

## APPENDIX A

### TOTAL FLUX DENSITY DISTRIBUTION FROM A HELIOSTAT

Flux distribution on cylindrical surface by multiple aimed points. The following algorithm explains the calculation involved in MATLAB language.

```
clear
```

```
% Define window on cylindrical surface
```

```
theta = [0:360]; % define dimension of theta (0 - 360 degree)
```

```
L_theta = length (cet);
```

```
height = [800:1:1200]; % define dimension of tower height
```

```
L_height = length(height);
```

```
Flux = zeros (s_height, s_cet);
```

```
tower_H = 10; % tower height 10 m above the ground
```

```
radius = 2; % radius of cylinder
```

```
B = 0.3; A = 0.2; %
```

```
% Calculate sun position
```

```
day = 1; month = 3; LT = 10; % input day , month, time
```

```
Ls = -105; %Longitude of Thailand
```

```
Lloc = -100.53; %Longitude of Bangkok, Thailand
```

```
La = 13.735; %Latitude of Bangkok
```

```
La = La*pi/180;
```

```

i_d = day;
j_m = month;
if      j_m == 1
    dn = i_d;
elseif j_m == 2
    dn = 31+i_d;
elseif j_m == 3
    dn = 59+i_d ;
elseif j_m == 4
    dn = 90+i_d;
elseif j_m == 5
    dn = 120+i_d;
elseif j_m == 6
    dn = 151+i_d;
elseif j_m == 7
    dn = 181+i_d;
elseif j_m == 8
    dn = 212+i_d;
elseif j_m == 9
    dn = 243+i_d;
elseif j_m == 10
    dn = 273+i_d;
elseif j_m == 11
    dn = 304+i_d;
else
    dn = 335+i_d;
end

```

```

day_angle = 2*pi*(dn-1)/365;
T = day_angle;

Et=229.18*(0.000075+0.001868*cos(T)-0.032077*sin(T)-0.014615*cos(2*T)-
0.04089*sin(2*T))/60;

ST=LT+(4*(Ls-Lloc)/60)+(Et);

H=15*(12-ST)*pi/180;

Dec=23.45*sin(2*pi*(dn+284)/365)*2*pi/360;

Al=asin((cos(La1)*cos(Dec)*cos(H))+(sin(La1)*sin(Dec))); %Altitude of sun
Az=acos((sin(Al)*sin(La1)-sin(Dec))/(cos(Al)*cos(La1))); % Azimuth of sun
if ST <=12
    A_z = Az;
else
    A_z = 2*pi-Az ;
end
x = cos(Al)*cos(A_z);
y = cos(Al)*sin(A_z);
z = sin(Al);
s = [x,y,z];
J2 = sqrt((x)^2+(y)^2+(z)^2);
S = s/J2; %unit vector of sun position relative to tower base

```

#### % position of heliostats

```

load (heli)
L_h = size(heli,1);
for quandant = 1 : 4
    for p = 1:L_h      % calculate (Xo,Yo,Zo) for each heliostat
        if quandant == 1

```

```

Xo=heli(p,1);
Yo=heli(p,2);
Zo=heli(p,3);

elseif quandant == 2

Xo=-heli(p,1);
Yo=heli(p,2);
Zo=heli(p,3);

elseif quandant == 3

Xo=-heli(p,1);
Yo=-heli(p,2);
Zo=heli(p,3);

else

Xo=heli(p,1);
Yo=-heli(p,2);
Zo=heli(p,3);

end

D = [ 0-Xo, 0-Yo, tower_H-Zo];

J1 = sqrt((0-Xo)^2+(0-Yo)^2+(tower_H-Zo)^2);

R = D/J1; % unit vector from mirror to aim point

Xd = R(1,1);
Yd = R(1,2);
Zd = R(1,3);

% find intercept point on cylindrical surface due to ray reflect from center of
mirror by ray tracing technique

F= Xd^2+Yd^2;
G=2*Xo*Xd + 2*Yo*Yd;
K=Xo^2 +Yo^2-radius^2;

