

## References

1. H. Jasik, *Antenna Engineering Handbook*. New York: McGraw Hill, 1961.
2. A. A. Oliner, "The Impedance Properties of Narrow Radiating Slots in Broad Face of Rectangular Waveguide," *IEEE Trans. Antennas Propag.*, AP-5, 1, (Jan 1957): 4–11.
3. A. F. Stevenson, "Theory of Slot in Rectangular Waveguides," *J. Applied Physics*, 19, (1948): 24–38.
4. B. N. Das, J. Ramakhrisna, and B. K. Sarap, "Resonant Conductance of Inclined Slots in the Narrow Wall of Rectangular Waveguide," *IEEE Trans. Antennas Propag.*, AP-32, 7, (July 1984): 759–761.
5. P. Hsu and S. H. Chen, "Resonant Length of Edge Slots," *IEEE Trans. Antennas Propag.*, AP09, 5, (1987): 364–367.
6. P. Hsu and S. H. Chen, "Admittance and Resonant Length of Inclined Slots in the Narrow Wall of Rectangular Waveguide," *IEEE Trans. Antennas Propag.*, 37, 1, (January 1989): 45–49.
7. R. Lakhani, D. Chadha, and S. Aditya, "Moments' Method solution for Accurate Self and Mutual Admittance of Narrow Wall Inclined Slots," *Asia-Pacific Microwave Conferenc*, 42, 12, (1992): 709–712.
8. C. G. Jan, P. Hsu, and R. B. Wu, "Moment Method Analysis of Sidewall Inclined Slots in Rectangular Waveguides," *IEEE Trans. Antennas Propag.*, 39, 1, (January 1991): 68–73.
9. V. V. S. Prakash, S. Christopher, and N. Balakhrisnan, "Hybrid Method of Analysis of Slot Discontinuity in a Rectangular Waveguide and the Validity of

- Circuit Representation,” *Intl. Journal of RF and Microwave Computer-Aided Eng.*, 8, 4, (December 7, 1998): 339–349.
10. E. A. Kraut, J. C. Olivier, and J. B. West, “FDTD Solution of Maxwell’s Equations for an Edge Slot Penetrating Adjacent Broadwalls of a Finite Wall Thickness Waveguide,” *IEEE Trans. Antennas Propag.*, 42, 12, (December 1994): 1646–1648.
  11. C. G. Jan, R. B. Wu, P. Hsu, and D. C. Chang, “Analysis of Edge Slots in Rectangular Waveguide with Finite Waveguide Wall Thickness,” *IEEE Trans. Antennas Propag.*, 44, 8, (August 1996): 1120–1126.
  12. C. G. Jan, P. Hsu, and R. B. Wu, “Corner Effects on the Mutual Impedance Between Edge Slots,” *IEEE Trans. Antennas Propag.*, 41, 4, (April 1993): 488–492.
  13. V. V. S. Prakash, S. Christopher, and N. Balakhrisnan, “Moment of Method Analysis of the Narrow Wall Slot Array in a Rectangular Waveguide,” *IEE Proc. Microw. Antenna Propag.*, 147, 3, (2000): 242–246.
  14. V. A. Katrich, S. A. Martynenko, and S. V. Pshenichnaya, *Leaky Wave Antenna with Inclined Slots in a Waveguide*. Sevastopol, Ukraine: International Conference on Antenna Theory and Technique, 9-12 September 2003.
  15. V. V. S. Prakash, S. Christopher, and N. Balakhrisnan, “Sidewall Inclined Slot in a Rectangular Waveguide: Theory and Experiment,” *IEEE Trans. Antennas Propag.*, 145, 3, (Juni 1998): 233–238.
  16. J. E. Akin, “The Generation of Elements with Singularities,” *International Journal for Numerical Method in Engineering*, 10, (1976): 1249–1259.
  17. C. G. Jan, R. B. Wu, and P. Hsu, “Variational Analysis of Inclined Slots in the Narrow Wall of a Rectangular Waveguide,” *IEEE Trans. Antennas Propag.*, 42, 10, (October 1994): 1455–1458.

18. R. F. Harrington, *Time-Harmonic Electromagnetics Theory*. New York: McGraw Hill, 1961.
19. C. T. Tai, *Dyadic Green's Functions in Electromagnetic Theory*. New York: IEEE PRESS Series on Electromagnetic Waves, 1993.
20. R. B. Wu and C. H. Chen, "On the Variational Reaction Theory for Dielectric Waveguides," *IEEE MTT*, IEEE Trans. Microwave Theory Tech., (Juni 1985): .
21. J. Jin, *The Finite Element Method in Electromagnetics*. New York: John Wiley & Sons Inc., 1993.
22. E. Kreyszig, *Advanced Engineering Mathematics*. Singapore: John Wiley & Sons, 1999.
23. R. E. Collin, *Antennas and Radiowave Propagation*. New York: McGraw Hill, 1985.
24. T. Angkaew and S. Kawahara, "Convergence Rate Improvement in FEM Modal Analysis of a Waveguides with Re-Entrant Corners," *PIERS 2003*, (Hawaii): .

