 | 1.755 | 0.712 | 0.106 | 16.397 |
| 22 | 0.000 | 0.110 | 0.372 | 1.092 | 2.152 | 2.595 | 2.758 | 2.692 | 2.356 | 1.839 | 0.738 | 0.090 | 16.793 |
| 23 | 0.000 | 0.086 | 0.348 | 1.075 | 2.191 | 2.628 | 2.766 | 2.703 | 2.343 | 1.802 | 0.757 | 0.116 | 16.814 |
| 24 | 0.000 | 0.083 | 0.354 | 1.049 | 2.136 | 2.592 | 2.759 | 2.708 | 2.390 | 1.837 | 0.769 | 0.123 | 16.800 |
| 25 | 0.000 | 0.080 | 0.358 | 1.027 | 2.081 | 2.505 | 2.696 | 2.657 | 2.357 | 1.818 | 0.790 | 0.120 | 16.490 |
| 26 | 0.000 | 0.086 | 0.432 | 1.016 | 1.983 | 2.440 | 2.651 | 2.555 | 2.276 | 1.725 | 0.766 | 0.144 | 16.073 |
| 27 | 0.000 | 0.072 | 0.361 | 1.005 | 1.981 | 2.402 | 2.619 | 2.573 | 2.287 | 1.715 | 0.768 | 0.140 | 15.926 |
| 28 | 0.000 | 0.073 | 0.370 | 0.873 | 1.854 | 2.488 | 2.578 | 2.494 | 2.095 | 1.605 | 0.730 | 0.173 | 15.332 |
| 29 | 0.000 | 0.069 | 0.382 | 0.986 | 1.952 | 2.446 | 2.677 | 2.603 | 2.277 | 1.727 | 0.794 | 0.215 | 16.134 |
| 30 | 0.000 | 0.077 | 0.380 | 0.895 | 1.914 | 2.391 | 2.624 | 2.591 | 2.264 | 1.744 | 0.795 | 0.159 | 15.836 |
| 31 | 0.000 | 0.072 | 0.377 | 0.947 | 1.908 | 2.359 | 2.581 | 2.508 | 2.267 | 1.753 | 1.003 | 0.203 | 15.981 |
| Average | 0.000 | 0.104 | 0.414 | 1.123 | 2.018 | 2.480 | 2.697 | 2.640 | 2.285 | 1.703 | 0.755 | 0.140 | 16.360 |

## A2. Hourly and daily ambient temperature (celsius) [87]

## January

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 13.3 | 13.2 | 15 | 17.4 | 19.8 | 23.7 | 24.1 | 26.2 | 27.6 | 27.8 | 27.4 | 27.4 | 23.7 |
| 2 | 13.9 | 13.5 | 14.5 | 17.1 | 20.2 | 22.4 | 24.1 | 26.1 | 27.3 | 26.7 | 27.8 | 26.6 | 23.6 |
| 3 | 13.6 | 12.9 | 14.8 | 16.7 | 19.5 | 22.1 | 23.6 | 25.6 | 26.4 | 27.9 | 27.6 | 27.4 | 23.1 |
| 4 | 13.9 | 12.3 | 14.5 | 17 | 19.7 | 21.8 | 24.4 | 26.2 | 27.3 | 28.3 | 28.6 | 28.3 | 24.8 |
| 5 | 14.5 | 13.8 | 15.7 | 18.2 | 21.7 | 25 | 26.9 | 27.5 | 29.1 | 29.5 | 29.3 | 28.8 | 24.7 |
| 6 | 15.8 | 15.4 | 16.3 | 19 | 22.8 | 25.5 | 28.9 | 28.6 | 30.4 | 29 | 31.3 | 29.5 | 25.6 |
| 7 | 15.5 | 14.9 | 16.7 | 18.1 | 21.2 | 25.4 | 26.5 | 27.8 | 27.7 | 27.9 | 28.2 | 27.4 | 25.2 |
| 8 | 17.6 | 17.1 | 17.8 | 19.7 | 21.7 | 24.8 | 25.9 | 26.8 | 26.8 | 28.7 | 28.7 | 27.4 | 24.8 |
| 9 | 14 | 13.5 | 15.7 | 19.2 | 22.3 | 24.7 | 25.8 | 26.8 | 26.9 | 27.8 | 27.5 | 27.2 | 24 |
| 10 | 14.7 | 14.3 | 15.4 | 18.3 | 21.5 | 25.3 | 26.3 | 27.3 | 27.3 | 28.5 | 28.3 | 27.6 | 24.5 |
| 11 | 15 | 14.6 | 15.3 | 18.4 | 22.4 | 23.6 | 26.3 | 27.1 | 29 | 29 | 28.9 | 28.4 | 25.1 |
| 12 | 14.7 | 15 | -16.2 | 19.5 | 22.2 | 24.4 | 26.4 | 27.5 | 28.5 | 29.5 | 29.2 | 28.9 | 24.9 |
| 13 | 14.4 | 14.6 | 15.8 | 19,6 | 21.3 | 24.7 | 26.6 | 28.4 | 28.7 | 29.2 | 29.6 | 29.5 | 25.8 |
| 14 | 15.6 | 15.3 | 16.7 | 19.3 | 21.1 | 24.3 | 26.9 | 28.8 | 29.2 | 30.5 | 30.3 | 30.8 | 26.4 |
| 15 | 15 | 14.6 | 16.8 | 19.2 | 21.7 | 24.5 | 27 | 28.4 | 29.5 | 29.9 | 31.3 | 31 | 26.6 |
| 16 | 14.1 | 13.8 | 16.7 | 21 | 22.4 | 24.5 | 26 | 28.5 | 29.4 | 30.4 | 31.1 | 30.7 | 26.1 |
| 17 | 13.7 | 13.7 | 15 | 18.4 | 21.1 | 23.7 | 25.8 | 28.7 | 29.7 | 30.7 | 31.7 | 30.7 | 26.6 |
| 18 | 13.9 | 13.4 | 16.4 | 19.6 | 21.8 | 24.1 | 26.7 | 29.3 | 30 | 31.4 | 32 | 30.9 | 25.5 |
| 19 | 12.1 | 12.2 | 14 | 17.7 | 20.4 | 25.1 | 25.8 | 27.8 | 29.1 | 30.5 | 31.5 | 30.9 | 26.6 |
| 20 | 13.1 | 12.8 | 14.1 | 18.6 | 21.9 | 25.2 | 27 | 28.8 | 30.5 | 30.1 | 30.8 | 30.9 | 25.6 |
| 21 | 13 | 11.8 | 13.8 | 17.5 | 21.1 | 23.7 | 26.3 | 28.6 | 29.6 | 29.8 | 31 | 30 | 28.5 |
| 22 | 12 | 12 | 14.2 | 16.6 | 19.1 | 23.4 | 26.3 | 27.7 | 29.3 | 29.9 | 30.2 | 31.3 | 25.2 |
| 23 | 12.1 | 12.3 | 13.8 | 17.2 | 20.6 | 24.1 | 26.9 | 27.5 | 29.3 | 29.9 | 30.3 | 29.8 | 26.6 |
| 24 | 17.6 | 17.7 | 18.1 | 20.2 | 22.3 | 26.9 | 27.4 | 29 | 30.6 | 30 | 31 | 30.1 | 29.1 |
| 25 | 20.3 | 20.6 | 21.3 | 23.8 | 24.1 | 26.1 | 27.6 | 28.9 | 30 | 30.2 | 30.2 | 30.6 | 27.8 |
| 26 | 18.7 | 17.9 | 19 | 20.9 | 23.8 | 27 | 28 | 29.1 | 30.6 | 30.5 | 31.4 | 31.2 | 28.5 |
| 27 | 19.3 | 19.6 | 20.4 | 22.4 | 25.2 | 26.9 | 28.1 | 28.9 | 29.7 | 30.5 | 29.7 | 29.3 | 28.3 |
| 28 | 20.5 | 18.5 | 19.7 | 21.6 | 22.5 | 23.9 | 24.5 | 23.7 | 24.6 | 24.1 | 23.8 | 22.7 | 21.6 |
| 29 | 17.6 | 17.2 | 17.9 | 19.5 | 22 | 23.8 | 24.4 | 24 | 25.6 | 25.3 | 26.2 | 25.4 | 24 |
| 30 | 13.8 | 13 | 14.3 | 16.6 | 19.6 | 23.4 | 25.6 | 25.6 | 28 | 28.4 | 28.3 | 27.5 | 24.5 |
| 31 | 13.1 | 13.7 | 14.1 | 16.6 | 19.2 | 22.8 | 24.1 | 25.4 | 27.5 | 27 | 27.3 | 25.8 | 23.6 |

