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Table 1 The Most Economical Depth of Pile Caps (10)

Pile size (mm.)	300	350	400	450	500	550	600	750
Depth of cap (mm.)	700	800	900	1000	1100	1200	1400	1800

Table 2 Mechanical Properties of Steel

Specimen	Diameter (cm.)	Tensile Stress		Modulus of Elasticity E_s (10^6 ksc.)
		f_y (ksc.)	f_u (ksc.)	
Ø9, plain bar	0.90	3,254	5,187	1.972
		3,458	5,580	1.976
		3,301	5,124	1.953
		3,521	5,612	2.108
		3,482	5,406	2.048
Average		3,403	5,382	2.011

Table 3 Mechanical Properties of Concrete

Specimen	Concrete Strength f'_c , (ksc.)	Average f'_c , (ksc.)	Modulus of Rupture of Concrete f_r , (ksc.)	Modulus of Elasticity E_c , (10^6 ksc.)
P3-1	260	258	31.93	0.230
	270			
	244			
P3-2	280	271	32.73	0.239
	262			
	272			
P3-3	207	228	30.02	0.221
	230			
	248			
P3-4	283	255	31.75	0.229
	254			
	227			
P4-1	220	226	29.89	0.213
	222			
	235			
P4-2	223	210	28.81	0.208
	181			
	229			
P4-3	232	232	30.28	0.220
	236			
	228			
P4-4	248	241	30.86	0.223
	226			
	250			

Note; $f_r = 1.99/\sqrt{f'_c}$

Table 4 Properties of Test Specimens and Test Results

Specimen	Effective Depth, d (cm.)	Steel Content	Concrete Strength f'_c , (ksc.)	Cracking Load, P_{cr} (ton)	Ultimate Load, P_u (ton)
P3-1	25	9- ϕ 9mm.	258	40.0	76.8
P3-2	25	9- ϕ 9mm.	271	46.0	76.6
P3-3	25	9- ϕ 9mm.	228	40.0	69.2
P3-4	25	9- ϕ 9mm.	255	45.0	86.5
P4-1	25	12- ϕ 9mm.	226	38.0	82.1
P4-2	25	12- ϕ 9mm.	210	35.0	80.0
P4-3	25	12- ϕ 9mm.	232	37.0	89.1
P4-4	25	12- ϕ 9mm.	241	44.0	83.1

- Notes :
1. The reinforcement arrangements of test specimens are shown in Fig. 3.11-3.12 .
 2. All cracking loads observed from load-strain curves of the reinforcement.
 3. Column size, $c = 15$ cm.

**Table 5 Comparison of Experimental and Theoretical
Cracking Loads**

Specimen	Observed Cracking Load, P_{cr}	Beam Analogy, P'_{cr}	$\frac{P_{cr}}{P'_{cr}}$	Truss Analogy, P''_{cr}	$\frac{P_{cr}}{P''_{cr}}$
P3-1	40.0	47.6	0.84		
P3-2	46.0	48.8	0.94	34.2	1.35
P3-3	40.0	44.8	0.89		
P3-4	45.0	47.4	0.95	19.1	2.36
P4-1	38.0	45.2	0.84		
P4-2	35.0	43.5	0.80	25.2	1.39
P4-3	37.0	45.8	0.81	21.0	1.76
P4-4	44.0	46.6	0.94	27.4	1.61

- Note; 1. All load values are in tons.
2. Sample of calculations are shown in Appendix B.

Table 6 Comparison of Experimental and Theoretical
Ultimate Loads

Specimen	Observed Ultimate Load, P_u	Beam Analogy, P'_u	$\frac{P_u}{P'_u}$	Truss Analogy, P''_u	$\frac{P_u}{P''_u}$
P3-1	76.8	33.6	2.29		
P3-2	76.6			45.9	1.67
P3-3	69.2	54.8	1.26		
P3-4	86.5			26.5	3.26
P4-1	82.1	55.6	1.48		
P4-2	80.0			39.5	2.03
P4-3	89.1			55.9	1.59
P4-4	83.1			44.9	1.85

- Note; 1. All load values are in tons.
2. Sample of calculations are shown in Appendix B.

Table 7 Comparison of Experimental Ultimate Loads and
Calculated Design Loads (Working Stress Design)

Specimen	Observed Ultimate Load, P_u	Calculated Design Load, P_d	$F.S. = \frac{P_u}{P_d}$	$\frac{(F.S.)_{cap}}{(F.S.)_{pile}}$
P3-1	76.8	16.79	4.57	1.52
P3-2	76.6	22.97	3.33	1.11
P3-3	69.2	27.97	2.47	0.82
P3-4	86.5	13.26	6.52	2.17
P4-1	82.1	28.42	2.89	0.96
P4-2	80.0	19.75	4.05	1.35
P4-3	89.1	27.93	3.19	1.06
P4-4	83.1	22.47	3.70	1.23

Notes; 1. All load values are in tons.

2. $(F.S.)_{pile} = 3.0$

Table 8 Comparison of Factor of Safety in Each Specimen

Specimen	$F_1 = \frac{P_u}{P_{cr}}$	$F_2 = \frac{P_{cr}}{P_d}$	$F_3 = \frac{P_u}{P_d}$	$\frac{(F_1)}{(F_1)^*}$	$\frac{(F_2)}{(F_2)^*}$	$\frac{(F_3)}{(F_3)^*}$
P3-1*	1.92	2.38	4.57	1.00	1.00	1.00
P3-2	1.67	2.00	3.33	0.87	0.84	0.73
P3-3	1.73	1.43	2.47	0.90	0.60	0.54
P3-4	1.92	3.39	6.52	1.00	1.42	1.43
P4-1*	2.16	1.34	2.89	1.00	1.00	1.00
P4-2	2.29	1.77	4.05	1.06	1.32	1.40
P4-3	2.41	1.32	3.19	1.12	0.99	1.10
P4-4	1.89	1.96	3.70	0.88	1.46	1.28

Note; * corresponding to the conventional type of reinforcement

**Table 9 Comparison of Calculated Ultimate Loads Capacity
Due to Shear and Flexure and Experimental Ultimate
Loads at First Yield of Reinforcement**

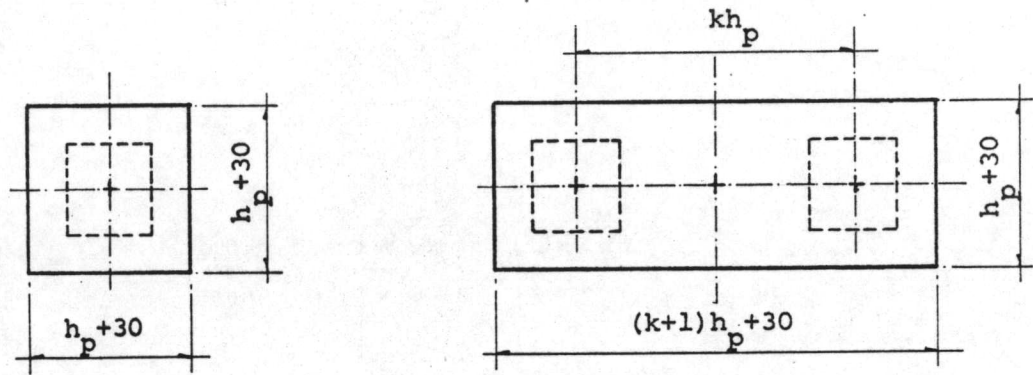
Specimen	Observed Ultimate Load, P_u	Yield Load of Steel, P_y	Cal. Ultimate Load	
			Shear, P_{vu}	Flexure, P'_u
P3-1	76.8	*	85.7	33.6
P3-2	76.6	60.5	88.3	45.9
P3-3	69.2	63.0	80.6	54.8
P3-4	86.5	*	80.2	26.5
P4-1	82.1	66.2	68.6	55.6
P4-2	80.0	53.8	66.2	39.5
P4-3	89.1	65.5	73.8	55.9
P4-4	83.1	71.5	72.3	44.9

- Note;
1. All load values are in tons.
 2. P_y observed from load-strain curves of the reinforcement.
 3. P_{vu} , see Appendix B.

Table 10 Prediction for Strength of Full-Scale Caps from
Model Test Results

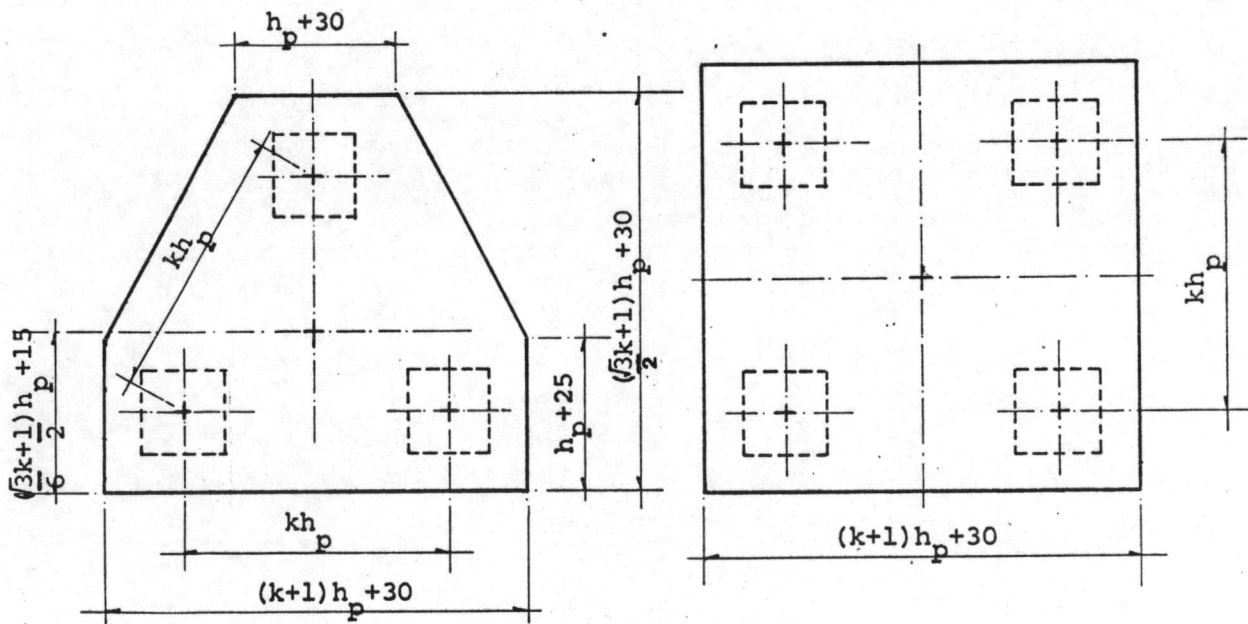
Specimen	Cracking Load (ton)	Ultimate Load (ton)
P3-1	360	691.2
P3-2	414	689.4
P3-3	360	622.8
P3-4	405	778.5
P4-1	342	738.9
P4-2	315	720.0
P4-3	333	801.9
P4-4	396	747.9

Note ; The prediction for strength of full-scale caps from model tests are obtained by multiplying the force scale factor, 9.0, to the model test results.



(a) Single-Pile Cap

(b) Two-Pile Cap



(c) Three-Pile Cap

(d) Four-Pile Cap

Fig. 3.1 Standard Pile Caps

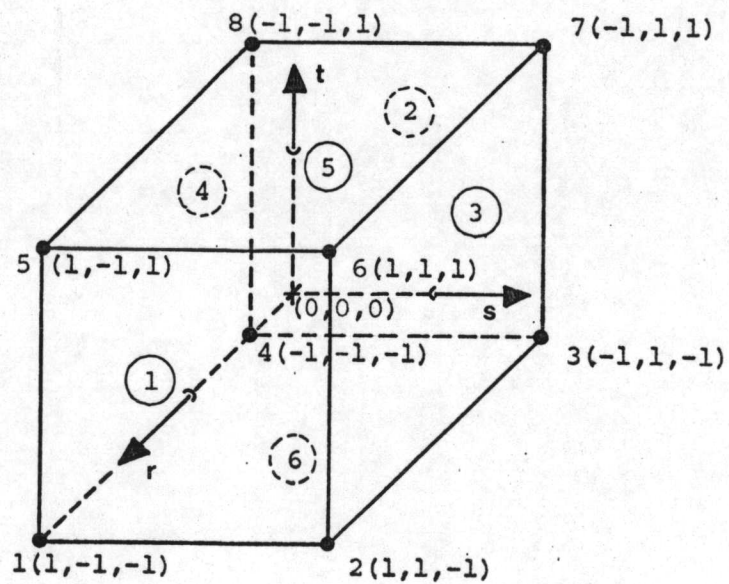
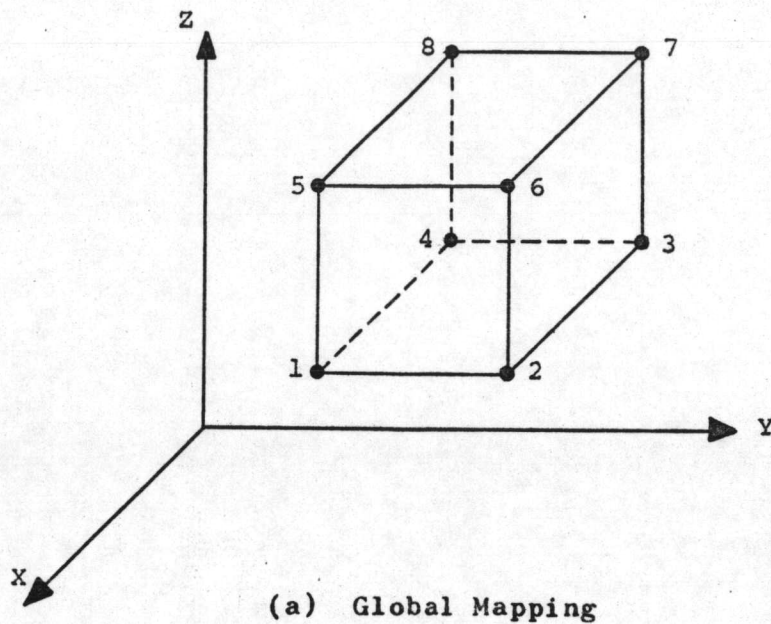
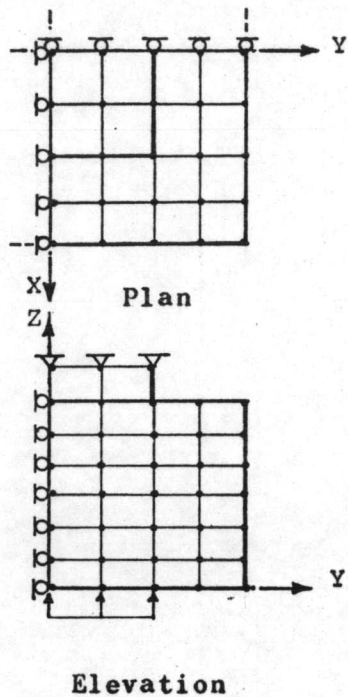
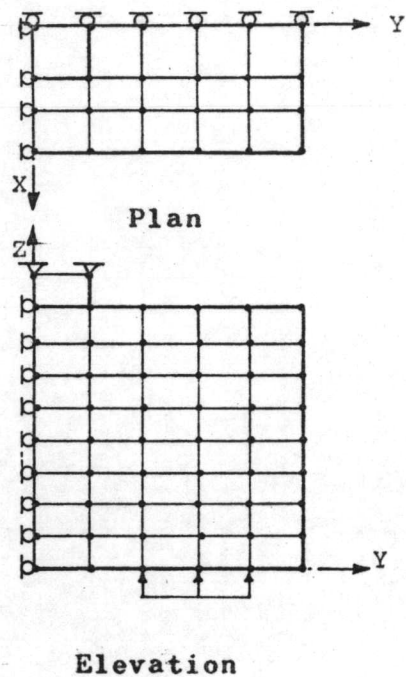


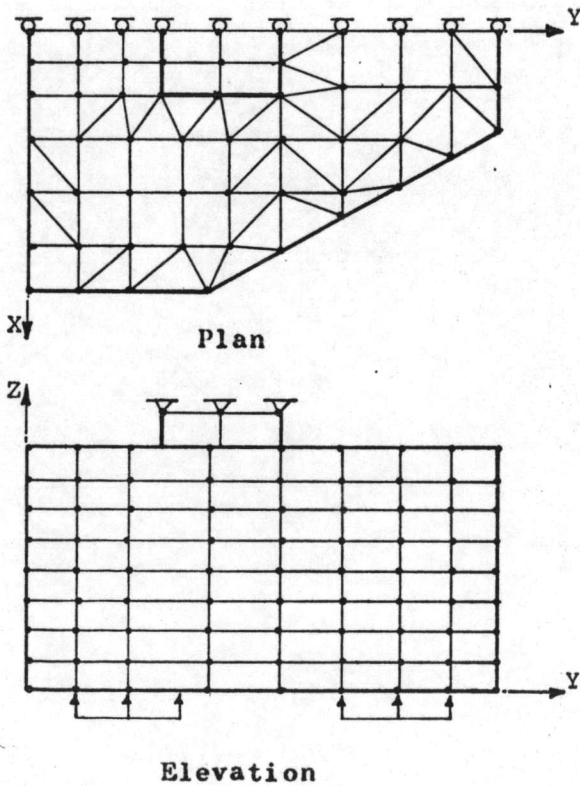
Fig. 3.2 Three Dimensional Finite Element in Global and Local System of Coordinates



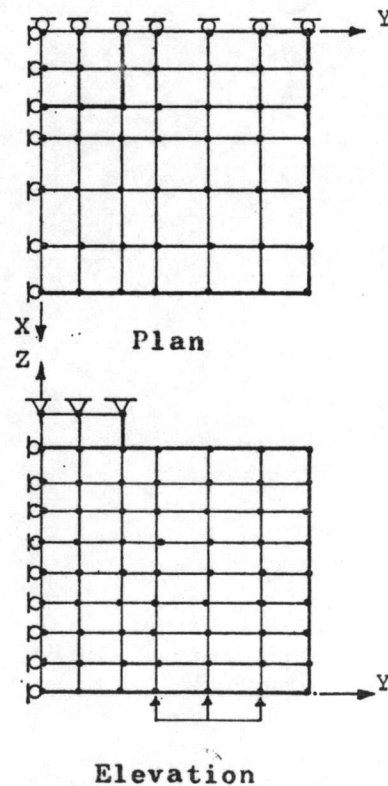
(a) Single-Pile Cap



(b) Two-Pile Cap



(c) Three-Pile Cap



(d) Four-Pile Cap

Fig. 3.3 Finite Element Models for Standard Pile Caps

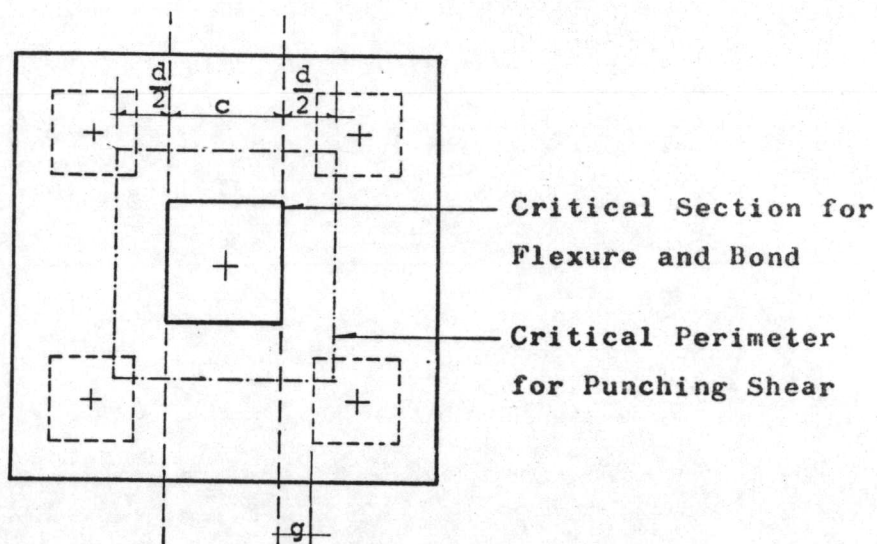


Fig. 3.4 Critical Sections for Flexure, Bond and Shear in Pile Cap Based on Beam Analogy