```

```

t10= (-G + sqrt(G^2-4*F*K))/(2*F);
t20= (-G - sqrt(G^2-4*F*K))/(2*F);
if t10 > t20
    t30 = t20;
    t40 = t10;
else
    t30 = t10;
end
t40 = t20;
if t30 > 0
    t0 = t30;
elseif t40 > 0
    t0 = t40;
else disp (' no t0 ')
end

%% X0p, Y0p , Z0p are coordinate of intercept point on cylindrical surface
X0p = Xo + t0*R(1,1);
Y0p = Yo + t0*R(1,2);
Z0p = tower_H;
Dop = [X0p-Xo,Y0p-Yo,tower_H-Zo];
Jop = sqrt((X0p-Xo)^2+(Y0p-Yo)^2+(tower_H-Zo)^2);
Rs=Jop*tan(0.25*pi/180); % Radius of solar disk
Rop = Dop/Jop; % unit vector from mirror to target
mirror_azi = atan2 (Y0p, X0p); % position azimuth of center point of mirror
if mirror_azi >= 0
    mirror_azi = mirror_azi ;
else

```

```

mirror_azi = 2*pi+ mirror_azi;
end

% find normal vector of each heliostat

N=(S+Rop);

N = N/abs(N); %% unit normal vector of each heliostat

Alt = asin(N(1,3))*180/pi; %Altitude of mirror in degree

Azm = atan2(N(1,2),N(1,1)); % Azimuth of each mirror

if Azm >= 0

    Azm = Azm;

else

    Azm = 2*pi+Azm;

end

```

**%%% vector on mirror surface when mirror parallel with ground ( from mirror center to four corner of mirror)**

```

u_old1 =[A/2;B/2;0];
u_old2=[-A/2;B/2;0];
u_old3=[-A/2;-B/2;0];
u_old4 =[A/2;-B/2;0];

Euler1=[cos(pi/2-Alt) 0 sin(pi/2-Alt);
         0          1  0;
        -sin(pi/2-Alt) 0 cos(pi/2-Alt) ] ;

Euler2 = [cos(Azm) -sin(Azm) 0;
           sin(Azm) cos(Azm) 0
           0      0      1];

Euler=Euler2*Euler1;

```

**% vector on mirror surface when operate with Euler ( from mirror center to four corner of mirror)**

```

u_new1 = Euler*u_old1 ;
u_new2 = Euler*u_old2;
u_new3 = Euler*u_old3 ;
u_new4 = Euler*u_old4;

%%%%% position of mirror after operate with Euler
new_0=[Xo;Yo;Zo];
new_1 = u_new1+[Xo;Yo;Zo];
new_2 = u_new2+[Xo;Yo;Zo];
new_3 = u_new3+[Xo;Yo;Zo];
new_4 = u_new4+[Xo;Yo;Zo];

```

**% find intercept point on image plane by ray tracing**

```

d=-(Xod*X0p+Yod*Y0p+Zod*Z0p);

% point 0 ( center point of mirror)

t0=-
(Xod*new_0(1,1)+Yod*new_0(2,1)+Zod*new_0(3,1)+d)/(Xod^2+Yod^2+Zod^2);

X00p= new_0(1,1) + t0*Rop(1,1);
Y00p= new_0(2,1) + t0*Rop(1,2);
Z00p= new_0(3,1) + t0*Rop(1,3);

% point 1

t1=-
(Xod*new_1(1,1)+Yod*new_1(2,1)+Zod*new_1(3,1)+d)/(Xod^2+Yod^2+Zod^2);

X1p= new_1(1,1) + t1*Rop(1,1);
Y1p= new_1(2,1) + t1*Rop(1,2);
Z1p= new_1(3,1) + t1*Rop(1,3);