## February

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 12.7 | 12.7 | 13.5 | 16 | 18.8 | 22.5 | 24.9 | 25.5 | 26.4 | 26.9 | 27.1 | 26.6 | 23.9 |
| 2 | 14.9 | 15.3 | 16.1 | 19 | 20.6 | 23.9 | 24.1 | 24.6 | 27.3 | 25.4 | 25.6 | 24.8 | 22.5 |
| 3 | 13.4 | 13.3 | 13.6 | 15.7 | 19 | 22.7 | 23.7 | 23.2 | 24.5 | 25.4 | 25.4 | 24.7 | 22.4 |
| 4 | 12 | 12.9 | 13.1 | 15.1 | 17.7 | 21.4 | 22.8 | 23.8 | 25.7 | 26.5 | 27.2 | 26.8 | 23.2 |
| 5 | 13.4 | 12.6 | 13.8 | 16.7 | 19.1 | 22.4 | 23.9 | 25.8 | 27.7 | 28.4 | 29.1 | 27.6 | 24.5 |
| 6 | 13.5 | 12.4 | 13.5 | 16.9 | 19.6 | 22.8 | 25.1 | 26.2 | 27.9 | 29.1 | 28.8 | 28.7 | 25.4 |
| 7 | 14 | 13.7 | 14.7 | 17.2 | 19.5 | 22.2 | 25.9 | 27.1 | 28 | 29.4 | 29.4 | 28.7 | 25.7 |
| 8 | 14.4 | 14.3 | 14.8 | 18.7 | 19.6 | 23 | 25.6 | 27.7 | 29.2 | 29.8 | 29.5 | 29.4 | 25.6 |
| 9 | 17.1 | 16.1 | 16.6 | 19.4 | 22.4 | 24.7 | 27.3 | 29.6 | 31.3 | 32.7 | 32.8 | 30.4 | 28.2 |
| 10 | 15.1 | 15.5 | 16.7 | 19.5 | 23.1 | 26.8 | 30.8 | 31.6 | 32.4 | 32.3 | 33.2 | 31.3 | 28.9 |
| 11 | 16.2 | 16 | 17.2 | 21.8 | 24.8 | 26.7 | 28.6 | 29.4 | 31.3 | 32 | 32.1 | 31.7 | 29 |
| 12 | 16.2 | 16 | 17.8 | 21 | 23.9 | 26.6 | 28.4 | 30.8 | 32 | 33.1 | 32.8 | 32.7 | 29.4 |
| 13 | 16.8 | 16.9 | 20 | 22.6 | 25.4 | 28.6 | 29.8 | 30.7 | 32.1 | 32.7 | 33.3 | 32.8 | 30.9 |
| 14 | 16.6 | 15.1 | 17.5 | 21.7 | 24.4 | 26.7 | 29.2 | 30.4 | 31.9 | 33.3 | 33.6 | 34 | 30.4 |
| 15 | 18.2 | 17.9 | 20.4 | 25 | 26.4 | 28.7 | 30.1 | 32.5 | 32.6 | 32.3 | 32.1 | 31.2 | 30.8 |
| 16 | 17.9 | 17.2 | 20 | 25.2 | 26.3 | 27.8 | 29 | 30.2 | 31.5 | 30.6 | 30.9 | 32.6 | 30.8 |
| 17 | 18.3 | 18.1 | 20.5 | 24.5 | 27.2 | 28.2 | 31.6 | 32.4 | 32.1 | 31.9 | 32.4 | 31.9 | 27.5 |
| 18 | 17.2 | 16.1 | 18.6 | 21.8 | 25.6 | 29.1 | 30.4 | 29.9 | 32.5 | 32.1 | 32.2 | 31.8 | 30.5 |
| 19 | 16.2 | 16.1 | 18 | 22.9 | 25.6 | 28.9 | 31 | 31.5 | 33 | 32.8 | 33.3 | 32.4 | 30.2 |
| 20 | 14.3 | 14.6 | 17.3 | 19.8 | 23.3 | 26.3 | 29.6 | 31.3 | 32 | 32.8 | 32.9 | 32.8 | 29.7 |
| 21 | 16 | 14.2 | 17.1 | 20,7 | 24.8 | 28.5 | 30.7 | 31.4 | 33.4 | 34.2 | 34.5 | 33.8 | 31.1 |
| 22 | 16.4 | 14.8 | 17.6 | 23.4 | 26.9 | 29.6 | 32.2 | 32.4 | 33 | 33.5 | 33.9 | 33.3 | 29.9 |
| 23 | 15.9 | 15 | 18.4 | 22.1 | 25.1 | 28.1 | 32 | 32.8 | 34.3 | 34.1 | 34.3 | 34.6 | 30.6 |
| 24 | 18.6 | 17.4 | 20.4 | 23.5 | 26.7 | 30.8 | 32.5 | 33.8 | 34.3 | 34.8 | 36.1 | 35.1 | 33.3 |
| 25 | 19.2 | 18.8 | 20.6 | 24.4 | 27.1 | 30.4 | 32.2 | 33.7 | 35.1 | 35.2 | 36.5 | 35.7 | 33.4 |
| 26 | 21.2 | 19.7 | 23.3 | 27.1 | 29.4 | 31.3 | 33 | 34.4 | 35.2 | 34.7 | 36 | 36.3 | 34.1 |
| 27 | 20.8 | 20.1 | 24.8 | 27.9 | 29.3 | 31.1 | 32.3 | 34 | 35.2 | 34.2 | 35.6 | 36 | 33.6 |
| 28 | 20.3 | 18.5 | 21.1 | 24.6 | 28.7 | 31.4 | 33.1 | 33.4 | 33.7 | 33.7 | 33.4 | 33.3 | 30.6 |

## March

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 17.3 | 16.8 | 18.3 | 21.2 | 26.3 | 29.8 | 31.6 | 33.3 | 34.5 | 34.2 | 34.1 | 34 | 29.9 |
| 2 | 16.6 | 15.8 | 18.1 | 21.1 | 26 | 27.9 | 30.5 | 32.5 | 33.9 | 34.7 | 35.6 | 35.1 | 31.5 |
| 3 | 16.2 | 16.1 | 18.3 | 21.3 | 26 | 28.2 | 31.2 | 32.7 | 33.3 | 34.1 | 34.6 | 34 | 30.8 |
| 4 | 16.5 | 17.4 | 17.8 | 20.3 | 24.3 | 28.1 | 30.4 | 33.7 | 33.4 | 33.8 | 33.9 | 33.9 | 30 |
| 5 | 17.1 | 16.8 | 18.1 | 21.4 | 23.9 | 27.2 | 29.3 | 30.8 | 32.6 | 34.2 | 34.8 | 34.1 | 30.5 |
| 6 | 17.9 | 16.8 | 17.4 | 21.1 | 23.5 | 26 | 28.1 | 31 | 32.8 | 33.9 | 34.1 | 33.7 | 30.7 |
| 7 | 17 | 15 | 19 | 23.8 | 25.5 | 28.6 | 30.8 | 32.5 | 34.3 | 35.1 | 35 | 35.2 | 32.1 |
| 8 | 15.8 | 15.5 | 19.1 | 23.3 | 26.5 | 30 | 30.6 | 31.7 | 33.3 | 34.7 | 34.9 | 34.3 | 32.5 |
| 9 | 16.1 | 15.2 | 18.9 | 23.4 | 26.3 | 29.4 | 31.5 | 32.4 | 33.2 | 34.2 | 34.5 | 34.2 | 32.3 |
| 10 | 16.2 | 15.7 | 17.7 | 20.5 | 22.8 | 26.5 | 28.6 | 31.8 | 32.9 | 33.5 | 33.6 | 33.3 | 30.5 |
| 11 | 15.2 | 14.7 | 16.2 | 20.1 | 23.5 | 26.6 | 28.8 | 31.4 | 32.8 | 33.6 | 34.5 | 34.4 | 30.6 |
| 12 | 15.7 | 15.8 | 17.4 | 20.6 | 23.2 | 26.7 | 29.6 | 31.9 | 34 | 35 | 35.3 | 35.1 | 30.1 |
| 13 | 17.9 | 17 | 18.3 | 21.3 | 4.3 | 28.3 | 30.7 | 32.4 | 33.5 | 33.8 | 33.4 | 32 | 30.5 |
| 14 | 17.7 | 17.3 | 19.3 | 22 | 25.1 | 29 | 31.8 | 33.5 | 35.2 | 35.8 | 36 | 35.7 | 31.2 |
| 15 | 19.3 | 19.4 | 20.6 | 25.7 | 28.3 | 31 | 33.3 | 34.8 | 36.7 | 36.9 | 37 | 36.3 | 33.3 |
| 16 | 19.1 | 18.7 | 21.1 | 25.7 | 27.4 | 30.8 | 32.3 | 34 | 34.8 | 35.8 | 36 | 35.8 | 32.9 |
| 17 | 21.8 | 20.8 | 23.6 | 26.2 | 28.4 | 29.8 | 31.5 | 33.3 | 33.8 | 33.8 | 33.4 | 33.2 | 31.8 |
| 18 | 19.4 | 18.7 | 21.5 | 23.6 | 27 | 29.1 | 32 | 34.8 | 35.5 | 36.1 | 35.6 | 34.8 | 31.5 |
| 19 | 19 | 19.5 | 21.1 | 23.4 | 27.1 | 30.5 | 31.8 | 33 | 33.7 | 35.1 | 35.8 | 34.8 | 33.4 |
| 20 | 22.7 | 23.1 | 24.9 | 28.9 | 29.5 | 31.2 | 33.1 | 34.1 | 34.6 | 36.1 | 35 | 34.6 | 33.5 |
| 21 | 20.5 | 20.1 | 22.4 | 25.1 | 26.2 | 28.3 | 29.8 | 30.7 | 32 | 32.4 | 33.5 | 32.5 | 31.6 |
| 22 | 21.5 | 20.7 | 23.8 | 26.3 | 28.8 | 29.5 | 32.1 | 32.4 | 34.1 | 35 | 33.2 | 33.2 | 32.4 |
| 23 | 20.7 | 20.4 | 23.6 | 27.4 | 28.9 | 30.7 | 32.9 | - 33.9 | 35.1 | 35.4 | 35.3 | 34.9 | 34 |
| 24 | 20.4 | 19.8 | 22.3 | 24.5 | 26.9 | 29.7 | 31.7 | 33 | 34.4 | 35.4 | 35.4 | 35.1 | 33.3 |
| 25 | 20 | 20.6 | 23.1 | 26.5 | 27.9 | 29.9 | 32.3 | 33.9 | 36.1 | 37.6 | 36.5 | 36.6 | 34.5 |
| 26 | 21.7 | 22.1 | 25.1 | 27.2 | 29.2 | 31.7 | 33.8 | 34.7 | 36.7 | 36.5 | 37.3 | 36.9 | 35.9 |
| 27 | 22.1 | 21.4 | 24.7 | 28.6 | 30.5 | 32.3 | 35.9 | 36.3 | 37.5 | 38.5 | 38.3 | 37.7 | 36.4 |
| 28 | 21.5 | 22.8 | 24.9 | 27.5 | 29.8 | 32.3 | 34.6 | 36.2 | 37.6 | 37.5 | 38 | 37.2 | 35.7 |
| 29 | 22.9 | 21.5 | 24.4 | 27 | 30.2 | 33.2 | 35.5 | 37.2 | 37.2 | 38.2 | 38.5 | 37.5 | 36.7 |
| 30 | 26.3 | 25.7 | 28 | 30.4 | 31.5 | 33.9 | 36.2 | 35.3 | 37.7 | 32.6 | 31.4 | 34.3 | 33.1 |
| 31 | 22.9 | 23 | 25.9 | 28.2 | 30.4 | 32.2 | 34.4 | 36.3 | 37.7 | 37.8 | 37.6 | 37 | 36.2 |