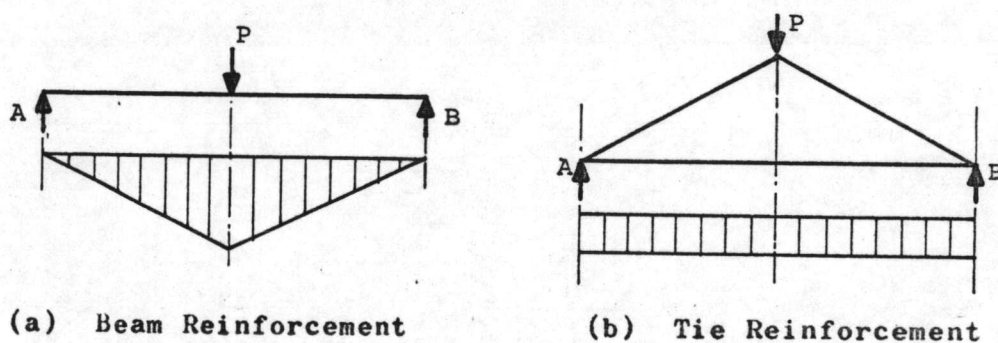


Fig. 3.5 Variation of Tension in Reinforcement

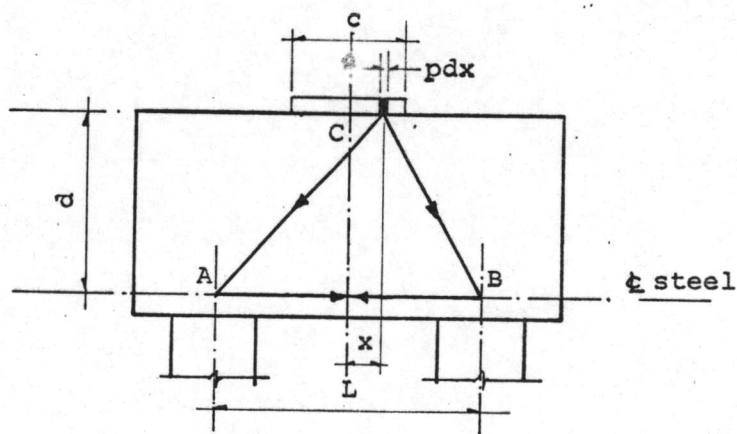


Fig. 3.6 Internal Force System in Two-Pile Cap Based on Truss Analogy

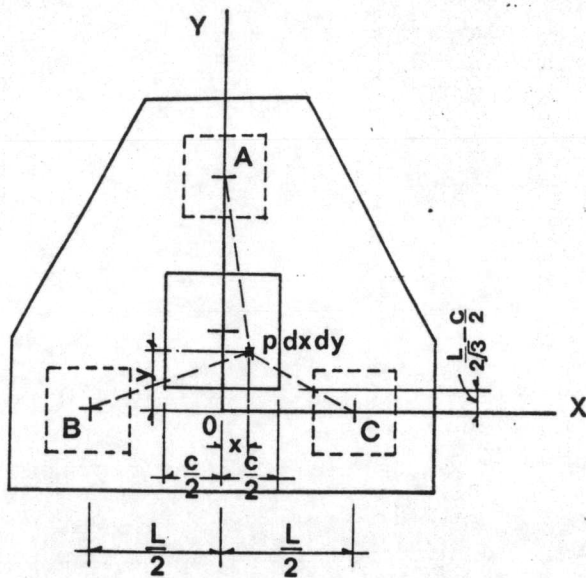


Fig. 3.7 Internal Force System in Three-Pile Cap Based on Truss Analogy

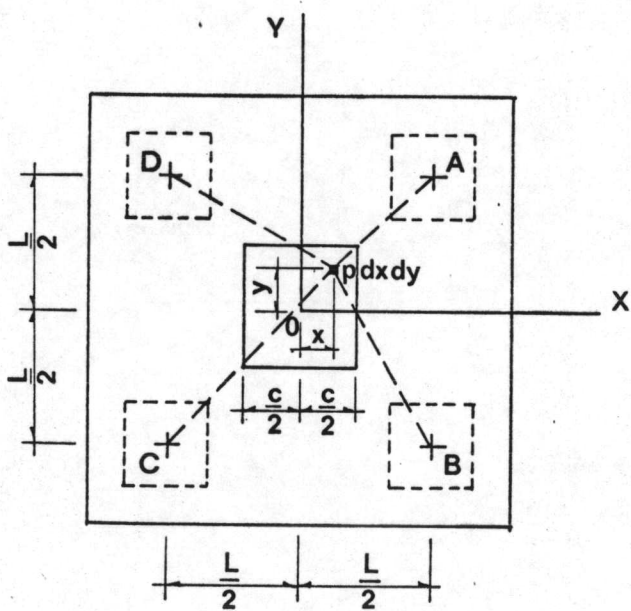
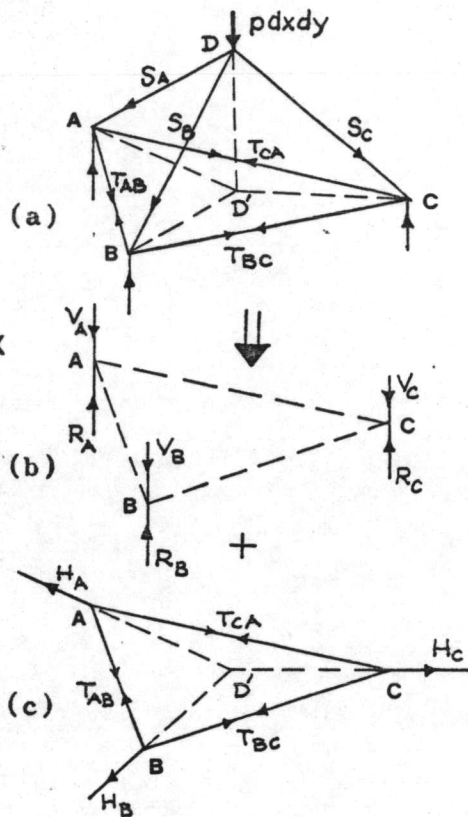
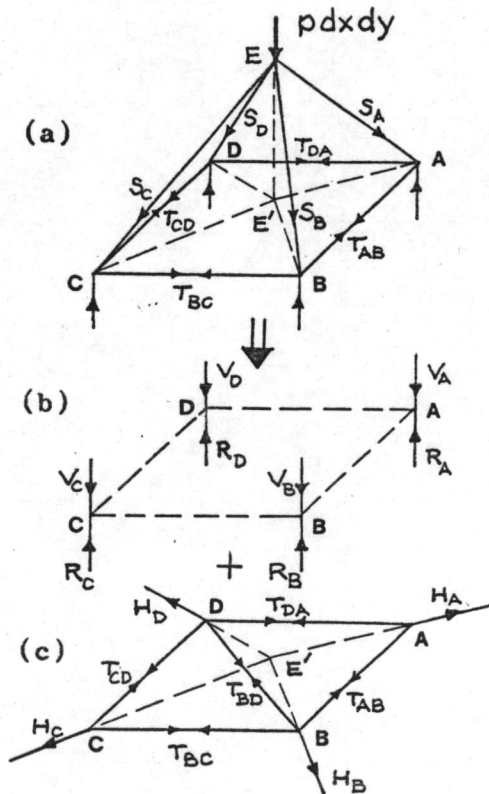


Fig. 3.8 Internal Force System in Four-Pile Cap Based on Truss Analogy



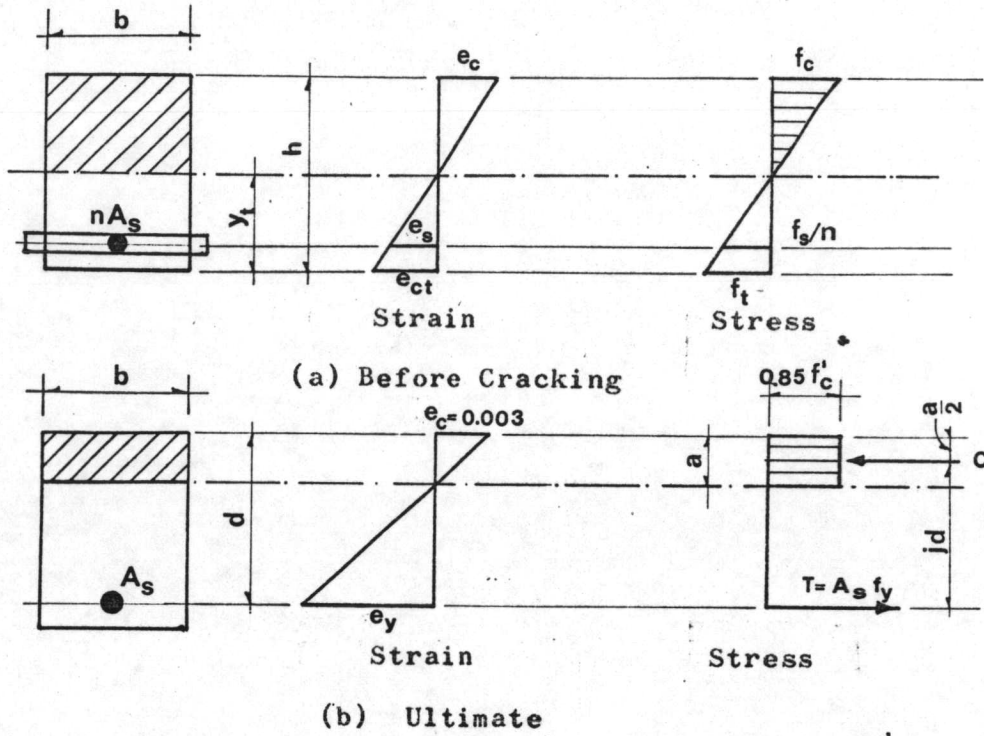


Fig. 3.9 Stress Distribution in Concrete on Beam Cross Section Under Bending Moment at Cracking and Ultimate Conditions

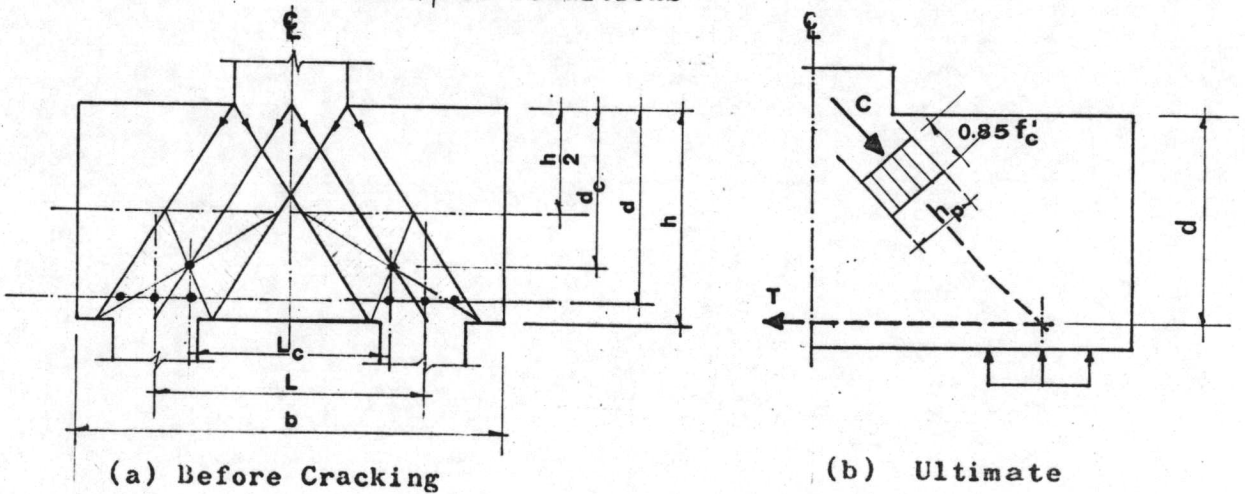
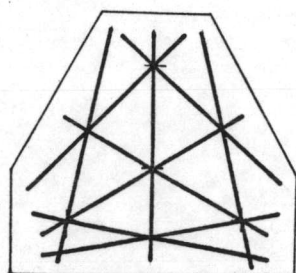
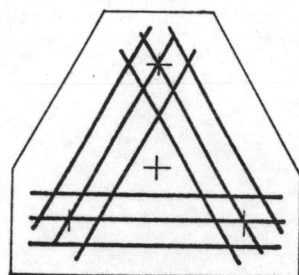


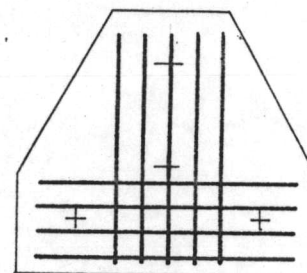
Fig. 3.10 Equivalent Transformed Section of Concrete Subjected to Tension Based on Truss Analogy at Cracking and Ultimate Conditions



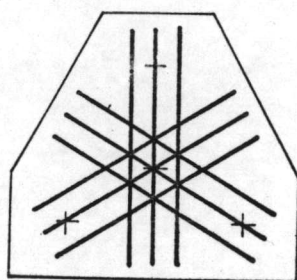
(a) P3-1



(b) P3-2

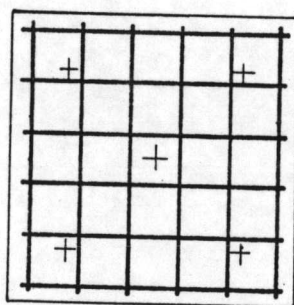


(c) P3-3

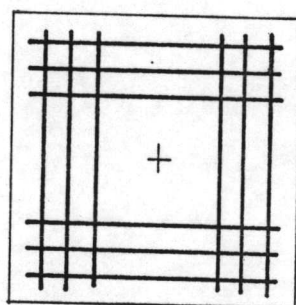


(d) P3-4

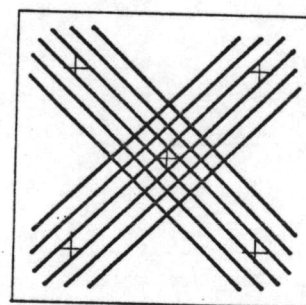
Fig. 3.11 Proposed Reinforcement Arrangements in Three-Pile Caps