```

```

% point 2

t2=-
(Xod*new_2(1,1)+Yod*new_2(2,1)+Zod*new_2(3,1)+d)/(Xod^2+Yod^2+Zod^2);

X2p= new_2(1,1) + t2*Rop(1,1);

Y2p= new_2(2,1) + t2*Rop(1,2);

Z2p= new_2(3,1) + t2*Rop(1,3);

% point 3

t3=-
(Xod*new_3(1,1)+Yod*new_3(2,1)+Zod*new_3(3,1)+d)/(Xod^2+Yod^2+Zod^2);

X3p= new_3(1,1) + t3*Rop(1,1);

Y3p= new_3(2,1) + t3*Rop(1,2);

Z3p= new_3(3,1) + t3*Rop(1,3);

% point 4

t4=-
(Xod*new_4(1,1)+Yod*new_4(2,1)+Zod*new_4(3,1)+d)/(Xod^2+Yod^2+Zod^2);

X4p= new_4(1,1) + t4*Rop(1,1);

Y4p= new_4(2,1) + t4*Rop(1,2);

Z4p= new_4(3,1) + t4*Rop(1,3);

%%% find effective area of principal image

Area_i=1/2*abs(((X1p*Y2p)+(X2p*Y3p)+(X3p*Y4p)+(X4p*Y1p))-
((X2p*Y1p)+(X3p*Y2p)+(X4p*Y3p)+(X1p*Y4p)));




% calculate principal image size (LH,LT) and θ*
%Azm_M =Azimuth of position mirror measure from south to eastward direction
(depend on position)

%Azm_M = Azimuth of mirror (depend on time)

%Azm_S= Azimuth of sun

%Altitude of sun

```

```

%Al_M= Altitude of mirror (depend on time)

Azm_= atan2(Yo,Xo);

if Azm_>= 0

    Azm_= Azm_;

else

    Azm_= 2*pi+Azm_;

end

tower_al=acos((tower_H-Zo)/Jop);

L_1=sqrt((sin(Azm_M-Azm_))^2*(cos(tower_al))^2+(cos(Azm_M-Azm_))^2);

b1=(sin((pi/2)-Al))^2+(sin(tower_al))^2-2*sin((pi/2)-Al_S)*sin(tower_al)*cos(Azm_S-Azm_);

b2=2+2*cos(pi/2-Al_S)*cos(tower_al)-2*sin(pi/2-Al_S)*sin(tower_al)*cos(Azm_S-Azm_);

b=sqrt(b1/b2);

L_2=sqrt((sin(Azm_M-Azm_))^2*(cos(Al_M))^2+(b*sin(tower_al)-cos(Azm_M-Azm_)*cos(tower_al)*cos(Al_M))^2);

theta_11=asin((sin(Azm_M-Azm_)*cos(tower_al))/L_1);

theta_12=acos((cos(Azm_M-Azm_)/L_1));

sa = asin((b*sin(tower_al)-cos(Azm_M-Azm_)*cos(tower_al)*cos(Alt))/L_2);

sb = acos((sin(Azm_M-Azm_)*cos(Al_M))/L_2);

theta_sta r= (sa-theta_12);

theta_star_dd = theta_star*180/pi;

theta_star_d = (round(abs(theta_star_dd)/5))*5;

if theta_star_d == 50

    fluxXX=flux50;

elseif theta_star_d == 55

    fluxXX=flux55;

elseif theta_star_d == 60