## April

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 24 | 24.7 | 29.1 | 31.3 | 33.2 | 34.7 | 35.8 | 36.8 | 38.1 | 39.1 | 39.8 | 38.4 | 37 |
| 2 | 23.5 | 23.6 | 27.7 | 30.6 | 31.7 | 34 | 35.9 | 37 | 38.1 | 38.9 | 39 | 37.8 | 35.4 |
| 3 | 21.6 | 21.1 | 23.9 | 28.2 | 30.3 | 32.3 | 34 | 35.5 | 37.7 | 37 | 37.5 | 37.1 | 34.7 |
| 4 | 20.1 | 21.2 | 23.4 | 28.5 | 31.5 | 33.5 | 34.2 | 36 | 36.1 | 36.9 | 36.6 | 36.2 | 34.9 |
| 5 | 23.9 | 23.2 | 26.3 | 30 | 31 | 32.6 | 33.5 | 34.6 | 35.7 | 36.5 | 36.9 | 36.6 | 35 |
| 6 | 23.6 | 23.6 | 26.5 | 28.8 | 31 | 32 | 32.9 | 34 | 34.5 | 35.5 | 35.9 | 35.5 | 34.2 |
| 7 | 24.4 | 24.1 | 26.5 | 28.2 | 30.9 | 31.6 | 33 | 34.6 | 35.4 | 36.3 | 36.6 | 36 | 33.3 |
| 8 | 23.9 | 23.8 | 26.6 | 28.5 | 30.6 | 31.6 | 33.2 | 34.2 | 34.9 | 35.8 | 36.4 | 36.5 | 35.1 |
| 9 | 24.3 | 23.6 | 28 | 29 | 30.4 | 31.9 | 33.6 | 34.5 | 35.6 | 36.3 | 36.6 | 36.3 | 34.9 |
| 10 | 23.4 | 24.9 | 27.6 | 29.7 | 30.3 | 31.7 | 33.4 | 34.7 | 35.4 | 36.1 | 36.3 | 36.5 | 35.2 |
| 11 | 22.2 | 23 | 26.9 | 29.1 | 30.9 | 31.1 | 32.1 | 32.1 | 33.4 | 29.4 | 32.3 | 32.7 | 29.9 |
| 12 | 24.2 | 24.2 | 26.8 | 28.1 | 30 | 30.7 | 32.7 | 32.9 | 31.8 | 34.1 | 35.8 | 30.7 | 27.5 |
| 13 | 23.5 | 23.5 | 26.1 | 28 | 28.8 | 30.8 | 32.1 | 33.7 | 35 | 35 | 31.7 | 33.1 | 31.9 |
| 14 | 24.5 | 24.2 | 25.5 | 28.2 | 30.1 | 30.2 | 30.7 | 32.5 | 32.2 | 31.3 | 31.7 | 30.8 | 28.6 |
| 15 | 24.4 | 24.5 | 25.8 | 28.1 | 29.1 | 32.7 | 33.3 | 34.4 | 34.6 | 34.1 | 33.4 | 29.6 | 27.8 |
| 16 | 23.8 | 24.2 | 26.1 | 27.4 | 29.3 | 31.2 | 31.4 | 33.9 | 33.3 | 33.8 | 33.1 | 33 | 31.5 |
| 17 | 24.7 | 24.9 | 27.1 | 29.8 | 31.8 | 33.1 | 34.4 | 35.2 | 34.3 | 34.5 | 36.3 | 34 | 34.1 |
| 18 | 23.5 | 24.8 | 28.4 | 29.9 | 31.4 | 33.8 | 35.3 | 36.1 | 38.6 | 37.1 | 37.1 | 24.3 | 25.6 |
| 19 | 24.9 | 25.6 | 26.4 | 27.4 | 28 | 30.9 | 31.6 | 32.8 | 33.6 | 34.3 | 34.6 | 35 | 34.3 |
| 20 | 23.3 | 24 | 27.1 | 30.2 | 31.2 | 32.4 | 34.8 | 35.5 | 35.6 | 36.4 | 35.8 | 37.5 | 36.6 |
| 21 | 24.3 | 25 | 28.8 | 31.3 | 33.3 | 34.6 | 35.6 | 37 | 37.4 | 38.3 | 38.4 | 39.5 | 38.6 |
| 22 | 25.7 | 26.6 | 30.8 | 32.4 | 33.1 | 34.4 | 36 | 37.7 | 38.3 | 39.1 | 38.4 | 38.9 | 38.5 |
| 23 | 25.8 | 26.2 | 30.1 | 32.3 | 34.6 | 34.6 | 36.2 | 36.7 | 37.5 | 38.2 | 38.5 | 38.6 | 37.3 |
| 24 | 24.4 | 26.6 | 29.4 | 31.4 | 33.8 | 36.4 | 36.6 | 37.2 | 38.2 | 38.5 | 38.9 | 38.2 | 37.8 |
| 25 | 24.4 | 26.4 | 28.8 | 31.3 | 33.7 | 35.2 | 37.2 | 38 | 40.3 | 39.3 | 38.9 | 38.7 | 37.9 |
| 26 | 23.7 | 22.2 | 22.5 | 23.4 | 26.1 | 26.8 | 30.3 | 32.1 | 33.5 | 34.3 | 32.6 | 31.9 | 31.2 |
| 27 | 21.1 | 21.6 | 24.5 | 26.5 | 29.1 | 30.5 | 30.9 | 33.6 | 33.9 | 35.3 | 35.4 | 33.6 | 33 |
| 28 | 21.6 | 21.5 | 21.6 | 22.9 | 24.8 | 28.2 | 28.7 | 30.6 | 29.7 | 30.3 | 30.1 | 30.7 | 29.9 |
| 29 | 24.8 | 25.5 | 27.3 | 29.4 | 30.7 | 32.5 | 32.4 | 32.9 | 35.9 | 32.7 | 30.6 | 32.4 | 31.5 |
| 30 | 23.2 | 23.9 | 27 | 29.1 | 31 | 32.3 | 33.3 | 34.4 | 36.2 | 32.2 | 31.3 | 32.3 | 32.3 |

## May

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 23.5 | 24.2 | 25.8 | 27.8 | 30.8 | 33.1 | 33 | 34.3 | 34.7 | 36.3 | 35.9 | 36.3 | 35.3 |
| 2 | 25.6 | 26.4 | 27 | 28.1 | 29.5 | 29.8 | 31.1 | 29.9 | 30.8 | 30.9 | 30.4 | 28.8 | 27.9 |
| 3 | 24.2 | 24.3 | 23.9 | 24 | 24.4 | 25.6 | 26.5 | 31.5 | 29.4 | 31 | 26.5 | 24.7 | 24.8 |
| 4 | 23.5 | 23.3 | 23.5 | 24.3 | 24.3 | 25.3 | 24.4 | 24.6 | 24.8 | 24.4 | 24.5 | 24.1 | 24.2 |
| 5 | 22.3 | 22.3 | 22.4 | 22.4 | 22.7 | 23.2 | 24.5 | 24.7 | 26.7 | 26.2 | 23.7 | 24 | 23.7 |
| 6 | 22.6 | 22.3 | 22.5 | 22.3 | 22.8 | 23 | 22.9 | 23.2 | 23 | 23.3 | 24.4 | 25.2 | 24.9 |
| 7 | 23.2 | 23.5 | 24.1 | 24.5 | 24.7 | 26.2 | 26.7 | 25.9 | 26.9 | 28.9 | 29.2 | 28.4 | 27.8 |
| 8 | 22.5 | 22.6 | 22.9 | 23.4 | 25.2 | 25.7 | 27.8 | 29.5 | 28.5 | 30.1 | 29.8 | 30 | 27.4 |
| 9 | 23.7 | 23.8 | 25 | 25.8 | 27.2 | 28.6 | 29.2 | 29.6 | 30.3 | 31.5 | 32 | 31.7 | 31.2 |
| 10 | 24.8 | 24.5 | 25 | 26.1 | 27.9 | 28.3 | 30.5 | 28.8 | 31.7 | 32.1 | 32.2 | 32.2 | 31.5 |
| 11 | 21.4 | 23.5 | 23.1 | 24.3 | 25.5 | 26.5 | 28.4 | 29.5 | 30.7 | 29.3 | 26.7 | 27.7 | 27.2 |
| 12 | 23.5 | 23.6 | 24.8 | 26.3 | 27.9 | 27.9 | 28.7 | 30 | 27.2 | 25.1 | 23.5 | 24.5 | 24.7 |
| 13 | 23.8 | 23.8 | 24.2 | 24.2 | 24 | 24.4 | 26.3 | 27.1 | 26.6 | 26.1 | 26.2 | 27.6 | 27.5 |
| 14 | 23 | 23.1 | 23.6 | 25.6 | 5.4 | 26.8 | 27.7 | 27.8 | 29.9 | 29.2 | 29.2 | 29 | 24.2 |
| 15 | 23.6 | 23.7 | 25.6 | 26.3 | 26.8 | 27.7 | 28.7 | 29.9 | 31.2 | 23.7 | 24.9 | 27.4 | 26.1 |
| 16 | 22.6 | 23 | 25.7 | 27.1 | 27.4 | 28.3 | 29.4 | 30.4 | 31.5 | 31.7 | 32.2 | 31.7 | 31.2 |
| 17 | 23.5 | 23.9 | 24.9 | 26.6 | 28 | 29.2 | 30.6 | 30.4 | 30.2 | 31.3 | 30.6 | 30.9 | 30.8 |
| 18 | 24 | 24.4 | 24.9 | 26.9 | 26.9 | 28.7 | 30 | 31.1 | 31.1 | 29.4 | 30.2 | 29.2 | 29.2 |
| 19 | 24.4 | 24.4 | 25.3 | 27 | 27.6 | 28.9 | 29.1 | 29.5 | 29.8 | 31.2 | 31.6 | 31.7 | 30.4 |
| 20 | 24.1 | 23.1 | 23 | 23.4 | 24.3 | 25.4 | 26.4 | 27.3 | 28.1 | 27.8 | 28.3 | 27.8 | 27.2 |
| 21 | 24 | 24.1 | 26 | 26 | 26.7 | 27.1 | 27.9 | 29.3 | 28.7 | 29.3 | 28.3 | 28.6 | 27.5 |
| 22 | 24.2 | 24.3 | 25.9 | 26.7 | 28.1 | 28.8 | 29.2 | 29.8 | 30.3 | 30.2 | 31.1 | 30.6 | 29.4 |
| 23 | 22.9 | 24 | 25.9 | 26.5 | 28 | 29.9 | 31 | 32.6 | 31.5 | 32.5 | 32.2 | 31.4 | 31.1 |
| 24 | 22.9 | 24.4 | 26.3 | 27.8 | 29.5 | 30.6 | 31.6 | 32.8 | 33.3 | 33.8 | 34.6 | 34.3 | 33.8 |
| 25 | 24.2 | 25.2 | 27.7 | 29.7 | 30.3 | 32.8 | 32.4 | 33.2 | 34.2 | 34.2 | 31.2 | 30.8 | 30.5 |
| 26 | 23.9 | 25.3 | 27.9 | 29.3 | 29.5 | 30.9 | 32.1 | 33.3 | 34 | 33.8 | 28.4 | 28.4 | 28.5 |
| 27 | 24 | 24.8 | 27.4 | 28.3 | 30 | 32.4 | 33.4 | 33.5 | 36 | 34.9 | 35.5 | 34.2 | 31.9 |
| 28 | 24.5 | 26.2 | 29 | 29.7 | 30.9 | 33.6 | 34.2 | 33.7 | 33.3 | 30.9 | 30.8 | 32.8 | 29.6 |
| 29 | 24.2 | 25 | 27.4 | 29 | 30.5 | 30.6 | 32.1 | 33.4 | 33.8 | 34.6 | 30.8 | 29.6 | 27.5 |
| 30 | 23.5 | 23.8 | 24.9 | 26.1 | 26.5 | 28.1 | 30.4 | 30.5 | 32.2 | 32.4 | 33.5 | 29.6 | 28.9 |
| 31 | 24.3 | 24.5 | 25.4 | 25.7 | 27.5 | 29.6 | 30.2 | 31.5 | 32.9 | 33.8 | 32.9 | 27.6 | 22.9 |