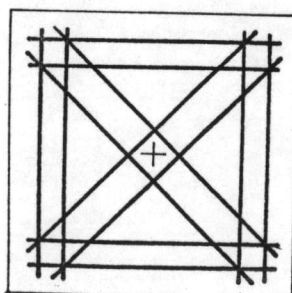
(a) P4-1



(b) P4-2

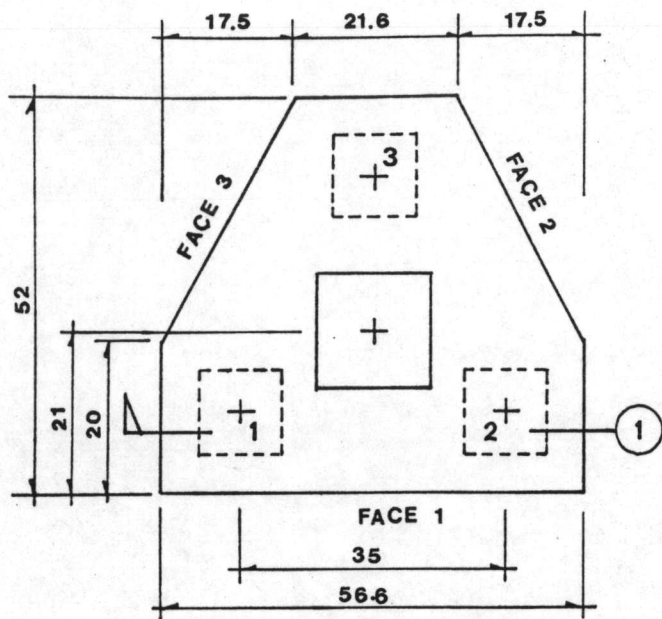


(c) P4-3

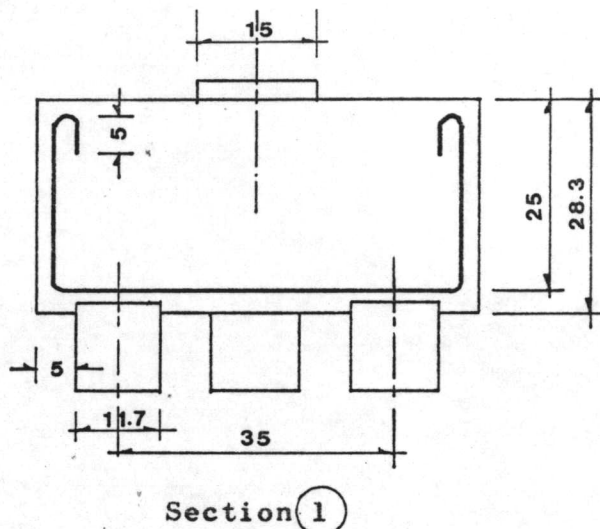


(d) P4-4

Fig. 3.12 Proposed Reinforcement Arrangements in Four-Pile Caps

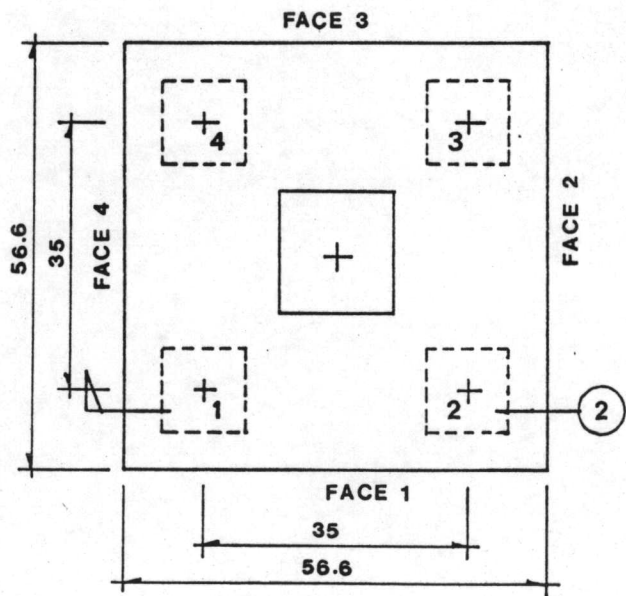


Plan

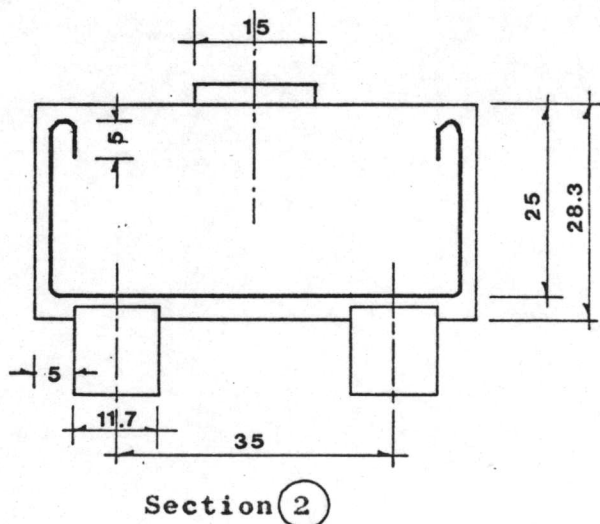


Section 1

(a) Three-Pile Cap Model



Plan



Section 2

(b) Four-Pile Cap Model

Fig. 5.1 Typical Dimensions of Model Specimens and Details of Reinforcement

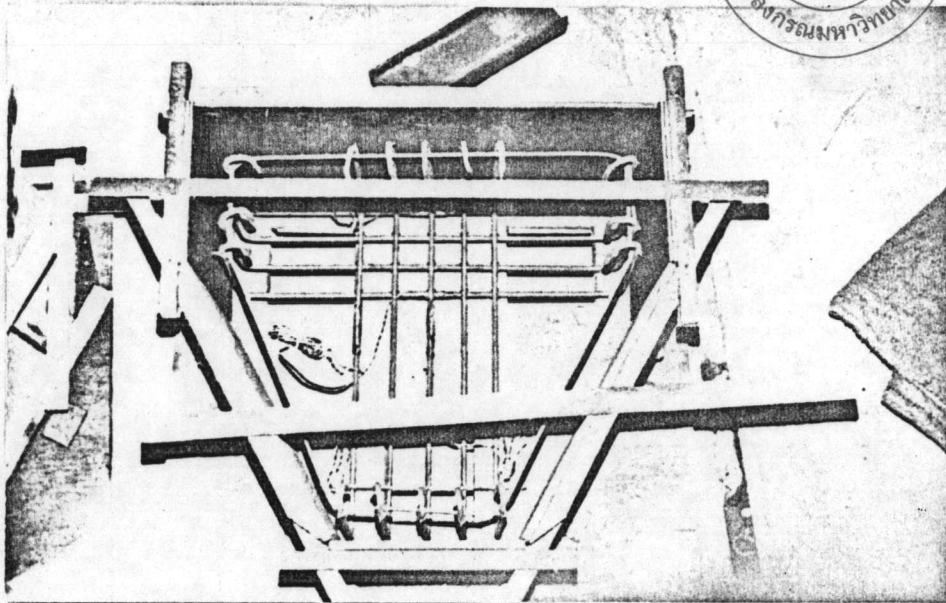


Fig. 5.2 Set-Up for Casting Three-Pile Cap Model

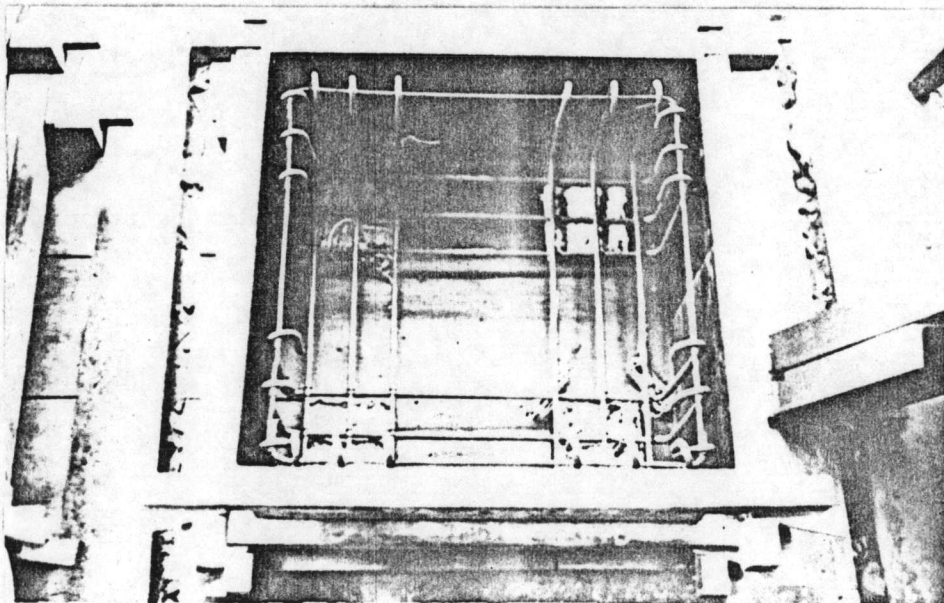


Fig. 5.3 Set-Up for Casting Four-Pile Cap Model

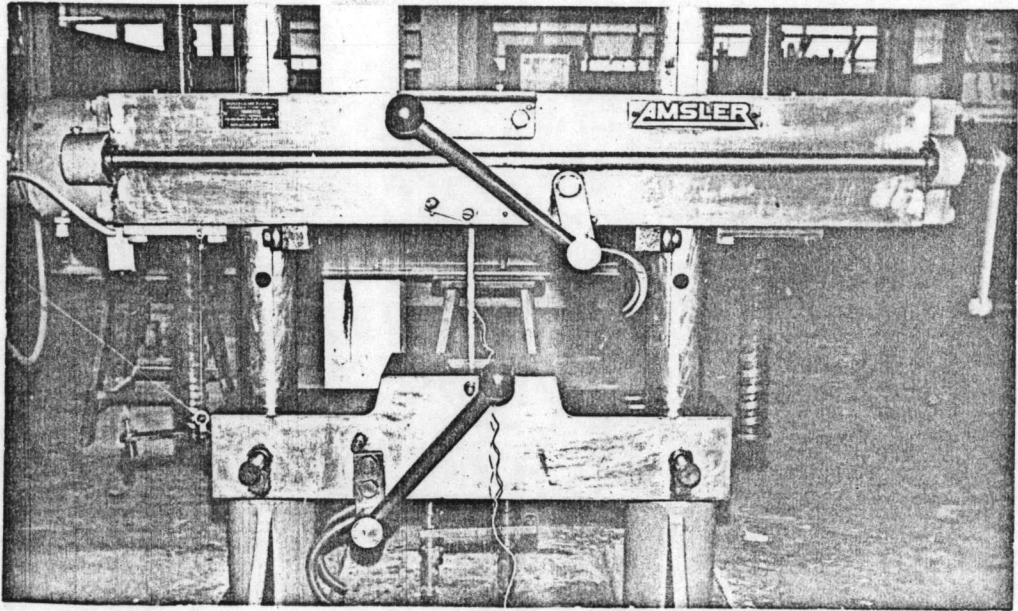


Fig. 5.4 Testing for Strength of Steel Under Direct Tension

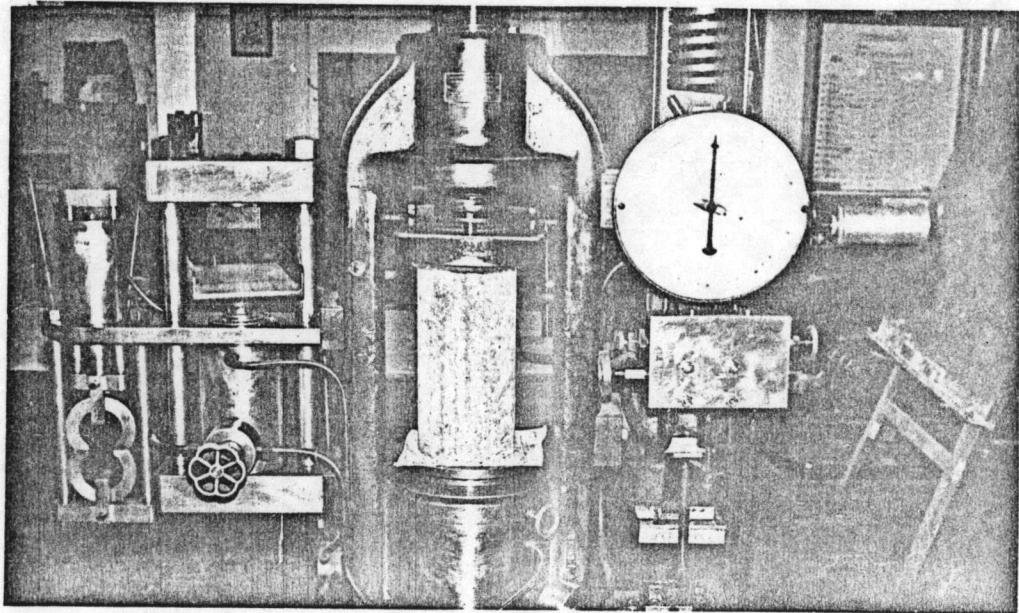


Fig. 5.5 Testing for Strength of Concrete Under Axial Compression