```

```
fluxXX=flux60;  
elseif theta_star_d == 65  
    fluxXX=flux65;  
elseif theta_star_d == 70  
    fluxXX=flux70;  
elseif theta_star_d == 75  
    fluxXX=flux75;  
elseif theta_star_d == 80  
    fluxXX=flux80;  
elseif theta_star_d == 85  
    fluxXX=flux85;  
elseif theta_star_d == 90  
    fluxXX=flux90;  
elseif theta_star_d == 95  
    fluxXX=flux95;  
elseif theta_star_d == 100  
    fluxXX=flux100;  
elseif theta_star_d == 105  
    fluxXX=flux105;  
elseif theta_star_d == 110  
    fluxXX=flux110;  
elseif theta_star_d == 115  
    fluxXX=flux115;  
elseif theta_star_d == 120  
    fluxXX=flux120;  
elseif theta_star_d == 125  
    fluxXX=flux125;
```

```

elseif theta_star_d == 130
    fluxXX=flux130;
elseif theta_star_d == 135
    fluxXX=flux135;
else
    fluxXX = flux140;
end

%change coordinate

Al_=acos (Rop(1,3));
Euler1=[cos(pi-Al_) 0 -sin(pi-Al_);
          0         1         0;
sin(pi-Al_) 0 cos(pi-Al_)];
Euler2=[cos(Azm_) sin(Azm_) 0 ;
        -sin(Azm_) cos(Azm_) 0;
          0         0         1];
Euler=Euler1*Euler2;

point1=[X1p;Y1p;Z1p]-[X00p;Y00p;Z00p];
point2=[X2p;Y2p;Z2p]-[X00p;Y00p;Z00p];
point3=[X3p;Y3p;Z3p]-[X00p;Y00p;Z00p];
point4=[X4p;Y4p;Z4p]-[X00p;Y00p;Z00p];
Y1=Euler*point1;
Y2=Euler*point2;
Y3=Euler*point3;
Y4=Euler*point4;
Z =[Z1p Z2p Z3p Z4p];
Z = sort(Z);

```

```

Y1=[Y1(1,1) Y2(1,1) Y3(1,1) Y4(1,1)];
Y2=[Y1(2,1) Y2(2,1) Y3(2,1) Y4(2,1)];
Y1=sort(Y1);
Y2=sort(Y2);
h_1=(Y1(1,1)/Rs);
k_1=(Y1(2,1)/Rs);
h_2=(Y2(1,1)/Rs);
k_2=(Y2(2,1)/Rs);
h_3=(Y3(1,1)/Rs);
k_3=(Y3(2,1)/Rs);
h_4=(Y4(1,1)/Rs);
k_4=(Y4(2,1)/Rs);
h1=(abs(sin(theta_star))/sin(theta_star))*(h_1*sin(sa)-k_1*cos(sb));
k1=(abs(sin(theta_star))/sin(theta_star))*(k_1*cos(theta_12)-h_1*sin(theta_11));
h2=(abs(sin(theta_star))/sin(theta_star))*(h_2*sin(sa)-k_2*cos(sb));
k2=(abs(sin(theta_star))/sin(theta_star))*(k_2*cos(theta_12)-h_2*sin(theta_11));
h3=(abs(sin(theta_star))/sin(theta_star))*(h_3*sin(sa)-k_3*cos(sb));
k3=(abs(sin(theta_star))/sin(theta_star))*(k_3*cos(theta_12)-h_3*sin(theta_11));
h4=(abs(sin(theta_star))/sin(theta_star))*(h_4*sin(sa)-k_4*cos(sb));
k4=(abs(sin(theta_star))/sin(theta_star))*(k_4*cos(theta_12)-h_4*sin(theta_11));
x=[h1 h2 h3 h4];
x=sort(x);
h_min=x(1,1);
h_max=x(1,4);
y=[k1 k2 k3 k4];
y=sort(y);
k_min=y(1,1);

```

```

k_max=y(1,4);
Ax=h_min;
Ay=k_min;
Bx=h_max;
By=k_min;
Cx=h_max;
Cy=k_max;
Dx=h_min;
Dy=k_max;

% Move the origin of coordinate  $(\xi^*, \eta^*)$  to the corner A, calculate  $\Phi_A$ .
h1_s=Ax-Ax;
k1_s=Ay-Ay;
h2_s=Bx-Ax;
k2_s=By-Ay;
h3_s=Cx-Ax;
k3_s=Cy-Ay;
h4_s=Dx-Ax;
k4_s=Dy-Ay;
p01=0.05;
h=[h1_s-6*Rs:p01:h2_s+6*Rs];
k=[k1_s-6*Rs:p01:k3_s+6*Rs];
h=h';
l_h=length(h);
l_k=length(k);
inter_h = zeros(1,l_h);
inter_k = zeros(l_k,1);
for j = 1:l_k