June

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 23.7 | 23.7 | 24.3 | 25.3 | 26.2 | 27.2 | 28.2 | 29.2 | 30.2 | 30.9 | 31.4 | 30.7 | 29.5 |
| 2 | 24.4 | 25.3 | 27.5 | 27.5 | 29 | 29.9 | 31.3 | 29.4 | 31.2 | 32.2 | 32.8 | 31.1 | 30.4 |
| 3 | 23.4 | 24.6 | 26.9 | 27.6 | 29.1 | 31.1 | 31.8 | 32.6 | 32 | 31.2 | 30.7 | 29.5 | 28.6 |
| 4 | 24 | 24 | 25.6 | 27.4 | 28.5 | 29.8 | 31.3 | 32.5 | 31 | 31 | 31.4 | 30.1 | 29.5 |
| 5 | 23.6 | 23.5 | 24.4 | 26.9 | 27.1 | 28.3 | 29.8 | 30.8 | 29.4 | 32.4 | 32.6 | 29.1 | 27.3 |
| 6 | 23.9 | 24.3 | 25.6 | 26.8 | 27 | 28.2 | 29.5 | 30.6 | 31.5 | 31.8 | 32.3 | 28.8 | 27.3 |
| 7 | 24.3 | 25.1 | 26.5 | 27.3 | 28.1 | 30.1 | 31.2 | 31.7 | 31.2 | 31.6 | 32.4 | 32.4 | 30.7 |
| 8 | 24.5 | 25.9 | 26.4 | 28.3 | 29.5 | 30.9 | 31.8 | 32.1 | 31.8 | 33.1 | 33.5 | 32.4 | 31 |
| 9 | 24.7 | 25.3 | 26.4 | 27.5 | 29.7 | 31.6 | 32.3 | 31.7 | 32.3 | 32.9 | 33.1 | 33.9 | 32.1 |
| 10 | 25.1 | 26.1 | 28.4 | 29.3 | 30.5 | 32.1 | 32.4 | 32 | 32.7 | 33.4 | 34.3 | 33.4 | 33 |
| 11 | 25 | 26.3 | 28 | 29.2 | 30.4 | 32.1 | 31.5 | 29.8 | 32.2 | 33.1 | 32.4 | 31.3 | 29.2 |
| 12 | 25.2 | 25.4 | 27.5 | 28 | 29.1 | 31 | 29.6 | 29.8 | 31.7 | 31 | 32.6 | 31.2 | 24.7 |
| 13 | 24.3 | 24.5 | 25.7 | 26.9 | 27.6 | 28.1 | 29.9 | 29.5 | 30.2 | 31.1 | 31.5 | 30.6 | 29.6 |
| 14 | 24.7 | 25.1 | 26.2 | 27.7 | 29.8 | 30.3 | 31.6 | 32.2 | 33.3 | 32.2 | 28.3 | 27.9 | 27.4 |
| 15 | 24.6 | 25.3 | 26.7 | 27.7 | 28.8 | 30.1 | 30.9 | 31.9 | 32.6 | 33 | 32.6 | 33.1 | 32 |
| 16 | 26.4 | 25.7 | 26.5 | 27.9 | 29.5 | 30.5 | 31.4 | 32.6 | 29.2 | 26.1 | 28.3 | 30 | 30.3 |
| 17 | 24.7 | 25.2 | 26.9 | 27.8 | 28.2 | 29 | 30.2 | 31.1 | 31.4 | 31.7 | 32.2 | 32.4 | 32.1 |
| 18 | 25.3 | 26.7 | 27.9 | 28.9 | 29.3 | 31.6 | 30.8 | 32.1 | 32.3 | 31.9 | 31.9 | 31 | 30.9 |
| 19 | 24.8 | 24.9 | 25.9 | 27.3 | 28.3 | 28.8 | 30.5 | 31.3 | 31.7 | 32.3 | 30.8 | 29.3 | 29 |
| 20 | 24.6 | 24.4 | 25.5 | 27.8 | 27.7 | 29.1 | 30.3 | 31 | 31.6 | 32.9 | 32.5 | 32.5 | 32.2 |
| 21 | 23.9 | 24.6 | 26 | 27 | 30.6 | 30.4 | 32.3 | 33.2 | 33.5 | 33.5 | 33.9 | 30.5 | 30.2 |
| 22 | 25.3 | 25.9 | 28.8 | 30 | 31.2 | 33.9 | 34.7 | 34.1 | 35.1 | 35.3 | 35.3 | 35.1 | 34.1 |
| 23 | 25.2 | 25.6 | 27.3 | 28.9 | 31.1 | 33.4 | 33.8 | 35 | 35.9 | 36 | 36.7 | 36.7 | 35.6 |
| 24 | 26.2 | 27.1 | 28.1 | 29.6 | 31 | 32.3 | 33.8 | 35.6 | 35.3 | 31.2 | 31.1 | 31.4 | 30.8 |
| 25 | 26.4 | 25.9 | 26.7 | 28.7 | 29.6 | 29.9 | 31.5 | 32.3 | 33.7 | 33.9 | 27.5 | 28.9 | 27.2 |
| 26 | 25.5 | 25.5 | 25.9 | 27 | 27.5 | 28.7 | 30.9 | 31.9 | 33 | 31.8 | 31.3 | 25.3 | 26 |
| 27 | 24.6 | 24.9 | 25.4 | 26.2 | 27.4 | 28.5 | 29.5 | 27.4 | 25 | 25.2 | 26.7 | 25.8 | 25.8 |
| 28 | 24 | 22.5 | 23.2 | 24.5 | 25.8 | 26.5 | 27.7 | 27.8 | 28.8 | 26.6 | 27.5 | 27.5 | 27.6 |
| 29 | 24.2 | 24.9 | 25.6 | 26.6 | 26.7 | 27.8 | 28.3 | 28.6 | 29.1 | 29.8 | 29.3 | 26.8 | 26.9 |
| 30 | 23.9 | 24 | 26.2 | 26.8 | 28 | 29.7 | 31.2 | 32.2 | 32.6 | 32.5 | 31 | 31.4 | 31.3 |

## July

| Dat/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 24.8 | 25.4 | 26.6 | 27.7 | 29.3 | 29.8 | 31.2 | 31.1 | 28.6 | 27.4 | 29.6 | 28.3 | 28.9 |
| 2 | 24.7 | 25.5 | 26.7 | 28.2 | 28.7 | 29.3 | 29.1 | 29.6 | 31.4 | 32 | 32.8 | 32.7 | 31.8 |
| 3 | 24.9 | 26.1 | 27.4 | 28 | 28.5 | 29.4 | 29.7 | 29.7 | 28.8 | 30.8 | 30 | 30.3 | 26 |
| 4 | 24.3 | 25 | 26.2 | 26.8 | 27.9 | 28.7 | 29.9 | 30.3 | 30.6 | 31.5 | 30.9 | 30.9 | 29.7 |
| 5 | 25.4 | 25.3 | 25.7 | 27 | 27.4 | 28.3 | 29.3 | 29.9 | 31.4 | 31.4 | 31.1 | 29.8 | 29.3 |
| 6 | 25.1 | 25.5 | 25.9 | 26.6 | 23.8 | 24.3 | 24.4 | 24.7 | 25 | 25.1 | 24.9 | 24.9 | 25.3 |
| 7 | 24.1 | 24.3 | 26.2 | 26.6 | 26.9 | 28.6 | 29.5 | 30.6 | 31.3 | 32 | 29.1 | 26.9 | 27.4 |
| 8 | 22.9 | 23.4 | 24.7 | 26.2 | 28.8 | 29.9 | 30.7 | 31.7 | 31.9 | 32.2 | 25.7 | 25.5 | 26.2 |
| 9 | 23.2 | 23.9 | 25.6 | 27 | 28.1 | 30.6 | 31.1 | 32.7 | 32.6 | 32.8 | 33 | 32.6 | 32.1 |
| 10 | 24.9 | 25.4 | 26.5 | 27.5 | 28.8 | 29.8 | 30.3 | 30.8 | 32 | 32.6 | 32.9 | 32.6 | 33.7 |
| 11 | 25.1 | 25.3 | 26.4 | 27.8 | 29 | 30.5 | 31 | 31.2 | 31.7 | 32.4 | 31.9 | 30.7 | 30.7 |
| 12 | 25.3 | 25.5 | 26.7 | 27.3 | 27.8 | 29 | 29.6 | 30.4 | 32.3 | 31.5 | 31.3 | 30.9 | 29.9 |
| 13 | 24.9 | 25.7 | 26.5 | 27.7 | 29.2 | 29.2 | 30.9 | 31.7 | 31.6 | 29.3 | 29 | 29.7 | 29.2 |
| 14 | 24.6 | 25.7 | 26.4 | 27.4 | 28.6 | 29.8 | 30.2 | 30.4 | 29.6 | 31.3 | 30.8 | 30.5 | 29.6 |
| 15 | 26.3 | 26.3 | 26.9 | 27.4 | 28.2 | 28.7 | 29.1 | 29.6 | 29.4 | 30.1 | 30.3 | 30.9 | 30 |
| 16 | 25.7 | 25.8 | 27.4 | 27.8 | 28.1 | 28.4 | 28.2 | 30.6 | 31 | 32.4 | 32 | 30.2 | 26.9 |
| 17 | 25.1 | 25.4 | 26.6 | 27.7 | 28.9 | 31.2 | 31.6 | 32.7 | 31.9 | 32.7 | 33.4 | 33.1 | 31 |
| 18 | 25.3 | 25.9 | 26.8 | 28.1 | 30.1 | 30.5 | 31 | 31 | 32.1 | 33.1 | 32.3 | 32.6 | 30.9 |
| 19 | 24.3 | 24.6 | 26.3 | 27.3 | 28.4 | 29.7 | 29.9 | 30 | 32.3 | 27.1 | 30 | 25.9 | 25 |
| 20 | 23.9 | 24.2 | 25.3 | 26.1 | 26.6 | 26.9 | 26.9 | 26.8 | 27 | 26.7 | 26.6 | 25.9 | 25.6 |
| 21 | 23.3 | 23.5 | 23.7 | 24 | 24.3 | 24.5 | 24.6 | 24.1 | 24.2 | 23.6 | 24 | 24.6 | 24.7 |
| 22 | 22.7 | 22.8 | 23.7 | 24.7 | 25.8 | 27.8 | 27.7 | 29 | 29.3 | 29.9 | 29.1 | 29.4 | 28.8 |
| 23 | 23.2 | 23.7 | 24.9 | 27.1 | 28.2 | 29.9 | 31 | 32.1 | 32.3 | 32.1 | 30.3 | 28.8 | 28.1 |
| 24 | 23.2 | 23.2 | 23.5 | 23.6 | 23.9 | 24.9 | 26 | 26.4 | 26.1 | 26 | 25.7 | 24.9 | 24.5 |
| 25 | 21.3 | 21.4 | 21.9 | 22.7 | 24 | 24.9 | 26.3 | 27.5 | 28.7 | 29.3 | 29.8 | 30.2 | 29.7 |
| 26 | 23.3 | 24.3 | 26.2 | 26.7 | 28.5 | 29.4 | 30.3 | 31.4 | 30.8 | 24.6 | 28 | 30.5 | 29.3 |
| 27 | 24.1 | 24 | 25.5 | 26.7 | 27.5 | 28 | 28.4 | 29.2 | 30.2 | 30.4 | 30.6 | 30.3 | 29.5 |
| 28 | 23.2 | 24.6 | 26.4 | 27.9 | 28.8 | 29.9 | 30.9 | 32.9 | 32.3 | 33 | 33.2 | 33.5 | 31.4 |
| 29 | 24 | 24.3 | 24.6 | 25.6 | 26.8 | 29.7 | 30.6 | 32.6 | 32.4 | 32.3 | 29.7 | 29.4 | 27.8 |
| 30 | 24.3 | 24.5 | 25.5 | 25.9 | 27.4 | 30.2 | 30.1 | 33.1 | 31.3 | 32.6 | 33.3 | 32.6 | 31 |
| 31 | 24.3 | 25.4 | 25.7 | 26.9 | 28.1 | 31.7 | 31.6 | 30.1 | 27.5 | 25.5 | 27.2 | 29.9 | 29.8 |