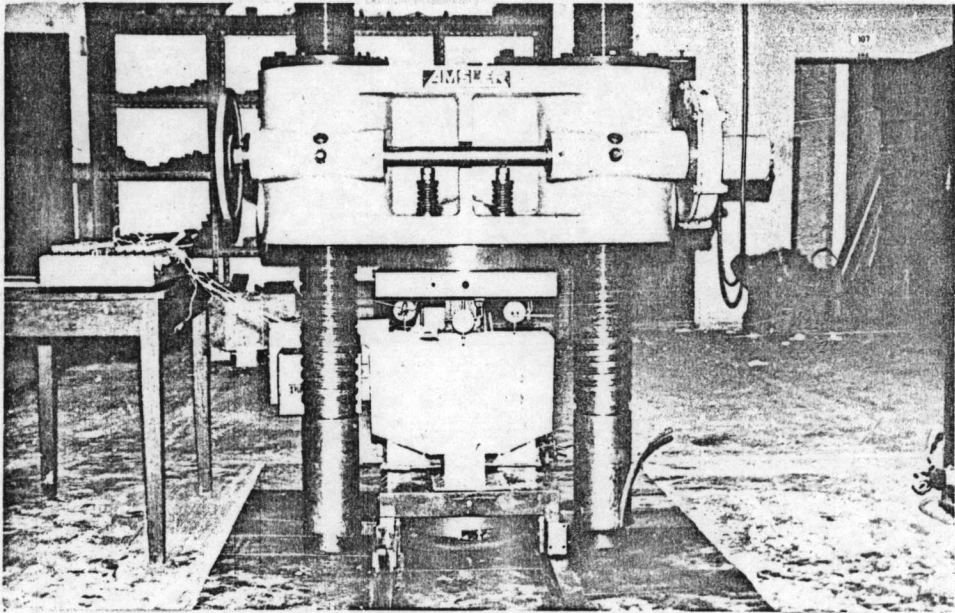


Fig. 5.6 General View of Pile Cap Test Set-Up

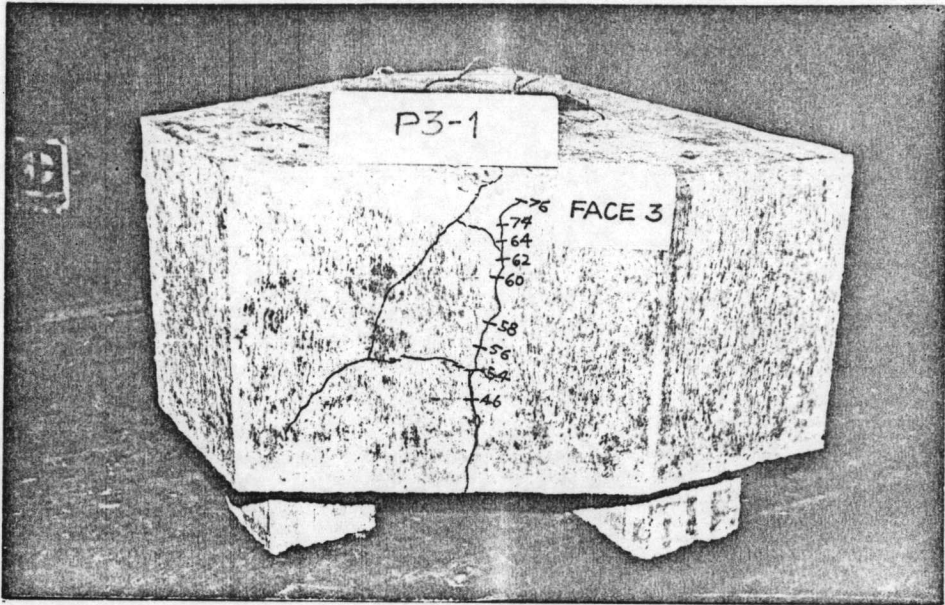


Fig. 5.7 Model P3-1 After Testing

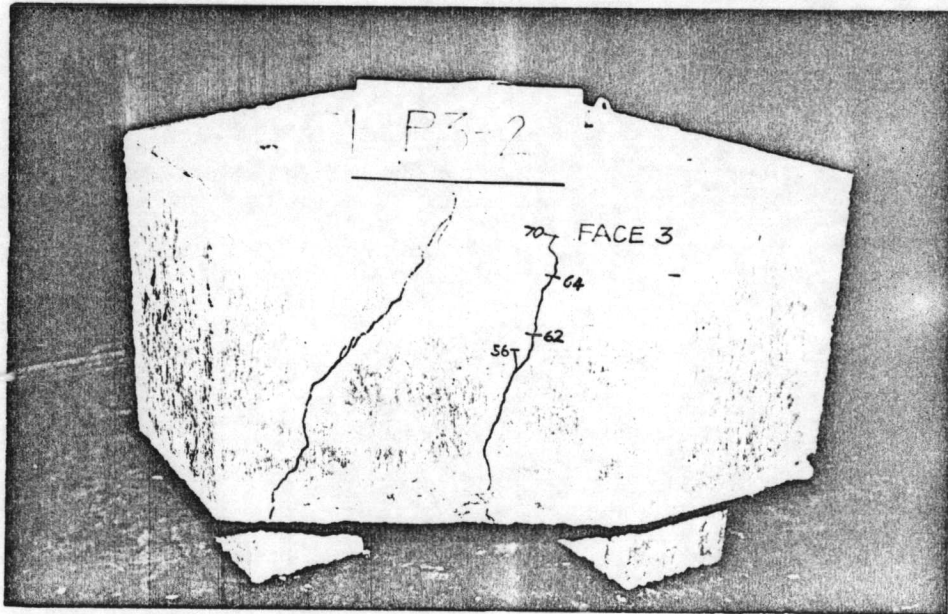


Fig. 5.8 Model P3-2 After Testing

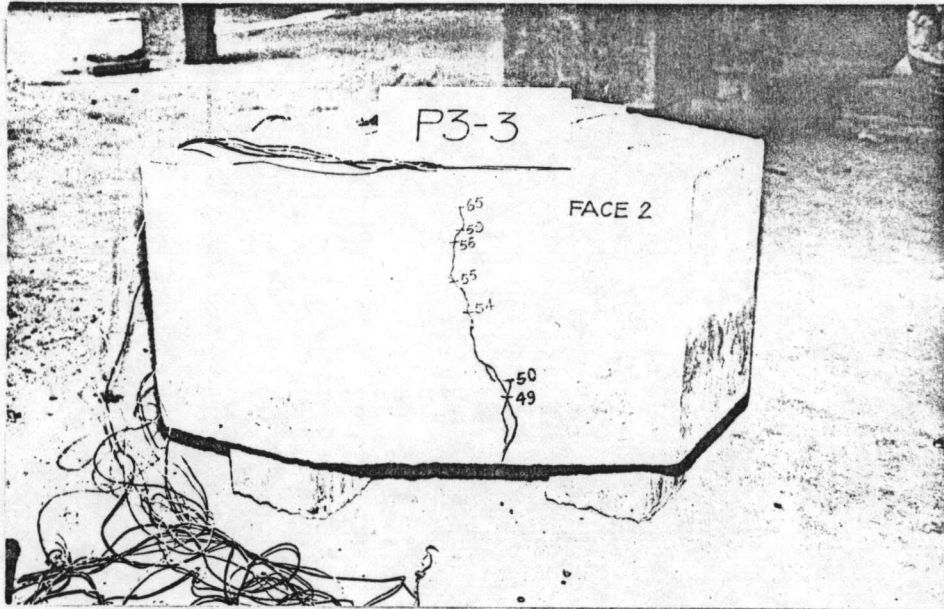


Fig. 5.9 Model P3-3 After Testing

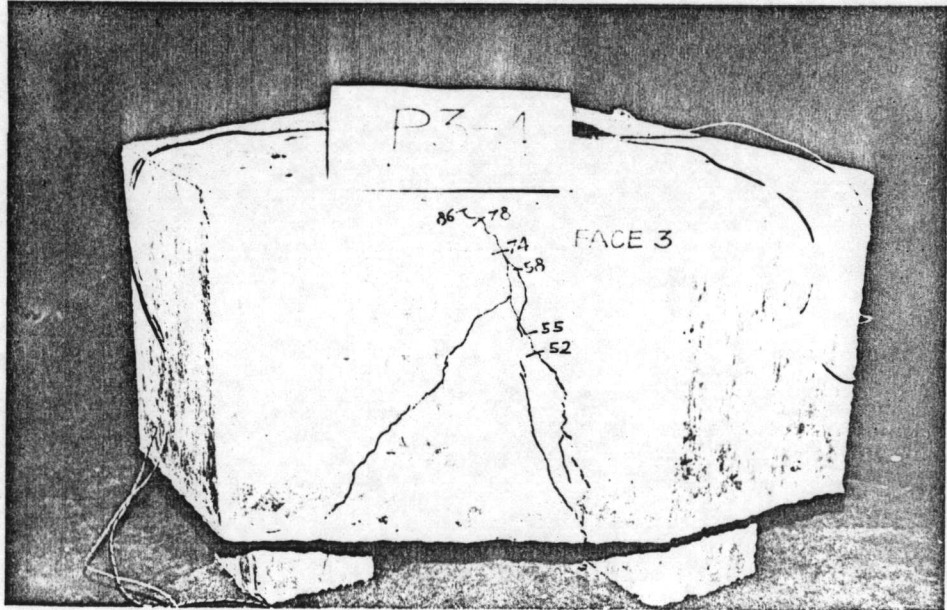


Fig. 5.10 Model P3-4 After Testing

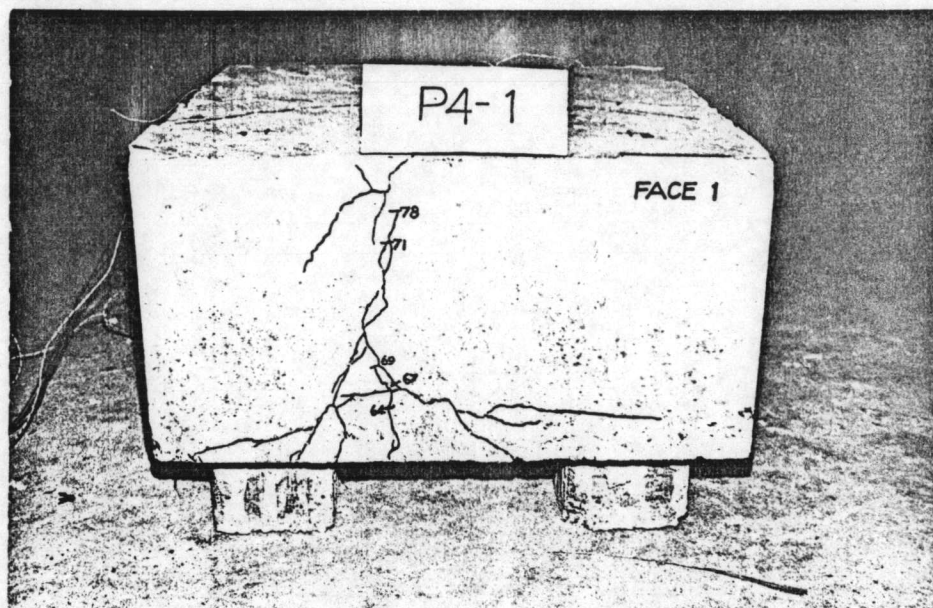


Fig. 5.11 Model P4-1 After Testing

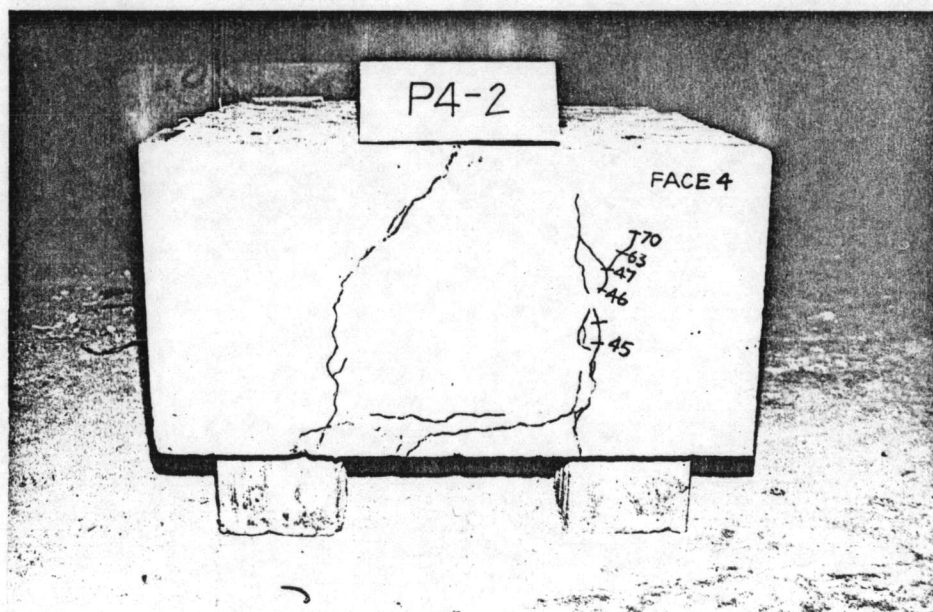


Fig. 5.12 Model P4-2 After Testing

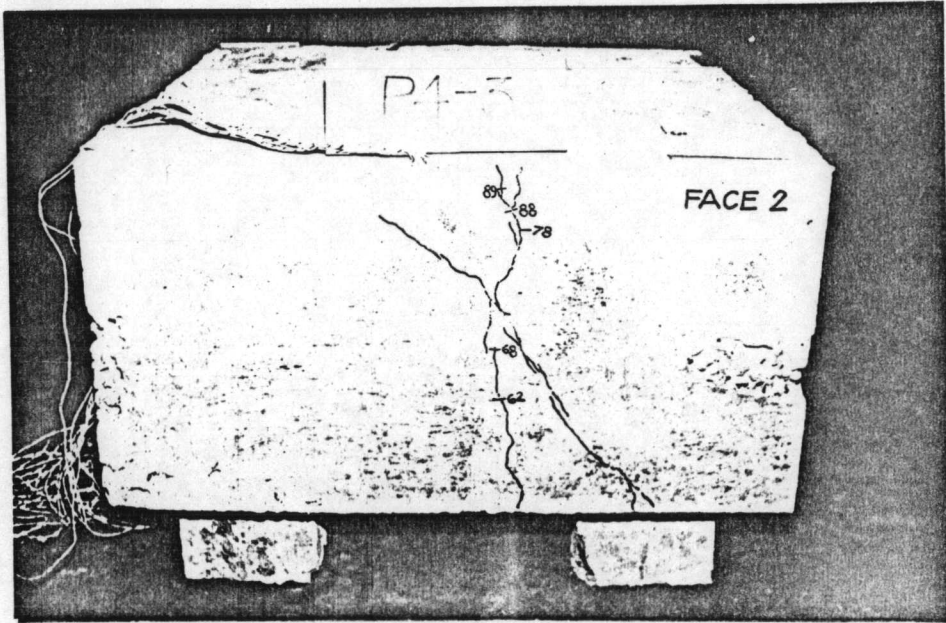


Fig. 5.13 Model P4-3 After Testing

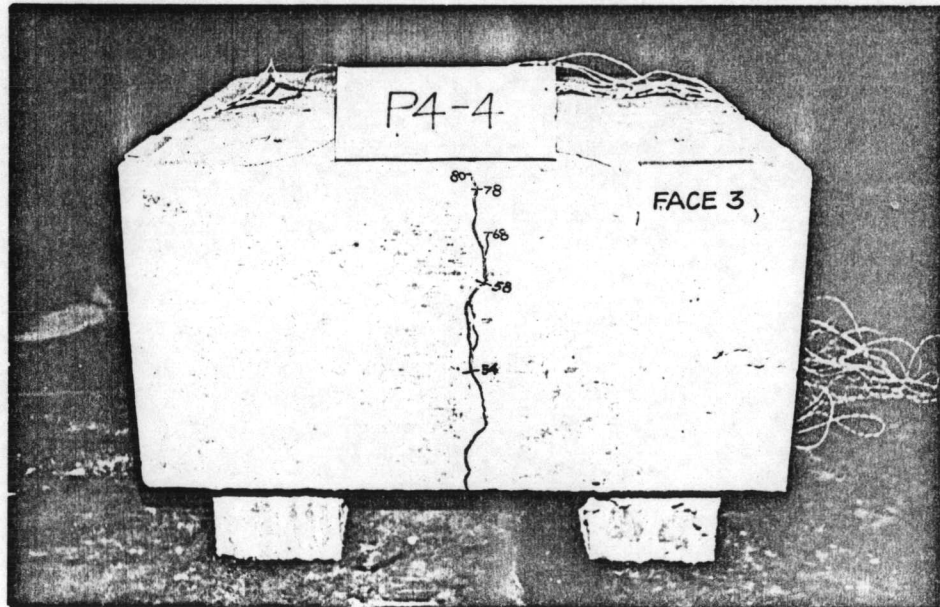


Fig. 5.14 Model P4-4 After Testing

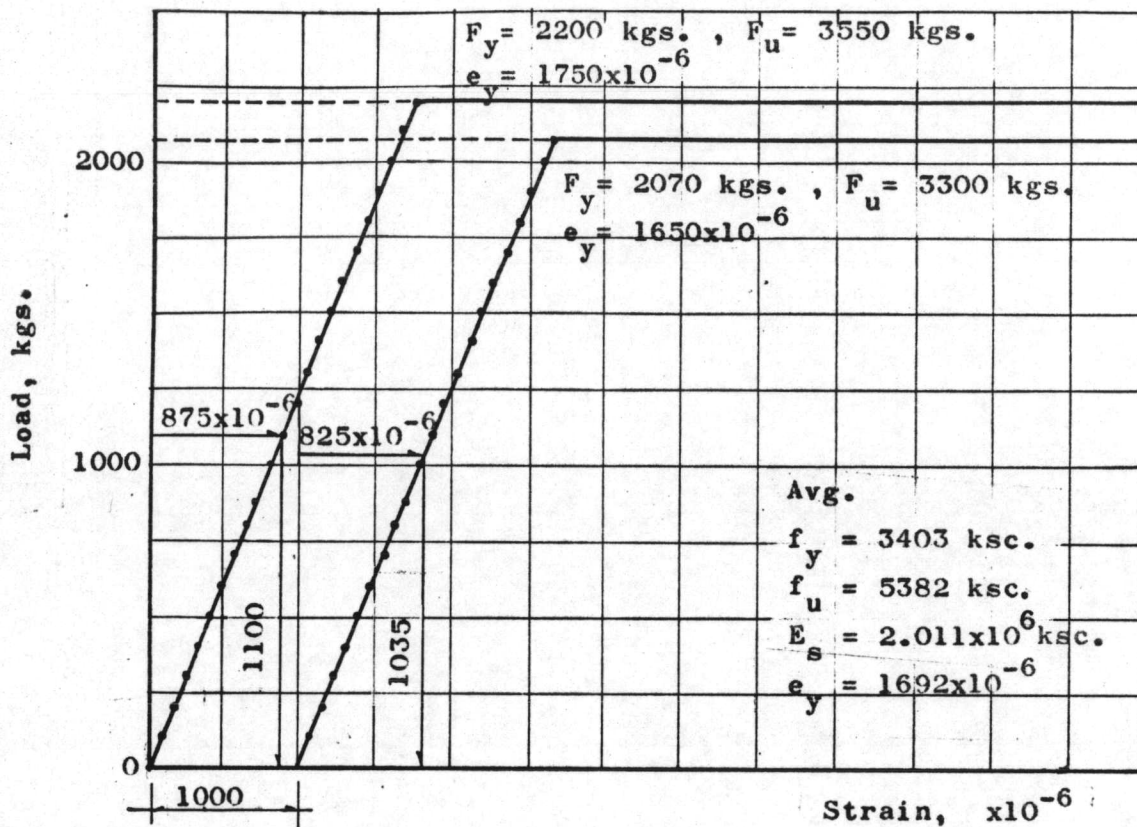


Fig. 6.1 Typical Stress-Strain Curves for Steel Under Direct Tension

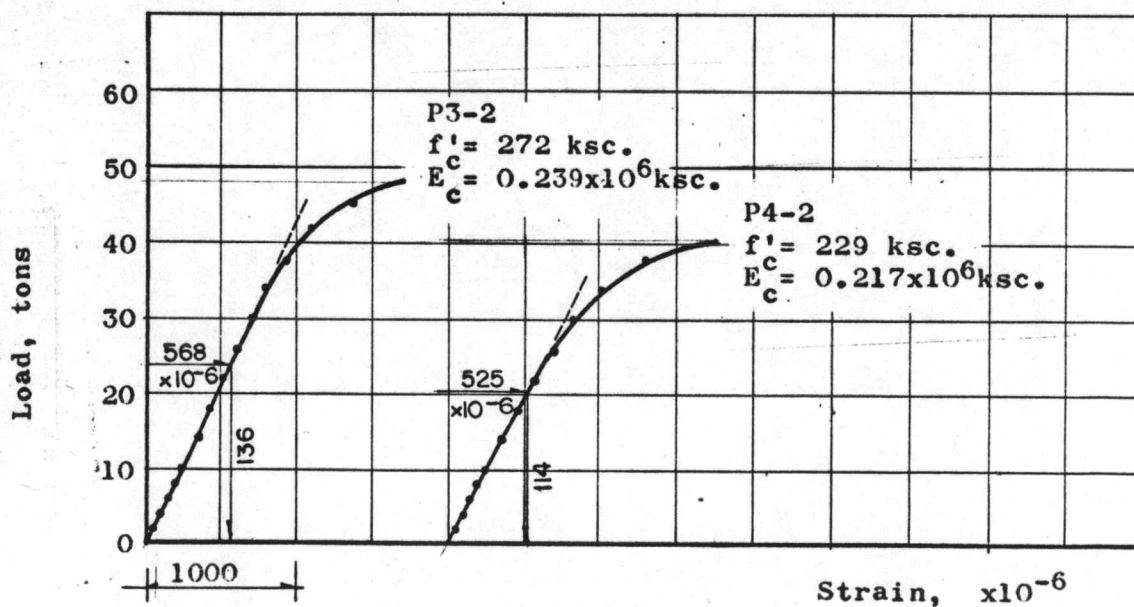