## Appendix

## Gauss Quadrature Integral Approximation

In the application of finite element method, the singular element shape function generally must be evaluated in term of integral equations. The  $\rho$ -quadratic form of shape function often makes the integral difficult to solve analytically. However, the integrals over triangular element can also be proceed by employing the Gaussian or Gauss-Legendre quadrature numerical integration. But the integration must be held in term of reference element coordinate system, thus the arbitrary shape triangular element must be transformed into reference element.

The geometrical transformation of real element (expressed in  $x$  and  $y$  coordinates) to the reference element (expressed in  $\xi$  and  $\eta$ ) can be seen on Figure 1. The relation of those element is denoted as

$$x(\xi, \eta) = \sum_{n=1}^3 N_n x_n = N_1(\xi, \eta) \cdot x_1 + N_2(\xi, \eta) \cdot x_2 + N_3(\xi, \eta) \cdot x_3 \quad (1)$$

$$y(\xi, \eta) = \sum_{n=1}^3 N_n y_n = N_1(\xi, \eta) \cdot y_1 + N_2(\xi, \eta) \cdot y_2 + N_3(\xi, \eta) \cdot y_3 \quad (2)$$

where  $N_n(\xi, \eta)$  is a geometrical function that must satisfy the condition of equal to unity on the node  $n$  and vanished on the other nodes.

The integration of real element area, then, can be evaluated using the gaussian

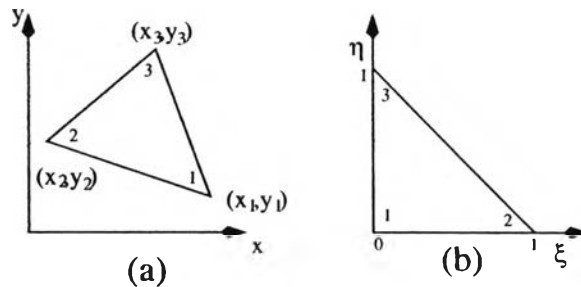


Figure 1: Geometrical transformation of triangular area

approximation.

$$\iint_e \phi(x, y) dx dy = \int_0^1 \int_0^{1-\xi} \phi(\xi, \eta) \cdot |J| d\eta d\xi \quad (3)$$

$$\int_0^1 \int_0^{1-\xi} f(\xi, \eta) d\eta d\xi = \sum_{i=1}^n w_i \cdot f(\eta_i, \xi_i) \quad (4)$$

where the points  $\xi_i$  are the point at which the function is evaluated and the coefficient  $w_i$  are called weights. Therefore, the integral can be expressed as

$$\iint_e \phi(x, y) dx dy = |J| \sum_{i=1}^n w_i \cdot f(\eta_i, \xi_i) \quad (5)$$

in which  $|J|$  is the determinant of the Jacobian matrix.

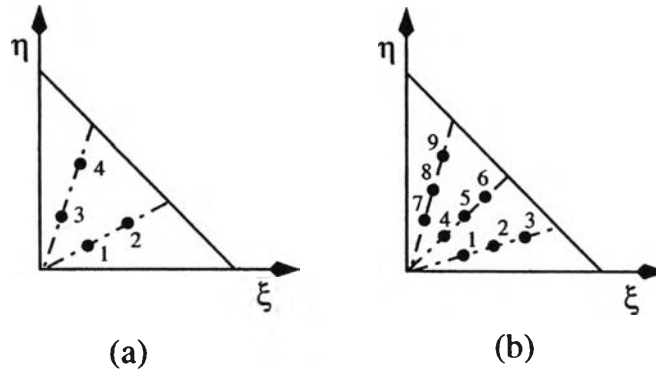


Figure 2: The sample point of gaussian integral approximation for  $n = 3$  (a) and  $n = 9$  (b).

Table 1: Sample point of Gauss quadrature integral approximation with 4 points

$i$	$\xi_i$	$\eta_i$	$w_i$
1	0.2800199155	0.0750311102	0.0909793091
2	0.6663902460	0.1785587283	0.1590206909
3	0.0750311102	0.0909793091	0.0909793091
4	0.1785587283	0.6663902460	0.1590206909

Table 2: Sample point of Gauss quadrature integral approximation with 9 points

$i$	$\xi_i$	$\eta_i$	$w_i$
1	0.188409406	0.023931132	0.019396383
2	0.523979068	0.066554068	0.063678085
3	0.808694386	0.102717655	0.055814420
4	0.106170269	0.106170269	0.031034213
5	0.295266568	0.295266568	0.101884936
6	0.455706020	0.455706020	0.089303073
7	0.023931132	0.188409406	0.019396383
8	0.066554068	0.523979068	0.063678085
9	0.102717655	0.808694386	0.055814420

## Biography

Iswandi was born in Kulon Progo, Central Java, Indonesia, on April 15, 1976. He received his bachelor degree in electrical engineering from Gadjah Mada University, Yogyakarta, Indonesia, in November 2000. Since 2002 he joined the faculty of Gadjah Mada University. His research topic interests include antenna, waveguide and numerical technique. In June 2003, he received a scholarship from the AUN/SEED-Net to continue his study at Graduate School of Engineering, Faculty of Engineering, Chulalongkorn University.