## August

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 24.4 | 24.6 | 25.7 | 28 | 28.5 | 29.5 | 30.5 | 31 | 29.5 | 29.8 | 29.7 | 29.5 | 29.3 |
| 2 | 24.5 | 24.5 | 25 | 24 | 24.4 | 25.4 | 26.7 | 27.6 | 28.9 | 28.8 | 29.7 | 30 | 28.8 |
| 3 | 23.8 | 23.9 | 24.4 | 25.8 | 26.5 | 28.2 | 28.6 | 28.6 | 29.6 | 29 | 29 | 29 | 28.3 |
| 4 | 24.2 | 24.7 | 26.2 | 27.4 | 27.7 | 29.4 | 29.7 | 30.6 | 31.1 | 31.9 | 32.9 | 29.5 | 27.3 |
| 5 | 23.7 | 23.9 | 25.1 | 26.1 | 27.7 | 28.6 | 29.4 | 30.6 | 31.3 | 31.7 | 31.3 | 32.3 | 31.6 |
| 6 | 24.3 | 24.9 | 25.8 | 27.3 | 27.7 | 29.8 | 30.8 | 30.7 | 32.1 | 32.6 | 32.7 | 31.4 | 30.1 |
| 7 | 24 | 24.3 | 26.5 | 27.6 | 29.6 | 31.3 | 32.8 | 32.4 | 31.1 | 32.2 | 31.5 | 31.4 | 31.6 |
| 8 | 24.9 | 25 | 25.5 | 26.7 | 27.6 | 29 | 30.3 | 31.4 | 31.5 | 31.6 | 32 | 26.1 | 24.6 |
| 9 | 24.5 | 24.6 | 24.7 | 26 | 27.2 | 29.3 | 29.5 | 25.6 | 26 | 27.9 | 28.5 | 27.2 | 26.4 |
| 10 | 24.1 | 24.6 | 25.6 | 26.5 | 27.4 | 28.7 | 28.7 | 29.4 | 28 | 27.8 | 27.4 | 27.9 | 27.3 |
| 11 | 24.9 | 25.1 | 25.1 | 26.4 | 26.8 | 26.8 | 27.8 | 28.3 | 29.8 | 29.7 | 30 | 29.1 | 28.4 |
| 12 | 24.2 | 24.7 | 25.1 | 25.6 | 26.5 | 28 | 29 | 28.8 | 30 | 30.3 | 29.3 | 29.2 | 28.6 |
| 13 | 24.6 | 24.8 | 26.2 | 26.9 | 28.4 | 29.5 | 31.1 | 30.9 | 31.8 | 32.5 | 33.1 | 32.8 | 31.8 |
| 14 | 25.2 | 25.3 | 26.3 | 27.8 | 28 | 29.8 | 30.4 | 31.9 | 32.1 | 32.8 | 31.7 | 32.6 | 31.1 |
| 15 | 25.1 | 24.9 | 26 | 26.7 | 28.1 | 28.4 | 29.3 | 30.3 | 31 | 31.9 | 31.6 | 31.6 | 31.2 |
| 16 | 25.6 | 25.4 | 25.7 | 25.3 | 25.6 | 26.3 | 29.7 | 29.1 | 27.1 | 28.7 | 27.8 | 24.8 | 24.4 |
| 17 | 23.6 | 23.7 | 24.6 | 25.2 | 26 | 26.9 | 28 | 29.5 | 30.5 | 31.3 | 31.3 | 31.1 | 29.9 |
| 18 | 23.1 | 23.2 | 25.4 | 26.7 | 27.1 | 28.6 | 29.5 | 29.8 | 30.9 | 31.9 | 32.1 | 32.1 | 32 |
| 19 | 23.4 | 24.1 | 25.7 | 27.5 | 28.5 | 29.8 | 30.1 | 30.8 | 29.8 | 29.4 | 31 | 31.9 | 30.4 |
| 20 | 23.3 | 23.8 | 25.9 | 27.1 | 28.7 | 29.9 | 31.3 | 32.5 | 32.3 | 32.3 | 30.7 | 30.9 | 30.1 |
| 21 | 25.2 | 24.8 | 25.6 | 28 | 28.8 | 29.7 | 31.2 | 32.4 | 33.1 | 31.3 | 25.2 | 28.2 | 27.4 |
| 22 | 24.6 | 24.8 | 25.7 | 26.8 | 27.8 | 30.1 | 30.4 | 31.4 | 30.7 | 31 | 30.7 | 30.8 | 26.5 |
| 23 | 24.1 | 24.3 | 25.1 | 25.9 | 27.2 | 28.5 | 30.2 | 28.6 | 30 | 31.6 | 30.8 | 27.3 | 24.3 |
| 24 | 24 | 24.1 | 24.7 | 25.4 | 25.9 | 26.4 | 26.4 | 27.2 | 28.1 | 28.9 | 28.7 | 28.1 | 26.7 |
| 25 | 23.5 | 23.8 | 24.2 | 25.3 | 25.9 | 26.2 | 26.8 | 27.6 | 28.3 | 29.3 | 28.9 | 26.6 | 25.3 |
| 26 | 23.7 | 23.5 | 24.1 | 26.1 | 26.9 | 29.6 | 29.8 | 30.4 | 31.4 | 32 | 31.9 | 30.2 | 29.7 |
| 27 | 24.1 | 24.5 | 25.6 | 26.7 | 28.1 | 30.5 | 31.8 | 31.3 | 32.5 | 33 | 33.2 | 32.9 | 32.6 |
| 28 | 25.1 | 24.7 | 26 | 27.8 | 29.4 | 30.4 | 31.5 | 31.1 | 30.2 | 28.1 | 27.5 | 27.2 | 27.8 |
| 29 | 24 | 23.9 | 24.9 | 27 | 29.2 | 30.8 | 31.8 | 31 | 32.4 | 31.9 | 28.2 | 28.9 | 30 |
| 30 | 23.7 | 24.2 | 24.5 | 25.6 | 26.1 | 26.9 | 28 | 30 | 30.5 | 31.8 | 27.4 | 24.9 | 25.9 |
| 31 | 23.2 | 23.6 | 24.2 | 25.9 | 26.5 | 28.2 | 29.3 | 30.2 | 30.7 | 30.9 | 30 | 29.3 | 28.1 |