Fig. 6.2 Typical Stress-Strain Curves for Concrete Under Axial Compression

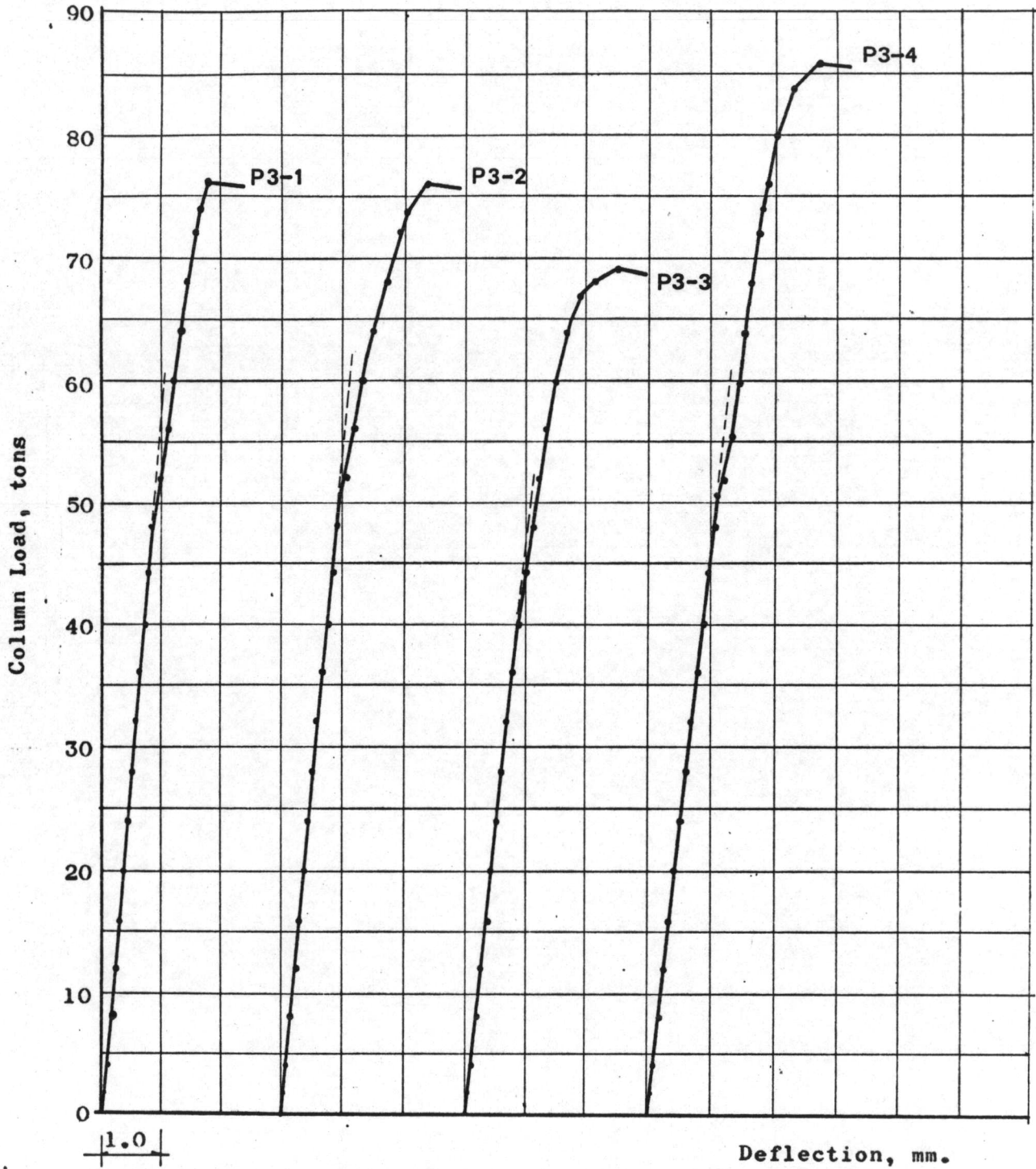


Fig. 6.3 Comparison of Load-Deflection Curves Between Three-Pile Cap Models

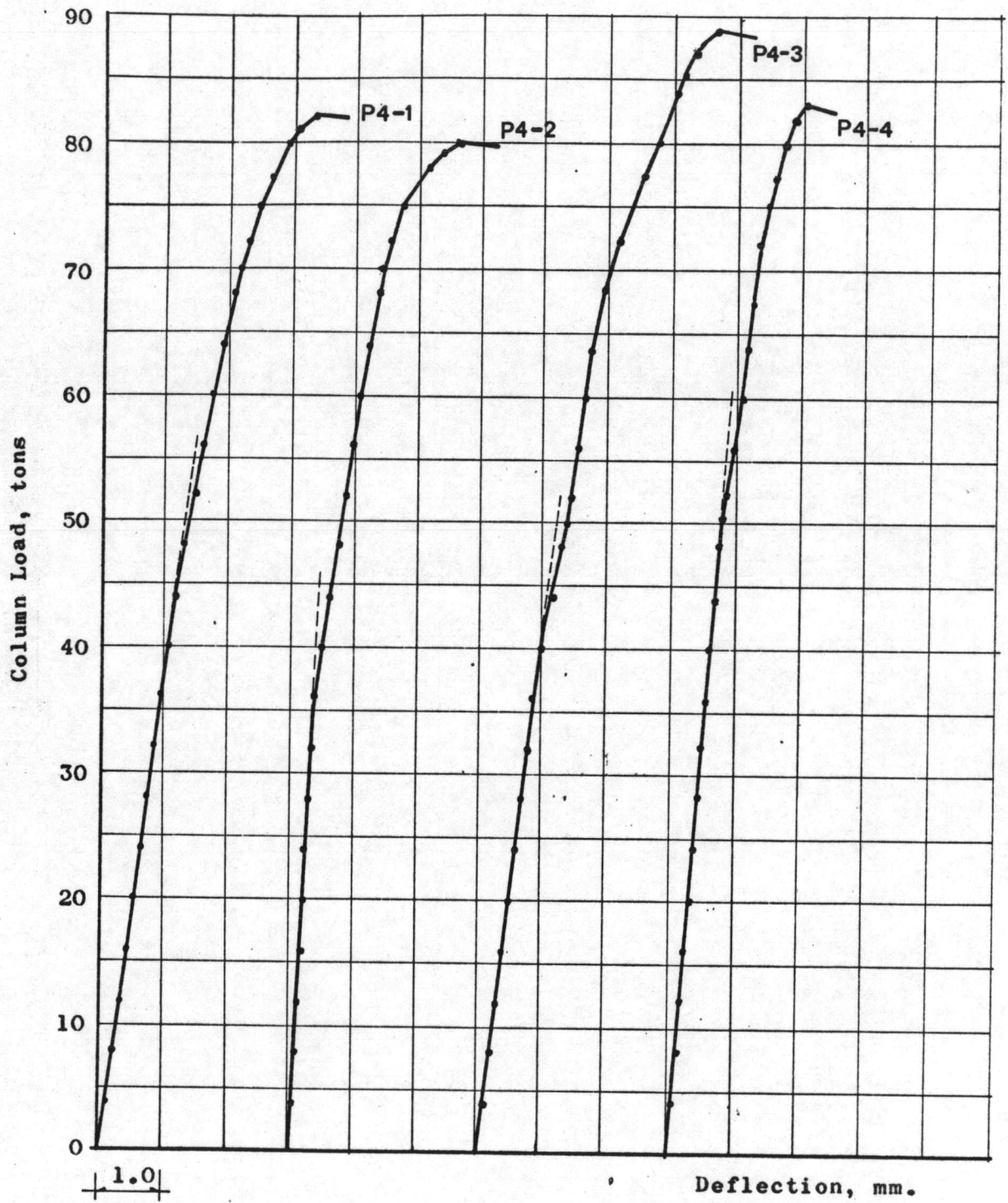


Fig. 6.4 Comparison of Load-Deflection Curves Between Four-Pile Cap Models

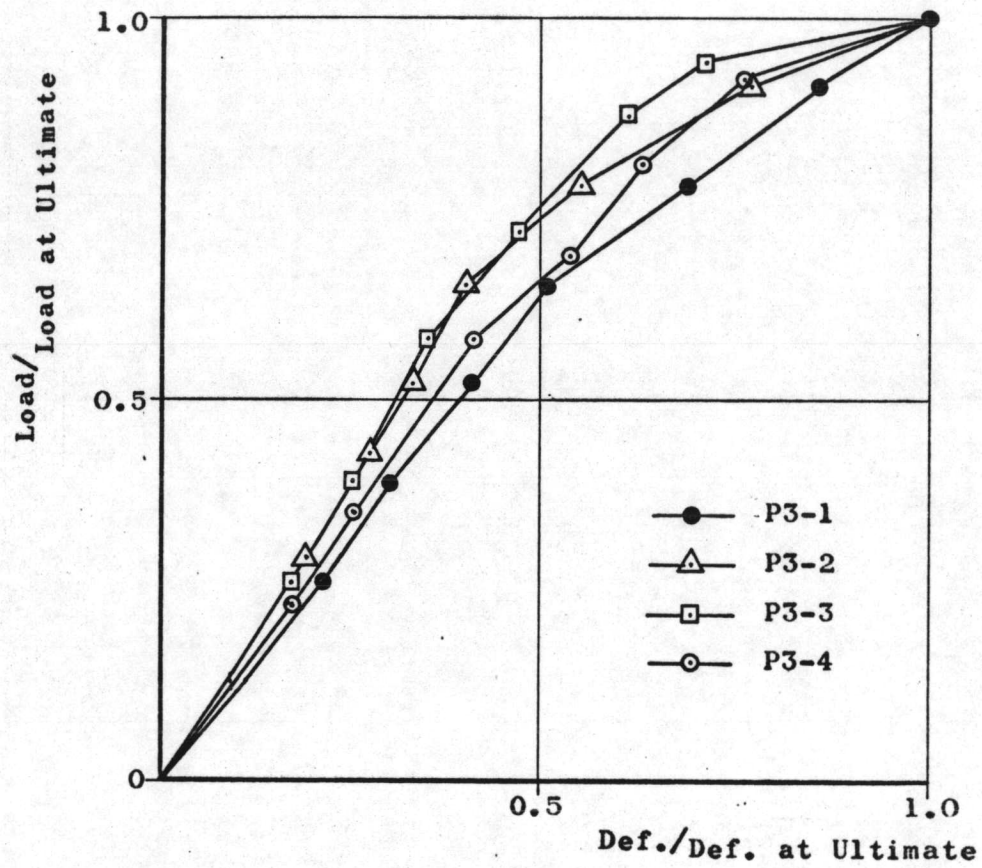


Fig. 6.5 Normalized Load-Deflection Curves for Three-Pile Cap Models

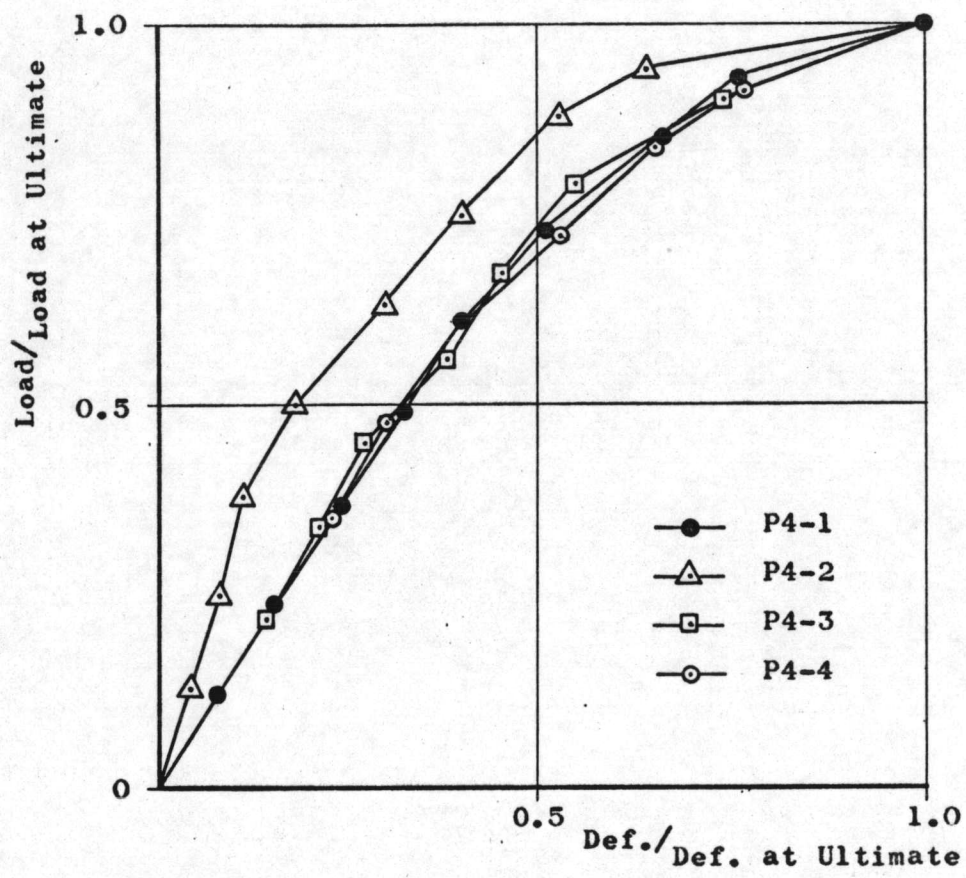


Fig. 6.6 Normalized Load-Deflection Curves for Four-Pile Cap Models

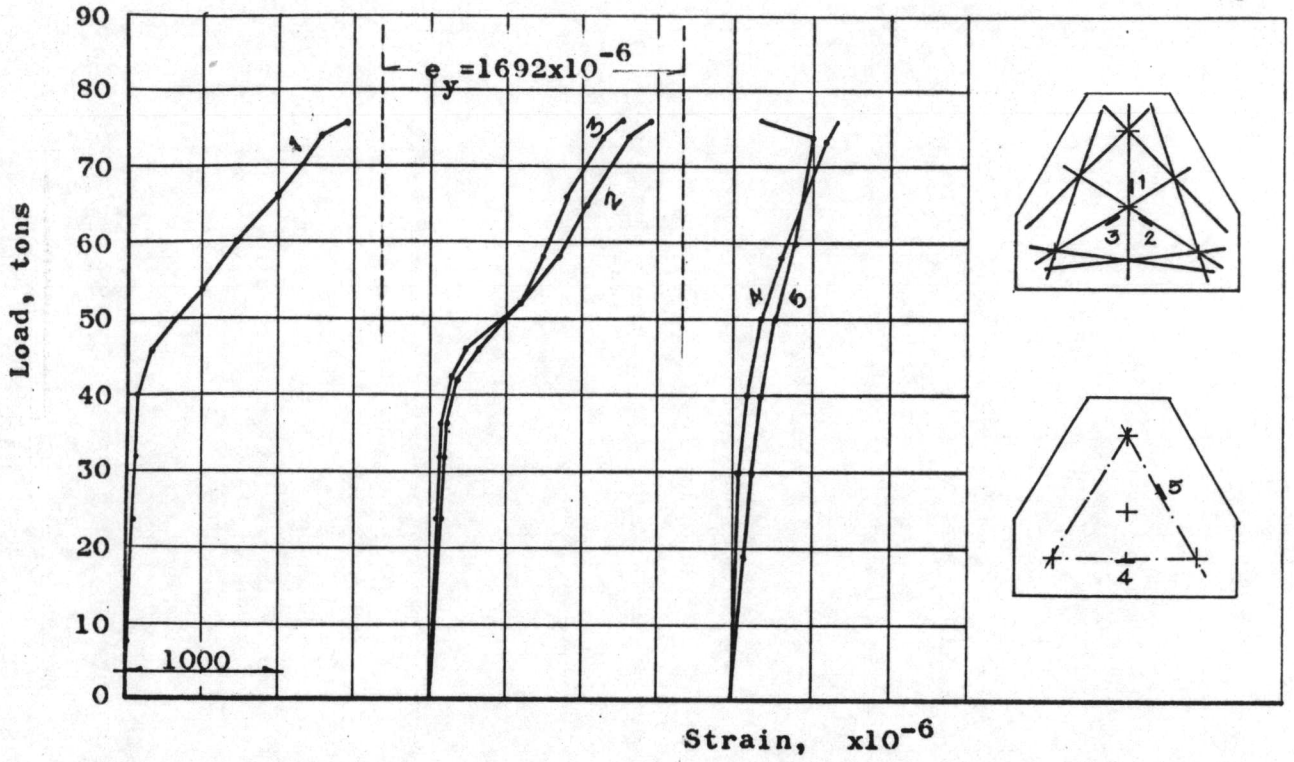


Fig. 6.7 Load-Strain Curves of Steel and Concrete for P3-1

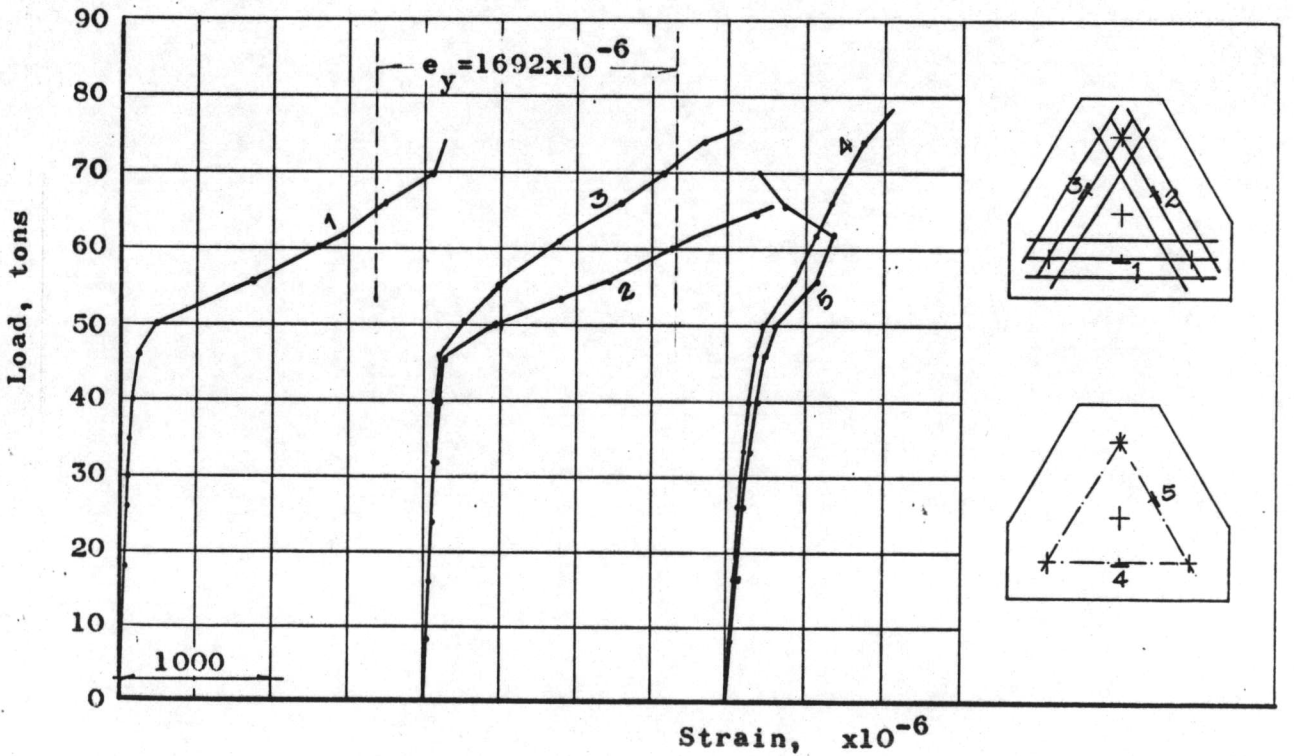


Fig. 6.8 Load-Strain Curves of Steel and Concrete for P3-2

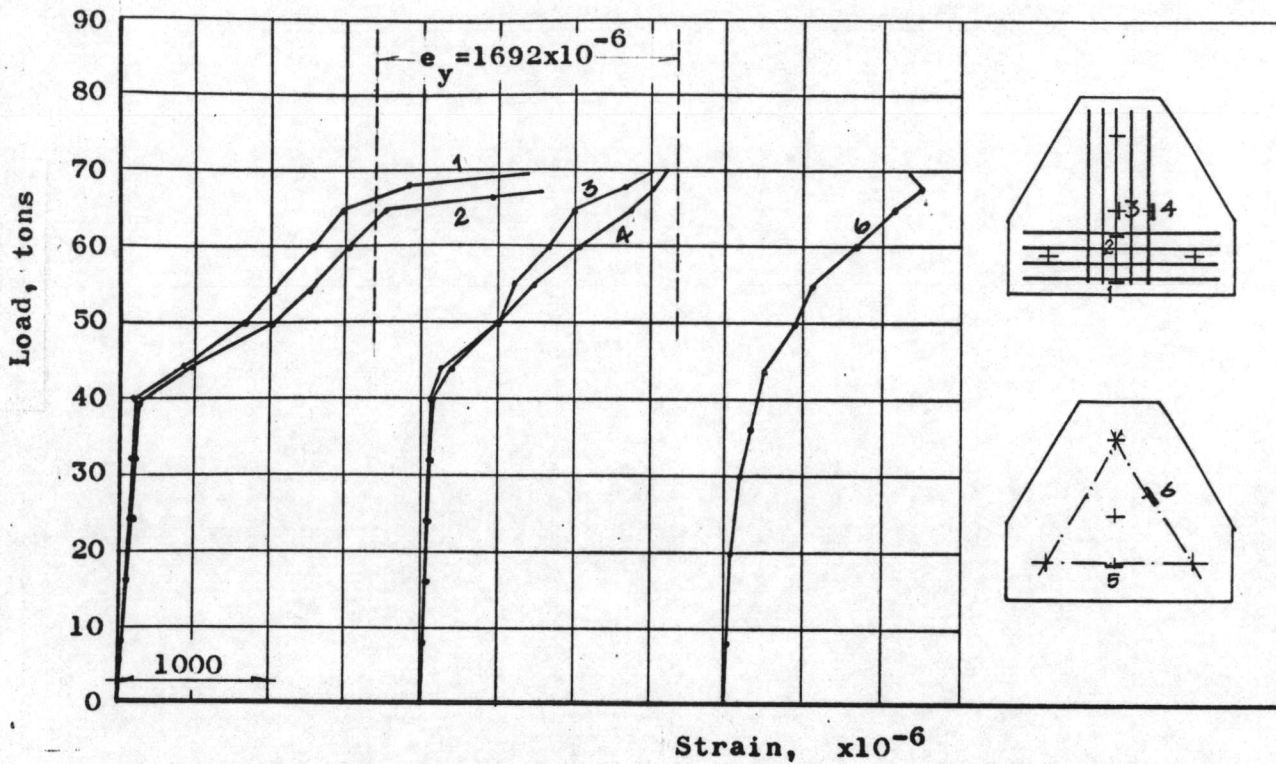


Fig. 6.9 Load-Strain Curves of Steel and Concrete for P3-3

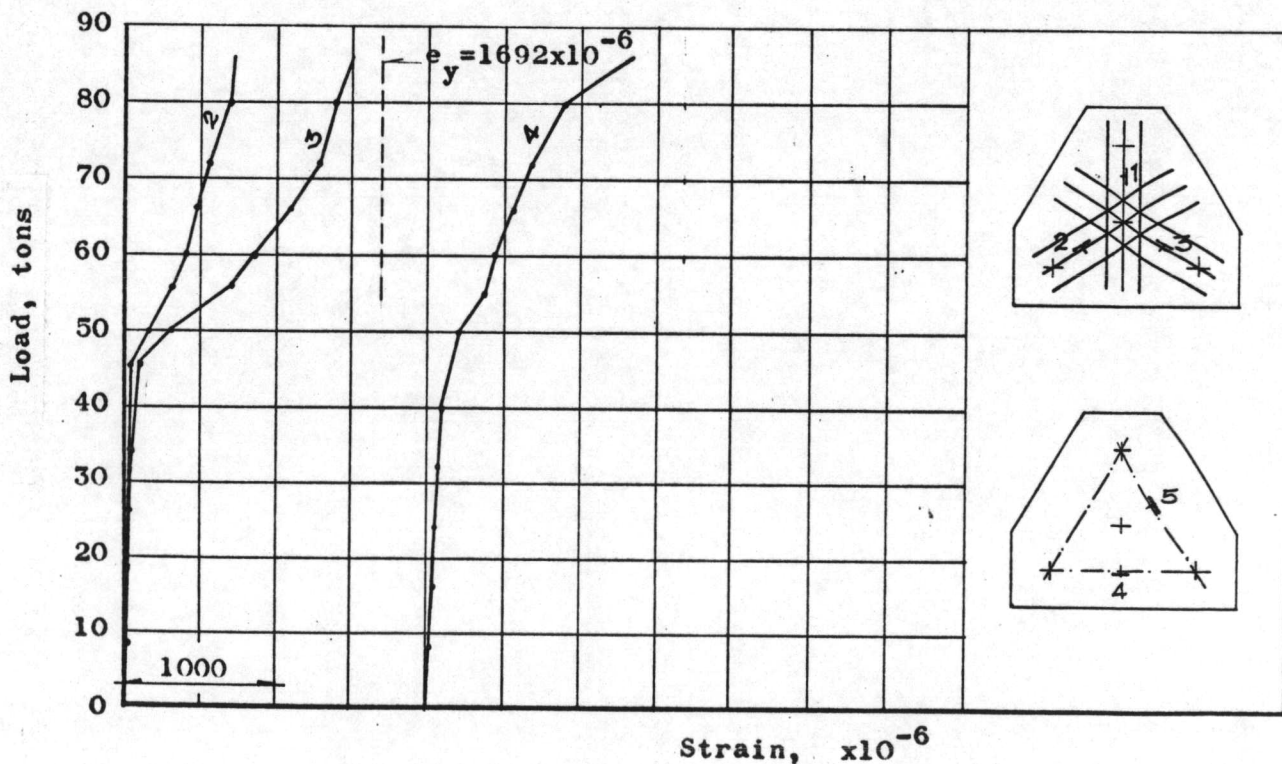