```

for i = 1:l\_h

if     h(i) > 1 & k(j) > 1

flA(i,j) = 1;

elseif   h(i) < -1 | k(j) < -1

flA(i,j) =0;

elseif  h(i) > 1 & k(j) < 1

h(i)=1;

n=(1+h(i))/0.05;

m=(1+k(j))/0.05;

n=round(n);

m=round(m);

flA(i,j) =fluxXX( n+1,m+1);

elseif  h(i) < 1 & k(j) > 1

k(j)=1;

n=(1+h(i))/0.05;

m=(1+k(j))/0.05;

n=round(n);

m=round(m);

flA(i,j) =fluxXX( n+1,m+1);

else

n=(1+h(i))/0.05;

m=(1+k(j))/0.05;

n=round(n);

m=round(m);

flA(i,j) =fluxXX( n+1,m+1);

```

    end
end

% Move the origin of coordinate  $(\xi^*, \eta^*)$  to the corner  $B$ , calculate  $\Phi_B$ 

h1_s=Ax-Bx;
k1_s=Ay-By;
h2_s=Bx-Bx;
k2_s=By-By;
h3_s=Cx-Bx;
k3_s=Cy-By;
h4_s=Dx-Bx;
k4_s=Dy-By;
h=[h1_s-6*Rs:p01:h2_s+6*Rs];
k=[k1_s-6*Rs:p01:k3_s+6*Rs];
l_h=length(h);
l_k=length(k);
inter_h = zeros(l_h,l);
inter_k = zeros(1,l_k);
fIB=zeros(l_h,l_k);
for j = 1:l_k
    for i = 1:l_h
        if h(i) > 1 & k(j) > 1
            fIB(i,j) = 1;
        elseif h(i) < -1 | k(j) < -1
            fIB(i,j) = 0;
        elseif h(i) > 1 & k(j) < 1

```

```

h(i)=1;
n=(1+h(i))/0.05;
m=(1+k(j))/0.05;
n=round(n);
m=round(m);
fLB(i,j)=fluxXX( n+1,m+1);

elseif h(i) < 1 & k(j) > 1
k(j)=1;
n=(1+h(i))/0.05;
m=(1+k(j))/0.05;
n=round(n);
m=round(m);
fLB(i,j)=fluxXX( n+1,m+1);

else
n=(1+h(i))/0.05;
m=(1+k(j))/0.05;
n=round(n);
m=round(m);
fLB(i,j)=fluxXX( n+1,m+1);

end
end

% Move the origin of coordinate  $(\xi^*, \eta^*)$  to the corner  $C$ , calculate  $\Phi_c$ 
h1_s=Ax-Cx;
k1_s=Ay-Cy;
h2_s=Bx-Cx;

```

```

k2_s=By-Cy;
h3_s=Cx-Cx;
k3_s=Cy-Cy;
h4_s=Dx-Cx;
k4_s=Dy-Cy;
k11=y(1,2)-Cy;
k12=y(1,3)-Cy;
h=[h1_s-6*Rs:p01:h2_s+6*Rs];
k=[k1_s-6*Rs:p01:k3_s+6*Rs];
l_h=length(h);
l_k=length(k);
inter_h = zeros(l_h,1);
inter_k = zeros(1,l_k);
flC=zeros(l_h,l_k);
for j = 1:l_k
    for i = 1:l_h
        if h(i) > 1 & k(j) > 1
            flC(i,j) = 1;
        elseif h(i) < -1 | k(j) < -1
            flC(i,j) =0;
        elseif h(i) > 1 & k(j) < 1
            h(i)=1;
            n=(1+h(i))/0.05;
            m=(1+k(j))/0.05;
            n=round(n);
            m=round(m);
        end
    end
end