## September

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 24.2 | 24.2 | 24.8 | 26.6 | 27.1 | 28.8 | 29.8 | 30.7 | 31.7 | 32.1 | 31.8 | 31.4 | 28.6 |
| 2 | 25.2 | 25 | 25.8 | 28.4 | 27.9 | 28.6 | 29.8 | 31.2 | 32 | 32.2 | 32 | 32.3 | 31 |
| 3 | 24.1 | 24.4 | 26.1 | 26.9 | 28 | 29 | 29.7 | 30.1 | 31.7 | 31.2 | 31 | 27.1 | 27.3 |
| 4 | 24.9 | 24.8 | 26 | 26.5 | 27.4 | 29 | 29.8 | 31 | 31.5 | 31.6 | 30.6 | 30.8 | 28.9 |
| 5 | 23.7 | 23.6 | 24.4 | 25.5 | 26.8 | 27.5 | 29.2 | 31.6 | 32 | 31.1 | 28.7 | 27.8 | 27.4 |
| 6 | 24.1 | 24.1 | 24.7 | 25.9 | 26.4 | 27.1 | 28.2 | 29.9 | 30.7 | 29.8 | 28.8 | 27.9 | 27.3 |
| 7 | 24.2 | 24.5 | 25 | 26.4 | 26.6 | 27.1 | 28.2 | 30.1 | 29.5 | 30.9 | 30.4 | 30.4 | 29 |
| 8 | 24.4 | 24.6 | 25.6 | 26.8 | 28 | 30.5 | 32.6 | 32.3 | 32.9 | 34 | 28.1 | 28.7 | 27.2 |
| 9 | 24.5 | 24.4 | 27 | 28.6 | 29.3 | 30.4 | 31.1 | 32.2 | 31.7 | 25.1 | 25.8 | 28.4 | 28 |
| 10 | 24.5 | 24.3 | 25.4 | 27 | 28.5 | 30.3 | 30.4 | 30.7 | 31.2 | 31.9 | 31.8 | 31.7 | 31 |
| 11 | 25.2 | 25.2 | 24.6 | 24.9 | 25.8 | 26 | 27.8 | 28.1 | 28 | 28.5 | 29 | 28.2 | 28 |
| 12 | 24.3 | 24.5 | 24.8 | 26.8 | 27.8 | 29.4 | 30.4 | 30.6 | 32.3 | 33 | 32.8 | 32.7 | 26.4 |
| 13 | 24.6 | 24.7 | 25.9 | 27.4 | 8.5 | 30 | 30.9 | 31.8 | 32.6 | 32.3 | 32.1 | 27 | 27.4 |
| 14 | 24.3 | 24.6 | 25.8 | 27.4 | 9.1 | 29.5 | 31 | 31.9 | 31.5 | 32.3 | 29.3 | 27.2 | 27.5 |
| 15 | 24.3 | 24.4 | 24.7 | 25.6 | 26.9 | 28.8 | 29.9 | 30.8 | 30.5 | 30.3 | 32.2 | 30.1 | 28.9 |
| 16 | 24.8 | 25.4 | 25.2 | 28 | 30 | 31.2 | 25.2 | 28.6 | 30 | 30.8 | 31.4 | 31.5 | 30.9 |
| 17 | 24.9 | 24.6 | 26.6 | 27.6 | 28 | 29.7 | 31.8 | 31.4 | 32.7 | 33.5 | 33.5 | 31.9 | 30.8 |
| 18 | 25.2 | 25.5 | 27.4 | 28.2 | 30.4 | 29.5 | 32 | 31.3 | 25.8 | 27.2 | 27.8 | 27.6 | 27.4 |
| 19 | 23.9 | 24.2 | 25 | 26.9 | 28.8 | 30.1 | 30.4 | 31 | 30.2 | 28.7 | 27 | 30.4 | 26.5 |
| 20 | 23.3 | 23.9 | 24.6 | 26.8 | 24.3 | 24.4 | 25.5 | 26.3 | 27.3 | 27.8 | 28.5 | 28.1 | 27 |
| 21 | 22.3 | 22.7 | 23.3 | 24.5 | 25.4 | 26.8 | 28.1 | 28.2 | 29.4 | 29.3 | 29.8 | 29 | 27 |
| 22 | 22.3 | 22.2 | 24.5 | 26.3 | 28.5 | 28.7 | 29.6 | 29.9 | 30.3 | 30.4 | 30.2 | 29.2 | 28.3 |
| 23 | 22.5 | 23.1 | 24.7 | 26.1 | 27.6 | 29.6 | 31.1 | 31.4 | 31.5 | 31.3 | 31.4 | 30.5 | 29.9 |
| 24 | 22.7 | 23.4 | 24.6 | 27.1 | 29.2 | 29.1 | 30.9 | 33.4 | 32.6 | 32.8 | 33.8 | 29.5 | 29 |
| 25 | 22.7 | 23 | 25.2 | 27.3 | 28.3 | 29.3 | 30.7 | 31.3 | 32 | 32.4 | 32 | 31.6 | 30.4 |
| 26 | 22.8 | 23.2 | 22.9 | 24 | 25.6 | 26.9 | 27.5 | 28.1 | 28.7 | 29.7 | 29.9 | 30.4 | 29.1 |
| 27 | 23.8 | 24.3 | 23.9 | 25.1 | 26.4 | 27.3 | 27.9 | 28.7 | 29.8 | 29.9 | 30.9 | 30.3 | 28.8 |
| 28 | 24.3 | 24.3 | 24.4 | 26.2 | 27.8 | 28.9 | 29.6 | 29.4 | 29.9 | 29.8 | 29.8 | 28.7 | 27.9 |
| 29 | 23 | 23.6 | 24.7 | 27.1 | 26.6 | 28.6 | 28.8 | 29.6 | 30.9 | 29.9 | 29.9 | 29.3 | 28.8 |
| 30 | 23.6 | 23.6 | 24.6 | 25.9 | 28.1 | 29.2 | 30.4 | 31 | 30.7 | 31.6 | 30.4 | 31 | 29.3 |

## October

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 22.9 | 23.1 | 24.5 | 26.4 | 27.7 | 29.6 | 30.7 | 30.9 | 30.8 | 31.7 | 32.1 | 30 | 29.2 |
| 2 | 23 | 23.3 | 24.1 | 26.1 | 28.9 | 30.8 | 32.9 | 33.8 | 33.2 | 29.5 | 31.1 | 31.4 | 29.7 |
| 3 | 24.4 | 24.7 | 25.8 | 26.2 | 27.3 | 30.2 | 31 | 31.8 | 33.5 | 34 | 34.1 | 32 | 29.9 |
| 4 | 24.1 | 24.4 | 25.6 | 26.3 | 29.3 | 29.8 | 30.9 | 29.9 | 32.9 | 32.6 | 32.8 | 32 | 31.2 |
| 5 | 24.8 | 24.6 | 24.9 | 25.9 | 27.8 | 30.1 | 30 | 30.9 | 28.8 | 24.8 | 24.3 | 24.3 | 24.2 |
| 6 | 23.9 | 24 | 24.6 | 25.1 | 24.5 | 25.7 | 26.9 | 27.2 | 28 | 28.4 | 25.8 | 26.2 | 24.6 |
| 7 | 23.7 | 23.8 | 24.6 | 24.1 | 24.2 | 25.2 | 25.3 | 24.7 | 25.4 | 24.9 | 25 | 25 | 24.8 |
| 8 | 22.6 | 22.7 | 23.5 | 24.7 | 26.2 | 27.9 | 28.6 | 29.8 | 30.1 | 30.4 | 31.1 | 30.4 | 28.3 |
| 9 | 24.4 | 24.4 | 25 | 25.8 | 27.4 | 29.5 | 30 | 30.9 | 27.2 | 25.6 | 25.9 | 26.2 | 24.7 |
| 10 | 22.7 | 22.8 | 23.4 | 25.7 | 27.4 | 28.8 | 30.3 | 28.6 | 30.2 | 30 | 30.4 | 28.6 | 27.7 |
| 11 | 23.6 | 23.4 | 23.9 | 26.8 | 27.8 | 29.1 | 29.2 | 30.3 | 29.3 | 28 | 29 | 28.2 | 27.4 |
| 12 | 22.7 | 22.8 | 23.7 | 26.9 | 28.2 | 29.1 | 28.3 | 28.9 | 29.6 | 28.1 | 30 | 29.5 | 27 |
| 13 | 23.4 | 23.5 | 23.8 | 25.9 | 26.6 | 27.3 | 26.7 | 24.9 | 24.6 | 25.2 | 25.3 | 25.6 | 25.1 |
| 14 | 22.2 | 22.4 | 22.9 | 24.1 | 8.1 | 28.6 | 29.1 | 29.6 | 28 | 29.3 | 25.9 | 27.6 | 26.1 |
| 15 | 23 | 23.2 | 23.7 | 24.2 | 26 | 26.6 | 27.3 | 27 | 29.8 | 28.6 | 26 | 25 | 24.2 |
| 16 | 22.4 | 22.2 | 23.1 | 25.5 | 26.4 | 27.9 | 28.5 | 28.3 | 28.3 | 28.6 | 28.2 | 27.3 | 26.8 |
| 17 | 23.3 | 23.4 | 24.4 | 25.5 | 27.7 | 28.9 | 28.7 | 28.5 | 28.5 | 28.7 | 28.9 | 27.6 | 26.2 |
| 18 | 22.4 | 22.5 | 24.4 | 26.2 | 27.2 | 28.7 | 29.7 | 30.7 | 30.3 | 30.2 | 31.6 | 30.2 | 28.6 |
| 19 | 22.3 | 22.5 | 24.8 | 26.4 | 28.9 | 29.9 | 30.3 | 31.8 | 32.3 | 31.6 | 31.8 | 30.6 | 28.1 |
| 20 | 21.8 | 21.5 | 23.2 | 25.4 | 26.8 | 28.2 | 29.4 | 29.9 | 29 | 29.2 | 28.3 | 28 | 27 |
| 21 | 20.9 | 21.1 | 22.8 | 24.9 | 27.5 | 28.7 | 29.1 | 28.6 | 29.5 | 29.5 | 29.9 | 29 | 26.6 |
| 22 | 20.9 | 21 | 22.2 | 24.4 | 25.8 | 27.7 | 30.3 | 29.3 | 30.3 | 30.8 | 30.3 | 29.7 | 28 |
| 23 | 20.9 | 21 | 21.5 | 24.8 | 26.9 | 28.4 | 29.8 | 30.7 | 30.7 | 31.6 | 31.4 | 31 | 27.9 |
| 24 | 21.3 | 21.5 | 22.3 | 24.4 | 27.9 | 30.3 | 30.4 | 31.6 | 31.4 | 32 | 32.3 | 31.2 | 28.3 |
| 25 | 21.2 | 21.6 | 22.9 | 26 | 28.1 | 29.2 | 30 | 29.5 | 30.8 | 30.8 | 31 | 30 | 27.4 |
| 26 | 20.5 | 20.2 | 21.4 | 23.8 | 26.2 | 27.7 | 29.9 | 30.6 | 31.1 | 31 | 30.6 | 28.6 | 26.4 |
| 27 | 20.4 | 20.8 | 21.8 | 24.7 | 26.7 | 28.6 | 29.9 | 30.7 | 31.1 | 30.9 | 30.9 | 29.3 | 26.2 |
| 28 | 19.9 | 20.1 | 22.3 | 24.5 | 26.5 | 28.4 | 30.2 | 31 | 31.6 | 31.5 | 31.2 | 30.6 | 27.9 |
| 29 | 21.3 | 21.5 | 24.2 | 25.4 | 28.1 | 29.7 | 30.8 | 31.3 | 31.7 | 31.7 | 32.4 | 31.5 | 30 |
| 30 | 22.4 | 22.4 | 22.7 | 24.3 | 28 | 30.3 | 30.6 | 30.7 | 31.5 | 32 | 32 | 30.8 | 27.9 |
| 31 | 20.3 | 19.7 | 20.3 | 22.1 | 23.6 | 25.8 | 28.4 | 30.4 | 30.2 | 29.9 | 29.4 | 24.6 | 22.9 |