Fig. 6.10 Load-Strain Curves of Steel and Concrete for P3-4

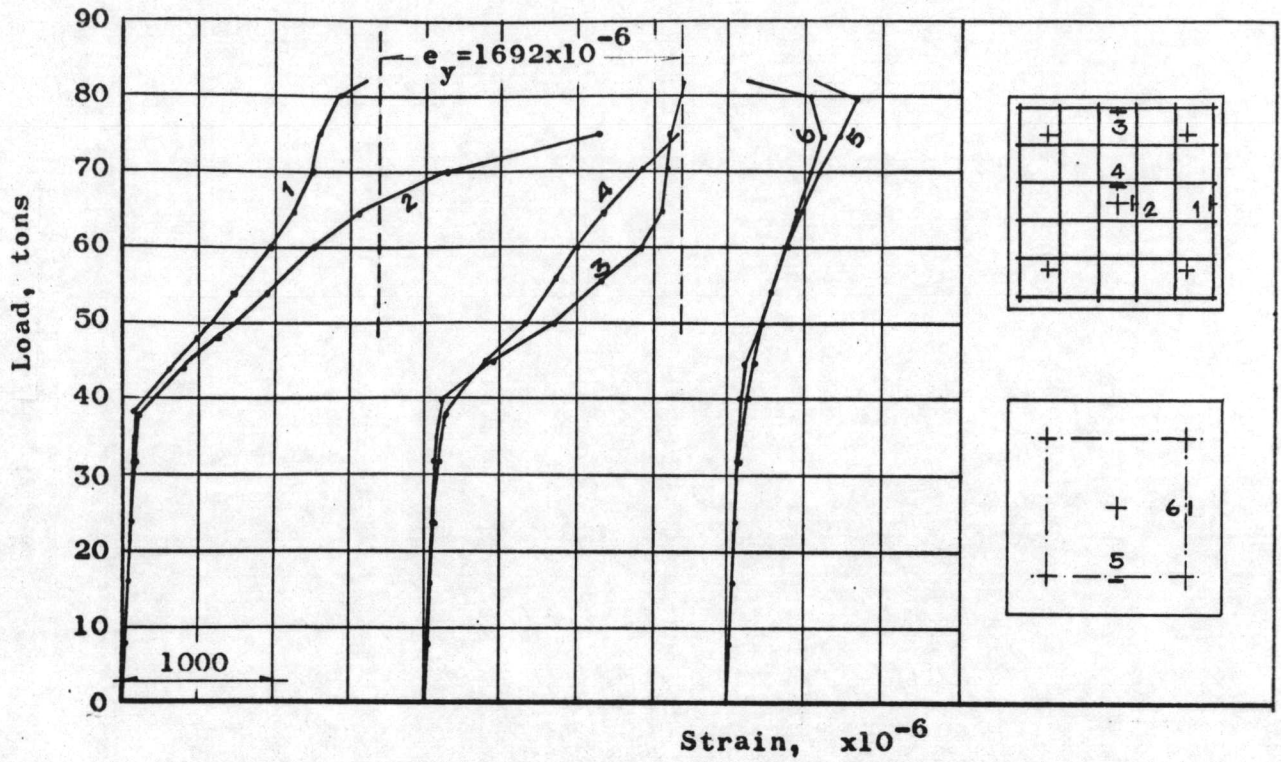


Fig. 6.11 Load-Strain Curves of Steel and Concrete for P4-1

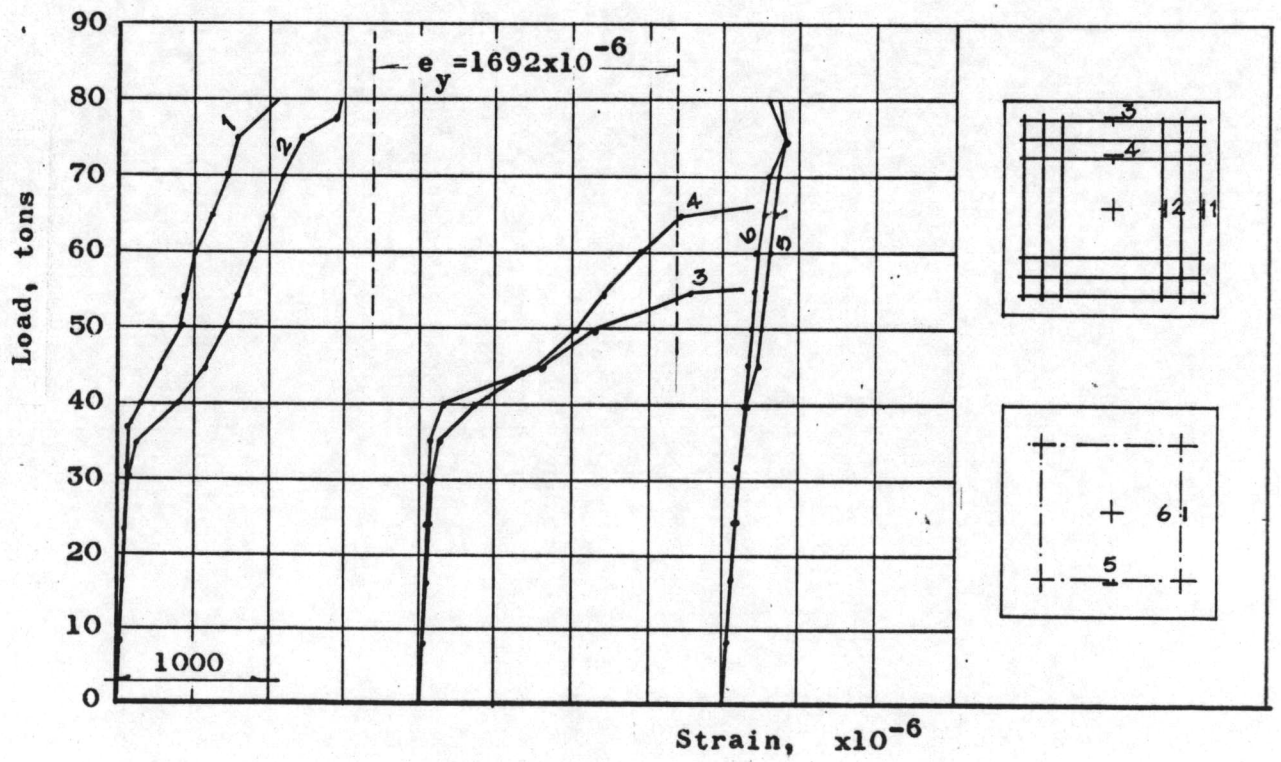


Fig. 6.12 Load-Strain Curves of Steel and Concrete for P4-2

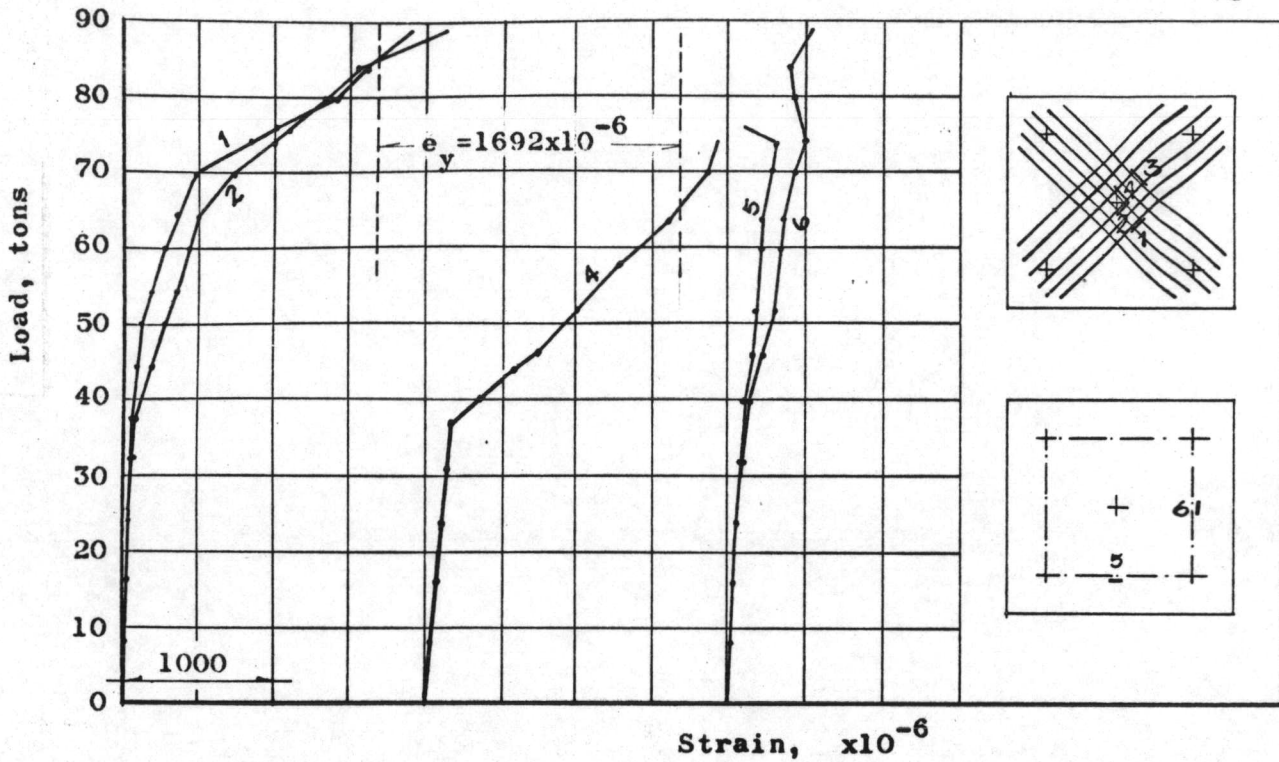


Fig. 6.13 Load-Strain Curves of Steel and Concrete for P4-3

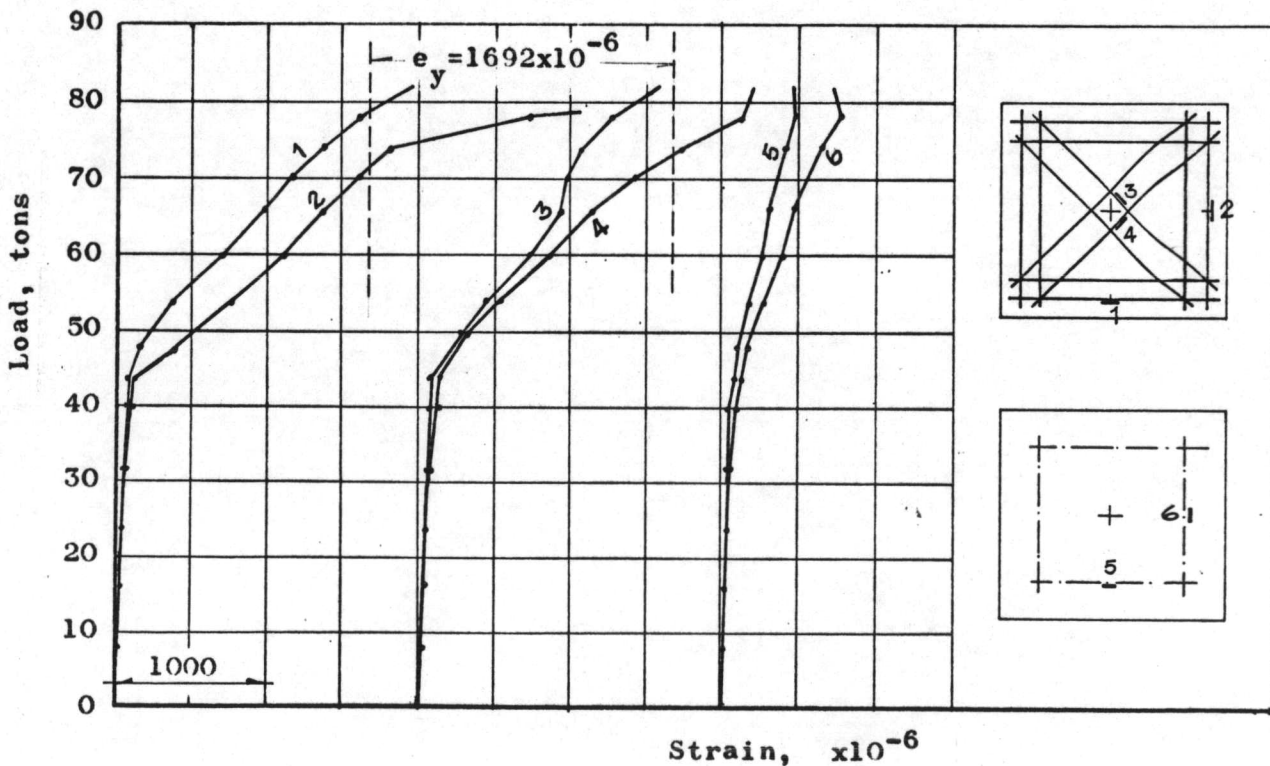
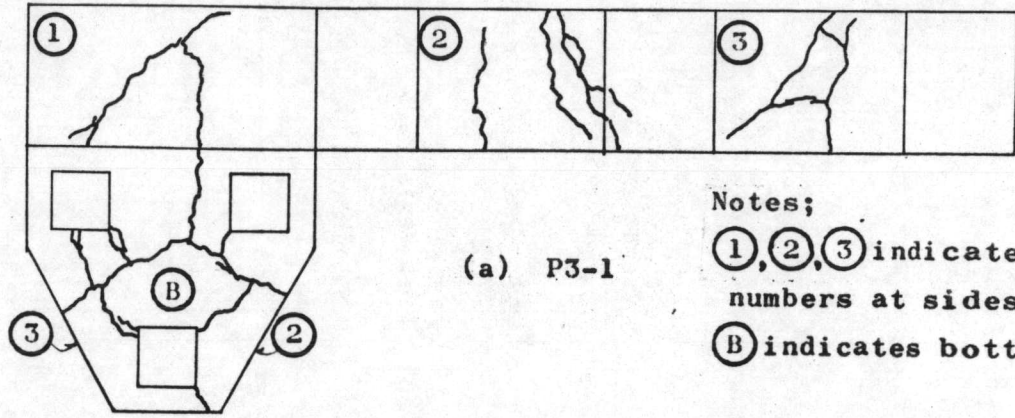


Fig. 6.14 Load-Strain Curves of Steel and Concrete for P4-4



Notes;

- ①, ②, ③ indicate face-numbers at sides
- ⓑ indicates bottom face

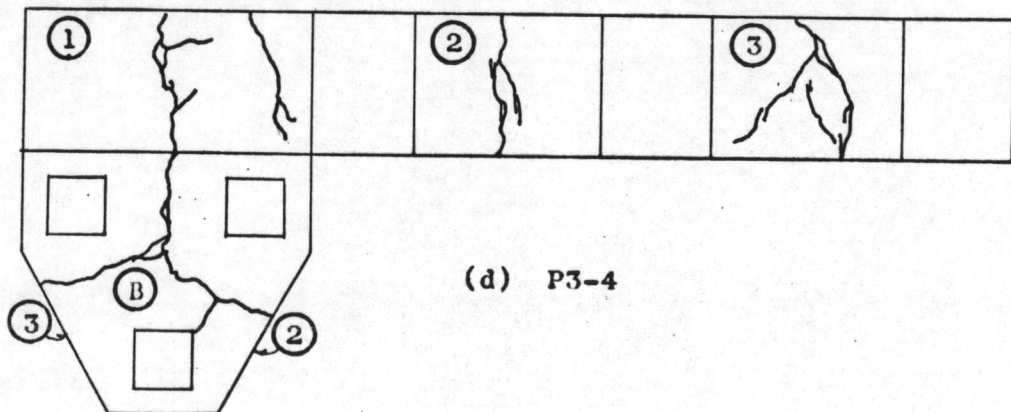
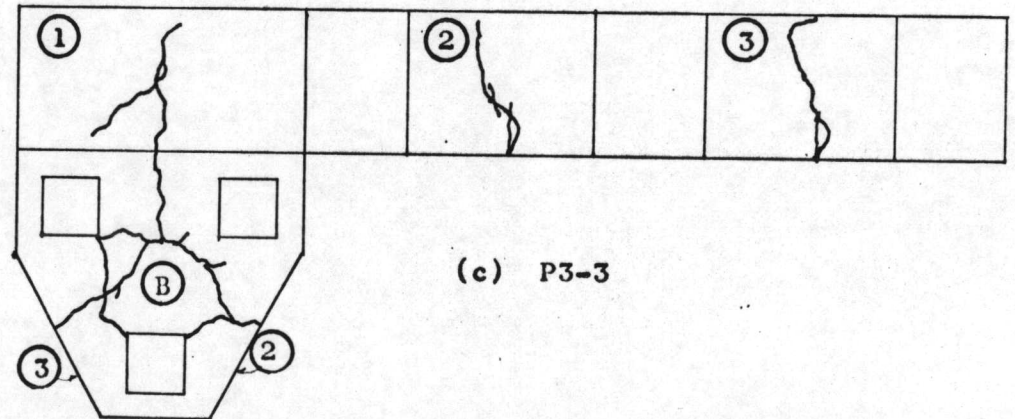
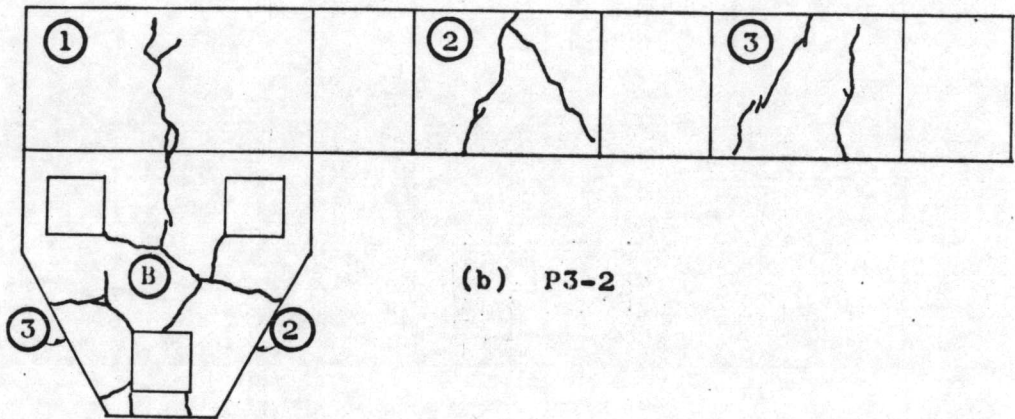


Fig. 6.15 Crack Patterns in Three-Pile Cap Models

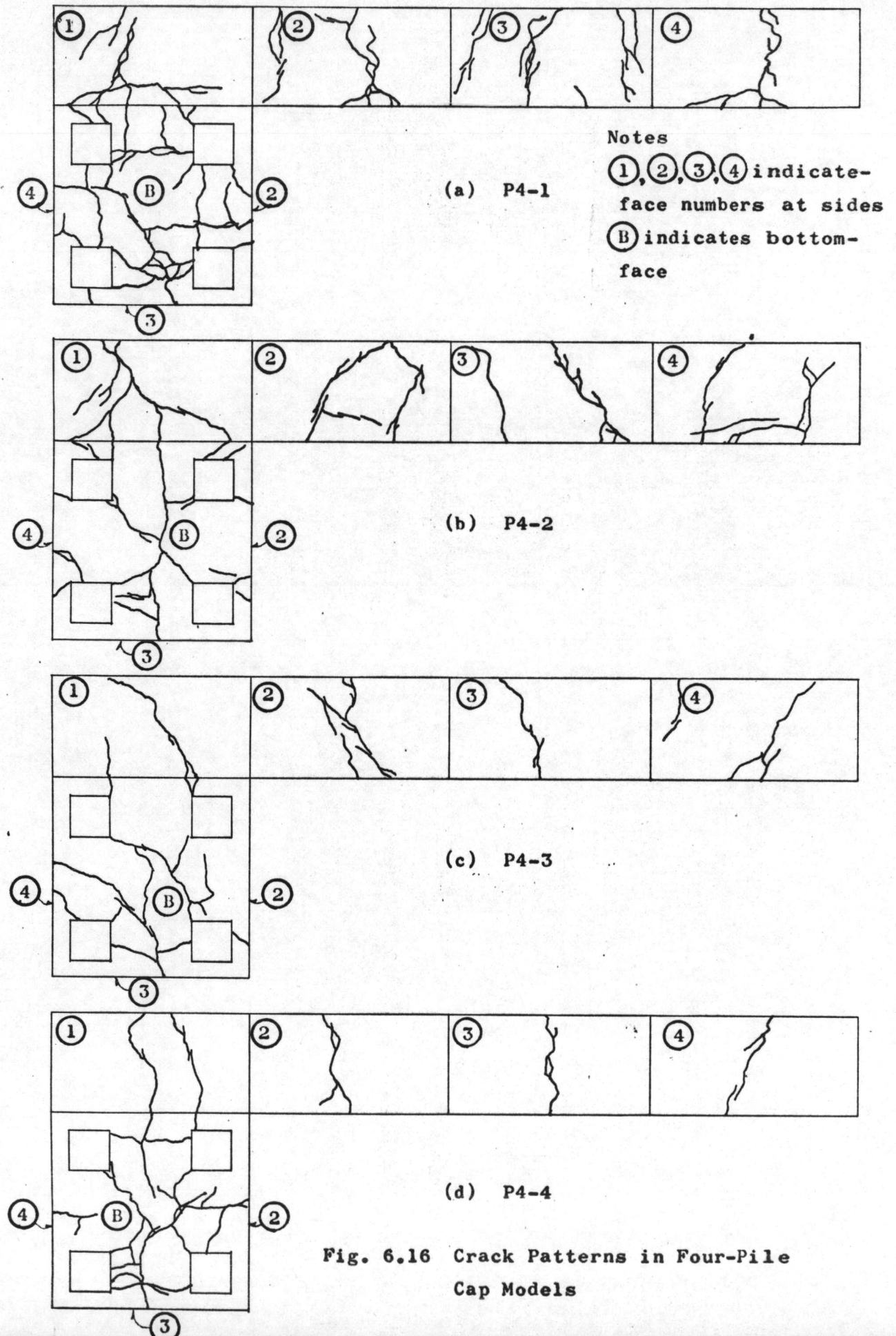
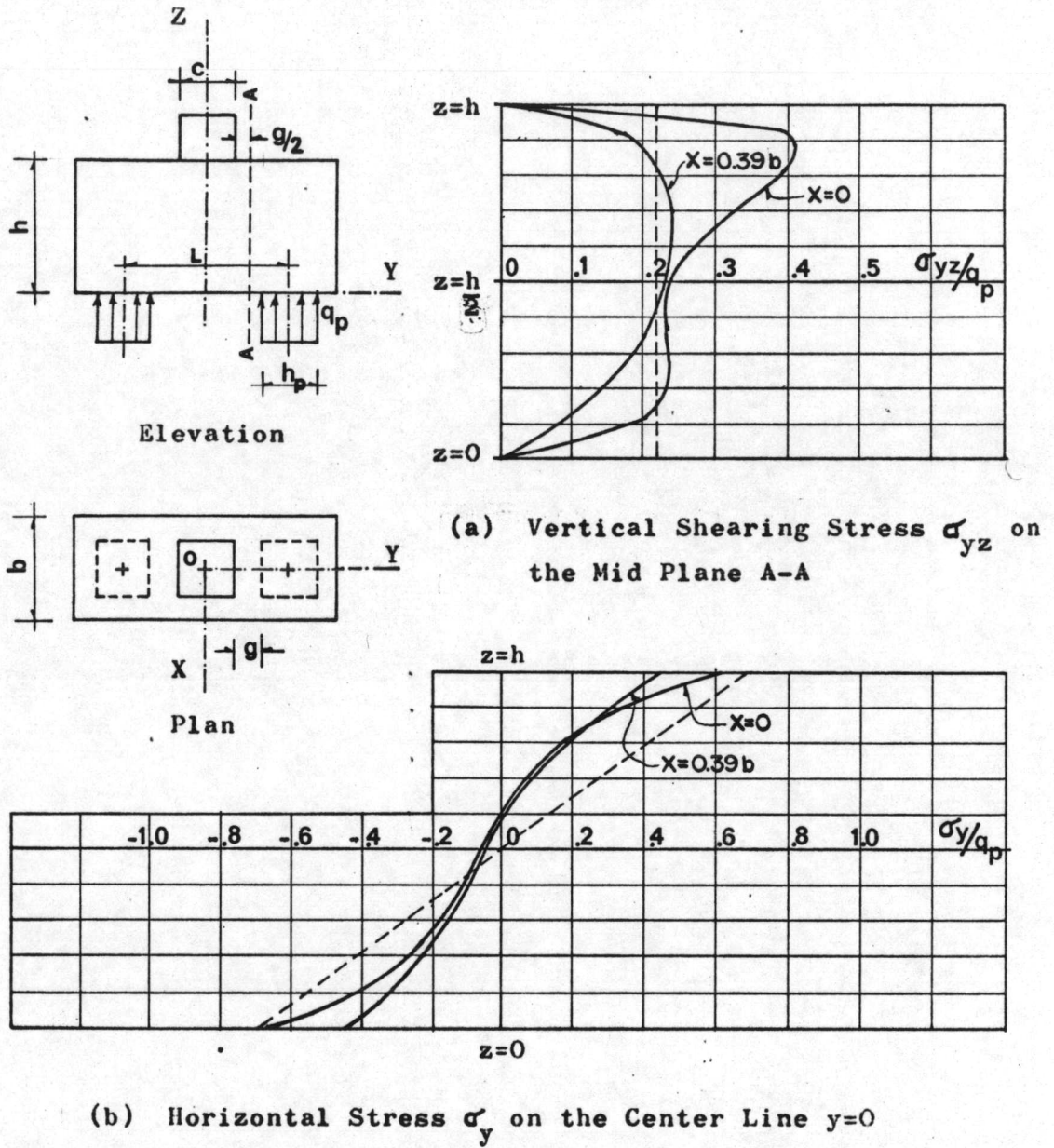