```

```

flC(i,j)=fluxXX( n+1,m+1);

elseif h(i)<1 & k(j)>1
    k(j)=1;
    n=(1+h(i))/0.05;
    m=(1+k(j))/0.05;
    n=round(n);
    m=round(m);
    flC(i,j)=fluxXX( n+1,m+1);

else
    n=(1+h(i))/0.05;
    m=(1+k(j))/0.05;
    n=round(n);
    m=round(m);
    flC(i,j)=fluxXX( n+1,m+1);

end
end

% Move the origin of coordinate  $(\xi^*, \eta^*)$  to the corner D, calculate  $\Phi_D$ 

h1_s=Ax-Dx;
k1_s=Ay-Dy;
h2_s=Bx-Dx;
k2_s=By-Dy;
h3_s=Cx-Dx;
k3_s=Cy-Dy;
h4_s=Dx-Dx;

```

```

k4_s=Dy-Dy;
k11=y(1,2)-Dy;
k12=y(1,3)-Dy;
h=[h1_s-6*Rs:p01:h2_s+6*Rs];
k=[k1_s-6*Rs:p01:k3_s+6*Rs];
l_h=length(h);
l_k=length(k);
inter_h=zeros(l_h,1);
inter_k=zeros(1,l_k);
fID=zeros(l_h,l_k);
for j = 1:l_k
    for i = 1:l_h
        if h(i) > 1 & k(j) > 1
            fID(i,j) = 1;
        elseif h(i) < -1 | k(j) < -1
            fID(i,j) = 0;
        elseif h(i) > 1 & k(j) < 1
            h(i)=1;
            n=(1+h(i))/0.05;
            m=(1+k(j))/0.05;
            n=round(n);
            m=round(m);
            fID(i,j) = fluxXX( n+1,m+1);
        elseif h(i) < 1 & k(j) > 1
            k(j)=1;
            n=(1+h(i))/0.05;
        end
    end
end

```

```

m=(1+k(j))/0.05;

n=round(n);

m=round(m);

fID(i,j)=fluxXX( n+1,m+1);

else

n=(1+h(i))/0.05;

m=(1+k(j))/0.05;

n=round(n);

m=round(m);

fID(i,j)=fluxXX( n+1,m+1);

end

end

fl=(fIA+fIC-fIB-fID);

A_i = sum(fI);

flu_i = sum(A_i');

energy = flu_i*(0.05*Rs)*(0.05*Rs);

factor = Area_i/energy;

if quandant == 2

if Xo > -0.15 | Yo < 0.15

fl = 0*fI;

else

fl= fl;

end

elseif quandant == 4

if Xo < 0.15 | Yo > -0.15

```

```

fl = 0*fl;
else
    fl= fl;
end
else
    fl= fl;
end

h12=[Ax-6*Rs:0.05:Bx+6*Rs];
k12=[Ay-6*Rs:0.05:Cy+6*Rs];
l_h=length(h12);
l_k=length(k12);
km=[ cos(theta_12) cos(sb);
      sin(theta_11) sin(sa)];
Euler_INV=inv(Euler);
cylindrical=zeros(s_height,s_cet);

% transform image plane to x-y-z

for j=1:l_k
    for i=1:l_h
        xx(i,j)=(h12(i)*km(1,1)+k12(j)*km(1,2))*Rs;
        yy(i,j)=(k12(j)*km(2,2)+h12(i)*km(2,1))*Rs;
        Xx(i,j)=xx(i,j)*Euler_INV(1,1)+yy(i,j)* Euler_INV (1,2)+X0p;
        Yy(i,j)=xx(i,j)* Euler_INV (2,1)+yy(i,j)* Euler_INV (2,2)+Y0p;
        Zz(i,j)=xx(i,j)* Euler_INV (3,1)+yy(i,j)* Euler_INV (3,2)+Z0p;
        Xx(i,j)=Xx(i,j)* l00;
        Yy(i,j)=Yy(i,j)* l00;
        Zz(i,j)=round(Zz(i,j)* l00);
    end
end