## November

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 21.1 | 21.8 | 22 | 22.7 | 23 | 23.9 | 25.1 | 26 | 26.5 | 27.1 | 26.9 | 25.9 | 25.2 |
| 2 | 22.3 | 22.2 | 23 | 23.8 | 24.7 | 27.1 | 27.5 | 28.8 | 29.8 | 29.2 | 28.6 | 28.2 | 27.1 |
| 3 | 22.5 | 22.3 | 22.2 | 21.6 | 21.8 | 21.8 | 21.7 | 21.4 | 21.1 | 21.2 | 20.8 | 20.4 | 20.9 |
| 4 | 19.8 | 19.5 | 19.7 | 20.4 | 20.5 | 21.3 | 22.7 | 22.8 | 22.7 | 23.4 | 23.2 | 23.1 | 22.3 |
| 5 | 21.6 | 21.8 | 21.8 | 21.9 | 22.5 | 24.6 | 26.2 | 26.5 | 25.9 | 25.2 | 25 | 24.2 | 23.4 |
| 6 | 20.8 | 20.8 | 21.5 | 23.9 | 25.5 | 26.9 | 28 | 28.7 | 28.1 | 27.7 | 27.5 | 27.1 | 25.1 |
| 7 | 19.1 | 19.3 | 19.5 | 22.3 | 26 | 27.8 | 28.5 | 28.3 | 30.2 | 30.7 | 30 | 28.4 | 26.7 |
| 8 | 19.1 | 19.8 | 21 | 22.9 | 26.3 | 28.1 | 28.8 | 29.7 | 30 | 30.1 | 30.2 | 28.8 | 25.3 |
| 9 | 16.2 | 16.2 | 18.7 | 20 | 22.8 | 27.4 | 28.6 | 29.6 | 29.2 | 29.6 | 29.3 | 26.7 | 24.5 |
| 10 | 17.4 | 16.7 | 18.5 | 21.8 | 22.5 | 26.8 | 28.5 | 29.5 | 30.2 | 30 | 29.9 | 28.3 | 24.3 |
| 11 | 18.3 | 20.6 | 20 | 22.9 | 23.3 | 26.8 | 26.9 | 28.9 | 30 | 29.9 | 30.6 | 29.1 | 26.3 |
| 12 | 20.4 | 20.5 | 22.8 | 24.3 | 26 | 28.3 | 29.5 | 30.5 | 30 | 29.7 | 30.3 | 28.7 | 27.7 |
| 13 | 21.2 | 21.4 | 22.8 | 23.7 | 5.1 | 27.2 | 28.5 | 28.9 | 30.4 | 30.4 | 30.2 | 28.3 | 26.2 |
| 14 | 22.4 | 22.6 | 23.1 | 24.1 | 25.7 | 27.9 | 27.5 | 28.3 | 28.3 | 28.5 | 25.5 | 25.7 | 25 |
| 15 | 22.6 | 22.9 | 23.6 | 24.9 | 26.9 | 26.4 | 26.4 | 26.8 | 27.5 | 28.4 | 28.5 | 27.4 | 25.8 |
| 16 | 20.8 | 22.7 | 21.9 | 23.7 | 25.2 | 27.9 | 30.6 | 29.2 | 29.9 | 31 | 30.4 | 30.1 | 27 |
| 17 | 20.5 | 20.3 | 21.4 | 24.5 | 26.2 | 27.9 | 29.1 | 31 | 31.8 | 31.8 | 31.9 | 30.4 | 27 |
| 18 | 19.1 | 19.1 | 19.6 | 22.4 | 24.8 | 28.1 | 29.7 | 31.1 | 31.7 | 32 | 31.6 | 30.6 | 28.2 |
| 19 | 23.5 | 23.2 | 23.8 | 24.6 | 28.2 | 29.1 | 30.6 | 29.2 | 29.8 | 29.3 | 28.8 | 27.3 | 26.2 |
| 20 | 23.1 | 23.1 | 23.8 | 26.3 | 27.2 | 28 | 29.8 | 29.9 | 29.9 | 27.1 | 25.7 | 26 | 24.3 |
| 21 | 21.4 | 21.5 | 22 | 22.4 | 22.9 | 24.1 | 24.6 | 25.9 | 27 | 26.2 | 24.7 | 21.8 | 20.9 |
| 22 | 20.3 | 20 | 21 | 22.4 | 23.4 | 24.2 | 27 | 26.9 | 28.4 | 28.2 | 28.8 | 27.1 | 24.8 |
| 23 | 19.7 | 19.3 | 19.5 | 21.4 | 25.1 | 26.1 | 26.7 | 26.6 | 26.8 | 26.7 | 27.9 | 25.4 | 24.8 |
| 24 | 18.6 | 18.9 | 19.4 | 20.2 | 24.5 | 25.7 | 26.4 | 27.4 | 26.9 | 25.9 | 25.6 | 24.9 | 24.1 |
| 25 | 17.1 | 16.5 | 18.1 | 19.5 | 23.1 | 25.4 | 26.7 | 27.5 | 27.9 | 28.1 | 27.9 | 26.2 | 23.2 |
| 26 | 15.7 | 15.5 | 16.3 | 18.4 | 20.3 | 23 | 26.2 | 27.9 | 28.4 | 28.4 | 28.3 | 26.5 | 24.1 |
| 27 | 15.6 | 15.5 | 16.4 | 18.2 | 20.6 | 24.3 | 26.6 | 27.5 | 27.5 | 27.9 | 27.7 | 26 | 22 |
| 28 | 15.2 | 14.7 | 15.6 | 17.5 | 20.2 | 22.6 | 24 | 24.5 | 26.5 | 25.9 | 26.1 | 25.2 | 21.3 |
| 29 | 14.5 | 14.4 | 15.8 | 18.3 | 19.3 | 21.9 | 23.2 | 24.8 | 25.7 | 26.6 | 25.9 | 25.1 | 21.9 |
| 30 | 14.7 | 14.2 | 15.5 | 17.4 | 20.6 | 23.5 | 23.5 | 23.3 | 23.8 | 24.4 | 24.7 | 23.6 | 20.2 |

## December

| Date/Time | 6.00 | 7.00 | 8.00 | 09.00 | 10.00 | 11.00 | 12.00 | 13.00 | 14.00 | 15.00 | 16.00 | 17.00 | 18.00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 13.1 | 12.9 | 13.8 | 16 | 18 | 21.7 | 22.6 | 24 | 24.5 | 24.7 | 25 | 24.3 | 20.2 |
| 2 | 12.6 | 12.6 | 14 | 15.6 | 18.3 | 21.4 | 22.5 | 24.2 | 26.2 | 27.1 | 26 | 25.4 | 21.7 |
| 3 | 14.3 | 14.5 | 15.4 | 17.3 | 20.4 | 22.4 | 24.3 | 26.6 | 26.8 | 27.6 | 27.1 | 26.4 | 24.5 |
| 4 | 15.7 | 15.6 | 16.4 | 18 | 21.2 | 23.5 | 25.6 | 26.1 | 26.6 | 27.1 | 26 | 25.4 | 23.1 |
| 5 | 17 | 17.3 | 17.7 | 19.3 | 21.3 | 24.8 | 27 | 27.7 | 27.4 | 28.6 | 28.2 | 26 | 23.3 |
| 6 | 16 | 15.6 | 16.8 | 18.7 | 21.5 | 25.1 | 26.9 | 28.1 | 28.6 | 29.3 | 28.8 | 27.4 | 23.9 |
| 7 | 16.1 | 16.5 | 17.8 | 19.7 | 22 | 24.7 | 26.7 | 27.7 | 28.8 | 28.7 | 28.6 | 28.4 | 24.4 |
| 8 | 17.3 | 17.1 | 18.5 | 20.4 | 22 | 24.4 | 26.5 | 27.9 | 28.5 | 29.4 | 28.9 | 28.1 | 24.3 |
| 9 | 17.1 | 17.7 | 19 | 21.4 | 22.2 | 24.5 | 26.5 | 27.8 | 28.8 | 29 | 29.2 | 28.3 | 24.5 |
| 10 | 17.8 | 17.4 | 18.2 | 20.1 | 22.7 | 25.1 | 27 | 28.1 | 28.3 | 28.8 | 29.2 | 28.7 | 24 |
| 11 | 16.9 | 16.4 | 18.4 | 21.1 | 23.8 | 26.2 | 29.8 | 29.4 | 30.1 | 30.3 | 30 | 29.3 | 24.8 |
| 12 | 16.3 | 16.4 | 19.1 | 20.2 | 20.8 | 22.5 | 26.2 | 28.6 | 28.5 | 28.9 | 28.3 | 26.2 | 22.3 |
| 13 | 14.9 | 15.2 | 16.5 | 19.7 | 22.7 | 24.8 | 26 | 26.8 | 28.7 | 29.2 | 29.6 | 29.1 | 23.8 |
| 14 | 14.4 | 14 | 16.4 | 19.8 | 21.3 | 24.6 | 26.8 | 27.8 | 29.1 | 30.3 | 30.6 | 28.6 | 23.3 |
| 15 | 14.7 | 14.4 | 16.5 | 18.7 | 22.2 | 24.6 | 26.7 | 27.7 | 28.9 | 29.5 | 29.6 | 28.8 | 24.5 |
| 16 | 17.2 | 17.3 | 18.9 | 19.9 | 21.9 | 25.6 | 27.4 | 27.6 | 28.8 | 29.4 | 29.6 | 29.1 | 26.1 |
| 17 | 19.6 | 19.3 | 20.7 | 24 | 25.7 | 27.4 | 28.6 | 30.1 | 30.3 | 30.6 | 31.1 | 30.6 | 26.9 |
| 18 | 19.9 | 19.4 | 21.2 | 24.2 | 24.7 | 26.8 | 29 | 30.2 | 30.8 | 31.1 | 31.6 | 31.2 | 27.5 |
| 19 | 20.1 | 20.1 | 20.7 | 22.2 | 24.6 | 27.3 | 29.2 | 30 | 31 | 31.5 | 31.8 | 31.1 | 27.7 |
| 20 | 20.5 | 20.1 | 21.4 | 24.1 | 25.4 | 27.7 | 29.2 | 30.1 | 31.3 | 31.7 | 31.9 | 31.4 | 28.6 |
| 21 | 20.1 | 19.7 | 21.6 | 23.8 | 25.4 | 27.1 | 29.7 | 30.4 | 31.5 | 31.8 | 32.5 | 32.5 | 28.3 |
| 22 | 18.2 | 17.6 | 20.3 | 22.9 | 24.6 | 26.1 | 28.5 | 29 | 30.8 | 31.7 | 32.2 | 31.6 | 26.4 |
| 23 | 16.4 | 15.5 | 17.2 | 19.8 | 24 | 25.4 | 27.4 | 28.3 | 28.9 | 28.6 | 29.4 | 28.3 | 23.9 |
| 24 | 14.2 | 13.9 | 16 | 17.8 | 20 | 22.5 | 24.6 | 26.2 | 27.7 | 28.7 | 28.8 | 28.7 | 23.3 |
| 25 | 14.3 | 13.8 | 15.7 | 17.3 | 19.8 | 22.8 | 24.5 | 25.8 | 27.5 | 28.6 | 28.9 | 28.6 | 24.5 |
| 26 | 15.4 | 15.3 | 15.8 | 18.5 | 21 | 24.6 | 27.2 | 27.9 | 28.9 | 28.8 | 29.1 | 28.5 | 24.9 |
| 27 | 17 | 16.8 | 17.3 | 19.9 | 22.1 | 26.3 | 27.9 | 28.2 | 28.5 | 29.2 | 29.3 | 28.8 | 25.5 |
| 28 | 16 | 15.8 | 16 | 18.1 | 20.3 | 23.4 | 26.6 | 26.8 | 28 | 28.4 | 28.5 | 27.4 | 24.3 |
| 29 | 16 | 15.9 | 16.8 | 18.9 | 21.8 | 24.3 | 26.4 | 28.4 | 28.6 | 29 | 29.2 | 28.9 | 25.7 |
| 30 | 16.3 | 16.2 | 16.7 | 19.4 | 22.8 | 25.2 | 26.6 | 28.2 | 28.7 | 28.8 | 29.3 | 28.7 | 25.7 |
| 31 | 17.2 | 17 | 18.1 | 20.1 | 22.3 | 25.3 | 26.2 | 27.4 | 28 | 28.9 | 29.6 | 28.8 | 25.6 |