Fig. 6.16 Crack Patterns in Four-Pile Cap Models

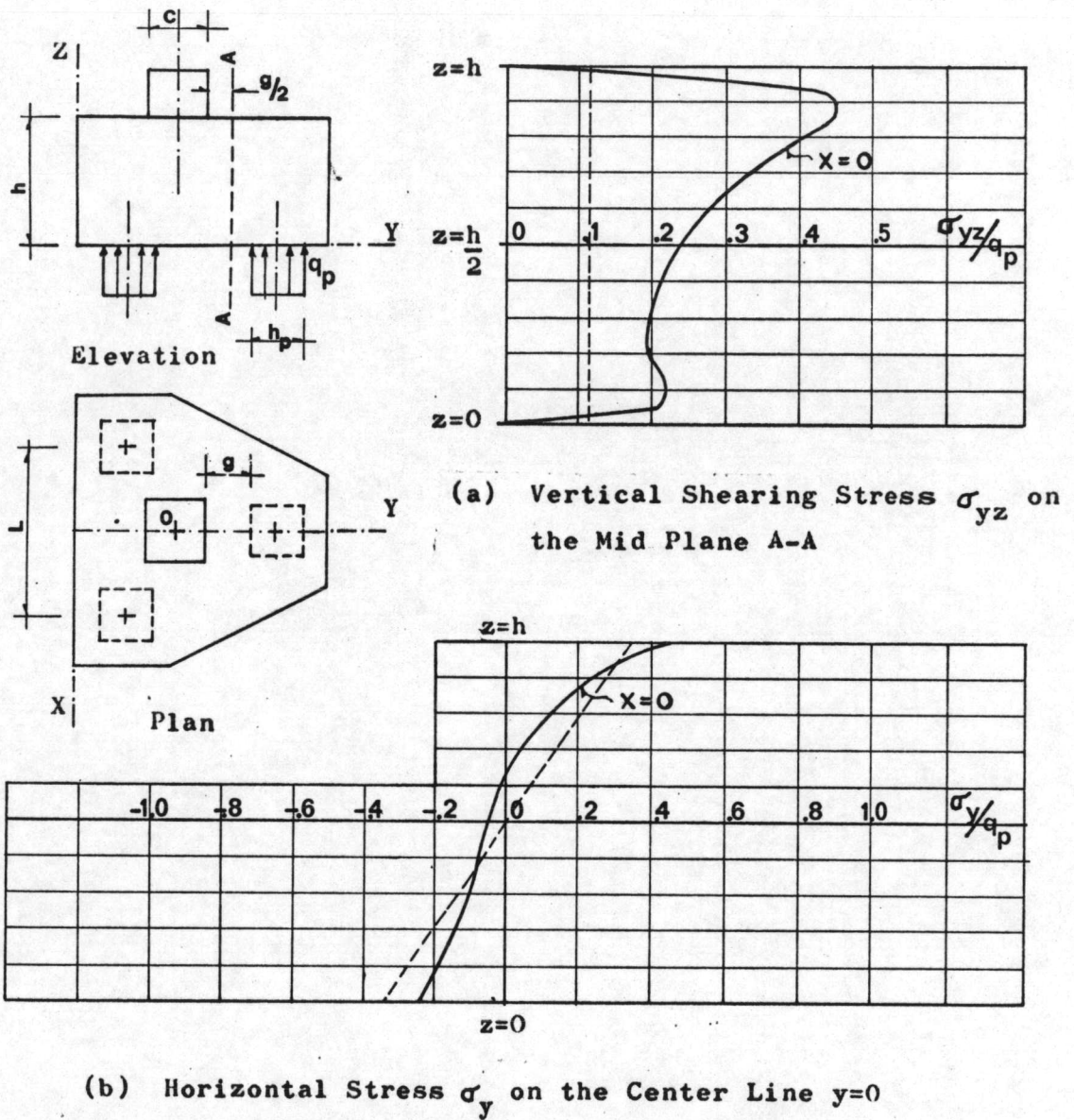
APPENDIX A

Stress Distributions in Pile Caps Obtained by Finite Element Method



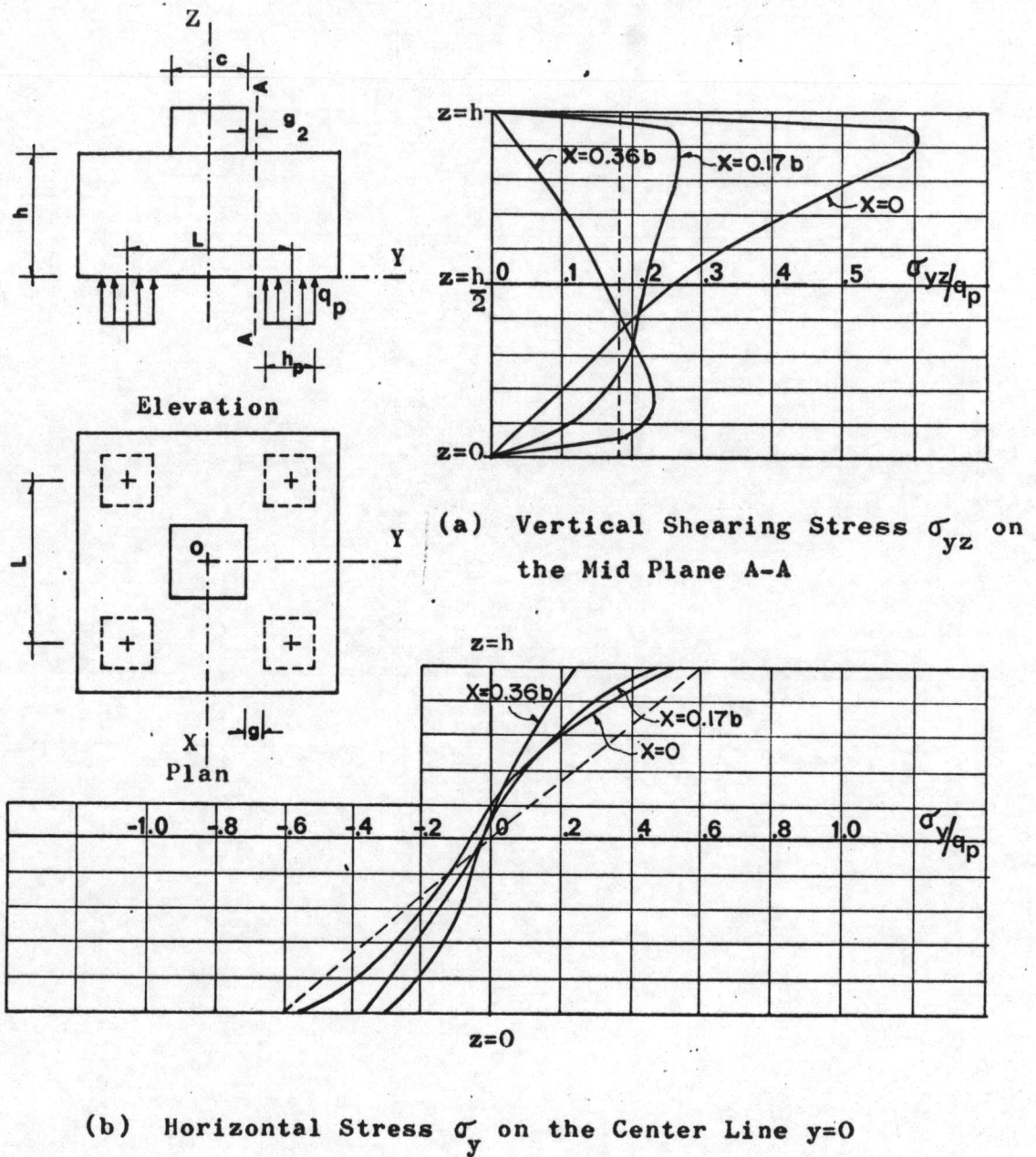
Note; ---- according to simple beam theory

Fig. A.1 Normalized Elastic Distribution of Horizontal Stress and Vertical Shearing Stress in Two-Pile Cap



Note; ---- according to simple beam theory

Fig. A.2 Normalized Elastic Distribution of Horizontal Stress and Vertical Shearing Stress in Three-Pile Cap



Note; ---- according to simple beam theory

Fig. A.3 Normalized Elastic Distribution of Horizontal Stress and Vertical Shearing Stress in Four-Pile Cap

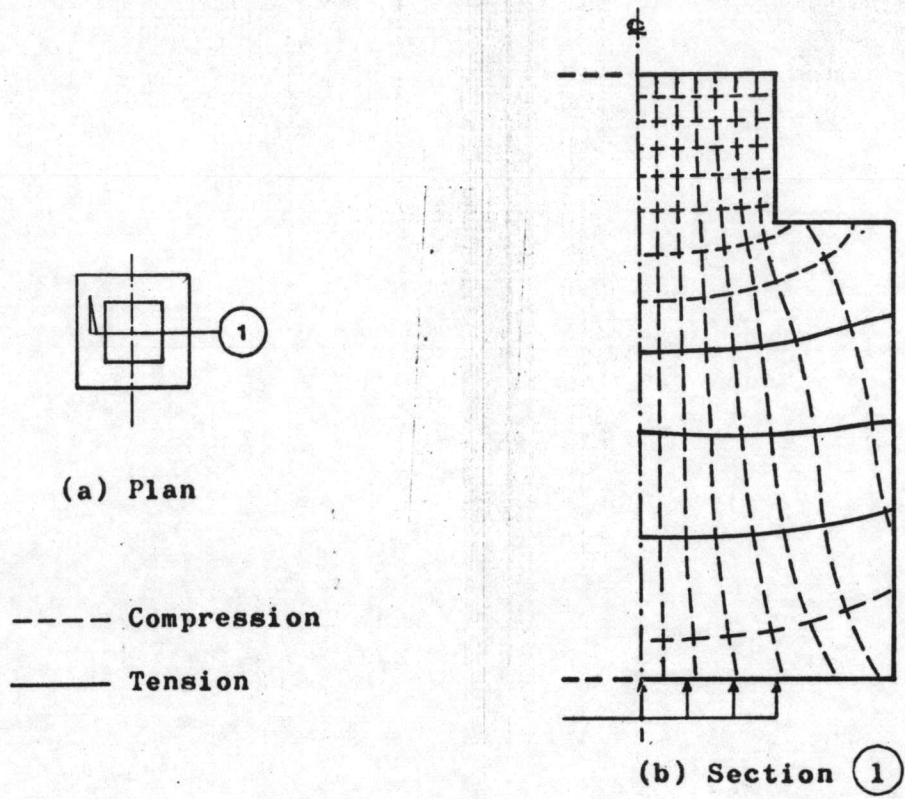


Fig. A.4 Principal Stress Trajectories in Single-Pile Cap

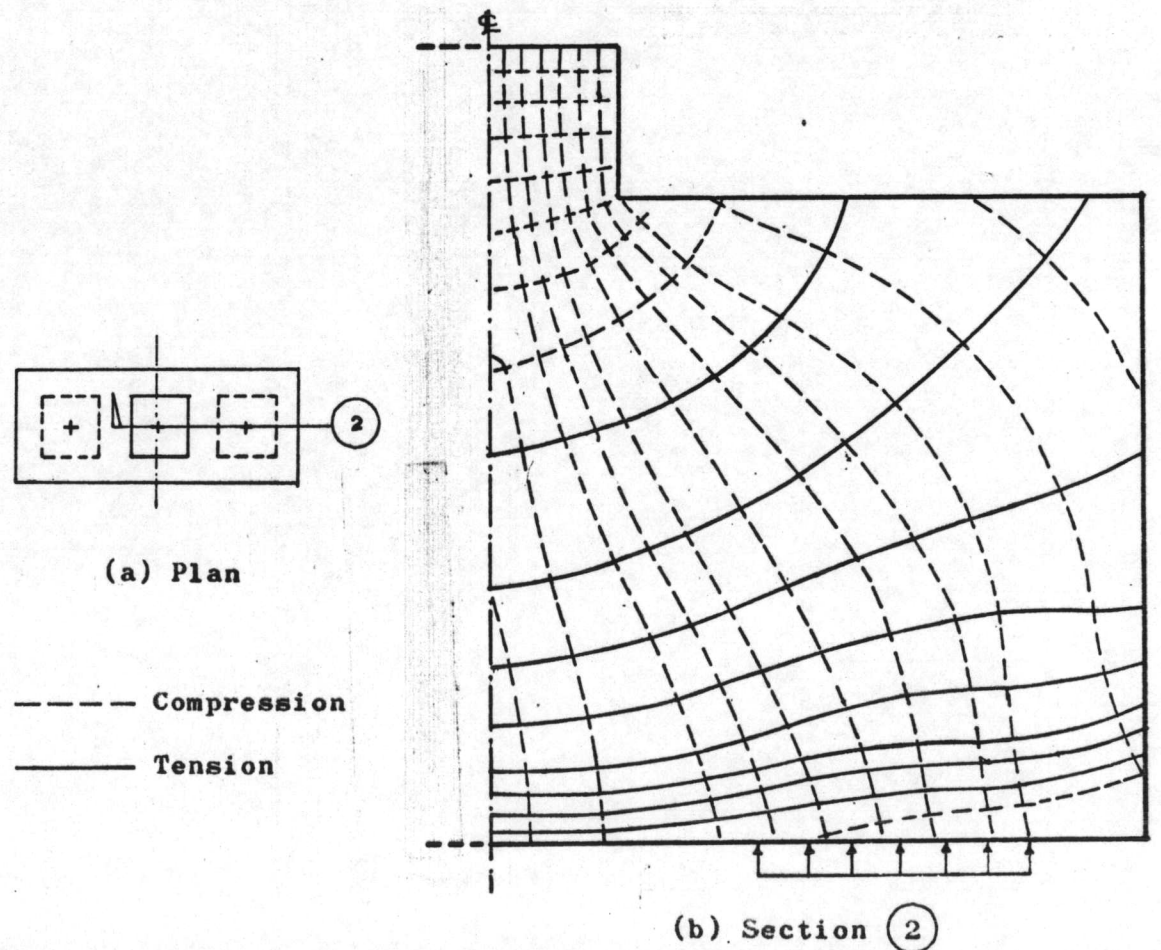


Fig. A.5 Principal Stress Trajectories in Two-Pile Cap

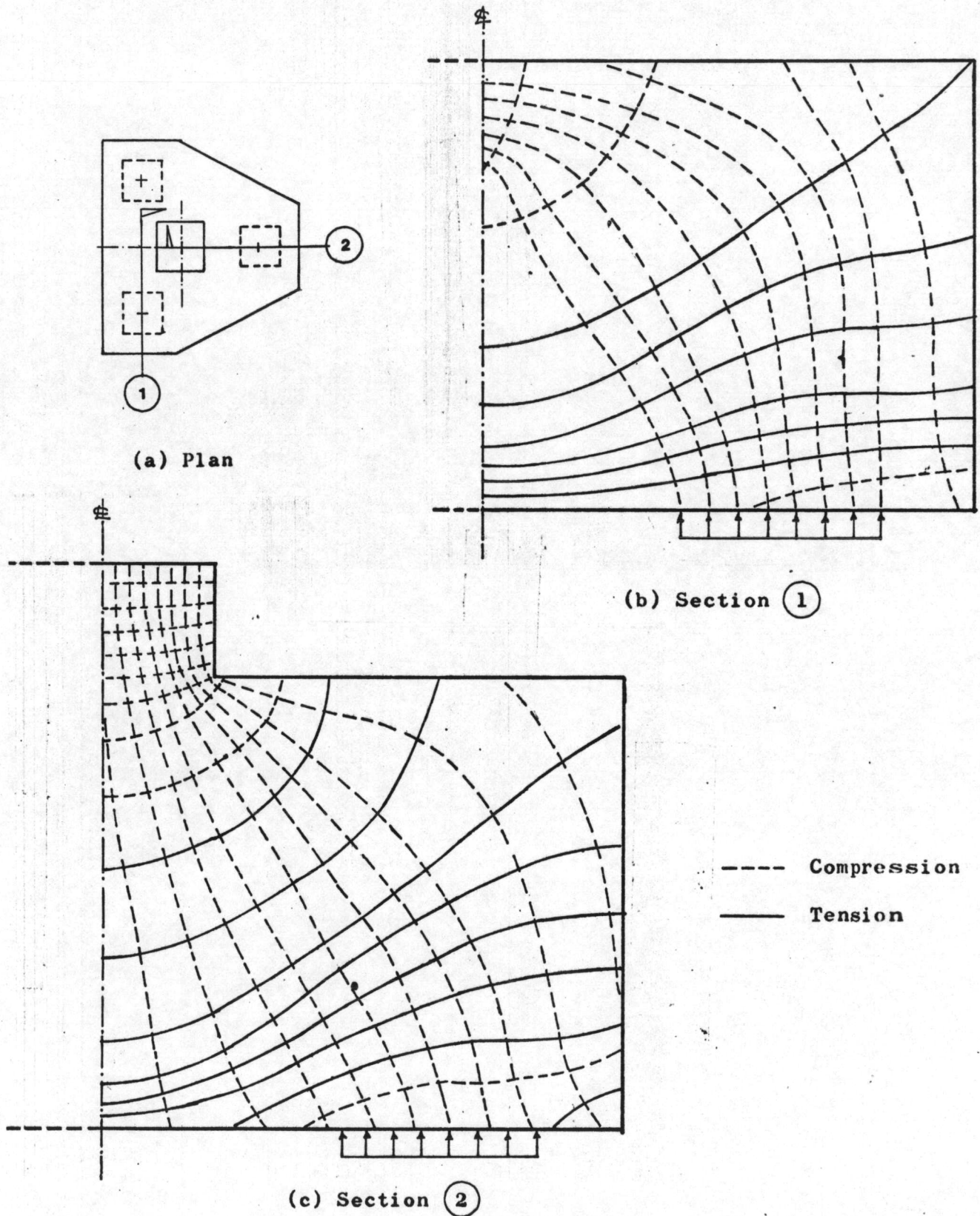
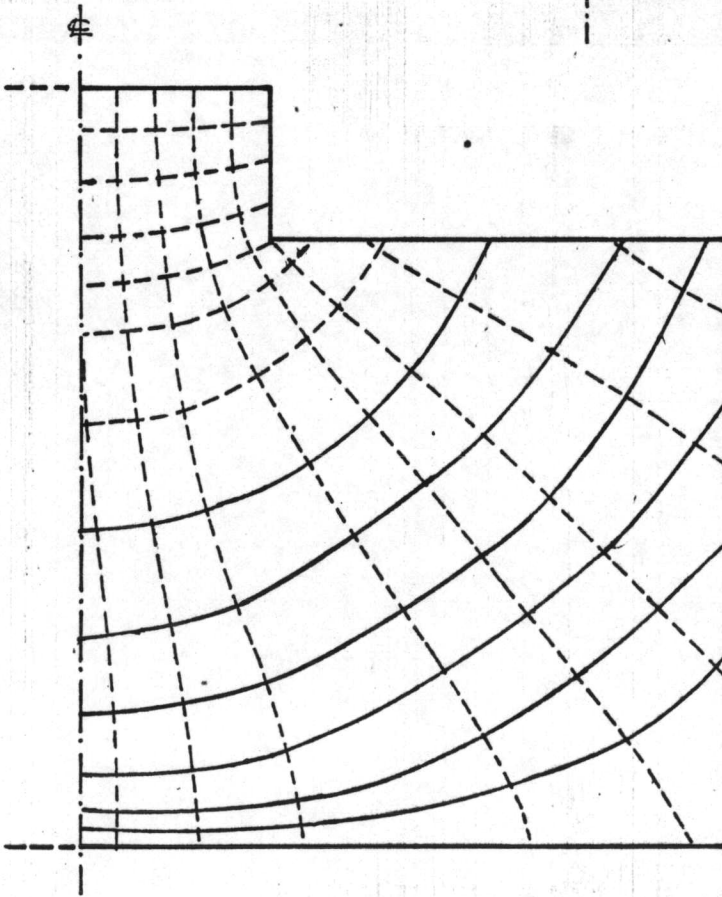
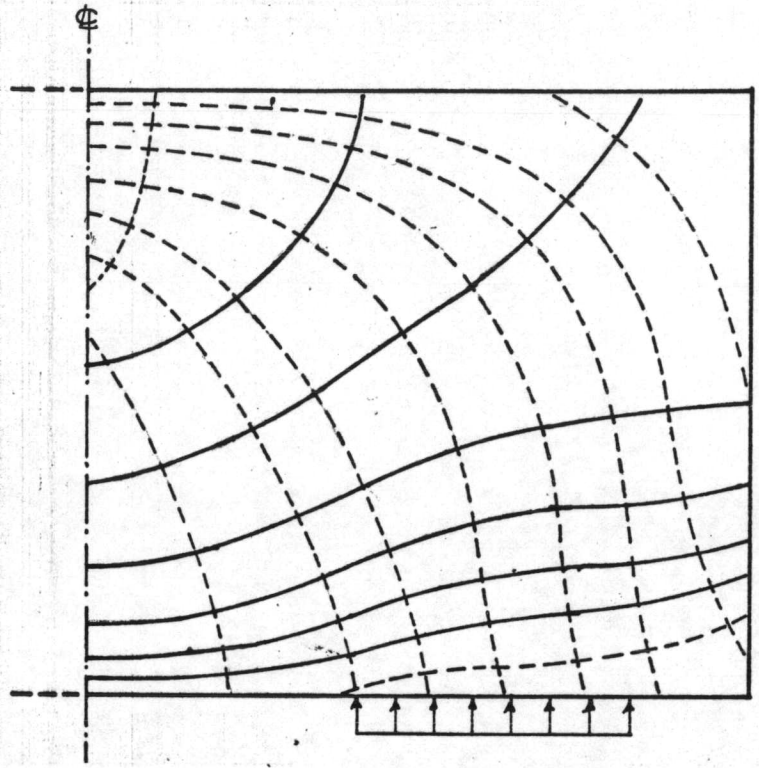
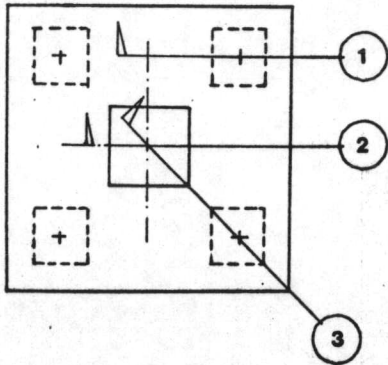
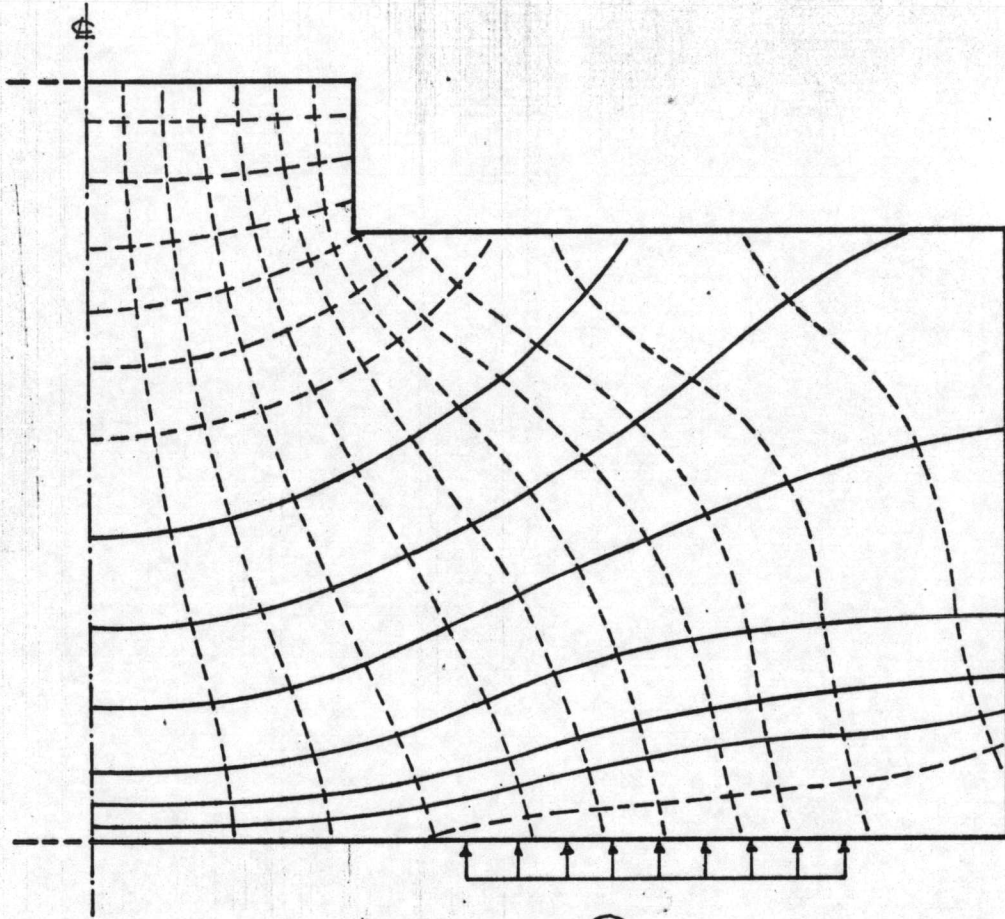