```

```

rho1(i,j)=atan2(Yy(i,j),Xx(i,j));
rho1(i,j)=rho1(i,j)*180/pi;
if rho1(i,j) >= 0
    rho1(i,j)= rho1(i,j);
else
    rho1(i,j)= 360+rho1(i,j);
end

rho1(i,j)=round(rho1(i,j));

tt(i,j)=(sqrt(Xx(i,j)^2+Yy(i,j)^2)-200)/sin(tower_al);

X(i,j)=Xx(i,j)+tt(i,j)*Rop(1,1);
Y(i,j)=Yy(i,j)+tt(i,j)*Rop(1,2);
Z(i,j)=Zz(i,j)+tt(i,j)*Rop(1,3);

Z(i,j)=round(Z(i,j));
rho2(i,j)=atan2( Y(i,j),X(i,j));
rho2(i,j)=rho2(i,j)*180/pi;
if rho2(i,j) >= 0
    rho2(i,j)= rho2(i,j);
else
    rho2(i,j)= 360+rho2(i,j);
end

rho2(i,j)=round(rho2(i,j));

if fl(i,j) > 1
    fl(i,j) == 1;
else
    fl(i,j) = fl(i,j);
end

cylindrical(Z(i,j),rho2(i,j)+1)=fl(i,j)*sin(tower_al)*factor;

```

```
end  
end  
Flux = cylindrical + Flux;  
end  
end  
xlabel('theta(degree)')  
ylabel('tower height (cm.)')  
zlabel('flux dimensionless / Fo')  
title('solar flux density distribution of 12/1/1')  
surf(Flux(900:1100,1:360))  
view([-27,66])
```

## APPENDIX B

### RELATION OF SOLAR INTENSITY AND SOLAR BEAM IRRADIANCE

The solar intensity is related to the solar beam irradiance at normal incidence  $G_{bn}$ . From equation (3.12) we can draw the relation between  $S_o(W.m^{-2}.sr^{-1})$  and the normal flux density  $G_{bn}(W.m^{-2})$  at the consider time.

$$G_{bn} = \int_0^{4\pi} S(\alpha) d\Omega$$

where  $\Omega$  is solid angle

Solid angle is defined as the ration of the area  $ds$  of a spherical surface to the square of its radius  $d$ , it can be written as follows

$$d\Omega = \frac{ds}{d^2}$$

$$\int_0^{R_s} d\Omega = \int_0^{R_s} \frac{d(\pi R^2)}{d^2}$$

$$\Omega = \int_0^{R_s} \frac{2\pi R d(R)}{d^2}$$

$$\Omega = \int_0^{R_s} \frac{2\pi (d \tan \alpha) d(d \tan \alpha)}{d^2}$$

$$\Omega = \int_0^{\alpha_s} \frac{2\pi d^2 \tan \alpha \sec^2 \alpha d\alpha}{d^2}$$

$$\Omega = \int_0^{\alpha_s} 2\pi \tan \alpha \sec^2 \alpha d\alpha$$

then

$$G_{bn} = \int_0^{\alpha_s} S(\alpha) \cdot 2\pi \tan(\alpha)(1 + \tan^2 \alpha) d\alpha$$

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## VITAGE

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### Conference Presentations:

1. Aparporn Sakulkalavek and Somchai Kiatgamolchai, "Design of Heliostat field for a Central Receiver System and Solar Flux Energy Calculation", *The 4<sup>th</sup> Conference on Science and Technology*, Thammasat University, Pathumthani, Thailand, March 16 (2005).
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