## Appendix B

Specification Sheets of Sharp 80 Wp NE-80E2E Photovoltaic Module


NE-80E2E - multr-purpose module


| Encapsulated Solar Cell Efficiency (nd) | 140\% |
| :---: | :---: |
| Module Efficiency ( $n \mathrm{~m}$ ) | 1260\% |
| Maximum System Voltage | DC540V |
| Series Fuse Rating | 109 |
| Type of Output Terminal | Leadwirewith oonnector |
| Specifications are subject to change without notice ${ }^{1}$ (STQ Standard Test Conditions: $25^{\circ} \mathrm{C}$, $\mathrm{Kv} / \mathrm{m}^{2}$, AMM 1.5 |  |


| AB 5 OLUTE MAXI MUMI RATINGS |  |  |
| :--- | :---: | :---: |
| Parameters | Rating | Unit |
| OperatingTemperature | -40 to +90 | ${ }^{\circ} \mathrm{C}$ |
| StorgeTemperature | -40 to +90 | ${ }^{\circ} \mathrm{C}$ |
| Dielectric Voltage Withstood | $2200 v D C$ max. | V-DC |



In the absence of confirmation by device specifications sheets, Sharp takes no responsibility for any defects that may occur in equipment using any Sharp devices shown in catalogues, data books, etc. Contact Sharp in order to obtain the latest device specification sheets before using any Sharp device.

## Appendix C

Radial Distribution Test System Parameters

## C1. Data for 51-Bus Base Case Radial Distribution Test System

| Branch$i-j$ | Line impedance (ohm) |  | Load demand at bus-j |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{R}$ | $\boldsymbol{X}$ | $P_{L}(k W)$ | $Q_{L}(k V a r)$ |
| 1-2 | 0.4214 | 0.7334 | 0 | 0 |
| 2-3 | 0.4214 | 0.7334 | 14.58 | 8.07 |
| 3-4 | 0.2107 | 0.3667 | 0 | 0 |
| 4-5 | 0.4214 | 0.7334 | 0 | 0 |
| 5-6 | 0.2107 | 0.3667 | 0 | 0 |
| 6-7 | 0.2107 | 0.3667 | 14.58 | 8.07 |
| 7-8 | 0.4214 | 0.7334 | 0 | 0 |
| 8-9 | 0.4214 | 0.7334 | 0 | 0 |
| 9-10 | 0.3996 | 0.67215 | 58.33 | 32.27 |
| 10-11 | -0.5328 | 0.8962 | 0 | 0 |
| 11-12 | 0.2664 | 0.4481 | 0 | 0 |
| 12-13 | 0.7992 | 1.3443 | 20 | 15 |
| 13-14 | 0.5328 | 0.8962 | 0 | 0 |
| 14-15 | 1.66675 | 1.102 | 0 | 0 |
| 15-16 | 2.0001 | 1.3224 | 0 | 0 |
| 16-17 | 0.6667 | 0.4408 | 29.17 | 16.14 |
| 17-18 | 1.3334 | 0.8816 | 72.92 | 40.34 |
| 18-19 | 0.6667 | 0.4408 | 20 | 15 |
| 3-20 | 5.3336 | 3.5264 | 145.67 | 80.69 |
| 4-21 | 1.3334 | 0.8816 | 62.88 | 33.33 |
| 5-22 | 3.3335 | 2.204 | 14.58 | 8.07 |
| 22-23 | 2.6668 | 1.7632 | 94.79 | 52.45 |
| 23-24 | 0.6667 | 0.4408 | 14.58 | 8.07 |
| 24-25 | 6.667 | 4.408 | 0 | 0 |
| 25-26 | 1.3334 | 0.8816 | 14.58 | 8.07 |
| 26-27 | 2.0001 | 1.3224 | 35 | 19.36 |
| 23-28 | 5.3336 | 3.5264 | 29.17 | 16.14 |
| 24-29 | - 1.3334 | 0.8816 | 29.17 | 16.14 |
| 7-30 | 5.00025 | 3.306 | 91.88 | 50.83 |
| 30-31 | 0.6667 | 0.4408 | 85.9 | 36.83 |
| 31-32 | 1.3334 | 0.8816 | 29.17 | 16.14 |
| 32-33 | -1.3334 | 0.8816 | 14.58 | 8.07 |
| 33-34 | 1.00005 | 0.6612 | 43.75 | 24.21 |
| 34-35 | 1.3334 | 0.8816 | 43.75 | 24.21 |
| 35-36 | 2.33345 | 1.5428 | 0 | 0 |
| 36-37 | 1.3334 | 0.8816 | 145.83 | 80.69 |
| 37-38 | 1.00005 | 0.6612 | 91.88 | 50.83 |
| 30-39 | 2.0001 | 1.3224 | 29.17 | 16.14 |
| 35-40 | 1.3334 | 0.8816 | 58.33 | 32.27 |
| 8-41 | 1.00005 | 0.6612 | 14.58 | 8.07 |
| 9-42 | 1.3334 | 0.8816 | 29.17 | 16.14 |
| 10-43 | 4.0002 | 2.6448 | 29.17 | 16.14 |
| 11-44 | 1.3334 | 0.8816 | 29.17 | 16.14 |
| 12-45 | 4.6669 | 3.0856 | 148.75 | 82.3 |
| 14-46 | 0.6667 | 0.4408 | 29.17 | 16.14 |
| 46-47 | 2.0001 | 1.3224 | 0 | 0 |
| 47-48 | 2.0001 | 1.3224 | 29.17 | 16.14 |
| 46-49 | 0.13334 | 0.08816 | 58.33 | 32.27 |
| 15-50 | 4.6669 | 3.0856 | 43.75 | 24.21 |
| 17-51 | 2.6668 | 1.7632 | 116.67 | 64.55 |

Note. 900 kVar shunt capacitor bank installed at bus-13

## C2. Data for 33-Bus Base Case Radial Distribution Test System



## Appendix D

## Deterministic Load Flow Solutions of Test Systems

D1. Load Flow Results for 51-Bus Base Case System

| Bus no. | $\|V\|(p u)$ | $\delta(\mathrm{deg})$ |
| :---: | :---: | :---: |
| 1 | 1.00000 | 0.00000 |
| 2 | 0.99800 | -0.15996 |
| 3 | 0.99603 | -0.31970 |
| 4 | 0.99510 | -0.39788 |
| 5 | 0.99328 | -0.55380 |
| 6 | $\square 0.99263$ | -0.62263 |
| 7 | $0.99201 \square$ | -0.69112 |
| 8 | - 0.99171 | -0.79377 |
| 9 | 0.99146 | -0.89472 |
| 10 | 0.99135 | -0.98312 |
| 11 | 0.99128 | -1.09890 |
| 12 | 0.99140 | -1.15139 |
| 13 | 0.99194 | -1.30381 |
| 14 | 0.99062 | -1.34773 |
| 15 | 0.98834 | -1.35728 |
| 16 | 0.98627 | -1.36573 |
| 17 | 0.98563 | -1.36830 |
| 18 | 0.98499 | -1.37055 |
| 19 | 0.98471 | -1.37182 |
| 20 | 0.99509 | -0.32495 |
| 21 | 0.99505 | -0.39813 |
| 22 | 0.99033 | -0.56718 |
| 23 | 0.98870 | -0.57464 |
| 24 | 0.98838 | -0.57613 |
| 25 | C 0.98687 | -0.58300 |
| 26 | 0.98663 | -0.58413 |
| 27 | 0.98646 | -0.58489 |
| 28 | 0.98826 | -0.57668 |
| 29 | 0.98803 | -0.57773 |
| 30 | 0.98405 | -0.73403 |
| 31 | 0.98326 | -0.73766 |
| 32 | 0.98178 | -0.74443 |
| (33 |  | -0.75095 |
| - 34 | 0.97942 | -0.75528 |
| 35 | 0.97834 | -0.76028 |
| $1-36$ | W -0.97654 | -0.76861 |
| - 37 | - 0.97607 | -0.77077 |
| 38 | 0.97599 | -0.77116 |
| 39 | 0.98372 | -0.73557 |
| 40 | 0.97828 | -0.76054 |
| 41 | 0.99162 | -0.79415 |
| 42 | 0.99135 | -0.89522 |
| 43 | 0.99102 | -0.98464 |
| 44 | 0.99071 | -1.10148 |
| 45 | 0.99101 | -1.15316 |
| 46 | 0.99037 | -1.34887 |
| 47 | 0.98987 | -1.35115 |
| 48 | 0.98954 | -1.35267 |
| 49 | 0.99035 | -1.34895 |
| 50 | 0.98678 | -1.36441 |
| 51 | 0.98493 | -1.37153 |

Note. $P_{\text {loss }}=29.83 \mathrm{~kW}$ and $Q_{\text {loss }}=39.93 \mathrm{kVar}$

## D2. Load Flow Results for 33-Bus Base Case System



Note. $P_{\text {loss }}=369.76 \mathrm{~kW}$ and $Q_{\text {loss }}=246.41 \mathrm{kVar}$

## BIOGRAPHY

Vichakorn Hengsritawat received the B.E. degree in electrical engineering from University of the Thai Chamber of Commerce, Bangkok, Thailand, in 1995. And he received the M.E. degree in electrical engineering from Chulalongkorn University, Bangkok, Thailand, in 1998. He has joined with the Sripatum University in 1998 as the instructor in the department of electrical engineering to pr esent. His research interests i nclude di stributed ge neration, pow er qua lity, renewable energy, e nergy saving and power system simulation.