Fig. A.6 Principal Stress Trajectories in Three-Pile Cap



----- Compression
———— Tension

Fig. A.7 Principal Stress Trajectories in Four-Pile Cap



(c) Section ③

Fig. A.7 Principal Stress Trajectories in Four-Pile Cap

APPENDIX B

Sample of Calculations



B.1 Flexural Strength

Fig. 3.9-3.10 illustrate the assumptions made in the analysis of flexural strength in pile cap at cracking and ultimate conditions. Two concepts of approach, beam analogy and truss analogy, are used in calculation for each form of reinforcement arrangement in pile cap. The mechanical properties of steel and concrete are summarized in Table 2-3.

a) Cracking Loads

Three-Pile Cap;

$$d = 25 \text{ cm.}, h = 28.3 \text{ cm.}, b = 47.3 \text{ cm.}, L = 35 \text{ cm.}, \\ n = 9, f_s = 1700 \text{ ksc.}, f_y = 3400 \text{ ksc.}, A_s = 1.909 \text{ cm.}^2$$

$$\text{P3-1; } M_{cr} = \frac{I f_r}{y_t} \quad (\text{eq. 3.16}) \\ = \frac{47.3 \times 28.3^3 \times 31.93}{12 \times 14.15} = 201,596 \text{ kg-cm.}$$

$$P_{cr} = \frac{3M_{cr}}{12.7} = \underline{47,620 \text{ kg.}}$$

$$\text{P3-2; } P_{cr} = \frac{18T_c L_c d_c}{(2L_c^2 - c^2)} + \frac{18T_s L d_c}{(2L^2 - c^2)} \quad (\text{eq. 3.20})$$

$$\text{where } T_c = (hc/2)(f_r/2) = \frac{28.3 \times 15 \times 32.73}{4} = 3,473 \text{ kg.}$$

$$T_s = n f_r A_s = 9 \times 32.73 \times 1.909 = 562 \text{ kg.}$$

$$L_c = \frac{3L}{4} = 26.25 \text{ cm.}, d_c = \frac{3h}{4} = 21.23 \text{ cm.}$$

$$\text{thus, } P_{cr} = \frac{18 \times 3473 \times 26.25 \times 21.23}{(2 \times 26.25^2 - 15^2)} + \frac{18 \times 562 \times 35 \times 25}{(2 \times 35^2 - 15^2)} \\ = 30,205 + 3,980 = \underline{34,185 \text{ kg.}}$$

$$\text{P3-3; } M_{cr} = \frac{I f_r}{g_r y_t} = \frac{47.3 \times 28.3^3 \times 30.02}{12 \times 14.15} = 189,536 \text{ kg-cm.}$$

$$P_{cr} = \frac{3M_{cr}}{12.7} = \underline{44,772 \text{ kg.}}$$

$$\text{P3-4; } P_{cr} = \frac{18T_c L d_c}{\sqrt{3}(2L_c^2 - c^2)} + \frac{18T_s L d_s}{\sqrt{3}(2L_c^2 - c^2)} \quad (\text{eq. 3.21})$$

$$T_c = (hc/2)(f_r/2) = \frac{28.3 \times 15 \times 31.75}{4} = 3,370 \text{ kg.}$$

$$T_s = n f_r A_s = 9 \times 31.75 \times 1.909 = 545 \text{ kg.}$$

$$\begin{aligned} \text{thus, } P_{cr} &= \frac{18 \times 3370 \times 26.25 \times 21.23}{\sqrt{3}(2 \times 26.25^2 - 15^2)} + \frac{18 \times 545 \times 35 \times 25}{\sqrt{3}(2 \times 35^2 - 15^2)} \\ &= \underline{19,149 \text{ kg.}} \end{aligned}$$

Four-Pile Cap ;

$$\begin{aligned} d &= 25 \text{ cm. , } h = 28.3 \text{ cm. , } b = 56.6 \text{ cm. , } L = 35 \text{ cm. ,} \\ n &= 9 , f_s = 1700 \text{ ksc. , } f_y = 3400 \text{ ksc. , } A_s = 3.817 \text{ cm}^2 \end{aligned}$$

$$\text{P4-1; } M_{cr} = \frac{I f_r}{g_r y_t} = 56.6 \times 28.3 \times 29.89 = 225,820 \text{ kg-cm.}$$

$$P_{cr} = \frac{2M_{cr}}{10} = \underline{45,164 \text{ kg.}}$$

$$\text{P4-2; } P_{cr} = \frac{24T_c L d_c}{(3L_c^2 - c^2)} + \frac{24T_s L d_s}{(3L_c^2 - c^2)} \quad (\text{eq. 3.22})$$

$$\text{where, } T_c = (hc/2)(f_r/2) = \frac{28.3 \times 15 \times 28.81}{4} = 3,058 \text{ kg.}$$

$$T_s = n f_r A_s = 9 \times 28.81 \times 1.909 = 495 \text{ kg.}$$

$$L_c = \frac{3L}{4} = 26.25 \text{ cm. , } d_c = \frac{3h}{4} = 21.23 \text{ cm.}$$

$$\text{thus, } P_{cr} = \frac{24 \times 3058 \times 26.25 \times 21.23}{(3 \times 26.25^2 - 15^2)} + \frac{24 \times 495 \times 35 \times 25}{(3 \times 35^2 - 15^2)}$$

$$= \underline{25,206 \text{ kg.}}$$

$$\underline{\text{P4-3;}} \quad P_{cr} = \frac{24T_c L_c d_c}{\sqrt{2}(3L_c^2 - c^2)} + \frac{24T_s L_d}{\sqrt{2}(3L^2 - c^2)} \quad (\text{eq. 3.23})$$

$$T_c = (hc/2)(f_r/2) = \frac{28.3 \times 15 \times 30.28}{4} = 3,214 \text{ kg.}$$

$$T_s = n f_r A_s = 9 \times 30.28 \times 3.817 = 1,040 \text{ kg.}$$

$$\text{thus,} \quad P_{cr} = \frac{24 \times 3214 \times 26.25 \times 21.23}{\sqrt{2}(3 \times 26.25^2 - 15^2)} + \frac{24 \times 1040 \times 35 \times 25}{\sqrt{2}(3 \times 35^2 - 15^2)}$$

$$= \underline{20,976 \text{ kg.}}$$

$$\underline{\text{P4-4;}} \quad P_{cr} = \frac{24T_c L_c d_c}{(3L_c^2 - c^2)} + \frac{24T_s L_d}{(3L^2 - c^2)} \quad (\text{eq. 3.22})$$

$$\text{where} \quad T_c = (hc/2)(f_r/2) = \frac{28.3 \times 15 \times 30.86}{4} = 3275 \text{ kg.}$$

$$T_s = n f_r A_s = 9 \times 30.86 \times 1.272 = 353 \text{ kg./ edge \& diag.}$$

$$\text{thus,} \quad P_{cr} = \frac{24 \times 3275 \times 26.25 \times 21.23}{(3 \times 26.25^2 - 15^2)} + \frac{24 \times 353 \times 35 \times 25}{(3 \times 35^2 - 15^2)}$$

$$+ \frac{24 \times 353 \times 35 \times 25}{\sqrt{2}(3 \times 35^2 - 15^2)} = \underline{27,446 \text{ kg.}}$$

b) Ultimate Loads :

Three-Pile Cap;

$$d = 25 \text{ cm.}, \quad b = 47.3 \text{ cm.}, \quad L = 35 \text{ cm.}, \quad f_y = 3400 \text{ ksc.}$$

$$A_s = 1.909 \text{ cm.}^2$$

$$\underline{\text{P3-1;}} \quad M_u = \phi A_s f_y \frac{(d-a)}{2} \quad (\text{eq. 3.18})$$

$$= 0.9 \times 1.909 \times 3400 \left(25 - \frac{1.909 \times 3400}{0.85 \times 258 \times 47.3} \right)$$

$$= 142,383 \text{ kg-cm.}$$

$$P_u = \frac{3M_u}{12.7} = \underline{33,634 \text{ kg.}}$$

$$\underline{\text{P3-2;}} \quad P_u = \frac{18A_s f_y L_d}{(2L^2 - c^2)} \quad (\text{eq. 3.25})$$

$$= \frac{18 \times 1.909 \times 3400 \times 35 \times 25}{(2 \times 35^2 - 15^2)} = \underline{45,945 \text{ kg.}}$$

$$\begin{aligned} \underline{P3-3}; \quad M_u &= \phi A_s f_y \left(\frac{d-a}{2} \right) \\ &= 0.9 \times 3.18 \times 3400 \left(25 - \frac{3.18 \times 3400}{0.85 \times 228 \times 47.3} \right) \\ &= 231,793 \text{ kg-cm.} \end{aligned}$$

$$\text{thus } P_u = \frac{3M_u}{12.7} = \underline{54,754 \text{ kg.}}$$

$$\begin{aligned} \underline{P3-4}; \quad P_u &= \frac{18 A_s f_y L d}{\sqrt{3}(2L^2 - c^2)} \quad (\text{eq. 3.26}) \\ &= \frac{18 \times 1.909 \times 3400 \times 35 \times 25}{\sqrt{3}(2 \times 35^2 - 15^2)} = \underline{26,526 \text{ kg.}} \end{aligned}$$

Four-Pile Cap ;

$$d = 25 \text{ cm.}, \quad b = 56.6 \text{ cm.}, \quad L = 35 \text{ cm.}, \quad f_y = 3400 \text{ ksc.}$$

$$A_s = 3.817 \text{ cm}^2$$

$$\begin{aligned} \underline{P4-1}; \quad M_u &= \phi A_s f_y \left(\frac{d-a}{2} \right) \\ &= 0.9 \times 3.817 \times 3400 \left(25 - \frac{3.817 \times 3400}{0.85 \times 226 \times 56.6} \right) \\ &= 278,059 \text{ kg-cm.} \end{aligned}$$

$$P_u = \frac{2M_u}{10} = \underline{55,612 \text{ kg.}}$$

$$\begin{aligned} \underline{P4-2}; \quad P_u &= \frac{24 A_s f_y L d}{(3L^2 - c^2)} \quad (\text{eq. 3.27}) \\ &= \frac{24 \times 1.909 \times 3400 \times 35 \times 25}{(3 \times 35^2 - 15^2)} \\ &= \underline{39,508 \text{ kg.}} \end{aligned}$$

$$\begin{aligned} \underline{P4-3}; \quad P_u &= \frac{24 A_s f_y L d}{\sqrt{2}(3L^2 - c^2)} \quad (\text{eq. 3.28}) \\ &= \frac{24 \times 3.817 \times 3400 \times 35 \times 25}{\sqrt{2}(3 \times 35^2 - 15^2)} = \underline{55,858 \text{ kg.}} \end{aligned}$$

$$\begin{aligned}
 \underline{P4-4}; \quad P_{cr} &= \frac{24A f Ld}{s_y (3L^2 - c^2)} + \frac{24A f Ld}{s_y \sqrt{2}(3L^2 - c^2)} \quad (\text{eq. 3.27 \& 3.28}) \\
 &= \frac{24 \times 1.272 \times 3400 \times 35 \times 25}{(3 \times 35^2 - 15^2)} + \frac{24 \times 1.272 \times 3400 \times 35 \times 25}{\sqrt{2}(3 \times 35^2 - 15^2)} \\
 &= \underline{44,939 \text{ kg.}}
 \end{aligned}$$

B.1 Shear Strength

a) Punching Shear: ACI⁽¹⁾

$$v = 1.06 \sqrt{f'_c}, \quad P_v = v b_o d$$

Three-Pile Cap;

$$\underline{P3-1}; \quad v = 1.06 \times 0.85 / \sqrt{258} = 14.47 \text{ ksc.}$$

$$P_v = 14.47 \times 160 \times 25 = \underline{57,889 \text{ kg.}}$$

$$\underline{P3-2}; \quad v = 1.06 \times 0.85 / \sqrt{271} = 14.83 \text{ ksc.}$$

$$P_v = 14.83 \times 160 \times 25 = \underline{59,329 \text{ kg.}}$$

$$\underline{P3-3}; \quad v = 1.06 \times 0.85 / \sqrt{228} = 13.60 \text{ ksc.}$$

$$P_v = 13.60 \times 160 \times 25 = \underline{54,419 \text{ kg.}}$$

$$\underline{P3-4}; \quad v = 1.06 \times 0.85 / \sqrt{255} = 14.39 \text{ ksc.}$$

$$P_v = 14.39 \times 160 \times 25 = \underline{57,551 \text{ kg.}}$$

Four-Pile Cap;

$$\underline{P4-1}; \quad v = 1.06 \times 0.85 / \sqrt{226} = 13.55 \text{ ksc.}$$

$$P_v = 13.55 \times 160 \times 25 = \underline{54,180 \text{ kg.}}$$

$$\underline{P4-2}; \quad v = 1.06 \times 0.85 / \sqrt{210} = 13.06 \text{ ksc.}$$

$$P_v = 13.06 \times 160 \times 25 = \underline{52,227 \text{ kg.}}$$

$$\underline{P4-3}; \quad v = 1.06 \times 0.85 / \sqrt{232} = 13.72 \text{ ksc.}$$

$$P_v = 13.72 \times 160 \times 25 = \underline{54,894 \text{ kg.}}$$

$$\underline{P4-4}; \quad v = 1.06 \times 0.85 / \sqrt{241} = 13.99 \text{ ksc.}$$

$$P_v = 13.99 \times 160 \times 25 = \underline{55,949 \text{ kg.}}$$

b) Ultimate Shear Strength : Corbel Design⁽²⁾

$$v_u = 1.72(1 - 0.5a/d)(1 + 64 \rho) \sqrt{f'_c}$$

where, a = shear span

ρ = steel ratio

Three-Pile Cap;

$$\underline{P3-1}; \quad v_u = 1.72(1 - .5 \times \frac{12.7}{25})(1 + 64 \times 0.00269) / \sqrt{258} = 24.16 \text{ ksc.}$$

$$P_{vu} = 3 \times 24.16 \times 47.3 \times 25 = \underline{85,697 \text{ kg.}}$$

$$\underline{P3-2}; \quad v_u = 1.72(1 - .5 \times \frac{12.7}{25})(1 + 64 \times 0.00279) / \sqrt{271} = 24.90 \text{ ksc.}$$

$$P_{vu} = 3 \times 24.90 \times 47.3 \times 25 = \underline{88,336 \text{ kg.}}$$

$$\underline{P3-3}; \quad v_u = 1.72(1 - .5 \times \frac{12.7}{25})(1 + 64 \times 0.00269) / \sqrt{228} = 22.71 \text{ ksc.}$$

$$P_{vu} = 3 \times 22.71 \times 47.3 \times 25 = \underline{80,561 \text{ kg.}}$$

$$\underline{P3-4}; \quad v_u = 1.72(1 - .5 \times \frac{12.7}{25})(1 + 64 \times 0.00161) / \sqrt{255} = 22.61 \text{ ksc.}$$

$$P_{vu} = 3 \times 22.61 \times 47.3 \times 25 = \underline{80,194 \text{ kg.}}$$

Four-Pile Cap;

$$\underline{P4-1}; \quad v_u = 1.72(1 - .5 \times \frac{10}{25})(1 + 64 \times 0.00270) / \sqrt{226} = 24.26 \text{ ksc.}$$

$$P_{vu} = 2 \times 24.26 \times 56.6 \times 25 = \underline{68,645 \text{ kg.}}$$

$$\underline{P4-2}; \quad v_u = 1.72(1 - .5 \times \frac{10}{25})(1 + 64 \times 0.00270) / \sqrt{210} = 23.38 \text{ ksc.}$$

$$P_{vu} = 2 \times 23.38 \times 56.6 \times 25 = \underline{66,175 \text{ kg.}}$$

$$\underline{\text{P4-3;}} \quad v_u = \frac{1.72(1-.5x10)}{25}(1+64x.00381)\sqrt{232} = 26.07 \text{ ksc.}$$

$$P_{vu} = 2x26.07x56.6x25 = \underline{73,790 \text{ kg.}}$$

$$\underline{\text{P4-4;}} \quad v_u = \frac{1.72(1-.5x10)}{25}(1+64x.00307)\sqrt{241} = 25.56 \text{ ksc.}$$

$$P_{vu} = 2x25.56x56.6x25 = \underline{72,327 \text{ kg.}}$$

VITA

Mr. Luck Siridanupath acquired Bachelor's Degree in Engineering from Chiangmai University in 1975. He joined the Engineering Institute of Thailand and the American Concrete Institute as a junior membership in 1976. He joined the firm of Metric Co.,Ltd, Consulting Engineers & Architects in 1978. Since then he has been concerned with aspects of reinforcement detailing in concrete structures and joint detailing in steel structures.

